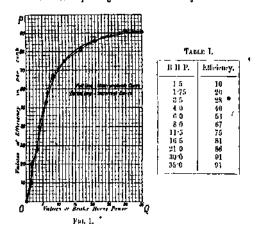
ELECTRICAL ENGINEERING TESTING

Curve Plotting.

Introduction.—The practice of recording the results of any .casurements or tests graphically, as well as in tabular form, in cases where this is possible, cannot be too strongly urged, and is a most important, as well as, in many cases, an indispensable operation. More especially is this the case with a large number of physical measurements, and particularly so with a majority of tests in Electrical Engineering. The practice of curve plotting, as these graphical representations may otherwise be termed, presents the following important features—

- (a) It enables the nature of the variation of one quantity with another to be seen at a glance much more clearly than is possible by aid of a table of results.
- (b) It enables prrors in experimental observations, of which there are sure to be some, to be corrected comparatively easily, which in a majority of cases would be impossible from the table of results.
- (a) In the case of the calibration of instruments it enables the law of that under test to be readily observed.
- (d) It has the enormous advantage of enabling any intermediate value between those actually observed and tabulated, to be at once obtained accurately. This, it will readily be conceded, is the most important and valuable feature of all, and the ease, as well as the rapidity with which the operation of obtaining intermediate values can be accomplished, will be dependent on the scales chosen in originally plotting the curve in question.

It may therefore be profitable to indicate the mode of procedure in plotting curves, and with a view to exemplifying it, the results of a particular test are given in Tuble I., and the corresponding curve or graphical representation in Fig. 1. They relate to the determination of the Brake Horse Power (B.H.P.) of anselectromotor and the corresponding value of its efficiency at each load.



In testing work generally at least six or eight different determinations throughout the range should be made, where possible, in order that the curve may be drawn more accurately. In most cases a curve constructed on three or four points only would, be practically useless and could not be depended on.

Directions for Plotting.—(1) Assuming that all the results have been worked out numerically and entered up in tabular form, the first thing to note is what two sets of quantities have to be plotted together, and secondly, the largest value of each set, for beyond this the scale need not extend.

(2) The left-hand vertical and bottom horizontal sides OP and OQ respectively of the squared sheet of curve paper are termed the axes and are rectangular. They intersect in a point O called the origin. Distances measured vertically are termed ordinates, and those horizontally, abscissa.

- 2 (3) Carefully note which set of readings have to be plotted on the ordinates and which on the abscisso, and then choose the scales of the axes OP and OQ such that they are as long as possible and include the maximum values to be plotted. Also, if possible, arrange such that one of the smallest divisions represents a simple whole number of one digit. For example, if 33 was the largest number to be plotted and the side of the squared paper contained 100 divisions, let 1 division represent 0.5 only, whence 66 will give the 33; this is far more convenient a scale for future reference in obtaining intermediate values than 1 division representing 0:33 (i. s. 99 to give the 33 approx.). While it is a great advantage for the numerical length of the axes to be as large as possible, so as to enable the curve to be drawn larger and more accurately, the length should be decided by considerations of future reference to it for intermediate values as just
- (4) The axes must be numbered every 10th division, and under no circumstances with the numbers obtained from experiment.
 - (5) Write along each axis the nature of the quantity plotted on it,
- (6) Each point must be plotted by finding the point of intersection of the axes representing the two corresponding quantities under consideration at the moment and a distinctive mark there
- (7) When all the points are plotted, a mean curve, as shown by the full line, Fig. 1, must be drawn through as many points as will allow of a uniform line being drawn.

Some points are always sure to lie on either side of this mean line and denote experimental errors. The object of the curve is to correct for these.

acteristic "determinations with direct current generators, it often happens that curves cross one another and lie close together. In such cases they must be drawn thin and a different notation for the respective sets of points used, such as that represented in Fig. 2,

(8) In some tests, as for example in "char-

All confusion will thus be avoided.



F10. 2.

Calibration and Standardization of Electrical Measuring Instruments.

General Remarks.—This subject is perhaps one of the most important in connection with electrical testing, and we shall therefore devote some considerable attention to it. It will at once he obvious to any one, without any consideration, that a measuring instrument which is reading incorrectly, or one that has been calibrated so long ago that its present readings may not be true, is a useless instrument, or even worse than this, as one is unconsciously liable to take its reading as correct. The importance of correct reading and accurately calibrated measuring instruments cannot be over-estimated, for on their being so hangs . the whole crux of further testing, the results of which would otherwise be quite worthless. This the author would emphasize most strongly, for it is unfortunately his experience, and no doubt that of many more like him, that the average experimentalist is only too ready to take the scale reading of any instrument as correct without in the least troubling bimself as to whether it actually is so or not. This no doubt arises from the little extra trouble required to calibrate such instruments prior to starting some particular test.

develop errors in their scale readings either from continued use, abuse, or in transit from one place to another, some of course being much more susceptible to alteration than others. Hence in all cases where it is desired to obtain accurate results and do good work, the instruments should be re-calibrated and restandardized frequently, and a calibration curve drawn whenever possible with the date of the test inserted. At the very least six determinations should be made, wherever possible, but preferably ten or twelve, as it is not possible to draw a reliable calibration curve on less than aix points. In all cases it is of the utmost importance to see that the connecting wires or cables do not magnetically affect the instruments, for it must be carefully remembered that a wire carrying a current, no matter whether it is straight or otherwise, acts as a magnet.

Measuring instruments may change their constants and

Such inductive effects will be minimized by running or twisting the "dead" and "return" togother, when the two equal and apposite magnetic effects noutralize. An ordinary flexible twinlead is non-magnetic externally, but it possesses a very small electrostatic capacity.

Instruments are usually calibrated by comparing their readings with those of very accurately calibrated standard instruments. Simultaneous readings must be taken on both to avoid errors due to variation in between. Ammeters are always connected in series and voltmeters are always connected in parallel with their standards.

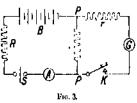
In the calibration of voltmeters, the employment of keys in any of the branched or parallel circuits containing voltmeters to be calibrated is usually a source of inconvenience and should be avoided, for a key which places, say, a voltmeter of 1500 Ohms resistance in parallel with a similar instrument already reading, will cause this reading to decrease owing to the alteration of the P.D. at the terminals due to inserting such a low resistance meter, and the consequent reduction in the terminal combined resistance.

Calibration of an Ammeter by comparison with a Standard D'Arsonval Ammeter,

Introduction.—When a standard current measurer, such as a Kelvin standard balance or a potentiometer set, is not available for comparing the animeter to be tested with, the following method a calibration may conveniently be employed. It consists in using a good reflecting D'Arsonval galvanometer in conjunction with a low resistance composed of platinoid or other suitable material having a small temperature co-efficient of resistance, which should preferably be known. The resistance of the D'Arsonval galvanometer may conveniently be something like 2000 to 4000 times that of the low resistance to which it is shunted. The instrument, its scale, and the resistance should be permanently fixed and standardized carefully by means of a copper or silver voltameter. Then if the current which produces a full scale deflection, with a certain known resistance in series with the galvanometer, is accurately known, the current producing any

other deflection with the same resistances will be very approximately in direct proportion and therefore at once known.. Some slight corrections might be necessary for great accuracy when subsequently using these particular constants, due to alteration of resistance through change of temperature and to the deviation of the D'Arsenval readings from the direct proportional law, for which correction see Appendix, p. 490.

Apparatus.—Secondary battery B capable of giving the maximum current required;



S; key K; carbon rheostat R (p. 597); resistance box (r); ammeter A to be calibrated; low resistante PP . either of the form shown (p. 605), or simply a sheet

of the metal.

reflecting D'Arsonval galvanometer G (p. 569); switch

N.B.—It is assumed that the galvanometer and low resistance in combination has been carefully standardized previously and now constitutes the standard D'Arsonval ammeter,

Observations .-- (1) Connect up as in Fig. 3, and adjust the pointer of A to zero and the spot of light from G to the left-hand end of the scale used as a temporary or false zero in this

- (2) Insert the proper resistance in (r) as given from the constants of standardization for the maximum current to be measured and corrected for the temperature of the room at the time of the test.
- (3) With K large, close S and adjust the current through the ammeter to be calibrated to about inthe of the maximum scale reading by means of R. Then note simultaneously its reading A
- and the deflection d on G when K is pressed. (4) Repeat 3 for about ten different readings on A rising by about equal increments to the maximum with no decreasings of current.
- (5) Repent 3 and 4 for a similar descending set of the same readings on G, noting the corresponding ones on A, avoiding all increasings of current, and tabulate your results as follows--

Name Ammeter tested : I Temperature of Rom	No		Days or year Resultance (*)= Ohme	Ohms,
Reading on Amuster leasted. Ascending Descriding	Deflection On D'Arronnel. d.	Corrected Resultings of D'Armanyal. D	True Current i.e. (B) toduced (a) Ange,	% Broot of Annual ar tested

(6) Plot curves having values of true current (a) as abscisse and A as ordinates.

Inferences.—Enumerate any sources of error in ammeters generally. What can you infer from your experimental results? "Why should the current be so carefully increased only in 4 above and decreased only in 5 above?"

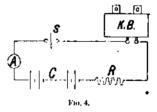
(2) Calibration of an Ammeter by comparison with a Kelvin Composite Balance used as a Centi-ampere Meter.

Introduction.—The following is a convenient and ready means of calibrating any ammeter reading up to 1 ampere, employing a Kelvin composite balance used in the manner mentioned, as a standard for comparison. A complete description of the construction and manipulation of the instrument will be found on p. 554, to which a reference should be made and the constants obtained therefrom.

Apparatus.—Kelvin composite balance K.B. (p. 554); ammeter A to be tested; switch S;

adjustable resistance R (p. 600, et seq.); source of current C at a P.D. of from 40 to 60 volts.

Observations.—(1) Connect up as in Fig. 4, adjusting both instruments carefully to zero. Make quite certain that the connections are as indicated.



(2) Turn the switch in front of the balance to "volts" so as to place the fixed and movable fine wire coils in series with each

other and with the circuit. Now adjust the balance and its sensibility by employing the proper weights as given in the table of constants (p. 556), so that the maximum current to be measured on A would give a reading on K.B. as nearly right across the scale as possible.

- (3) With R as large as possible close S and obtain about $\frac{1}{10}$ th of the maximum scale reading on A by varying R. Note this and simultaneously the corresponding position (d) of the slider
- (4) Ropest 3 for about ten different values of current on A (by altering R) rising by about equal increments to the maximum.
- (6) Repeat obs. 4 for a similar set of descending values of current, and tabulate your results as follows—

Name Composite Balting	n necit; No	. Cos	Dave			
Bilder Reading True Ampa.		Rodding on A.		% Error of	Meun X	
(4)	K.d.	Ascending,	Descending,	A.	Error,	
		i ———				

(6) Plot a calibration curve for the ammeter tested having readings on A sa ordinates and "True Currents" as abscisse.

Inferences.—What sources of error are ammeters in general liable to? Can anything in particular be inferred from your experimental results?

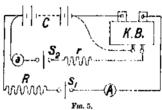
(3) Calibration of an Ammeter by comparison with a Kelvin Composite Balance used as a Hekto-ampere Meter.

Introduction.—The Kolvin composite balance can be used as a standard ammoter for the measurement of direct currents up to about 600 ampores, and hence any other ammoter can be feadily calibrated by comparison with it. A description of the construction of the balance will be found on p. 554, together with the method of using it to measure heavy currents. In this connection it will be seen that the current to be measured passes through the thick fixed wire coils only, which act on the movable

coils of fine wire carrying a small auxiliary current from preferably an independent source of E.M.F. The accuracy therefore of the calibration will depend on the accuracy with which the current through the moving coils is measured, and this is a disadvantage in the use of the composite balance for current measurement.

Apparatus.—Kelvin composite balance K.B.; ammeter A to be

tested; low reading accurately calibrated ammeter (a); rheostats R (p. 697) and r (p. 600); switches S₁ and S₂; battery C capable of giving the current corresponding to the highest scale reading on A.



Note,—If a second battery, such us six small cells, is available the auxiliary current circuit may preferably be fed from it, for then this current will remain unaffected when the main current through A is altered.

Observations.—(1) Connect up as in Fig. 5 if only one battery is used, and adjust the pointers of A and a to zero, and also that of KB, in the manner mentioned on p. 556. Make quite certain that the connections are as indicated in the diagram.

- (2) Turn the switch on the balance (in front) to "Batte" so as to put the fine wire movable coils only in connection with the small terminals, and therefore in series with the auxiliary circuit,
- (3) Adjust the balance and its sensibility by employing the proper weights as given in the table of constants (p. 557) so that the maximum current to be measured on A would produce as nearly as possible a full scale reading on K.B.
- (4) With r at its maximum close S₁ and adjust the current through the fine wire movable coil to its proper value, as given with the constant, by varying r. Always make quite sure that it has this value before taking each reading on K.B.
- (5) With R large, close S_1 and obtain about $\frac{1}{10}$ th of the maximum scale reading on A by varying R. Note simultaneously the reading on A and the position (d) of the slider of K.B.

- (6) Repeat 6 for some ton different values of current on A (by altering R) rising by about equal increments to the maximum.
- (7) Repeat obs. 6 for a similar set of decreasing currents and tabulate as follows—

NAME		DATE		•
Composite Balance : No	Constants meet	Current in Moving	Colles	Anips
Annualer tested		No	Range	

Hiblor Reading	True Amps.	Routing	on A.	% Birner of	Mean Z
(a).	K d.	Age teling,	Descending,	A.	Error.
— -					

(8) Plot "calibration" curves for the ammeter tested having readings on Λ as ordinates and true currents as abscisse.

Inferences.—What sources of error are ammeters in general liable to? Can you infor anything in particular from your experimental results?

(4) Calibration of an Ammeter by comparison with a Kelvin Centi-ampere Balance.

Introduction.—Any ammeter reading up to I ampere can be readily calibrated by comparison with a Kelvin standard centi ampere balance. A full description of this instrument, together with the table of constants, will be found on p. 546, and the method of using it is precisely the same as that of the composite balance used as a centi-ampere motor, except that there is no switch at all on the balance in question. The operator should refer to the Appendix (p. 546) for details in connection with the balance.

Apparatus.—This, with the exception of the balance, is precisely the same as is required for the corresponding calibration by the composite balance.

Observations...-Those, together with the diagram of connections and the inforences, are precisely the same as for the test on p. 7 and will not therefore be repeated here. The operator must refer to the similar test using the composite balance.

(5) Calibration of a Direct Current Ammeter.(Crompton Potentiometer Method.)

Introduction.—This method is a very convenient and accurate one for calibrating ammeters, and in it the measurements are referred to and obtained in terms of a standard Clark cell and standard resistance. The principle of the method is a direct application of Ohm's Law, and consists in measuring the fall of potential down an accurately known standard low resistance connected up in series with the circuit through which the current to be measured is passing. This fall of potential is measured in terms of the E.M.F. of the Clark's cell through the medium of the potentiometer, employing the principle of the Clark-Poggendorff method for comparing two or more E.M.F.'s. A detailed description of this will be found in a separate work by the author on Practical Electrical Testing for 1st and 2nd year students and others. The Crompton potentiometer is a specially arranged form of comparing instrument by means of which the calibration can be easily and quickly carried out. Before proceeding further the operator should refer to a detailed description of this piece of apparatus which will be found in the Appendix (p. 510) together with the method of using it. The present method possesses the all-important advantages that the measurements are all in terms of the Official Board of Trade standard-the Clark cell-that their accuracy is great, and without any very special means this can be obtained to at least 1 in 1000, and that the range is almost illimitable from 0 continuously up to maximums commonly met with in practice. The accuracy of the results in the present method is more particularly dependent on that with which the standard low resistance is known. The value of this must be such that the fall of potential down it due to the maximum current to be measured is not greater than I'5 volts, while at the same time the carrying capacity must be such as to allow it to pass this current without sensible heating, which would thereby alter its resistance.

Apparatus.—Crompton potentiometer P (p. 510); secondary that tery B capable of easily giving the maximum current required for a full scale reading on the ammeter A to be calibrated;

ewitch S; one secondary cell (b) for the "working cell" of the potentiometer; accumtely known standard low resistance R (p. 605); sensitive D'Arsonval or moving cell galvanometer (g) (p. 569); standard Clark cell E; carbon rheostat (rh) (p. 597f.

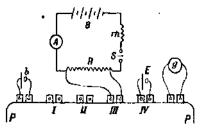


Fig. 6.

Observations.—(1) First place the levers of G and E (Fig. 208) on stude 14, and that of H on stude 1 or 2 for precention. Now connect up as in Fig. 6, in which only the row of terminals on the potentiometer P is shown symbolically for brevity.

- (2) Adjust the galvaneuter g approximately, and A carefully, to zero, levelling them if necessary. See that a suitable low resistance standard R is employed, and one that will give a fall of potential at its ends not exceeding 1.5 volts (= $A \times R$) for the maximum current to be used (vide p. 13).
- (3) "Set the potentiometer" by the standard cell in the way described on p. 514, the contact lever H above referred to being on study IV, thus inserting E (Fig. 6) in the circuit of g, which must be done so that its E.M.F. opposes that of b. Now close S and adjust rh so as to obtain about 1 to f the full scale reading on A.
- (4) With the positions of the resistances G and G₁ (Figs. 207 and 208) as found in 3, uncitered, turn the lever of H to stude III so as to throw into circuit with g the fall of potential down R which as seen is across terminals III. Now adjust the lever of the resistances E (Fig. 207) and the sliding key C so that no deflection occurs on g on pressing this latter.

N.B.—If it is impossible to get a balance owing to the deflection of g being always to one side, the P.D. across III is assisting, instead of opposing (as it should be) the fall due to b in the

stretched wire; the wires from R to III must then be interchanged.

• If the lever at E is on stud 1 (literally 1000) and the clider C at 315 on the scale, the P.D. across R=1315 volts and the true carrent A_1 through A if R=0.1 Ohm is $\frac{1315}{0.11}=1.315$ amps.

Note simultaneously the readings on P and A when balance is obtained. Turn H to IV again and see whether the balance in obs. 3 still helds. If it does not, re-set P.

- (5) Take about ten different scale deflections on A rising by about equal increments to the maximum by varying (rh) and repeat 4, noting the new values of P and A.
- (6) Repeat 4 and 5 for a similar descending set of readings on A and tabulate your results as follows—

Amuster	Potentioneter Rending,		True P.D.	True Corrent	Report of	
	Blud of A	Position of Bluler (f.).		Ties Content	(41-4)	Z Brown
	<u> </u>		<u> </u>			

It should be carefully noted whether a "Clark" cell or "Carhart-Clark" cell is being used before setting the potentiometer in 3, and that the assumed E.M.F. for this purpose at the sarticular temperature is correct, the temperature coefficient of 3.M.F. being very different in these two cells (vide p. 643).

Standard Westen (cadmium) cells have an international ralue of E.M.F. of 1 0183 volts at 20° C., with a temperature coefficient of -0 0000398 volt per rise of 1° C., between 0° and 10° C. In 1908, for a range of 0° C. - 40° C., Wolff obtained he relation giving the E.M.F. at °tC., namely—

$$E_6 = E_{30} - 0.0000406(t - 20) - (9.5 \times 10^{-3})(t - 20)^2$$

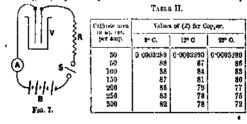
= 1.0183{1 - 0.0000398(t - 20)} volts approx. (see table 643)

(7) Plot calibration curves for the ammeter tested having values f A as ordinates and true amps A₁ as abscisse.

Inferences.—What can you infer from your experimental esults, and can you suggest any sources of error which might itiate the results?

(6) Determination of the "Constant" of a Galvanometer or Ammeter by Means of a Copper Voltameter.

Introduction, -- From the results of a large number of tests it has been found that, using the necessary precautions, the constant of an electric current instrument can be obtained with certainty to within $\frac{1}{10}\%$ of absolute accuracy by the electrolysis of copper. The voltameter (V) should consist of three or more pure copper plates dipping into a saturated solution of copper sulphate contuined in a suitable glass or earthenware vessel, there being one, more "anode" than "cathode," and the two sets arranged alternately with an anode at each end. The plates should be as square as possible, and placed from \$" to 3" apart; if too close, polarization will take place when strong currents are used, and the current density (reckoned in amps. per sq. cm.) is too great. There should not be less than 30 sq. cms, per amp.; if there is, the plate surface will be too small and the deposit on the cathode trrogular, some of it falling to the bottom of the vessel. The resistance of V will also become high and variable, due to the formation of copper oxide, and will give trouble in keeping the current constant. The solution should be a saturated one (sp. gr. 1-211) of pure copper sulphate crystals and distilled water, with 1% by vol. of strong sulphurie acid added, which is necessary to insure success. The vol. of solution should be about 1100 cc. per amp. The anodes may be made of about No. 18 S.W.G., and the cathodes or gain plates of No. 30 S.W.G. pure copper, all edges and corners being smooth and rounded. The electrochemical equivalent (Z) of any substance, in this case copper = No. gras, deposited by 1 coulomb.



Apparatus.—Voltameter (V); rheostat R (p. 597); switch S; ammeter A to be standardized; secondary battery; drying cupboard D, not shown; acid bath.

Observations .- (1) Connect up as indicated in Fig. 7, and adjust Acto zero. Light the gas jet under the steam boiler of D. after seeing that the latter contains enough water.

- (2) Determine the necessary area of cathode, and hence the number of gain plates required for the current to be used, reckoning both sides in contact with liquid as the effective area of cathode.
- (3) Carefully clean the cathodes all over with fine emery cleth until quite bright, then dust with a dry clean cloth, and do not touch the part to be immersed with the fingers. Clean the anodes if they look dirty.
- . (4) Carefully weigh the gain plates on a chemical balance to 1 m g_0 and note their weights (W_1) grams.
- (5) Insert the same area of trial plate to act as cathode, so as to adjust the current to the value required, then remove them, making sure that the + of buttery is joined to anode.
- (6) Insert the weighed gain plates, and at a convenient and noted instant of time switch on, quickly adjusting the current to its proper value.
- (7) Keen it flowing for at least thirty minutes, and maintain it constant all the time by altering R, if necessary. (Note,-1:177 grams of copper (capric) are deposited per amp.-hour approx.)
- (8) Note the exact instant of switching off. Very carefully remove the gain plates so as not to scratch them, rinse in seidulated water to prevent the nascent copper oxidizing, then in clean water, and place in D to dry.
- (9) When dry and cool re-weigh the gain plates and note the weights W. grams.
- (10) Repeat 2-9 for one or two other current strengths and tabulate as follows -

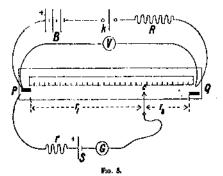
Kaus .

Cathode Area = . . . eq. cms. per amp. Terrorreture of Buth = . Weight of plates in Time in Beca. (1) ·(20'n-28'i) Before ZW After XIV-

(7) Calibration of Direct Current Voltmeters. (Poggendorff's Method.)

Introduction.—The following method is at convenient one for enabling low-reading voltmeters up to about 3 or 4 volts to be easily and rapidly calibrated by comparison with one or two Clark's standard cells. Some convenient form of metre bridge, either circular or ordinary, is required. The principle of the method will be seen to be practically the same as the "Clark-Poggendorff" method of comparing two R.M.F.'s.

Apparatus.—Metro bridge of some convenient type, either the ordinary straight or circular form; secondary battery B giving an E.M.F. a little in excess of the maximum voltage to be recorded on the voltmeter V to be calibrated; key k; carbon rheostat R (p. 597); sensitive galvanometer G (p. 572); high resistance $\langle r \rangle$ of about 10,000 ohms; standard cell $\langle S \rangle$ of known E.M.F. It will be observed that the metre bridge, of whatever form is used, is represented symbolically by PQ in Fig. 8, and if the general scheme of the connections is understood, there will be no difficulty with them when using any form of bridge.



Observations.—(1) Connect up as in Fig. 8, adjusting V carefully to zero and G to about zero. See that like poles of B and S

are connected to the same end P, when the respective E.M.F.'s will oppose one another.

- (2) Adjust R to a high value and likewise (r), which might preferably be about 10,000 ohms, and is merely for the purpose of preventing the standard cell S from sending but a very minute current when its circuit is closed at the tapping key or rolling contact C, which at first might be far from the correct position of balance. When C is moved to such a position that the deflection on G is small, (r) may temporarily be cut out of circuit so as to make the sensitiveness of the test a maximum.
- (3) Now close K and alter R so as to obtain about that of the maximum scale reading on V.
- (4) Find a position for C such that on making contact with the bridge wire by means of it, no deflection occurs on G, r being · manipulated as in obs. 2. Note the reading on the voltmeter V calibrated and the position of C where $PC = r_1$ and $QC = r_2$.
 - (5) Re-insert r and repeat obs. 3 and 4 for about ten readings on Frising by about equal increments to the maximum.
 - (6) Calculate the true volts Y. from the relation-

$$V_x = \frac{r_1 + r_2}{r_1} \times \text{ E.M.F. of standard cell,}$$
 and tabulate your results as follows—

NAME . . . E. H. F. of Standard Coll . . . Volta at O. $\theta = \dots$ Ohma $\theta = \dots$ Ohma
of reference only.

n	71 + 73	Ituading on V.	True Yults	X Error of Volumeter testoil,

Note.—The E.M.F. of a Clark's standard cell = 1:4340 legal volts at 15° C., and its E.M.F. at other temperatures may be found from the relation-

E.M.F. $\Rightarrow 1.4340\{1 - 0.0007 (t - 15)\} \text{ legal volts}$ where 0.0007 is the temperature coefficient of the cell and its temperature in degrees Centigrado. For a Carbart-Clark. coll the coefficient is 0.00038. For table of E.M.F.'s see p. 643.

(7) Plot a calibration curve of the voltmeter under test having values of V as ordinates and Vr as abscisses.

Inferences.-Does the accuracy of the above test depend on

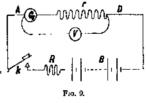
anything in particular? Show how the relation given in 6 can be obtained and state any assumptions made in deducing it.

(8) Calibration of a Voltmeter by Comparison with a Standard D'Arsonval Voltmeter. *

Introduction.—The method may conveniently be employed for calibrating a voltmeter when neither a Kelvin standard belance nor a "potentiometer set" is available for use as a standard with which to compare the instrument under test. In the present case a fairly sensitive and good form of D'Arsonval galvanometer combined with a high resistance placed in series constitutes the standard voltmeter which together with its scale is permanently fixed up. The arrangement is very carefully standardized and its constants found with the aid of a Clark's standard cell and Clark's potentiometer method (p. 16), and thus a reliable standard voltmeter is obtained.

If the voltage which produces a full scale deflection with a certain resistance in series with the instrument at a given temperature is known, then that causing any other deflection under the same conditions will be in direct proportion and therefore at once known. For considerable accuracy some small corrections would be necessary in using these constants at some other time owing to the difference in temperature alloring the resistances of the galvanemeter ceil and those in series with it, and to the D'Arsonval not exactly fulfilling the direct proportional Law, for which correction see p. 490,

The D'Arsonval and its



resistance can be arranged in one of two ways—(a) as represented in Fig. 9, assuming that a sufficiently high adjustable known resistance for placing in sories with it is available. If then the "figure of merit" of G, i.e. the am-

perces (a) per scale division, is accurately known, the extra high resistance (r) necessary to b. placed in series with it so that the

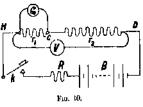
required maximum voltage applied to AD (Fig. 9) may produce a full scale deflection on G, can be found by Ohm's Law as follows— • If (d) = the maximum scale reading to be obtained by a maximum voltage V, then if (y) = the resistance of the galvano-

mater
$$G_i^{\bullet}$$
 we have $(r+g) = \frac{V}{c} = \frac{V}{\omega t}$
 $\therefore r = \left(\frac{V}{\omega t} - g\right)$ ohms.

(b) If G is very sensitive and sufficient resistance is not avail-

able the arrangement in Fig. 10 may be used, r now taking the form of two resistance boxes r, and rg.

In this case r, will be small, compared with the resistance of G and with $(r_1 + r_2)$, and this sum large compared with the



resistance of V_i the voltmeter to be calibrated.

If V and v are the voltages across HD and v_1 respectively and (g) the resistance of G, whose "figure of merit" is (a),

then
$$V: v = r_2 + \frac{r_1 q}{r_1 + g} : \frac{r_1 g}{r_1 + g}$$

 $\text{then } V: v = r_2 + \frac{r_1 g}{r_1 + g}: \frac{r_1 g}{r_1 + g}$ and if (d) has the same meaning as before $v = \omega lg$,

whence
$$V = \frac{r_1 g}{r_1 + g} = \alpha dy \left(r_2 + \frac{r_1 g}{r_1 + g} \right)$$

whence $V = \frac{r_1 g}{r_1 + g} = \alpha dg \left(r_2 + \frac{r_1 g}{r_1 + g} \right)$ assuming r_1 to be negligibly small compared with g and r_2 we have $\frac{r_1}{r_2} = \frac{ady}{V}$ approximately, which is obvious from a consideration of Ohm's IAW.

Referring to Fig. 8 it will at once be seen that discarding the cell S, the standard D'Arsonval G with its extra resistance r may be employed to actually measure the P.D. between P and $C_{i,j}$ whence knowing the ratio of PQ to PC the true volts corresponding to any reading on V(Fig. 8) can at once be obtained. Thus the arrangement just referred to practically brings us to hat shown in Fig. 10,

Apparatus.—Secondary battery B of a sufficient number of cells

to give the highest reading on the voltmeter (V) to be calibrated; a fairly high resistance D'Arsonval galvandmeter G (p. 569) spring tapping key k; one or two high resistance boxes r_1 and r_2 ; variable unknown high resistance rheostat R; this latter, however, will be of no use if the resistance of the rest of circuit is very high, and in this case the voltage due to B will have to be varied by altering the number of cells in the battery.

Observations.—(1) Connect up as shown in Fig. 10, which latter arrangement will be found to be the one most common in practice. Adjust the spot of light of G to the left-hand end of the scale as a temporary or false zero so as to obtain a full scale deflection up to the other end for the maximum voltage to be measured.

- (2) Insert the proper resistances in r₁ and r₂ as given from the constants of standardization for the maximum voltage to be measured and corrected for the temperature of the room at the time of the test.
- (3) Close k and adjust R, or after the number of cells in B so as to obtain about Toth of the maximum scale reading on V and note simultaneously the readings on V and G.
- (4) Repeat 3 for about ten different readings on V rising by about equal increments to the maximum.
- (5) Ropent 3 and 4 for a similar descending set of the same readings on G, noting the corresponding once on V, and tabulate your results as follows—

Hans Voltmeter : No Type		Dats Ohnu.		
Temperature of com-	- •C,	Resistance of $a=\dots$ Gives at *C.		

Reading in Yelts of	a Yultaneter texted.		Tene Voltage, f. c.	Z Error of
Ascending V	Descending V.	D.	D reduced (r) Volta.	Vollmeter tested.

Instead of the variable high Resistance theostat (B) shown in tests 8-11 which may not be available, the following arrangement for varying the voltage across the parallel combination of voltmeter tested and standard, will be found convenient, namely—connect two variable imap resistances B, R, n series across the supply and shunt one of them (B,) with the voltmeter and standard in parallel, the lamps of each rhrestat being operated in parallel and being for a voltage = to that of the supply. These by keeping 1 lamp in B, and varying B, the volts across B, can be varied from \(\frac{1}{2}\) that of the supply to its full value, while by keeping 1 lamp in B, and varying B, the volts across B, can be varied from \(\frac{1}{2}\) that of the supply to 0; thus powering the full range of supply volts on B.

(6) Plot "calibration curves" having values of true voltage (v) as ordinates and V as abscisse.

*Inferences.—Enumerate any sources of error in voltmeters generally. State clearly what you can infer from the results of your tests.

(9) Calibration of a Voltmeter by Comparison with a Kelvin Composite Balance used as a Voltmeter.

. Introduction.—The composite balance when used in conjunction with separate anti-inductive resistances may be conveniently employed as a standard direct or ulternating current volumeter capable of measuring pressures up to about 600 volts. The following method assumes the use of such an instrument, and the reader should refer to p. 554, et seq., for the construction and mode of using this form of balance and for the table of constants and sensibilities.

Apparatus.—Adjustable, fairly high resistance R (p. 603); switch S; voltineter V to be calibrated; Kelvin Composite Balance K.H., with its non-inductive resistance r (p. 553); battery of secondary cells capable of giving the maximum voltage to be used, which we therefore assume to be direct.

Observations.—(1) Connect up as in Fig. 11, adjusting both instruments carefully to zero, and make quite certain that the connections are as indicated.

- (2) Turn the switch in front of the talance to "Volte" so as to place the fixed and movehle fine wire coils in series with one another across the terminals. Observe that the anti-inductive resistance r is numbered the same as, and therefore belongs to the balance in use, and make quite sure of having the correct resistances in it in use (p. 556).
- (3) Adjust the balance and its sensibility by employing the proper weights as given in the table of constants (p. 556), so that

the maximum voltage to be measured on V would produce as nearly as possible a full scale reading on K.B.

- (4) With R as large as it can be, close S, and obtain about 70th of the maximum scale reading on V by altering R. Note simultaneously the reading on V and position (d) of the slider of K.B.
- (5) Repeat 4 for some ten different values of voltage on V (by altering R or the number of cells in the battery) rising by about equal increments to the maximum.
- (6) Reject obs. 5 for a similar set of decreasing voltages, and tabulate your results as follows—

	ив , псэ: No	Constants	. Voltmoter t	DATE Cericid To	
Sinder resuling d.	Volts &.d.	Consorted Yulta F _T		g on V. Describing	Z Li tot of

N.B.—The values Fy are the readings on the standard corrected for temperature,

(7) Plot a calibration curve for the voltmeter tested having realings on V as ordinates and true volts V_x as abscisse.

Inferences.—What sources of error are voltmeters in general

Inferences.—What sources of error are voltmeters in general liable to 1 Can anything in particular be inferred from the above results?

(10) Calibration of a Voltmeter by Comparison with a Kelvin Centi-ampere balance used as a Voltmeter.

Introduction.—The Kelvin Standard Centi-ampere balance when used in conjunction with extra anti-inductive resistances constitutes a most convenient standard voltnucter with which to compare any other voltnucter to be calibrated, up to about 800 volts.

For larger voltages, up to 2500 volts, special non-inductive high resistances are provided for inserting in series with the coils of the instrument. The combination then constitutes a standard voltmeter by means of which any other voltmeter, either for direct or alternating currents, reading up to 2500 volts, can be calibrated, by comparison, in the ordinary way.

A complete description of this balance, together with the

method of using it, will be found on p. 516 et seq., where the table of constants is given.

In the present test the apparatus, observations and inferences are precisely similar to that of the corresponding calibration by myons of the composite balance used as a voltmeter, the centiampere balance being substituted for this latter. They will consequently not be repeated here, but may be seen on p. 21.

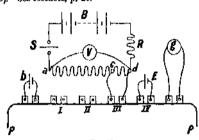
(11) Calibration of a Direct Current Voltmeter. (Crompton Potentiometer Method.) * Introduction.—The method is a very convenient and accurate

one for the purpose, and consists in calibrating the voltmeter to be tested in terms of the E.M.F. of a Clark's standard cell, a

known fraction only of the voltage applied to the instrument being actually compared with the standard E.M.F. The principle of the method is identical with that of the "Clark Poggendorff" method for comparing two or more E.M.F.'s, a full description of which will be found in a separate work, by the author, on Practical Electrical Testing, for 1st and 2nd year students and others. The Crompton Potentiometer is a specially arranged form of comparing instrument by means of which the calibration can be easily and quickly rarried out. A detailed description of t will be found on p. 510, to which the reader should in the first astance refer. There are three extremely important features in connection with the present method, using the potentiometer; irstly, the enormous range of applicability, for the instrument can be used equally well in the measurement of current and esistence as well as voltages from 0 to almost any practical amount; secondly, the measurements are in terms of the official Board of Trado Standard-the Clark cell-though any other tandard can be used; thirdly, the accuracy is great and under rdinary conditions the measurements are accurate to at least 1,% and with care, using a very accurately adjusted instrument, coursey to something like $\frac{1}{10}\%$ can be obtained. In this form f potentiometer the highest voltage which can be compared irectly is 1.5 volts, and hence the fractions employed of all igher pressures to be measured must fall within this limit. Apparatus.—Crompton potentiometer P (Fig. 208); secondary

Apparatus.—Crompton potentiometer P (Fig. 208); secondary attery B capable of giving the maximum voltage required for a

full scale reading on the voltmeter V to be calibrated; key or switch S; one secondary cell (h) for the "working cell" of the potentiometer; "volt hox," i.e. divided resistance acc for obtaining a fraction (less than 1.5 volts) of the total P.D. to be measured $\{p, 521\}$; sensitive D'Arsonval or moving coil galvanometer $\{p\}$ $\{p, 569\}$; standard Chark cell E; fairly high resistance rheostat R $\{p, 603\}$. See footnote, p, 20.



F16. 13.

Observations.—(I) After placing the levers of G and E on stude 14 and that of H on stude 1 or 2 for precaution, connect up as in Fig. 12, in which only the row of terminals on the potentiometer P is shown, symbolically, for the sake of brevity.

- (2) Adjust the spot of light of the gulvanemeter to somewhere about zero on the scale, and the resistance ad and cd in the "volt box" so that $cd = \frac{1}{10}$ of ad, supposing, of course, that not more than 150 volts is across ad. Carefully level and adjust V to zero if it requires it.
- (3) "Set the potentiometer" by the standard cell in the way described on p. 514, the contact lever H, Fig. 208, p. 512, being on stude IV, thus inserting E in the circuit of g in such a way as to oppose that of b, close S, and adjust R so as to obtain the full scale deflection on V.

Mote.—This last operation will only be possible when R is comparable with the parallel resistance of ad and V. If both these are very high thou altering R will have very little effect on the reading of V unless R is high also in comparison.

(4) With the positions of the resistances G₁ and G (Fig. 208, p. 512), as found in 3, unaltered, turn the lever of H to stude

III so as to throw into circuit with g the $\frac{1}{10}$ 0th part of the voltmeter P.D., which was across terminals III. Now adjust the liwer of the resistances E, Fig. 208, and the sliding key C, Fig. 208, so that no deflection occurs on pressing this latter.

a.N.B.—If no balance can be obtained owing to there being no reversal of deflection on g, the fractional P.D. across III is assisting instead of opposing (as it should be) the fall of potential due to (b) in the stretched wire. The wires from cd to III must then be interchanged. If the lever at E is on stud 12 (literally 12,000) and the slider C at 625 on the scale, the voltage agrees nd, i. e. at the terminals of V = 126.25 volts. Note these positions on PP, and simultaneously the reading V on the instrument to be calibrated.

- (5) Reduce V by about $\frac{1}{10}$ either by cutting out cells in B or by altering R or both, and repeat 4, noting the new values of V and PP. Turn H to IV for a moment and see whether the balance in obs. 3 still holds, if not re-set as in obs. 3 about 6(5) Repeat A and 5 for some top, or twelve different
- (6) Repeat 4 and 5 for some ten or twelve different readings on V decreasing by about equal amounts to the lowest,
- (7) Repeat 4 to 6 for a similar ascending set of observations, and tabulate your results as follows—

| Name | Dark C. | Dark C. | Dark C. | Temperature | C | S.M. F. Assumed | Nota | Volt Rov: Fraction of total used of a Potentiometer setting E on . . Cat . . . |

Voltmeler	l'otontione	ter Tkadıng.			Better of	
	Stud of E	Position of Hilder G	Fraction ed	Volkmeter Vi = set v.	Voltmeter V ₁ - V ₄	% Krror.

As it may sometimes be the case that a Carhart-Clark and not a Clark's standard cell has to be used, care should be taken that the E.M.F. assumed at the particular temperature is correct, the temperature coefficient of E.M.F. being very different in the two cases (vide pp. 17 and 643).

(8) Plot a calibration curve for the voltmeter tested having values of V as ordinates and true volts V₁ as abscisse.

Inferences.—What can you infer from the results of your test!

Are there any sources of error which might vitiate the results?

(12) Calibration of a High Tension Alternating Current Voltmeter.

Introduction.—In the ordinary high tension systems of distribution of electrical energy by alternating currents, the average working pressures are about 2000 or 2500 volts. The "electromagnetic" and "hot wire" types of voltmaters are unsuitable for measuring such high pressures, which can best be dealt with by means of a third class of instrument known as the electrostatic voltmeter, a description of two forms of which will be found in the Appendix (p. 562).

These instruments are almost universally employed for measuring alternating current pressure, and they have the all-important advantage of being unaffected by variation of frequency. Owing usually to the difficulty experienced in obtaining direct current pressures of the above magnitude for testing purposes, alternating currents have nearly always to be employed for calibrating high tension voltmeters. Thus it will be seen that none of the preceding methods are available in the present case, but the calibration can be effected by what may be termed the "fractional potential difference" method, using an accurately calibrated low tension electrostatic voltmeter for comparison in the manner to be described later.

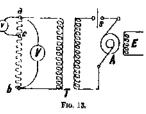
This low tension voltmeter, which may conveniently be one of Lord Kelvin's multi-collular electrostatic instruments reading to, say, 150 volts, should be very carefully calibrated by one of the preceding methods—preferably the potentiometer, one using a Clark's call as a standard of E.M.F. and direct current pressures of course. For accurate work, however, the following remarks should be observed. In these voltmeters the movable needle system is usually aluminium and the fixed system brass, whence owing to aluminium being electro-positive to brass, the instrument will read from 0.2 volt to 0.3 volt too lew when the + pole of the direct current source is connected to needle, and the same amount too high if the — is joined to the needle system instead. In ealibrating this low reading voltmeter by the potentiometer, it should be connected up through a reversing key to the rest of the apparatus and the mean of the readings, before

and after reversing the polarity on its terminals, taken as the correct one for alternating currents, since when used with such the above-named error does not occur. Again with direct currents an electrostatic voltmeter passes no current, but owing to it passessing a perfectly definite though very small capacity, it will behave like a condensor with alternating currents, i.e. a pulsating or "charge and discharge" current will be set up in its circuit. Thus it will be seen that if, as in the present method, such an instrument is shunted across part of a circuit carrying an alternating current, the current in the voltmeter branch may be quite comparable with that in the main circuit, in other words the P.D. between the points to which it is shunted would be lowered somewhat by the voltmeter, and ... would not bear to the whole P.D. the ratio of the resistance of the two portions of the circuit. To avoid such an error the resistance of the main circuit should be such that the maximum pressure to be used sends a sensible current such as from 1 to 1 an ampere through it, which will consequently be very large compared with the current in the voltmeter branch. Thus the presence of this latter will not affect the value of the P.D. between the two points to which it is applied, and consequently the ratio of the whole P.D. to the fraction thus tapped will equal the ratio of the whole resistance to the fraction across which the electrostatic voltmeter is placed.

Apparatus.—Alternator A, capable of supplying a low pressure,

and of being driven at any required speed by a direct current, electromotor (preferably), or other prime mover, its exciting circuit E consisting of the field coils of A (shown), together with switch, rheestat,

ammeter and source of



excitation (not shown), but which can be varied so as to vary the E.M.F. of A; step-up transformer T capable of increasing the pressure from that of A to the maximum required for a full scale reading on the high tension voltmeter V to be calibrated;

low tension electrostatic voltmeter (r) (p. 562), reading to say 150 volts, and which has been proviously carefully calibrated by reference to a standard Clurk cell on the potentiometer; switch s. A divided non-inductive high resistance (acb) capable of standing the highest pressure to be used on V, and of carrying an appreciable current, say of the order of $\frac{1}{4}$ to $\frac{1}{2}$ an ampere continuously without excessive heating.

Caution.—Under no circumstances whatever is any part of the high tension circuit to be touched while "alive," and the indiarubber gloves are to be worn throughout the test by the operator reading the electrostatic voltmeters.

Observations.—(1) Connect up as in Fig. 13, and carefully level and adjust the pointers of V and v to zero. For the high tension side use well-insulated wires for the connections, and keep them in mid-air as much as possible.

- (3) If the voltmeter V to be calibrated reads up to, say, 2500 volts, and r to only 150 volts, place this latter across a convenient fraction (a c), say ¹/₁₀th of the whole non-inductive resistance (a b), which in this case may conveniently be something like 5000 Ohms.
- (3) Start the alternator A, close s, and then adjust the speed and excitation so as to obtain the lowest scale reading on V. Note simultaneously that on (r) also.
- (4) Repeat 3 for ton or twolve different voltages on V, rising by about equal increments to the maximum, and tabulate as follows—

Nave	DATE		
H.T. Voltantier tested: No Whole resistance Reference Ohms,	Type Fraction used a	Ronge.,, tag≃.,, Chine.	Ratio Rob =

ν.	V. Currected P1		Time voltage Via Em 71	% Birot of mater tested $100 (Y-Y_1)$.	Mohn Error,	
L	·					

⁽⁵⁾ Plot a calibration curve for the high tension voltmeter having values of V as ordinates and true volts V₁ as abscisse.

Inferences.—Enumerate what you consider to be the advantages and disadvantages of electrostatic voltmeters.

(13) Complete Test of both Direct and Alternating Current Ammeters and Voltmeters for the various sources of Errors.

Introduction.—The principle involved in the action of any type of ammeter or voltmeter will come under one of the following heads—

- (1) Heating effect of the current or P.D. to be measured.
- (2) Electrostatic effect of attraction or repulsion between fixed and movable conducting surfaces, close to, but insulated from one another, when electrified to opposite potentials.
- (3) Electro-magnetic effect of the current in a coil of wire on iron or vice versit.
- (4) Electro-dynamic action of the current in one part of circuit, on the same current in another part of that circuit, causing electro-dynamic attraction or repulsion between the two.

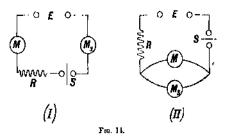
There are briefly eight principal sources of error to which ammeters and voltmeters in general are liable, namely—

- (a) Error in the calibration owing to the standards employed in the two cases being different,
- (b) Error through a partial demagnetization of the permanent field, causing an alteration in the sensibility, in the case of permanent steel magnet instruments.
- (c) Error caused by the sensibility of the instrument being temporarily altered by external magnetic influence.
- (d) Error due to a current producing a different deflection depending on the magnitude of the current previously measured compared with the one in use at the time.
- (a) Error due to the instrument giving a different scale reading for different directions of the same current.
- (f) Error in the case of voltmeters due to alteration of the resistance of the instrument caused by change of temperature, whether from the room or passage of the current.
- (g) Error in alternating current instrument due to alteration of frequency.
 - (A) Error due to friction at the pivots in all classes.

Error (a) applies to all four classes of instruments, and cannot very well be remedied except by re-calibration.

It is clear that classes 1 and 2, being entirely non-magnetic,

may be dismissed as not being liable to magnetic errors. Class 3, however, and 4, which latter type may or may not contain iron, are liable to large errors arising in the case of direct currents from the retentivity of the iron used (error d), or magnetic hysteresis, and from the proximity of, and the external magnetic effect of currents in neighbouring wires and of magnets (error c). In the case of alternating currents from hysteresis, eddy currents in the metal work about the instrument reacting on the coil, and change of frequency (error g) in the alternating currents.



In this latter class of work the instruments should contain no iron at all, and very few metal fittings. In good direct current instruments where iron is a necessity, it should be very soft, and well laminated, and there should not be much of it.

Apparatus.—Animoter or voltmeter M to be tested; suitable variable risestat R, which in the case of the ammeter test must be capable of carrying the maximum current required by M, and in the case of the voltmeter test must have a large resistance so as to be quite comparable with that of M; switch, or key S; source of electrical supply E, whether direct, or alternating current; standard accurately calibrated ammeter or voltmeter M_t which must not contain any iron, and preferably no metal fixings.

N.B.—The standard M_s may be either a Kelvin standard balance (p. 546); Siemens electro-dynamoneter (p. 577); Cardew, or electrostatic voltmeter (p. 562), preferably the latter, which not only is non-magnetic, but also has no temperature error. See footnote, p. 20.

Observations. —(1) If an animeter is being tested, connect up as in Fig. 14 (I), but if it is a voltmeter, then as in Fig. 14 (II). Carefully adjust the pointers of M and M_s to zero if they require it, levelling them also when necessary so that all moving parts can move quite freely. Place M and M_s at some distance apart so that there can be no possibility of one affecting the other. Also run the connecting leads close together so that their magnetic effect due to the current in them may not affect the instruments.

(2) Enror due to External Magnetic Effect. (A.)

With R at its maximum, close S, and obtain about 1 Iull scale reading on M. Note the corresponding reading of M_s, which must be kept quite constant and steady when no magnet is near. Now move a powerful permanent magnetin a plane perpendicular to the axis about which the moving system of M escillates and passing through its centre, the axis of the magnet pointing to M always, and its pole nearest to M being movel so as to be always at about 12" say from M. Note the alteration (if any) of the reading of M.

- (3) Repeat 2 for a full scale deflection on M.
- (4) Repeat the last part of 2, pertaining to the motion of the magnet, with no current flowing, i.e. S open, and tabulate your results as shown in the table below.

N.B.—The magnet must not be allowed to affect Ms in any way, and the latter must be far enough away to ensure that this is the case.

If M is an alternating current instrument, and an alternating supply is being used, the frequency must be maintained constant in 2 and 3 above, as well as the reading of M_d in the particular test.

(5) Error due to Retentivity or Risidual Magnetiem. (B.)

With R a maximum, close S, and corefully take a gradually increasing set of about ten simultaneous readings on M and Me from the lowest to full scale, by gradually diminishing R, gently tapping the instruments to eliminate any pivot friction.

(6) Repeat for a similarly obtained decreasing set, the same scale reading of the standard M, being obtained when descending as was obtained on ascending. Tabulate your results as indicated in the following table.

N.B.—This test of course only applies to direct current instruments, and the error in question may amount to over 20%. Standard instrument used; Type... No... Meker... Constante...

Instrument tested: Type... Ro... Maker...

A, External !	degree!	liana.	B. Retentivity or Residual Magnetiam.				
	Reading on		Reading on				Programmer
Position of influencing magnet.	Цe	R.	Me seconding and descending.	of uscending.	descending.	Error.	(constant) It alternating current need.

(7) Error due to variation of "frequency" with Alternating Current instruments. (C.)

Close S, and adjust R to give some convenient scale deflection on M and M_S , which latter must be kept constant by means of R. Now vary the frequency, by altering the speed of the alternator if this is under control, from the smallest to the greatest possible so as to obtain about ten different values, and note the simultaneous readings on M and M_S at each.

(8) ERROR DUE TO EDDY CURRENTS IX METAL FIXINGS WITH ALTERNATING CURRENTS. (D.)

If either M or M₅ possesses a moving coil, the terminals of which can be got at to send a current through this coil only of the instrument, as in either a Kelvin belance, Siemens dynamometer, or Parr direct reading dynamometer instruments. Proceed as follows—Adjust the pointer of this instrument carefully to zero, and send the maximum alternating current through this moving coil alone, noting whether it deflects. If it does, eddy curronts are being set up in the metal fixings and re-act on the moving coil causing it to deflect.

(9) Repeat 8 for the same current at different frequencies, and tabulate your results as in the following table—

Ko. . . .

Haker . . .

Standard Instrument used : Type

Instrument tosted:

C. Rifert of Frequency.			D. Eddy Carrents.			
Рицинсу	Head	ויס אַטּוּ	Frequency us per sec.	Reading on		
to lest non-	Ma.	,M,		Mr.	ж.	

(10) ERROR DUE TO REVERSAL OF CORREST THROUGH THE INSTRUMENT. (E.)

Connect up as shown in Fig. 14, but instead of connecting M directly in series as shown, join it up now to the circuit through a reversing switch or key, so that the current through it may be reversed in direction through that in the rest of the circuit and therefore through Mr is still unidirectional.

With R large, close S_i and obtain say $\frac{1}{2}$ full scale deflection on M_i noting that on M_i which must be constant; now reverse correct in M and again note its value for the same one as before on M_i . Next re-reverse and note it again.

(11) Repeat this operation for about 5 scale readings on M up to the maximum at roughly equal intervals.

N.B.—This test of course only applies to direct current instruments. Tabulate as follows—

Mandard instrument used: Type..., No..., Maker..., Constant = ...
Instrument lasted: Type..., No..., Maker...

is, lette	et of Cans at Reseastl.	F, Brut ng Rifert.			
	Realing of		Reading on		
Afe (constant).	A direction of current. Hoversed Reserves ed.	Time of Districting Money	Ns.	Ж	
		;	[

(12) Error in Voltmeters (only) due to Heating of Colls by passage of Current. (P.)

Close S, and adjust R to obtain about $\frac{1}{2}$ scale reading on M_2 , note the corresponding reading on M_2 which must be an electrostatic voltactor. Maintain M_3 constant for, say, quarter of an hour and again read M_2 .

(13) Repeat 12 for a full scale reading on M, and tabulate as before.

N.B.—The error in voltmeters due to change in the temperature of the room is readily calculable when the latter is obtained by a thermometer.

- (14) Plot the following curves for tests-
- B. Having readings on M as ordinates, and M, as abscisses for both ascending and descending curves.
- C. Having realings on M as ordinates and frequency in w per sec, as abscisse.
- D. Having readings on M as ordinates and frequency in \wp per sec. as abscissor.

Inferences. - State very clearly and concisely what you can infer from the results of your observations.

(14) Calibration of a Wattmeter by Comparison with a Kelvin Composite Balance used as a Wattmeter.

Introduction.- The following is a convenient method of calibrating a Wattmeter by means of direct currents, using a Kelvin composite balance as the standard Wattmeter with which to compare the one to be tested. The construction of the balance is detailed on p. 554, where the mode of using it as a Wattmeter is also given, and it will merely suffice to say here that it is used very similarly to the Hekto-ampere meter, the only difference being that as a Wattmeter, the fine wire movable coils (only) are placed in series with an extra antiinductive resistance across the mains supplying the power measured by both Wattmeters. It may here be noted that it is not necessary for the current through the thick winding and the pressure across the thin coils to be developed by one and the same source. For since the Wattmeter deflection is at to the products of the currents flowing through the two coils. clearly these may come from two totally different sources. In fact it is distinctly preferable to have them separate when possible, for then the variations of the main current will not affect the constancy of the pressure on the fine coils.

This same test serves to determine the "constant" (K_W say) of the Wattmeter, or in other words the number by which the scale reading must be multiplied so as to obtain the power in Walts.

The following reasoning will no doubt render this clearer.

Assuming the general principle and construction of, suppose, a Siemens Wattmeter to be understood. Let C and a = the currents flowing through the fixed thick- and movable thin-wire coils respectively when a deflection of the tersion head and its pointer on the scale is D^* or divisions. Then the force acting between the coils is ∞ $C \times c$, but $(c) \infty$ to the pressure V at the terminals. Hence the deflecting couple acting between the coils ∞ $C \times V$ ∞ Watts. Now when the index is brought back to 0 again by turning the tersion head, thereby twisting up the spring and introducing the control, we have—tersion of spring ∞ Watts ∞ CV; but the force of tersion is ∞ to angle of tersion of such a spring.

 $\therefore D \propto CY$

or KD = CV =Watts measured and causing a deflection D, where K is the "ronstant" of the Wattmeter tested. It may be found that K is not perfectly constant throughout the whole scale. In this case the Watts should be obtained from a calibration curve rather than by the product KD.

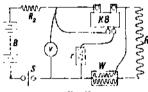


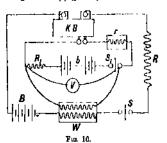
Fig. 15,

Apparatus.—Kelvin composite balance (K.R.) (p. 564), with its anti-inductive resistance r (p. 553); switch S; variable power-absorbing resistance R (p. 686); accurate voltmeter V (preferably electrostatic); main current battery R; Wattmeter (W) to be calibrated; [pressure battery δ and adjustable resistance R_1 if available (Fig. 16)]; adjusting rheostat R_2 (p. 597).

Observations.—(1) Connect up either as in Fig. 15 or 16, and in the present test assume the latter for actual experiment, and make quite certain that the connections are as indicated in Fig. 16, (2) Carefully level the instruments that require it, adjusting their pointers to zero, and if W has a suspended coil see that this

their pointers to zero, and if IV has a suspended coil see that this is quite free to move.

- Note.—Care should be taken to run the "leading in" and "out" wires earrying the main current to W and in the rest of the circuit close together or twisted in order that the carrents flowing in them shall exert no magnetic influence on the instruments.
- (3) Turn the switch on the balance to "Watts" so as to place the movable fine wire coils across the small terminals. Observe whether (r) is numbered the same as, and therefore belongs to the balance in use, and make quite certain that the correct resistance is being used in (r) (p. 5¹.3).



(4) Adjust the balance and its sensibility by using the proper weights as given in the table of constants (p. 558), so that the maximum Watts to be measured on W would give, as nearly as possible, a full scale reading on K.B.

- (5) With R_1 fairly large, class S_1 and adjust the voltage as read off on V to the desired amount by altering R_1 , and then maintain this voltage constant, observing that it is so before
- taking every reading.

 (6) R being fairly large, close S, and after R so as to obtain about γ_{S}^{*} th of the maximum scale reading on W. Note simultaneously the reading on W and position (d) of the slider of $K.B_{*}$
- (7) Repeat 6 for some ten different deflections on B (by varying R) rising by about equal increments to the maximum, the pressure remaining constant all the time.
- (8) Repeat obs. 7 for a similar set of decreasing readings on W, and tabulate your results as follows—

Nava O mj osite Balance Waltmeler terted	No		riants e+e4 &			inra*O
filter Tr Rowling Wa	ile An	Readin	g on IP. Descending	1	% Kerror of	

(9) Plot a "calibration" curve for the Wattmeter tested having values of D as ordinates and true Watts as abscisse.

Inferences.—What can be inferred from the results of your test! Are Wattmeters subject to any sources of orror, and if so, how can they be minimized or get rid of 1

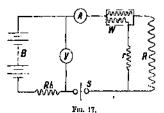
(15) Calibration of a Wattmeter by Comparison with a Standard Ammeter and Voltmeter.

Introduction.—The following method of calibration by direct currents entails the use of an accurately calibrated standard ammeter and standard voltaneter. These may be either Kelvin balances or ordinary instruments which have recently been carefully compared with accurate standards, and a record of the calibration curves of which are obtainable.

It should be remembered that the constant of a Wattmeter obtained with direct currents will only be true for alternating currents providing the solf-induction of the fine wire moving coil or its circuit is practically zero or very marly so. In other words, the instrument must contain no iron and also be very nearly "non-inductive." This is a matter of great importance, for Wattmeters are in most cases only required to measure power in alternating current circuits.

Apparatus.—Standard ammeter (A) and volunctor (V); Wattmoter (W) to be calibrated with its anti-inductive resistance
(r) if there is one; battery of secondary cells B; switch S;
suitable resistance R for absorbing power (p. 606), which must
be non-inductive if alternating currents are employed; carbon
rheestat (RA) (p. 597).

Observations.—(1) Connect up as shown. Carofully level all the instruments, adjusting their pointers to zero, and see that the swing coil of the Wattmeter is quite free to move. Care should be taken to run the "leading in" and "out" wires carrying the main current to the Wattmeter, close together of



twisted. Also the main wires of the rest of the circuit close together in order that the current flowing in them shall exert' magnetic influence on any of the instruments.

- (2) R being at its maximum value, close S, and adjust R so as to obtain about 1,6th of the full had current through W, the pressure being maintained at standard voltage by varying the carbon rhoostat (Rh). Note the readings of all the instruments.
- (3) Repeat 2 for about ten different readings on W rising by about equal increments to the maximum current allowable, and calculate for each the percentage error of the Wattmeter and the mean. Tabulate as follows—

	SAME .				DATE	
Non-Inductiv	e Wallincler	: No	Maker	'	Temperature	= • C.
_ 		·				
Trun Volts. P.	Ting Anys A.	Trun Walte IV= A.V.	Wattmeler Reading. D.	Willingster Constant. Kr D	Percentage Error of Wattaurier	Menu Yaror.
		i · · · · · · · · · · · · · · · · · · ·	·			

(4) Plot a curve having values of (W) as abscisse and the corresponding Wattmeter readings (D) as ordinates.

(16) Calibration of a Wattmeter with Alternating Currents, (Three-Voltmeter Method.)

Introduction .-- Wattmeters form a class of measuring instrument the chief application of which consists in measuring

accurately the power taken up in alternating current circuita. The ereat value of a Wattmeter in such measurements practically disappears with direct currents as the individual factors of power, namely "volts" and "amperes," are usually here required, and in addition the product of the two can easily be obtained and at once gives the "true power." With alternating currents, however, this last remark is not true, and herein lies the great value of the properly constructed Wattmeter, in that it measures the true power in such a circuit. For it to be capable of doing this, however, it must be carefully constructed, and there must be no iron and preferably no other metal work near the coils. Wattmeters when used on alternating current circuits are liable to the following sources of error: (a) owing to the fine wire coil possessing some self-induction and consequently impedence, "the current in it is not able to rise to the same maximum strength which it would do for a direct P.D. of similar magnitude; (b) this impolence causes a lag in phase of the current in the fine wire coil behind the P.D. across which it is placed.

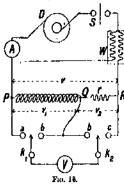
(c) A third source of error common also to all voltmeters, and occurring both with direct and alternating currents, is that due to the alteration of the resistance of the fine wire coil due to change of temperature, and which can be minimized in the manner described later on. From the preceding remarks it will therefore be evident that when a so-called "Non-inductive Wattmeter" is calibrated with direct currents (which is usually the case) its "constant" so obtained will not be correct for alternating currents. The instrument will also read differently for variation of the "frequency" of the current even though the actual power being measured remains the same. Thus a Wattmoter, may with advantage be calibrated with alternating corrents on a circuit having the same "constants," namely voltage, frequency and "wave form," etc., as that in which it is eventually desired to measure the power. The calibration can be performed by what is commonly known as the 3-voltmeter a method of measuring power in alternating current inductive circuits, and by it the "true power" may be obtained with almost any degree of accuracy desired by using an accurately calibrated voltmeter and by repeating the observation two or three times, noting the mean. It has the advantage that only

one alternating current voltmeter is required, though three similar ones may be used if available.

nilar ones may be used if available.

Apparatus.—Alternator D and its exciting circuit (not shown)

under rheostatic control or



other convenient sturce of alternating current supply; inductive portion PQ of the circuit in series with a strictly non-inductive portion QR; two 2-way koys k₁, k₂ (p. 587); Cardew or low-reading electrostatic voltmeter V accurately calibrated; main switch S; Wattmeter W to be calibrated; alternating current ammeter to indicate the current merely

for reference only.

Note.—The resistances of PQ and QR should both be

fairly small compared with that of the voltmeter V.

Observations.—(1) Connect up as in Fig. 18, and adjust the pointers of all the instruments to zero, levelling such as need it.

See that all lubricators in use feed properly, and then start D. (2) Adjust the speed of D so as to obtain the desired "frequency," say 100 - per see, at the same time varying the excitation to get the proper voltage, suppose 100 volts across PR. Adjust the resistance of PR so as to pass about γ_{c}^{1} th of the full load current (necessary to give a full scale reading on W) through W. Then the speed and voltage being constant, note the reading on A, W, and in quick succession the voltages Y_1 , Y_2 and Y_3 across PR, PQ, and QR respectively by moving k_1 and k_2 simultages.

- (3) Repeat 2 for about ten different currents rising by about equal increments to the maximum allowable.
 - (4) Calculate the power absorbed in PR from the relation

$$W_1 = \frac{1}{2s} (V^2 - V_1^2 + V_2^2)$$
 Watts,

where r is the ohmic resistance of QR.

taneously.

If r is unknown or liable to be altered by the heating effect

of the current, its value $r = \frac{V_2}{A}$ may be substituted in the above relation. If the current and voltage are sine functions, $\cos \theta = \frac{V^2 - V_1^{3} - V_2^{3}}{2V_1V_2}$.

(5) Repeat 2—4 for a different frequency, say 60 per sec., to see whether the Wattmeter "constant" (K) alters, and tabulate your results as follows—

NAME		D _A :	
Wattincler leaded : No	Maker	Range	Temperature
Byadd guency Factor of or F2/A	Correct Volts, in Auge.	Power. W Apparent/True Read AV. W1 d	fattineter. Eaver. ing Constant $K = W_1/d$

Note.—Errors made in measuring the voltages V, V_1 and V_2 or in the graduation of the voltmeter scale will have least effect on the results when $V_1 = V_2$. If the formula in 4 is used with the substituted value of (r), this latter may consist of glow lamps, as the resistance may vary with the different mean current strengths.

(6) Plot a calibration curve for the Wattmeter tested, having values of deflection d as ordinates and true power W, as abscisses.

Inference.—Prove the formula given in 4 and state any assumption made in obtaining it. What inferences can you draw from the results of your test? and explain why the resistance of the voltmeter V should be large compared with either PQ or QR.

(17) Calibration of a High Tension Wattmeter. (By Ohm's Law, using an auxiliary transformer.)

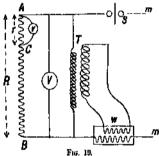
Introduction.—It is not always possible in actual practice and testing work to avoid the use of a Wattmeter on a high tension circuit, as for instance would be the case in measuring the efficiency of a high tension transformer run off the terminals of a high tension alternator. The Wattmeter in such a case should be a specially arranged one for the following reasons—

- (1) Owing to the high pressure in the fine wire moving coil circuit, an extremely high non-inductive resistance, capable of standing the full pressure across its terminals, would otherwise have to be put in series with the fine wire swing coil if an ordinary Wattmeter was employed.
 - (2) Owing to the difficulty in obtaining the above resistance.
- (3) The risk entailed in handling such an instrument, and of the breakdown of the insulation of the whole arrangement under the high pressure.

The best arrangement of a high tension Wattmeter, and which gets over these difficulties, is that shown symbolically in Fig. 19, together with the connections for its calibration.

together with the connections for its calibration.

The Wattmeter IV consists of an ordinary Siemons electro-



dynamometer; the mercury cups, forming the terminals of the swing coil, are connected to a separate pair of terminuls by the side of the other pair forming those of the fixed ceil. There is thus no electrical connection between the fixed and moving coils. These latter are connected to the low pressure

coil of a small auxiliary transformer T. The high tension side of T is placed across the high pressure mains (m.m.), hence the moving coil of W passes a current which depends on the E.M.F. of m.m., and at the same time there is no fear from a breakdown of insulation since both coils of W are passing ordinary currents. The actual current which T sends through the swing coil of W may be as small as convenient.

Apparatus.—High tension Wattmeter W to be calibrated arranged as mentioned above, with its fixed and movable coils separate. Small auxiliary (H.T.) transformer T; high and low tension electrostatic voltmeters V and v respectively; strictly non-inductive resistance ACB capable of being placed

across the (H.T.) mains m.m., and of carrying enough current at that pressure to enable a considerable scale deflection to be obtained on W. A part AC of the whole resistance AB should have such a value (r) and be of such a carrying capacity as not to be heated and changed by the current through ACB and as will have a P.D. across its terminals capable of being read on r.

Note.—As a precaution, india-rubber gloves must be worn, and an india-rubber mat provided to stand on.

Observation.—(1) Connect up as in Fig. 19, and adjust the instruments carefully to zero.

(2) Close switch (S) and adjust V to read the desired amount which W has to deal with on future occasions. Note the readings of V, V, and W, and tabulate as follows—

Naug			DATE			
Waltmeler tested : No	. M	mker	Range	Temperature		
Non-Inductive Resistances R. r.	Voltages	Current through ACH	True mean Waite in ACS Wile VA	Bending on Constant of Wattmeter d _w Widge = F		

Inferences.—Is the method liable to any sources of error 1 and if so, state them,

(18) Calibration of an Electricity Meter (on Constant Supply).

Introduction.—An electricity meter, which performs the same kind of office to a consumer of electrical energy that a gas-meter does to one using ordinary gas, is an electrical instrument that requires carefully calibrating or standardizing at some time or another. There are a great number of different forms of electricity meters, but they all come under one or other of four main classes, namely—Electrolytic, Thermal, Moton, Clocks affected. It is not, however, our intention to dilate on these further as their theory and description comes under the scope of the ordinary textbook, but there are some points in general which may be remarked. Practically all meters measure one or other of two things, namely,

across the (H.T.) mains m.m., and of carrying enough current at that pressure to enable a considerable scale deflection to be obtained on W. A part AC of the whole resistance AB should have such a value $\langle r \rangle$ and be of such a carrying capacity as not to be heated and changed by the current through ACB and as will have a P.D. across its terminals capable of being read on F.

Mote.—As a precaution, india-rubber gloves must be worn, and an india-rubber mat provided to stand on.

Observation.—(1) Connect up as in Fig. 19, and adjust the instruments carefully to zero.

(2) Close switch (S) and adjust V to read the desired amount which W has to deal with on future occasions. Note the readings of V, v, and W, and tabulate as follows—

NAME		DAT	9
Waitmeter tested : No. , .	. Maker	Range	Temperature
Non-Inductive Resistances	Voltages Current through ACR	Trne mean Walts in ACB Wa	ading on Constant of timeter Waltmeter

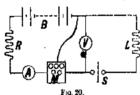
Inferences.—Is the method liable to any sources of error? and if so, state them.

(18) Calibration of an Electricity Meter (on Constant Supply).

Introduction.—An electricity meter, which performs the same kind of office to a consumer of electrical energy that a gas-meter does to one using ordinary gas, is an electrical instrument that requires carefully calibrating or standardizing at some time or another. There are a great number of different forms of electricity meters, but they all come under one or other of four main classes, anamely—Electrolytic, Thermal, Motol, Clocks affected, is not, however, our intention to dilate on these further as their theory and description comes under the scope of the ordinary textbook, but there are some points in general which may be remarked. Practically all meters measure one or other of two things, namely,

(a) Ampere-hours, when they are called quantity- or Coulomb-meters, (b) Watt-hours, when they are termed Energy- or Joulémeters. In most cases, though by no means all, meters are graduated and read directly in the official "Board of Trade Unit" (1000 Watt-hours). It must not, however, be supposed that because a motar reads Board of Trade units on its dials it is a true energy meter in the real sense of the word, i.e. a meter containing a current and pressure coil acting on one another in a suitable manner, for if the pressure is pre-assumed and taken as being constant it is an easy matter to graduate and calibrate the dials of a Coulomb meter to read directly in B.O.T. units. This it may be remarked is generally done now.

Apparatus.—Accumutely calibrated ammeter A, and voltmeter V secondary battery B, or steady source of supply; switch S_1 power absorbing resistance L, or



bank of lamps (p. 598); rheostat R (p. 597), which might be required for adjusting the pressure on the mains; meter M to be tosted. When possible, it is best and mestoconomical in power used, to employ two

distinct circuits, one giving the necessary voltage for the fin wire coil of M, if there is one, the other the necessary curren through the current circuit of M. These two sources must be secondary batteries if possible so as to be quite constant.

Note.—If the meter to be tested is an alternating current one then A and V should be alternating current instruments, such a a Siemens electro-dynamometer and electrostatic voltmeter respectively, or the author's instruments. R also should be non inductive, and L may preferably consist of a bank of lamps (p. 598 or other non-inductive resistance. If an accurately calibrated age inductive Wattmeter is available, then the true power given to a can at once be obtained irrespective of the nature of R and L and also without using A. In such cases the meter should be tested at different frequencies and on inductive loads.

Observations.—(1) Fix up the meter in a position as nearly vertical as possible and connect it in circuit so as to register the quantity (amp.-hours) or energy (Watt-hours) as the case may be, given to L.

- •(2) If the meter is intended for use on 100 or 200 volt circuits, close S and vary L so as to absorb the full load current of the meter, and adjust R so that V reads the required voltage.
 - (3) Open S and take the dial readings of the meter.
- (4) At a known tabulated instant, switch on, and keep the current (A) and pressure (V) constant for about ½ hour by altering R and L if necessary. Then switch off at a noted instant and take the dial readings again.
- (5) Repeat 2, 3, and 4 for $\frac{3}{4}$, $\frac{1}{4}$, and $\frac{1}{16}$ full load currents through the meter, and tabulate as follows—

•	NAME Mutor togel: T_{11}	. Vol	Makez tago (11 mi)			DATE No al reading in	
	Noter rewing	Amorast Registered Q-Q_1.	Anjw	Volts V.	Time T (Home)	or Watt- hours, Moter.	,

Inferences,—State the chief conditions which a meter of the above type should fulfil,

(19) Complete Test of an Electricity Meter.

Introduction.—In order to completely test an electricity meter in the way that would be advisable with any new type of instrument, three or four additional tests other than the preceding one should be carried out and are as follows:—.

- (a) Starting power of the Meter. Obtained by carefully measuring the least current or Watts that will just cause the meter to start. It is obvious that such should not exceed the amount used up in the smallest lamp employed.
- (b) Effect of external Magnetism.—Which can be investigated by sending a steady current or number of Watts through the meter according to what it measures, and then bringing a strong magnet into a number of different positions about the outside of the meter. The record of the instrument taken over a sufficient

period for each position of the external magnet should remain unaltered.

- (o) Power absorbed in the Shunt-coil.—Some meters possess a fine shunt coil of considerable resistance for the purpose of providing the instrument with a sufficient magnetic field townable it to start with a very small current. The amount of power absorbed in this coil, if there is one, should be currefully measured and the cost of it per annum calculated on the basis of say 3d. to 4d. per B.T.U. if the supplier pays for it as he should. It should also be observed whether this coil is across the lamp or supply side of the meter in order to see if the consumer or supplier pays for the power so wasted, for in the aggregate the cost of this may amount to a considerable sum in the course of the year.
- (d) Gradual deterioration of working parts.—This is most important, but can only be determined by a "time test" extending over a considerable period amounting to months.

Thus to furnish a true and accurate report on an electricity meter, investigations (a-d) should be undertaken, and in addition the test immediately preceding them.

(20) Measurement of a Resistance heated by an Electric Current.

Introduction.—When a resistance is heated by the passage of a current its value so heated may or may not be very different from that when it is cold. Thus, for example, a resistance composed of the alloys Manganin or Eureka, etc., would alter its resistance very little for considerable changes of temperature; whereas if made of carbon, the specific resistance of which diminishes rapidly as the temperature rises, the resistance would be very different when hot to what it would be while cold. In practice, however, one of two conditions may occur in connection with heated resistances, namely, (1) The type and form may be such that the temperature does not fall very quickly immediately the current is cut off, thus enabling time measurements of resistance to be taken with, say, a Wheatestone Bridge or other suitable means, and the resistance hot, at the moment of breaking the current, to be obtained graphically by plotting the results; owing,

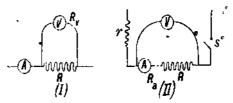
however, to the difficulty of taking rapid time measurements of resistance and the introduction of other errors we shall not consider this method further. (2) The type of resistance may be such that the temperature falls very rapidly and far too quickly to enable any measurements, as in I above, to be taken. Such is the case with the filament of an electric incandescent lamp, and in order to obtain its resistance (warm), accurately, during the passage of a current, and which is absolutely necessary, another method has to be employed other than that of the Wheatstone Pariller etc.

Though the results of the present test will disclose the fact, it may be mentioned here that the filament resistance of an electric glow-lamp when burning normally is very different from that when cold. Thus this latter, which can best be obtained by the Wheatstone Bridge, would not in any way represent the true resistance while the filament is under working conditions.

We will assume that the resistance in question is of the nature of an electric glow-lamp and therefore cools far too rapidly to allow of the employment of the first method mentioned. For a concrete case suppose that the resistance of the filament of an electric incandescent lump is required at different luminosities, i. c. when different currents are passing through it. This resistance will diminish as the current increases, or as the temperature increases, owing to the specific resistance of carbon diminishing as the temperature rises. This property of carbon, in having a negative coefficient of variation of resistance with temperature, should be remembered as compared to the same property of all the metals and nearly all the alloys, of which "Mangania" may be cited as an exception in having a negative coefficient. The present method is a direct application of Ohm's Law, and consists in measuring the current through the lamp and the voltage across its terminals. There are, however, some precautions which have to be adopted in order to obtain the true voltage and current, and these we may now point out in connection with the two arrangements possible with this method. In each of the cases I, and II. (V) represents the voltmeter, (A) the ammeter, and R the glowlamp or other resistance to be measured while hot. The rest of the main circuit is omitted for simplicity, but may comprise a

suitable secondary battery and a rheostat for varying the current

through R. In Case I, the voltmeter V is connected directly to the terminals of R, hence the ammeter A will measure the sum of



Pia. 21

the currents through Y and R together. But the method requires the actual current through R only, which is found as follows— Let R_Y = the true resistance of the volumeter in clams.

Then $\frac{V}{R_T}$ = the true current flowing through it in amperes,

whence the actual current through $R=A-\frac{V}{R_F}$ amperes and the

resistance of
$$R$$
 (hot) = $\frac{y}{A - \sqrt{V}}$ ohms,

To see the magnitude of the error caused by neglecting the correction for the voltmeter current, suppose V=100 volts, $R_{P}=10,000$ ohms and A reads 0.61 ampere. Then without correction:

10,000 ohms and A reads 0.61 ampero. Then without correction:

$$R \text{ (hot)} = \frac{V}{A} = \frac{100}{0.61} = 163.93 \text{ ohms, and with correction } R \text{ (hot)}$$

$$\frac{V}{A - \frac{V}{R_F}} = \frac{100}{0.61 - \frac{100}{V_{0.000}^{1.000}}} = \frac{100}{0.60} = 166.66 \text{ olims,}$$

In other words the error made in the resistance, neglecting the correction, = 1.64%. It should, however, be remembered that the average commercial voltmeter has a resistance much less than 10,000 ohms, and hence the above error would be much greater when using such. If $R_r =$ Infinity then no correction is necessary; for, the resistance of R (hot) then $=\frac{V}{A-\frac{V}{R_r}}=\frac{V}{A-\frac{V}{R_r}}$

ohms or the voltmeter passes no current.

Such is the case with any electrostatic instrument such as the Kelvin anulticellular voltmeter, the resistance of which is practically infinite. It is therefore a good one to use for the purpose.

In Case II. the voltmeter is connected across the ammeter and resistance combined, and it will therefore measure the sum of the voltages across R and A. But the actual voltage across R only, is required by the method, and this is obtained as follows—

Let R_{A} = the true resistances of the ammeter in ohms. Then AR_{A} = the true voltage across the ammeter terminals, whence, the actual voltage across $R = V - AR_{A}$ volts and the

registance of R (hot) = $\frac{V - AR_A}{A}$ ohms.

To see the error caused by neglecting the voltage lost in the ammeter. Let V read 100 volts and A read 0.6 ampere, assume $R_A = 0.1$ ohm, which is about the value for an instrument reading such small currents. Then we have

without correction R (hot) = $\frac{V}{A} = \frac{100}{0.6} = 166.66$ ohms.

and with correction
$$R$$
 (hot) = $\frac{V - AR_A}{A} = \frac{100 - 0.06}{6} = \frac{99.94}{6}$
= 166.57**

Or the error made in not allowing for the loss of voltage in A is 0.054%. Thus, although the resistance of V can easily be measured on a Wheatstone Bridge and that of A either by the

bridge or by the "fall of Potential" method (wide p. 84), when these cannot be readily obtained, we see that Case II. will give the best results and the freest of the two from error by neglecting any corrections.

Apparatus.—Accurate ammeter A and voltmeter V; the resistance R or glow-lamp to be measured while hot. The rest of the main circuit, if this is not already set up, comprising secondary battery, rheostatr, switch s, etc. Arrangements should be at hand for measuring the resistance of V and A, viz.—P. O. Bridge, galvanouneter, Leclanché cell and standard known 0.1 olum resistance, etc.

Observations.—(1) Connect up as in Case II. Fig. 21, and adjust the pointers of V and A to zero.

(2) Measure the resistance of the ammeter, volumeter, and

 \sim (2) Measure the resistance of the ammeter, voltmeter, and lamp (cold) by suitable means.

- (3) Take a series of simultaneous readings on A and V for different voltages, rising by intervals of 10% from 0 to within about 5% of the normal, and then by steps of 1% to 5% above normal voltage
- (4) Repeat (3) above, using a motal filament lamp instead of the carbon one, and tabulate thus—

Nature of Ro	estance tentra		Resistance Cold =				
		Aminete Voltanete	•	$R_{I'}$			
Reading on Voltageler.	True Volts (V) seroes Lamp.	Current through Lamp (A) Ampri.	Resolate V = AR q	e (Jwt) Olmer	dı	Z in Ried Wi	rrmae or e of rosist. en hot, e

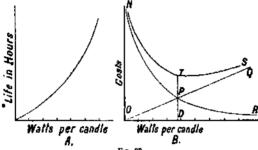
(5) Plot curve for each lamp having values of lamp resistance as ordinates and corresponding currents through it and voltages, across it, both as abscisse.

(21) Measurement of the Efficiency and Candle Power of Electric Glow Lamps.

Introduction.—At the present day, when new forms of electric incandescent lamps are frequently making their appearance before the general public, or otherwise, it becomes of scientific interest and often of practical importance to theroughly test the advantages claimed for these particular forms, and to discover their disadvantages. Amongst others, the chief investigations should be—

- (a) The efficiency at and about the normal or rated voltage, stamped on the lamp by the makers. This is reckened in "Watts per candle" for commercial purposes, though it should more correctly be termed its "in-efficiency." The number of "candles per Watt" more properly denotes the efficiency of a glow lamp as a light-emitting source.
- (β) The candle power (C.P.) at the rated voltage and in a given direction.
- (γ) At what efficiency, the total cost of operating this particular form of lamp, is a minimum.
 These three investigations are of considerable moment to the

These three investigations are of considerable moment to the user of such lamps, and the results practically decide whether his annual expense of electric lighting, using such a form of lamp, would be greater or less than with the present lamps in use. It may probably be the case that it is impossible to do anything with the investigation marked (y), owing to there being insufficient data to hand, the data required being (1) the cost of energy supplied, (2) the cost of lamp, (3) rate of variation of the life with Watts per candle, which is the most difficult item of the



Fra. 22.

three to obtain. For purposes of discussion, however, as this particular question is of considerable interest, we will assume that very carefully-made tests give the relation between the life in hours of the lamp and the efficiency, or Watts per candle used, as shown in curve A, Fig. 22. Then on plotting curves B of the same fig., the cost of lamp renewals per hour will give us the curve NPR, and the cost of onergy per candle-hour will give us the straight line OPQ. Summing the ordinates of the two curves, we get the third curve NTS convex to the abscisse and representing the total cost of the only two sources of expenditure, namely, cost of lamps and cost of energy. If now an ordinate through the lowest point T of this third curve cuts the obscisses in the point D, then DD (in this case 3-8) gives the efficiency, or Watts per candle, at which the total cost of operating this form of lamp is a minimum for the particular electrical supply taken

The two first-named investigations (a and β) are contained in the following relations, which must be determined, viz.—the variation of C.P. with (1) amperes, (2) volts, (3) Watts, (4) efficiency (Watts per candle), (5) resistance of filament, and

. (6) the cost per candle-hour for energy with efficiency.

69

The candle power may be obtained by employing some convenient form of photometer, such as any one of those described on p. 589. We shall, however, here assume the use of Bunson grease-spot photometer, the carriage of which slides along an ordinary straight graduated bank or bench containing the

to be described later, is obtained, also if D = distance between

standard and hamp to be tested, then the C.P. of this lamp is $K = C \, \frac{(D-d)^2}{c!}.$

Now to facilitate working out the results of the tests, a calibration curve for the photometer bench may be drawn from calculations in which values of (d) are abscisse, and the corresponding ones for $\frac{(D-d)^2}{d^2}$ as ordinates. Thus the ordinates of this curve \times by the C.P. of the standard will give directly the C.P. of the lamp to be tested corresponding to the particular distance (d). The values of $\left(\frac{D-d}{d}\right)^2$ for various values of d

when D=2, 3, 4, 5 and 6 metro, are given in the Table, p. 651, and they will be found to save a great deal of time in working out the results of photometric tests in general. Intermediate values not given in the table can best be obtained from the curve plotted between the numbers pertaining to the value of D used in the

test and the values of $\left(\frac{D-d}{d}\right)^2$.

Referring to the above formula for calculating the unknown C.P., we see that any error made in reading the true position of the carriage carrying the "grease spot" or other balancing device will have minimum effect when K = C or d = (D-d), i. e. when this carriage is at the midway position between the two sources of light.

have minimum effect when K = C or d = (D - d), i. e. when this carriage is at the midway position between the two sources of light.

The same kind of thing occurs in the case of measurements of resistance by the "Metre Bridge." To fulfil, however, the relation just mentioned, it will in most cases be necessary to employ a subsidiary or intermediate standard of light, such as a good electric glow lamp, which has itself been very carefully standardized by reference to an ordinary smaller standard.

Canaderable difficulty may sometimes be experienced in balancing on the photometer with the naked eye when different sources of light are being compared owing to the difference in colour of the lights. In such cases it is of advantage to observe the "sight-box" containing the Bunsen grease spot or other arrangement through coloured glass when balancing; that known commercially as "signal red" and "green" being the bost for the purpose, and two pieces should be chosen, so that on looking through the two together in bright daylight next to no light passes through each separately, the mean of the readings will afford a correction to a certain extent for any difference in colour of the two sources of light.

The principal object gained in using coloured glasses is that the eye then observes a less bright surface, and is consequently better able to gauge its illumination relatively to the surrounding surface. It is a fact that when the eye looks at a very bright surface, the pupil of the eye partially contracts, thus causing the effect of temporary partial blindness, hence the use of coloured glass to prevent this.

It should be carefully remembered that if the resistance of the voltmeter, which measures the pressure, is not very high compared with that of the lump (say exceeding 100 times), and the annueter resistance not very low compared with that of the lamp (seldom the case), then corrections must be applied to one or other of these instrument readings, in order to obtain either the true voltage on the lamp or true amps. through it. For such see test on p. 48.

Apparatus.—Low reading ammeter A with long open scale (p.

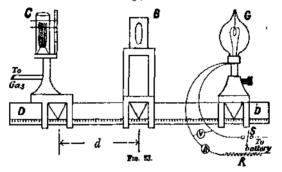
Esparatus.—Low reading ammeter N with long open scale (p. 559); high resistance R (Fig. 272); secondary battery and photometer bench DD complete, containing "Methven screen" 2 C.P. standard (C) of light (p. 595), or Fleming standard glow lump; glow lamp G to be tested; and "sight-box" B containing a Bunsen grease spot (p. 592), or Flicker photometer head; switch S.

N.B.—For particulars on the adjustment and use of the Methven standard, see Appendix, p. 595. The lamp G to be tested may be run as low as will give measurable luminosity, but not higher than 5% above its normal voltage

Observations.—(1) Fix, in a manner most convenient for calculation, the distance D between standard and lamp to be tested (500 cms. say), and adjust the standard to the certified standard value of C.P.

If a standard glow lamp is used instead of C connect it to a constant voltage supply through an exactly similar circuit to that shown for C, but without an animeter (A).

- (2) Connect up the glow lamp as indicated in Fig. 23, and adjust the pointers of V and A to zero, levelling the instruments carefully if necessary.
- (3) Measure the resistance of the lamp filament while cold by means of the Wheatstone Bridge, and note its value.



(4) Close S and adjust R, so as to obtain just measureable luminosity on G, then move the carriage carrying the "grease spot" until the whole surface of the latter appears equally illuminated. Great care being taken to keep the standard of light properly adjusted all through the tests at its certified value.

N.B.—The true scale position will be found more accurately by taking the mean of the two positions of the carriage when the spot is just perceptibly darker and lighter respectively than the surrounding paper, or with a Flicker head when the Flicker disappears.

Note in each case the distance (d) from standard to grease spot when the plane of the lamp filament is (a) parallel, (b) perpendicular to the axis of the bench, coloured glass being used in each case if necessary.

- (5) Repeat 4 in 10% intervals of voltage across the lamp terminals up to within about 5% of the normal voltage for the lamp tested, and afterwards in 1% intervals to the maximum allowable.
- (6) Calculate the C.P. (K) of the lamp at each voltage from the relation

$$K = C \frac{(D-d)^2}{dt}$$

where C=0.P, of the standard and (d)—mean of all the bench readings of the grease spot as found in 4 above. Tabulate all your results as follows—

•	Carrent F.) (.f) (F Augs. Vol) (#/) Witte,	ADCB .	Plane of Filament and axis of Bench. Parallel. Perpendicular Spat just percept bly dark light dark light	Total	CP.	Jiller- eney in Walts Jee candle	Gust per candis- hour for power P	
---	-------------------------------------	------------------	--------	---	-------	-----	---	---	--

- (7) Plot the following curves, to the same pair of axes and same scale for C.P. (K) on the ordinates, between K and (1) amperes, (2) volts, (3) Watts, (4) resistance, (5) distance (d), (6) efficiency, (7) the cost P.
- (8) Calculate the ratio of the resistance "hot" to that "cold" for the lamp filament.

Note.—In calculating the cost P at the various C.P.s, assume that electrical energy costs 6d. per Board of Trade unit (1000 Watt-hours).

Inferences.—State at some length all the inferences which can be drawn from the above experimental results and curves.

(22) Variation of Candle Power with direction around an Electric Incandescent Lamp.

Introduction.—With the introduction of new designs of electric glow lamps at the present day it is of considerable interest and often of importance to see the way in which the magnitude of the C.P. along a fixed or given direction changes as the lamp is turned through various angles in both horizontal and vertical azimuths.

The glow lamp to be tested should be capable of being turned in any direction about a point which is the centre of the principal part of the filament, and, further, this point must be in a line with

part of the filament, and, further, this point must be in a line with the standard of light and centre of the Bunsen greats spot or other "sight-bdx."

If the lamp thus adjusted is supplied at constant voltage and the C.P. measured at different angles in the horizontal plane as

the C.P. measured at different angles in the horizontal plane as the lamp is turned completely through the circle, then the man of all those C.P.s gives what is termed the "mean horizontal C.P." If in addition the C.P. is now measured all round, a vertical circle, the plane of which successively makes different angles with the axis of the photometer bench around a horizontal plane, then the mean of all the results will give what is termed the "mean spherical C.P.," and it will be found that the ratio

mean spherical C.P.
mean horizontal U.P. = K,

a constant which may be determined in the manner to be described presently.

The variation of C.P. around the lamp, as found in the present

test, can best be seen by plotting "polar curves" for the different planes in which the filament is turned, using "polar co-ordinates."

We will now consider briefly the approximate general form and method of plotting such curves.

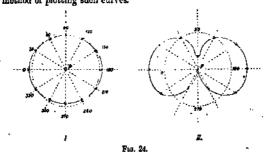


Fig. 24 I. and II. represent polar curves showing the distribution of luminosity in a horizontal and vertical plane respectively.

To obtain I, take any point or pole (P), and with it as centre describé a circle, the radius of which represents to a suitable scale either the normal rated C.P. of the lamp, stamped on it by the makers, or else, the mean horizontal C.P. as determined from the experimental results. Divide the circle (shown dotted) into 12 equal divisions of 30° each all round from 0° to 300, and draw a radial line from P through each, then setting off the C.P.s measured at the respective angles on these radial lines, the continuous curve is obtained on suitably joining them. In Fig. 24 I, the starting-point 0° would be that position of the lamp when the plane of the filament is parallel to the axis of the photometer bench. In II, the datum circle is drawn in the same way as before (and is shown dotted), and on setting off the C.P. measured at the respective angles as the lamp is now turned in a vertical plane, the continuous curve, somewhat of the shape shown, will be obtained. This polar curve II. will only represent the distribution of C.P. in that particular vertical plane which makes some noted angle with the above-mentioned zero on the horizontal plane or circle.

Apparatus.—Precisely the same as that mentioned in the preceding test, with the single exception that the glow lamp is now held in a special form of holder capable of turning through known angles in horizontal and vertical planes,

Observations.—(1) Connect up as indicated in Fig. 23, and adjust the pointers of the instruments V and A to zero, levelling the meters if necessary.

- (2) Fix, in a manner most convenient for calculation, the distance D between standard and lamp to be tested (500 cms. say) and adjust the standard of light used to the proper C.P., either using the gas carburetter or otherwise.
- (3) Close S and adjust R so as to obtain exactly the normal rated voltage across the lamp terminals, which must be kept perfectly constant throughout the whole set of tests.
- (4) Adjust the lamp and its holder so that the principal part of the filament can rotate in a horizontal or vertical plane about some fairly definite point, the line joining which to the standard passes through the grease spot and is parallel to the photometer bench.
 - (5) With the voltage at exactly the normal value and the index

at zero on the horizontal scale for the plane of the filament parallel to the bench, measure the C.P. every 30° on the horizontal scale as the lamp is turned round (vide obs. 4 and 6 of the last test).

- (6) With the index at 0° on the last-named scale measure the C.P. every 30° on the vertical scale as the lamp is turned rough.
- (7) Repeat 6'for the index at 45° and 90° on the horizontal scale, and tabulate all your results as follows—

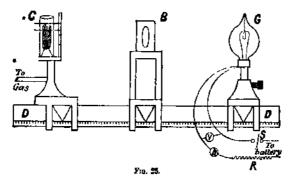
	NAME				Date		
famy ketal Standard of	: Makp . Light. Typ	Cln99.	,, Normal	C P		. Resistan	re Puid . , . D⊶
Horizontal scale tendings.	Vertical realist	de readings (elandal ang	inz dillestatis lea.	Distance d	u.p.	Moan K	Ratio M.S.K. M.H.K.

(8) Plot the polar curves for horizontal and vertical distributions in the manner set forth above. The latter for each of the angles 0°, 45° and 90°.

(23) Measurement of the Percentage Absorption of Light by different kinds of Shades and Lamp Globes.

Introduction.—In electric lighting particularly, and also in other methods of illumination, it is almost invariably the case that the lamp is partly or wholly enclosed in a globe or shade which is partly for use in softening the light, as we may express it, and partly for ornament. In are lighting the epalescent globe is very generally used, while in the case of electric incandescent lighting either the hulbs of the lamps themselves are often made of opalescent, ground, frested, coloured or other translucent forms of glass, or separate shades of such material enclose the ordinary clear glass bulb of the lamp. In all cases the result is a more evenly diffused light and a more uniform illumination, and one that is softer, so to speak, and less trying for the eyes. The introduction of such shades, however, usually diminishes considerably the outside illumination of the source owing to the absorption of light by the shade, but it should be borne in mind

that some of the light which is apparently absorbed is actually lost by reflection. As, in some cases, so much as 70% of the light produced is thus absorbed, it becomes of importance to determine the amount in particular cases, for it will be seen to materially affect the number of lamps really needed to illuminate satisfactorily a room of given area. The present test is arranged with the object of doing this, but no account will be taken of loss of light through reflection, as the measurements of this and absorption separately requires more elaborate methods.



Apparatus.—Low reading ammeter A with long open scale (p. 559); high resistance voltmeter V; adjustable fairly high resistance R (p. 603); secondary battery and photometer bench DD complete, containing "Methyon serven" or other standard (C) of light; "sight-box" B containing a Bunsen grease spot (p. 592); switch S; and an electric glow lamp G (say of S C.P.); shades to be tested.

N.B.—For particulars on the adjustment and use of the Methven screen standard of light, see Appendix, p. 595.

Observations.—(1) Fix, in a manner most convenient for calculation, the distance D between standard and glow lamp (500 oms. say), and adjust the standard to the proper U.P., either using the gas carburettor or otherwise.

(2) Connect up the glow lamp G as indicated in Fig. 25, and

adjust the pointers of V and A to zero if necessary and levelling them if required.

(3) Close S and alter R so as to obtain the normal voltage acress the lamp terminals as read off on V. Then move the carriage , carrying the "grease spot" until the whole surface of the latter appears equally illuminated, great care being taken to keep the standard of light properly adjusted throughout the tests.

N.B.—The true scale position will be found more accurately by taking the mean of the two positions of the carriage when the spot is fust perceptibly darker and lighter, respectively, than the surrounding paper. In this way the mean distance (d) from standard to grease spot should be taken when the plane of the lamp filament is (a) parallel, (b) at 45°, (c) perpendicular to the axis of the bench, and the volts and current noted at each (which must be kept constant).

- (4) Now place a given shade to be tested for absorption over this plain glass bulbed lamp and repeat 3 for this and all other shades in succession, keeping the lamp voltage quite constant.
- (5) Calculate the C.P. (K) of the light with and without shades from the relation

$$K = C \frac{(D-d)^3}{d^2} \text{ candles,}$$

NAME . . .

Glow Lamn : Normal Validate

where C = the candle power of the standard and d = mean of all the bench readings of the grease spot as found in 3 above, and tabulate your results as follows—

DATE . . . Katum of class bulbs:

			Туро	C.P	-,	Total d		e D=
Mature or Mad of Made turied.	Voita Y.	Amps.	Parallel, At 4	and axis of Rench 5°. Perpendicular, perceptably light dask light	Total mem of all post-tions (d).	With out shade	W.U.	*Absorp- flon *y sisule 100 <u>#q - #1</u>)

Inferences.—State carefully all you can infer from the results of your experiments and point out their bearing on the lighting of rooms in general.

The Photometry of Electric Arc Lamps.

General Remarks.-In photometric measurements of the present mature, many little difficulties exist which do not appear in the study of nearly all other sources of light. They arise from the fact that, in the first place, the intensity of the light is extremely fluctuating and very difficult to maintain constant for any appreciable length of time. In the next place, the intensities are usually so large that special standards of light have to be employed, and in addition, the general arrangements of the are light source relatively to the photometer and standard have to be such that only a known fraction of the light to be measured is balanced against the standard. The chief difficulty, ·however, arises from the great difference between the colour of the are light and that from all other common standards of light. So marked is this, both in the case of direct and alternating current area, that frequently the unpractised eye is unable to form anything like an accurate judgment between the amounts of illumination on a given surface due to each. Lastly, the arc is continually travelling round the carbons, thereby causing wide variations in the light emitted along the axis of the photometer bench. This effect on the correct readings of the photometer "sight-box" for given positions can be minimized by taking the mean of several readings of the sight-box on the bench for as nearly as possible the same values of voltage and current supplied to the lamp.

As is well known there are some characteristic differences between continuous (direct) and alternating current ares. In the former, the positive and negative carbons burn away at rates approximately in the proportion of 12:7 respectively, which, however, may vary from 12 to 4, according to the quality and type of carbons and the voltages and current supplied to the arc, the first-named ratio only holding approximately true for ordinary lamps with carbons of equal diameter, and using from 10 to 12 amps. at 46 to 50 volts and run with continuous currents. Peculiar to this type of lamp is the formation of a recess or "cruter," as it is commonly called, at the end of the +" carbon, the -" assuming a conical pointed shape at the end.

For lighting purposes the lamp is always connected up and suspended so that the + re curbon is uppermost, and no second consideration is necessary to at once see that the distribution of light all round the arc (i.e. the spherical distribution) is fur

from being uniform. This determination, together with that of the spherical cundle power (C.P.) for a given amount of power absorbed by the lamp and the regulation of the lamp mechanism, amongst other tests, is the object of the following investigation.

The distribution of intensity requires for its determination somewhat special arrangements for enabling the C.P. to be taken at different angles to the horizon line. This variation is measured in a vertical plane only, and there are several devices for carrying it out. One is to suspend the lamp from the coiling by means of cords and pulleys or a pulley block, so that it can be raised or lowered to different heights above the central axis of the photometer bench; the light is then reflected by a suitably placed plane mirror (making an angle of 45° to the bench) along the axis of the bench to the sight-box; the centre of the mirror forming a right angle between the axis of the bench and the

so erranged that the reflected rays always make an angle of 45° with the axis. The absorption of light or coefficient of reflection by the mirror at this angle is carefully measured and allowed for. Let this co-efficient or percentage of the total light striking the mirror, which is reflected, = K. Then C.P. of reflected beam = $\frac{K}{100} \times \text{C.P.}$ of beam from the arc, and this reflected beam is then measured against the standard. The distance of

direction of the incident beam from the arc. The mirror is

are lamp from photometer sight-box then is reckoned as = distance between lamp and mirror + that between mirror and sight-box. This enables large C.P.s to be compared with comparatively small ones, which would otherwise necessitate a bench many yards long.

STANDARD OF LIGHT,—This should be as large as possible in

magnitude, so as to keep the sight-hox near the centre of the photometer bench, and thus minimize errors in its true position. In addition the colour of the light should approximate to that of the arc. The standard which fulfils these conditions in a fairly satisfactory manner is one consisting of an over-ran glow lamp of,

say, 32 C.P. at normal voltage. If this is over-run some 5-8% in voltage, it will emit a much whiter light and one that is more nearly the colour of the arc. This lamp must be carefully standardized against a known standard of light at two or three definite and accurately noted voltages above normal. Probably 5% over normal will give a C.P. = about 40 or 45, and 7% over normal about 50-60 C.P. At this abnormal voltage the bulb will blacken inside fairly soon, and hence the lamp should not only be kept on for the shortest time, but should frequently be restandardized.

Differences in colour between the two lights to be compared mdy to some extent be corrected by taking the readings of the slider carrying the sight-box when observing the balance of illumination of the latter through red and green glass in succession, the best kinds for the purpose being what are known commercially as "signal-red" and "green," and which should be so chosen that a bright sunlight viewed through the two together appears quite dark. The effect and object in using coloured glass is explained on p. 53.

There are really two kinds of efficiency determinations recessary in connection with are lamps which are automatically self-regulating, namely—

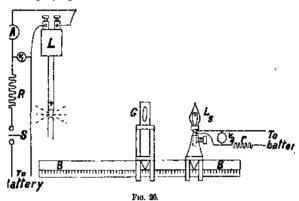
- (a) The "Commercial Efficiency" of the lamp as a whole reckoned in Watts per candle emitted, and which takes into account the total power in Watts absorbed by the lamp, i.a. in the arc and regulating mechanism.
- (b) The "Nett Optical Efficiency," reckened also as above, but taking into account only the power given to the arc itself and neglecting that absorbed in the regulating mechanisms.

The following tests are devised for the purpose of investigating these separately and comparing the results, and also of examining other very important points pertaining to are lamps in general.

(24) Measurement of the Commercial Efficiency of an Arc Lamp.

Introduction.—In the present instance the photometer bench being of considerable length, presumably, the two sources of light are placed one at each end and in a line with the photometer sight-box, which will in future be termed the screen, for brevity sake.

Apparatus.—Photometer bench BB; fitted with a Bunger greas-spot screen (G) (p. 592), placed inside a sight-box to prevent stray light, due to reflection from the walls of the room, falling on the screen, the walls and ceiling being as dull black as possible; standard known source of light (L^s) consisting of an over-run 32 C.P. glow lamp, excefully standardized at a known voltage by a previous test.



A voltmeter $V_{\rm p}$ preferably the same used in the calibration of the glow lamp, together with a rheestat r (p. 603) for reproducing

the voltage of calibration. Arc lamp (L) to be tested, supported on a suitable stand, and placed in circuit with an ammeter A; voltmeter V₁; rhoostat R (p. 606), and switch S. A secondary battery should be available to feed both circuits in preference to a dynamo current, as the former gives a far more steady E.M.F. and better results than the latter.

Observations.—(1) Adjust the arc lamp in its cradle or stand, so that the point of contact of the carbons is at the same height; above the bench as the centre of the screen and standard light.

(2) Fix the distance D between are and standard at some con-

venient amount for future calculations (say 600 cms.), and adjust the arc lamp so that the carbons are vertical.

- (3) Connect up as shown in Fig. 26, and adjust the pointers of A, V_1 and V_1 to zero if necessary. Vary r so as to give L_2 the voltage as read off on V_2 , at which it was standardized last, when it will then give a definite known C.P.
- (4) With R full in, close S, and vary R so that the arc just burns with the carbons in equilibrium. Now quickly adjust the position of the sight-box, so that the grease spot appears equally illuminated all over each side. Note its scale reading (d) from the standard, the volts V_1 , V_2 and the samps, A.

Note.— V_1 must be kept rigorously constant during this and the following observations. The scale reading d can be obtained most accurately by reading it when the grouse spot is just perfeptibly darker and lighter respectively than the surrounding paper. This should be done, using red and green glass in addition to the naked eye, and the mean of all the readings recorded. The reading of V_1 and Λ must be constant during the taking of the above readings.

(5) Re-adjust R and repeat 4 for about ten different values of Y₁, rising by about equal increments to 60 volts or so, Y₂ being constant.

Each of the readings in 4 and 5 should consist of a group of 3 or 4 observations with V_1 and A constant, so that a mean may be taken which would allow for alteration in C.P. due to the arc travelling round the carbons.

Tabulate your results as follows-

(6) The voltmeter used for V_{II} especially if a hot wire, must be shunted, not directly to the lamp, but to the lamp and ammeter A combined. The volts lost in A can be calculated and sub-

tracted from that shown on V_1 in order to get the true volts on the lamp.

The ammeter resistance is required for this correction and can a be found approximately by the Wheatstone Bridge.

- (7) Plot the following curves on the same sheet of curve-paper between C.P. as ordinates in each case, and (i) Volts V₁, (ii) Amps, A, (iii) Watts AV₁, (iv) Efficiency as abscisso.
- (8) Compare the above cost per candle hour for power at 64, per unit at normal voltage across the arc lamp with that of a glow lamp of equal C.P., taking 3 Watts per candle at normal voltage. The price of energy being the same.

Inferences. -- State clearly all you can infer from your experimental results.

(25) Determination of the Nett Optical Efficiency of an Arc Lamp.

Introduction.—This test is similar to the last, with the following exceptions—

Place the voltmeter V_1 , which should be of a sensitive high resistance type, across the arc instead of the lamp terminals as in the preceding test. This can be done by connecting it to two spring clips, which make good contact with the carbons about two inches from their ends next to the arc. The ammeter (A) must now be so arranged in the circuit that it measures the current through the arc without taking into account that passed by any shunt-coil which the lamp may happen to have.

Apparatus.—The same as for the commercial efficiency test, and in addition the two necessary spring clips.

Observations.—Repeat those of the foregoing test exactly as there indicated.

Connect up as in Fig. 20, with the exceptions noted above as regards the position of the ammeter and voltmeter.

Compare the efficiencies obtained from the two tests, and also the costs per candle hour for power at the same price,

(26) Determination of the Distribution of Light from an Electric Arc.

Introduction.—The distribution in the case of an arc light is obtained by measuring the C.P. at various angles to the horizon, in one single vertical plane containing the central axis of the photometer har.

To enable this to be done some arrangement, similar to the one briefly described under "General remarks" on are light photometry, is necessary.

The author, however, has devised a simple form of "crudle" in which to fix the lamps, and which is illustrated and described in the Appendix, p. 587.

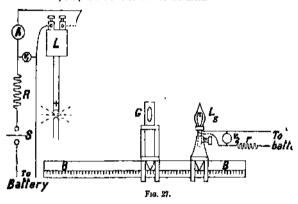
• The difficulty arising in the use of such an arrangement is due to the fact that most are lamps will not continue to self-regulate when placed in a slauting position. The author, however, finds that, with a suitable type of lamp, there is practically no difficulty from the above cause, until the cradle makes an angle of about 50° with the horizontal, and for just the one or two readings after this it is easy to help the mechanism by hand in order to maintain the "intake" of electrical power by the lamp constant.

Apparatus.—Precisely that mentioned for the test No. 24, p. 63, on "Commorcial Efficiency," except that the cradle is now required where just an ordinary stand would have done in that test.

Observations.—(1) Repeat 1-3 of the above-cited test, seeing in addition that the carbons touch at a point which is in a line with the centre of the axle of the cradle, and that their axes coincide.

- (2) Set the endle with its pointer at zero, when the carbons will be vertically over one another. With R full in, close S, and vary R so that the lamp takes its normal voltage and current and burns quite steadily, then quickly balance (by moving the screen), in the manner set forth in observation 4 of the test uited; repeat this three or four times for the same values of A and V_1 , and record the mean in the table.
- (3) Repeat 2 above, for the same values of A and V₁ for every 10° through which the cradle is turned, up to 70° or 80°, when

the axis of the carbons will be nearly parallel with the photometer bench, and tabulate as in the table for test 24 cited, substituting the heading "Angle between carbons and horizon" for the cost, etc., in the last column of the table.



- (4) Repeat 2-3 for a considerably lower current A than the normal, but one at which the arc buras properly.
- (5) Plot the Polar Diagram or curves of distribution of light from the are at various angles for each current used in the manner described below.

Inferences.—State clearly all you can infer from your experimental results, and point out their bearing on the lighting of streets and large areas by means of are lamps.

streets and large areas by means of are lamps.

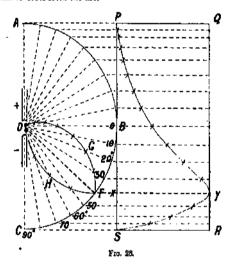
Determine from your results the mean spherical efficiency which = (1 horizontal efficiency + 1 max, efficiency).

Rota.—This may vary from 0.050 to 0.200, depending on the diameter and quality of the carbons, and is the ratio of the nosmal power in Watts, as given to the lamp in observation (2) above, to the mean spherical C.P. resulting.

PLOT OF POLAR DIAGRAM AND DISTRIBUTION OF LIGHT FROM ARC.

Let D be the junction of the + and - carbons, $\dot{\epsilon}$, $\dot{\epsilon}$ centre of arc.

Let DB represent the maximum C.P. obtained for some position of the arc, then with D as centre and DB as radius, draw the semi-circle ABC. Divide this into eighteen equal parts, each of which will therefore = 10° of arc, and draw radii to the points of intersection so formed. Now set off to the same scale as DB, the various C.P.s measured, along the respective radii from D, representing the angles in which they were measured. Then the curve DGFH drawn through these points is the polar diagram of C.P.s from the arc.



The distribution corresponding to this polar diagram is obtained as follows--

Draw PBS through B parallel and equal to ABC.

Through each of the points of division on the semi-circle ABC draw lines parallel to DB, and therefore perpendicular to PBS. From PS on these set off lengths proportional to the respective C.P.s at the corresponding angles. Thus, for instance, XY=DF = maximum C.P., and so on for the rest. Now complete

the rectangle PQYRS and draw the second curve PYS. Then we have for the arc lamp—

Mean spherical C.P. = $\frac{\text{Area of curve } PYS}{\text{,,,, rectangle } PQRS} \times \text{max. C.P.}$

- (1 horizontal C.P. + 1 max. C.P.) approx.

The curve PYS shows the manner in which the illumination of streets falls off with direct current are lamps at different distances from the lamp for a given height above the ground.

(27) Other Tests on Arc Lamps.

DETERMINATION OF THE EFFECT OF CARBONS OF DIFFERENT DIAMETERS AND QUALITY ON THE SPHERICAL C.P. AND SPHERICAL EFFICIENCY.

Notes. —In this test care must be taken to vary only one thing at a time, as for instance—

- (a) Vary the diameters only for exactly the same quality of carbon, all other conditions being constant.
- (b) Vary the quality only for exactly the same diameter of carbon, all other conditions being constant, as for instance the amount of power supplied to the arc. The spherical C.P. and efficiency is then measured in each of the cases a and b in the manner just described.

The results should be tabulated in a convenient manner. If possible a curve should be drawn between each separate pair of variables, and, lastly, inferences deduced from the experimental results.

(28) Determination of the Relation between Voltage and Current respectively, and the loss in grammes per hour of Positive and Negative Carbons.

Notes.—In this test, as was also mentioned in the last, only one thing must be varied at one and the same time. Thus.—

(a) For the same voltage, measure the loss in grammes of the

same or exactly similar $+^{\tau c}$ and $-^{\tau c}$ carbon occurring in the same interval of time with different currents.

(b) For the same current, measure the loss in grammes of the same or exactly similar $+^{*a}$ and $-^{*o}$ carbon occurring in the same time with different voltages.

The results should be tabulated in a convenient manner, and if possible the following curves drawn—

Two between volts and amps. respectively on the abscissm and losses in grammes per hour of + *o carbon as ordinates.

Two between volts and amps. as before, with losses in grammes per hour of $-\infty$ carbon as ordinates.

All on the same sheet of curve paper.

Carefully deduce the inferences obtainable from the results of the tests.

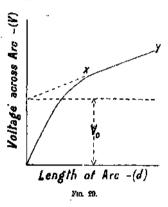
(29) Relation between Voltage and Length of Arc (with Constant Current through it).

Introduction.—This test, like the next one, is important, as it indicates why certain types of lamps can be run at higher voltages than others, while in conjunction with the results of a corresponding test for obtaining the Polar Diagram of the lamp, the effect of the length of are on the distribution of light over the lower hemisphere is clearly indicated. The reader should peruse the remarks under "introduction" in the next test which apply to the present one also.

Apparatus.—Precisely that for test No. 30,

Observations.—(1) Connect up as in Fig. 30, and set A and V to zero if necessary.

- (2) With (R) full in, close S and "strike" the arc by bringing the carbons together for an instant, and then quickly separating them, R being reduced to keep the arc burning.
- (3) By varying R, obtain a series of arc lengths between about $\frac{1}{4}$ " and the maximum possible by applying different voltages across it, the current being kept as constant as possible all the time at the most convenient value to be found by trial. Then after rapidly moving L to obtain the sharpest image I on G of each arc length, quickly measure I, and note x_i y_i A and V.



Note.—Time should be allowed for the carbons to burn to shape, and for the arc to become steady before readings are taken.

y Tabulate your results

exactly as in the last test, and plot curves having values of V and It as ordinates with length of are (d) as abscisse.

Find the constant (d)

in the equation— $Y = Y_0 + a.d.$ to the working part xyof the curve, Fig. 29.

Inferences. - What

can you deduce from the results of your test?

(30) Relation between the Current through an Electric Arc and the Voltage across it (for a constant Length of Arc).

Introduction.—The present test has an important bearing on the supply of electrical energy to "open," "enclosed," and "flame" are lamps in view of the length of are normally employed in those three distinctive types being different in practice. The voltage across the arc can be obtained by a high resistance voltmeter connected to two spring clips placed on the

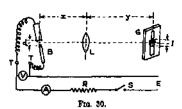
The voltage thus measured will be that necessary for evercoming the apparent resistance of the arc made up of the back EMF of the arc + the "ohmic drop" in the arc due to its ohmic resistance.

If the voltmeter is connected to the lump terminals it will measure the above-named apparent resistances + the additional "ohmic drop" between carbon tips and terminals.

carbons as close to their tips as is safe without risk of fusion.

The length of arc may be found in one of two ways: (I) by throwing an image of the arc on to a screen at a known distance away, by means of a double convex lens, when from the length of image and the distances of the lens from arc and screen the length of arc itself is at once obtainable; (2) by placing a gauge of known length, about equal to that of the arc in front of the latter, and measuring the shadow of the gauge on the screen, when from the length of shadow, gauge and the distances, the length of arc is obtained.

Apparatus.—Hand-feed are lamp B with terminals TT; double convex lens L, mounted on sliding base; ground or milk glass screen G; animeter A; voltmeter V; variable thoostat R; switch S and source of supply E.



Observations.—(1) Connect up as in Fig. 30, and adjust the pointers of A and V to zero if necessary.

- (2) With (R) full in, close S and "strike" the are by bringing the carbons together for an instant, and then quickly separating them, R being reduced to keep the are burning, which must be carefully watched.
- (3) Adjust the arc to a convenient length, say $\frac{1}{4}$ " to $\frac{1}{4}$ ", and move L until the clearest image I is obtained on U, then quickly measure the length of I on U, and note the readings of V and A and the distances x and y.
- (4) With the length of I constant, vary R so as to obtain a series of values of V and A between 0 and, say, 25 smps. x and y being constant, and the arc adjusted to keep I constant.
- (5) Repent 3 and 4 for constant lengths of arc of about \(\frac{1}{2}'' \) and \(\frac{1}{2}'' \), and tabulate your results as follows—

Dista	Inces,	Leng	the of			Apparent
т.	y.	Junage (7).	= \frac{1}{2} \times \text{T'}	Volta P.	Amps.	Resistances R = V chr 4.
		<u> </u>	\ 	` -	·	

(6) Plot to the same axes, curves having values A as abscisses with both V and R as ordinates.

Inferences,—What can you deduce from the results of the test?

(31) Examination of Alternating Current Arcs.

General Remarks.—The alternating current are possessed many characteristic and interesting features which are absent in the case of the continuous current are. Thus for instance the two carbons consume away at approximately equal rates. The colour of the rays is quite different, being much more purple than in the direct current are. Again, more energy is needed for the same volume of light emitted, and the are gives out a rhythmic hum if it is burning properly.

In addition the true power W given to the lamp may be considerably less than the apparent power AV, i. s. the product of the alternate current ammeter and voltmeter readings. Thus the power factor which $=\frac{W}{AV}$ may be very low and even down to 0.50 in an alternating current are lamp.

The following additional investigations should be carried out on this type of lamp, namely—

The effect on the C.P. of variations of (a) voltage, (b) current, (c) frequency, (d) quality of carbon.

The effect on the angle of phase difference or power factor of (s) quality of carbon, (f) cored and uncored carbons, (g) hissing of the arc.

The relative amounts of power absorbed by the arc itself and by the regulating mechanism should be investigated.

Many of the above tests can only be employed on handregulated lamps.

(32) .Measurement of the Internal Resistance of Secondary Cells.

Introduction.—The following method is the best for measuring the working value of the internal resistance of a storage cell or battery of such. Owing to the very low resistance met with usually in this kind of cell the ordinary methods are practically inapplicable, and in the present case the cell is being tested more on less under working conditions.

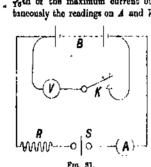
If a battery is being tested the total internal resistance can be obtained at once, and if the cells are all of the same size, make, and type, the resistance of each cell can be deduced, probably with considerable accuracy, by dividing the total resistance so obtained by the number of cells and thus obtaining the average resistance per cell. It should be remembered that the internal resistance of any cell is not a fixed and invariable quantity but depends on several things, thus, for instance, on the density of the sulphuric acid solution which is continually changing according to the amount of discharge, or charge of the cell. It is interesting to note in this connection that the resistance of a solution of dilute sulphuric acid is least at a specific gravity of about 1220 and increases from this in either direction, i.s. for a rise or fall in density. Again, the internal resistance will depend on the condition the plates are in, and will be greater if they are "sulphated" than if in good condition,

Apparatus.—The cell or cells (B) to be tested; voltmeter V of sufficiently large resistance, and having a long open scale, enabling small differences to be read accurately; ammeter A capable of reading up to the maximum current to be taken from the cell; key K; switch S; carbon rheostat R (p. 597).

Observations.—(1) Connect up as in Fig. 31, and adjust the pointers of V and Λ to zero, levelling the instruments if necessary.

- (2) With S open, close K and note the reading E on the voltmoter. This is therefore the E.M.F. of the cell in volts, since only an extremely small current is flowing.
 - (3) Close both K and S and adjust R so as to obtain about

taneously the readings on A and V, which latter now gives the terminal P.D. (V) in volts.



ing value of the internal resistance b of the cell or lattery from the relation $b = \frac{E - V}{A}$ ohms, and tabulate your results as

(4) Repeat 2 and 3 for about ten different currents rising by about equal increments to the maximum.
(5) Calculate the work-

follows -

(6) Plot 2 curves having values of V and (b) as ordinates and A as abscisse. Show that the tangent of the angle of slope (from the herizontal) of the V and A curve = the internal resistance (b).

(33) Measurement of the Efficiency and Storage Capacity of Secondary Cells.

Introduction.—Secondary cells may be divided into two main divisions, namely—the "Fauré" or pasted type, and the "Planté" or non-pasted type. The chemical changes occurring in either class, during charge and discharge, are precisely alike, but the reader is referred to ordinary text-books of Electrical Engineering—for instance, Electrical Engineering in Theory and Practice,

scope of the present work.

The secondary or storage cell has taken up so prominent a

by the author-for such changes which hardly come under the

position at the present day in both electric lighting and electric traction that the method of measuring the efficiency and storage capacity of any type of cell, or perhaps more particularly the relative behaviour of different types under the same conditions, is a matter now of paramount importance to every electrical engineer. A good deal may be said with regard to the precise mode of testing such cells, and in this connection much depends on the duty which they have to perform in actual practice. Any laboratory test of such cells will be worthless almost, from a practical point of view, unless it is carried out under conditions as nearly as possible alike to those the cell will work under in its everyday uso. Thus, for instance, take a battery employed for merely lighting purposes, say at a central electricity supply station. It is never resting idle and never merely giving either the full load discharge or any other constant output, for the load which it has to take varies with the hour, day, and season of the year, from often next to nothing, to full load and sometimes a considerable percentage overlead for short periods. Thus it will be seen that in this instance any test to be of value must be carried out as nearly as possible under these conditions, and for months continuously, too, instead of, perhaps, only for two or three weeks always at full load and with, say, a night's reet in between each such discharge.

Again, in the case of electric traction work, the above remarks do not all apply, for instance, usually a battery used in this kind of work in sub-stations is relieved of discharge between midnight and about 7 a.m. in the morning, during which period it is charged. When used for portable work, as in autocars and transcars, it is subject to both rapid and wide fluctuations of output and often to excessive jolting. Honce the test on a cell required for this kind of work should be a very stringent one, automatic jolting gear being v provided to operate on the cell while being discharged, while this latter must often be abnormal. Practically the Fauré or pasted type of cell is the only one available for self-contained autocar truction, as weight forbids the use of the Planté type. As one instance of a traction type of pasted cell which will stand periods of excessive discharge and the wash of the solution against the plates and yet have a long life, the Hendland secondary cell may be instanced, and tests extending over years amply justify this.

respectively.

The efficiency of any secondary cell or battery can be reckoned in one of two ways, namely, the—

Quantity efficiency, or Ampere-hour efficiency Ampero hours given out

Ampero-hours put in

Energy efficiency, or Watt-hour efficiency

Watt-hours given out
Watt-hours put in

Each of these will depend to a certain extent on the relative periods of charge, rest, and discharge, and also on the current density or rate of discharge reckoned say in amperes per unit of area of positive plate. The greater this is the less will be the quantity efficiency, and also the energy efficiency, though the latter not to the same extent as the former.

It may here be remarked that the quantity efficiency may be as high as 94% when the current density is low and the cell used under favourable conditions, whereas the energy efficiency cannot exceed 80% from the fact that the average normal voltage of a cell on discharge is 2.0 volts approximate and the average voltage needed to charge being 2.5 about. These two efficiencies in practice may be taken more nearly as about 75% and 65%

The CAPACITY of any secondary cell may be expressed in one of two ways, namely, either as the ampere-hours or as the Watthours which it is capable of giving as a useful discharge. The term commercial capacity might be given to the number denoting the ampere-hours or the Watt-hours per lb. of plate (taking both + ** and - * together) or per lb. of cell complete, including acid, etc.

At the present day, owing to there being so many forms and

methods of building, the latter mode of reckoning the capacity is the only one available when comparing different types of cells. A secondary cell may be charged either (1) at constant P.D. or (2) at constant current. In the first case a fairly heavy rush of current takes place at storting, and the method would be unsuitable for use on some types of pasted cells from the risk of the plates buckling. The second method is the one nearly always employed in practice and is the one which will here be considered.

The cell should not be discharged normally below 1:80 volts on closed circuit, since it will then become practically useless for lighting circuits, and there is also the danger of the plates "subplicting" rapidly below this limit. For the latter reason it should not be allowed to rest in this discharged condition.

Apparatus.—Cell B to be tested; sensitive voltmeter (V) with

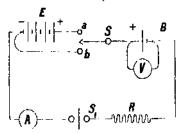


Fig. 32.

open scale; anumeter (A); switch S_1 ; carbon rhocstat R (p. 697); two-way switch S; source of charging E.M.F. (B); hydrometer and weighing arrangements if the latter should be required.

Observations.—(1) Assuming that the cell to be tested is not already set up, but is still as received from the reakers. First weigh each complete set of plates, "Positives" and also "Negatives," separately after dusting them. Also weigh the containing vessel, and the dilute sulphuric acid solution (of the specific gravity authorized for that particular cell), which is sufficient to cover the plates and be about one inch above their tops. Measure the size and thickness of the plates.

(2) Set up the cell properly, connecting up as indicated in Fig. 31, and adjust the pointers of V and A to zero if necessary.

(3) More as a matter of interest than otherwise, carefully note the sp. gr. of the acid solution before and immediately after putting it into the cell by means of the hydrometer, and then note the readings of this latter and the time frequently, while the sp. gr. is rapidly altering and until it becomes constant.

Note.—In all cases exercise great care in keeping the hydrometer away from the aides of the vessel and plates; if this is not done it will give totally erroneous readings due to adhesion.

 $\tau_{\tau_{1}, \cdot, \cdot, \cdot}$

,

more slowly.

(4) If the sp. gr. of the acid solution is constant note it, then with Rat its maximum and S on contact a, note the time on closing S, and quickly adjust the current on A to the "normal" for this cell by means of R.

(5) Keep this current constant in strength until the acid becomes milky in appearance throughout-commonly known as boiling and due to bubbles of gas liberated from the plates. Note the readings of the hydrometer and voltmoter and the time frequently while they are varying rather rapidly, but less often as they vary more slowly, and, lastly, open S_1 when the cell is

completely charged. N.B.—Probably this first charge will last from at least 15 to something like 30 hours before the cell thoroughly comes up to the "boil," and in no case should it be stopped in the first 12 hours except for a minute or so. Beyond keeping the current constant from beginning to end the other readings during the middle stages of charge need probably be only taken every 1 or 2

bours about.

Tabulate your results as follows-

DATE . . . Mama of Coll . . Normal rated capacity . . . Type . Amp, hours : Positive - . . . ibs. : Negative - . . . ibs.: Verwels To

CHARGE

		= bg . ft, ;]			volume= , , ,	Ratio=	
Number of	Amperes	Terminal	Time	Sp. gr. of	lupat	Injut	
Charge.	J.	P.D. (V) Volla.	in Hours.	Arid,	Ampbours.	Watt-houss.	

had since the last charge, note the open circuit P.D. at its terminals and the sp. gr. Then put S to (b) and close S_1 at a noted instant of time, quickly adjusting A to the normal discharge value for the cell, which must be kept constant by R. Note the P.D. on V and the sp. gr., and the time frequently while they are varying somewhat rapidly, but less often as they vary

(6) Take note of the period of rest (if any) which the cell has

Open S₁ every half-hour, say for the shortest time necessary to just take the "open circuit" volts. noting the time at each.

(7) Continue the discharge until the terminal voltage falls to 180, then open S, and tabulate your results as follows-

DISCITATION.

	Warmhan.	Time	en en		Termin	al Volta.	Internal	Ontput (aped ty.	E(Ac)	ency.
•	of Discharge.	in Ranto,	of Acid.	Ampu.	Closed circuit V.	Open citruit R	Internal Resistance b.	Amp bours.	Walt- hours.	Amy.	Watt- hour
									•		

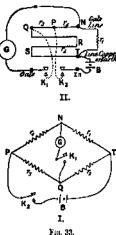
- (8) Repeat tests 4-7 until the charge and discharge curves practically coincide, indicating that the cell has attained a good normal working state, and take note of the length of rests between charge and discharge.
- (9) Take a discharge, as per 6 and 7, for 50% under- and also "over"-normal rate.
- (10) At the conclusion of all the tests carefully observe whether any appreciable "buckling" or disintegration of the plates has occurred.
- (11) Calculate the capacity of the cell in both amp.-hours and Watt-hours per lb. of total plates and per lb. of cell complete with acid. Also calculate the current density used per sq. ft. of + plate, reckoning both sides of each.
- (12) Plot the following curves, all like ones being on one sheet-
- (a) Internal resistance in ohms as ordinates and times in hours during discharge as abscissæ.
- (b) Time in hours as abscisse, with voltage and sp. gr. as ordinates in each case for both charge and discharge.
- (c) Current density as abscisse and amp.-hours output as ordinates.
- (d) Current in amps as abscisse and the quantity and energy efficiency as ordinates.

(34) Measurement of Resistance by the "Post Office" Pattern of the Wheatstone Bridge.

Introduction.—It is assumed that the first principles of a Wheststone Bridge (W.B.) have already been studied from an ordinary text-book. The Post Office (P.O.) pattern, Fig. 33 II., is merely a specially-arranged and compact form of W.B. placed in

a suitable box for portable purposes. If the principle and action of a W.B. is understood at all, and the stamping opposite the various terminals in the P.O. form observed, it ought to be impossible to couple up incorrectly. Each of the "proportional" arms " τ_3 and τ_4 consists of three resistance coils of 10, 100, and

1000 ohms such respectively, hence the ratio $\frac{r_3}{r_4}$ or $\frac{r_4}{r_3}$ can be made a very simple number. QRST



(Fig. 33 II.) is the "adjustable arm" r2, and it consists of 16 different coils and one infinity plug either at Q, R, or S. The value of r2 can be made anything from 1 to 11,110 ohms. Opposite two of the terminals (N and T) is marked (Galvanometer Line) and (Line Copper or Earth) respectively. This is because the P.O. form is primarily intended for measuring the motallic and insulation resistauce of telegraph lines, and bence in the first case that line would be joined to N and T_* and in the second case only one end to N, the other being free and insulated, T then being put

to earth. As therefore we are measuring metallic resistance (r_1) it is put between N and T. The terminals to which the battery B must be connected are equally obvious. The white dotted lines on the top show where the under contacts of the keys K_1 and K_2 are joined to, inside the box. In any form of W.B. variation of the battery E.M.F. or its resistance or that of the galvanometer (G) has no effect on the accuracy of the measurement. The sensitiveness of the tost, though principally depending on that of G, can be increased within limits by using a larger E.M.F. and making r_1, r_2, r_3 and r_4 as nearly equal as possible. The battery key K_2 must always be pressed before the galvanometer key K_1 to allow the currents in the

arms to become steady before pressing K_1 . The battery key should be pressed for no longer in order to prevent the coils being heated by the current and their resistance thereby altered, "It should also be broken last to avoid the risk of dumaging G by inductive kicks when measuring inductive resistances. In inserting plugs press in lightly and give about $\frac{1}{2}$ of a turn to insure good electrical contact. Reverse this operation when resnoving them. The ends of all connecting wires should be scraped clean.

Apparatus.—P.O. Bridge; sensitive galvanometer G (p. 571); 2 or 3 Leclanché cells B.

Observations.—(1) Connect up as indicated in Fig. 33 II., and adjust the galvanometer needle to zero.

(2) Note once for all the direction in which G deflects when $\langle r_2 \rangle$ Fig. 33 II. is too large to give balance (done by taking out "Inf" in r_2 with, say, $r_3 = r_4 = 10$).

Note.—Until balance is nearly obtained, only tap K_1 for a fraction of a second.

(3) Make $r_3 = r_4 = 10$ and balance the bridge by altering r_2 so as to get no deflection on pressing K_2 and then K_1 . If it is impossible to get exact balance, note the steady deflection when r_2 is just too large and too small, and calculate the correct intermediate resistance to give balance, by proportion. Thus if $d_1 = \text{steady deflection of the galvanometer to one side of zero for the adjustable arm = <math>R_1$, and $d_2 = \text{that to the other side of zero for the adjustable arm = <math>R_2$, then if R_1 is greater than R_4 we have $(R_1 - R_2)$ ohms corresponding to a deflection of $(d_1 + d_2)$ scale divisions,

and
$$\therefore$$
 d_2 corresponds to $(R_1 - R_2) \frac{d_2}{d_1 + d_2}$ ohms.

Hence the resistance of the arm, which would give just no deflection (the required condition)

$$=R_2+(R_1-R_2)\frac{d_2}{d_1+d_2}$$
 ohms= r_2 .

(4) In order to obtain the true resistance (r_1) of the unknown which is being measured, without the process of interpolation mentioned in the latter part of 3 above, the value of r_2 or r_4 may

be varied. Thus instead of $\frac{r_4}{r_1}$ boing $=\frac{20}{10}$ or 1 as in 3 above, we

might have $r_3 = \frac{1000}{10}$, r_{000} , r_{000} , or r_{000} , depending on the value of the unknown r. In many cases this will be equivalent to having decimals of an ohm in the adjustable arm (r_2) . Hence

increase or decrease the ratio of $\frac{r_4}{r_8}$ and adjust r_3 so that on pressing K_2 and then K_1 no deflection whatever occurs on the galvanometer. Then note the values r_2 r_3 and r_4 .

N.B.—If the unknown resistance r1 is greater than 11,110 ohms, then r_4 will be greater than r_3 , but if (r_1) is less than 11,110 ohms, then r may be either - , or less than r. Tabulate as follows—

Real-dances Contect.	Proportional Arms.		Adjustable	Unknown Resistance	Wast a
tested.	73	*+	Árqi 💤	ก=ปั×เช	Meat ry.
	†				

Note.—The limits of the P.O. Bridge are $(\frac{10000}{10000} \times 1) = 0.01$ ohm and $(\frac{1000}{10} \times 11,110) = 1,111,000$ ohms, but measurements become less accurate as they approach these limits.

(35) Measurement of the Armature Resistance of Dynamos and Motors, and of the Copper Resistance of Transformers and Electric Light Cables. (Potential Difference Method.)

Introduction.—The Wheatstone Bridge is inapplicable for measuring very low resistances, and even if such were just within its range, the measurement would not be accurate owing to errors introduced by the variable contact resistances in the circuit. The following method, which depends directly on the definition of resistance, can be used to accurately measure very low resistances, such as are met with in large electric light cables, the armatures of dynamos and motors, and the low tension coils of transformers. The P.D. at the terminals of each resistance can be measured

relatively by a sensitive galvanameter, whose resistance is large

compared with that between the two points to which it is applied. Under these conditions its insertion will not lower the P.D. to be measured. If it is a reflecting instrument the scale deflections will be proportional to the P.D.

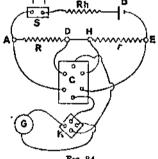
The most suitable instrument for a workshop test, which as a rule does not admit of the use of a delicate galvanometer, is a low reading voltmeter, having fairly large resistance, and reading to about 1 or 1.5 volts for a full scale deflection. Such an instrument, although not nearly as sensitive to small differences of potential as the galvanometer, has the advantage usually of being more portable, and also less easily affected by magnetic fields in the vicinity.

Apparatus.—Known standard low resistance R of about 0.01 ohm (Fig. 273); low resistance r

to be tested; Pohl's commutator C(p. 584); secondary cell B; rheostat Rh (p. 597); fairly high resistance galvanometer (p. 569) or low reading volt-

meter G, preferably of the moving coil type; reversing key K (p. 585); switch S.

Note.—The ends H and E of the low resistance (r) to be tested will of course be the terminals of the transformer



Frg. 34.

coil, the onds of the cable or the brushes of the machine, the field coils being disconnected temporarily. The length of lead between D and H in the Fig. is immaterial.

Observations.—(1) Connect up as indicated in Fig. 34, and adjust the galvanometer or voltmeter needle to zero. Clean the collecting arrangement at the part where the brushes press with fine emery cloth, assuming, for example, we are dealing with a dynamo or motor. To prevent the armature rotating, see that the field circuit switch is open, and that the brushes press on opposite ends of a diameter in the case of a direct current commutator.

(2) With Rh full in, close S, and adjust the current to give about quarter-scale deflection with the largest resistance of the two, for then the deflection with the other is bound to be on the scale; then note the galvanometer deflection on each side of zero by turning K, when G is across each resistance in turn.

N.B.—The resistance $R\lambda$ should be sufficiently high to prevent the current strength altering during any one pair of observations,

and to provent this current being strong enough to sensibly warm the resistances. The more sensitive the galvanometer the smaller this will be. After taking deflections with the second resistance, it is advisable to rotate those with the first in case the current has altered. If they are not the same, take the mean of those on the respective sides of zero. For very accurate work a reversing key should be used with B to climinate any thermo-

current effects.

(3) Repeat 2 for half, three-quarter, and full scale deflections, and calculate the unknown resistance r from the formula— $R \div r = d_R \div d_r$

Tabulate as follows -

Defic	ohion acr	œu R.	Defic	ction ner	068 F,		Unkcova.
Tegld.	Left.	Menn da	Right.	Left.	Meun d,	Rain, di di	$+$ ohus= $R\frac{dr}{d\mathbf{g}}$
		<u></u>			! !		

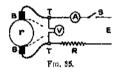
Inferences.—Prove the formula given in 3, and state any assumptions made in deducing it. What sources of error is the method liable to? How can they be minimized?

(36) Measurement of Low Resistances by Voltmeter and Ammeter Method.

Introduction.— The following method, applicable to the measurement of the low resistances met with in the armatures of dynamos, motors, transformer coils and electric cables, is one of the simplest and a direct application of Ohm's law. It is not usually susceptible of the accuracy obtainable by the last method (Test No. 35) and depends on the accuracy of the ammeter and voltmeter used, and on that of observation.

Apparatus.—Low resistance (r) to be tested; accurate ammeter (A) and low reading voltmeter (V), both preferably of the moving coil type; switch S; variable current rheostat (R), the form of which will depend on the current supply (E) available. If E comprises two or three large secondary cells, then R may be a carbon rheostat (p, 597), but if E should be a 100 volt supply, then R may be a bank of lamps (p, 598).

Observations.—(1) If, as is indicated, an armature resistance is to be measured, connect up as indicated in Fig. 35. Adjust



the pointers of A and Y to zero, and see that the field circuit of the machine is kept open throughout the whole text by keeping the field switch open or otherwise.

(2) With V connected to the terminals TT of the machine, as actually shown, and with (R) full in, close S and take simultaneous ascending and descending readings on V and A for some five or six currents on A, differing in strength by about equal amounts between O and full-load armature current by suitably varying R—the armature being at rest all the time.

Note.—This measurement will give the Static "brush contact" resistance + resistances of armature and both brush leads BT.

- (3) Repeat (2) with the armature rotating (by hand) while taking readings.
- (4) Report (2) with the armature at rest, but with the ends of the voltmeter wires disconnected from TT and carefully inserted under the brushes RB, so as to press against the proper commutator segments, the straight ends of the wires so inserted being parallel to the length of segment. Tabulate all your results as follows—

(5) Plot, on the same axes, curves having values of V as, ordinates, and (A) as abscisse for tests 2, 3 and 4.

values of (*) obtained!

(37) Measurement of the Armature Resist-

Inferences.-What can be deduced from the curves and

ance of Machines and other Low Resistances by simple Potentiometer Method.

Introduction.—Since by Ohm's Law V = I.R., where V = the

P.D. across the ends of a resistance R carrying a current I, it follows that when the same current I flows through two resistances, the P.D. (V) across each is α to that resistance. The previous test (No. 35) was based on this fact, but since actual deflections (α to the P.D.s) had to be compared, the

accuracy depended to some extent on the current-deflection law of the instrument used, and on the instrument having a high resistance relatively to those measured. The present test, based on the Clark-Poggendorff method of comparing two E.M.F.s, and unlike the deflection method No. 35, is a null or zero method or one in which no deflection is the condition to be obtained. Hence the law of the instrument is immatarial, and

an increase in its sensibility increases the necuracy of the test. Since also in this method the E.M.F.s to be compared are in turn placed in series with the instrument, the contact resistances of the connection to those E.M.F.s, as also the resistance of the connection are investorial, hence the greater accuracy with

of the connection to these E.M.F.s, as also the resistance of the connections, are immaterial; hence the greater accuracy with such a null method. Test No. 39 employs precisely the same principle as, but is a greater elaboration of, and a little more accurate than, the present method, in which we shall use a single or multiple metre bridge having a stretched undamaged wire

of high resistance material, of uniform cross sectional area and size, and which will not sag due to heating by the current from one secondary cell connected direct to its extremities. Thus the E.M.F.s to be compared can be balanced against the uniform fall of potential along the wire due to a constant current flowing through it, and the ratio of the lengths so

balanced will be that of the E.M.F.s across them.

Apparatus.—Armature A to be tested; known standard low resistance R; switch S; variable rheostat r; secondary cells. R and E; Pohl's commutator or change over key C; metre bridge PQ with sliding contact key; sensitive galvanometer C.

Observations.—(1) Connect up as shown in Fig. 36 and

adjust G to about zero. Ensure the connections being such that when G is

turned so as to include the fall of potential of either R or A in the circuit of G, each P, D, opposes that along PQ

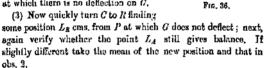
due to E.

(2) With r full in, close S, and

adjust r so that with C turned to the larger of the two resistances, a posi-

tion, say, L_A ems. from P, is obtained at which there is no deflection on C.

MINE . . .



(4) Obtain several pairs of positions such as L_A and L_B by altering (r) and tabulate as follows—

DATE . . .

	of unknown Re Luown Resist		Oime.	Galv 3	¥0
Wires as con- need d to which points of d	Unknown Resistance measured, liet or Cold,	Distance of S		Unknown lieusinges $R_A = \frac{L_A}{L_R} \times R$	Mean value of R _A obnus.

Inferences.—On what does the accuracy of the test depend, and how can it be made more sensitive?

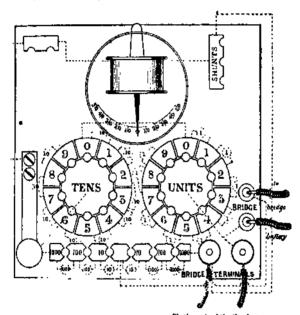
(33) Measurement of Metallic or Conductor Resistance by the Silvertown Portable Testing Set.

Introduction.—The method used in measuring the resistance of the conductor of the circuit under examination is that of Whoatstone's Bridge.

Fig. 37 below shows only those parts of the instrument which are employed in this test, and omits the parts and their connections which relate only to insulation testing. The parts employed are the following—

- 1. The adjustable resistance. This it will be seen consists of two sets of 9 soils, each connected to circular plug commutators or dials. One set of coils has nine resistances of ten ohms each, making ninety ohms in all, the other has nine resistances of one olm each, making nine ohms in all. If the hole marked with any number, say 5, is plugged in the ten-ohm dial, a resistance of fifty olims is inserted between the connecting leads entering and leading away from the dial; and a similar rule applies to the one-ohm dial. Hence if the hole 6 be plugged in the tens dial and the hole 8 be plugged in the units dial, a total resistance is inserted in the two in series of 68 chms. The lowest resistance that can be obtained is given when both the 0 holes are plugged, when the coil resistance inserted is zero. The highest resistance is obtained by plugging the two 9 holes when the total resistance is 99 ohms. If no plug is inserted in one or both dials, the circuit is broken and the resistance is infinity,
- 2. The second part of the apparatus is the double set of proportional resistances, consisting of two coils of 10 chms each, two of 100 chms and two of 1000 chms. Of these only one on each side of the centre is to be unplugged for any given test, and a rule is given later on for selecting the resistances to be employed to obtain the greatest possible sensitiveness; that is to say, for selecting those coils which will give the largest deflection on the galvanometer, when the resistance plugged in the dials varies by a given error from that of the circuit under test.
- 3. The third part is the galvanometer. Its two terminals are connected to the two ends of the Wheatstone Bridge by depressing

the contact key. It will be noticed that the shunt coils, with their plug commutator, are omitted from the diagram. This is-done because they are not essential to the test, though they may be conveniently used when the balance of the bridge is not



To the ends of the Conductor,

Connections for Testing Conductor Resistance. Frg. 37,

yet approximately correct, and very large deflections are being obtained.

4. The battery may consist of three Leclanohé cells, having an electro-motive force of about 5 volts. One pole of the battery is connected in the usual way to the middle of the Wheatstone

93 ... * BLECTRICAL BNGINEERING TESTING

Bridge, and the other to the point where the end of the adjustable dial coils is connected to one of the terminals, to which the con-

ductor under test is attached. The connections are made by inserting the plugs at the end of the battery leads, in the two holes marked batter, and immediately this is done the current is established in the coils; the galvanometer circuit is of course not completed till the key is depressed.

5. The ends of the conductor to be tested are to be secured under the two terminals marked uninest terminals, and in measuring low resistances care must be taken that they are very

securely attached. This may be done for very large or stranded conductors, either by soldering to their ends thin brass plates with holes in them of a suitable size to go under the heads of the terminals, or the connection may be made by means of finer wires soldered to the end of the main conductor. The resistance of these must be independently ascertained and subtracted from the

gross result.

Providing an idea is first obtained as to the magnitude of the resistance to be measured, the following table will be found

helpful in expediting any test with the "set."

		T.	ADLE III.		
For Resist-		ni.~ Judiourpous	No. of Signifi-	Battery	Remarks.
angen is sted between	Laft-hand Corl.	Right-hand Coll.		Power.	ACIIZ AL
1 and 10 15 and 100 100 and 1000 1000 and 10,000 0:1 and 1 0:1 and 1 0:01 and 0:1	100 100 100 10 100 1000 1000	10 100 1000 1000 10 10 10	9	Onlinery Increased	An extra alguid- cast figure can be obtained, calcilluded by projection from the deflections.

A third figure can always be found in measuring resistances between one ohm and 1000 ohms, by observing the deflections of the galvanometer needles on both sides of the zero for different adjustments of the dial resistances near the balancing point.

The opening we will suppose that the 10 ohms will in the wight.

For example, we will suppose that the 10-ohm coil in the rightband side of the bridge, and the 100-ohm coil on the left-hand side are unplugged, and that when 45 ohms are plugged in the dials, and the key depressed, a throw of three divisions of the galvanemeter needle is observed to the right; and when 46 ohns are plugged we get a throw of two divisions to the left on the galvanemeter scale. It is clear that the resistance to be measured lies between 45 and 46, and is nearer to 46 than 45, as two is less than three; that is, the resistance is 456 ohns. As a further example, suppose 100 ohns to be unplugged on each side of the bridge, and 82 ohns to be plugged in the dials; on depressing the key, no deflection of the needle is observed. On plugging 81 ohns in the dials, a throw of six divisions to the right is obtained, and on plugging 83 ohns we get the same deflection to the left. We are then amply justified in putting the third figure in the result as 0, and the resistance to be measured is 82 0 ohns.

Except in testing at the extreme range of the instrument, i.e. quantities less than one ohm or greater than 1000 ohms, the galvanometer will be found amply sensitive, and it is better to place the south end of the controlling magnet uppermost, thereby reducing the time of the oscillations of the galvanometer needle.

The battery should be in circuit as short a time as possible to avoid running down the cells, and it is well to take out one of the battery lead plags when any alterations are being made in the plag commutators, only replacing it just before pressing the galvanometer key.

Observations.—(1) Connect up as indicated in Fig. 37, using the "set" precisely as there indicated. The box should be placed on a table, or some other approximately level surface in front of the operator, he facing the magnetic east, and the controlling magnet being in a vertical position. The pointer of the galvanometer will then be found to be swinging near its zero, and may be brought exactly to it by slightly turning the controlling magnet.

- (2) Find roughly the resistance to be measured by unplugging ten in each of the proportional arms, and then adjusting the dial resistance so as to give a minimum deflection on pressing the key, the dial readings will roughly be the value of the unknown.
- (3) Now proceed to balance according to the foregoing table and remarks, and tabulate as follows—

NAME . . .

Dave . . .

('alogi#ted

ice tested Proportional Arms. Adjust

Tembout			•
Grafe =	٠	•	

dule Right with Left with to balance the

 11-	12 41.	-	42 75.		72	
	resistance s—Assumi					

Delications to the

calculated thus—Assuming
$$r_2$$
 to be greater than r_2 ", then $(r_3''-r_2''')$ ohms corresponds to a deflection of (d_1+d_2) scale divisions, and d_2 corresponds to a resistance of

$$(r_3' - r_3'') \frac{a_2}{d_1 + d_2}$$
 ohms = r ,

 $(r_3'-r_5'')\frac{d_2}{d_1+d_2} \text{ ohms}=r,$... the correct dial resistance requisite to give no deflection $= r_3 + r = r_3 + (r_3' - r_3'') \frac{d_2}{d_1 + d_2}$ ohms.

(39) Comparison of Resistances. (Crompton Potentiometer Method.)

Introduction.—This method is a valuable one for comparing two or more resistances of almost any value, within reasonable limits, and consequently of determining the actual resistance in chms of one of them, the other being an accurately known standard, such as one of the forms described on p. 605, which are some of the acressories of the potentiometer. The method, which is very simple and susceptible of great accuracy, is more particularly applicable to low resistances such as short lengths of electric light cubies and the amountures of dynamors, etc., rather than multiples of the ohm, and it can be worked in such a way that the unknown resistance can be read off by inspection directly in ohms. Thus it will be seen that the present measurement is a practical development of that known as " Measurement of Low Resistance by the Fall of Potential Method," given on p. 84, and is a direct application of Ohm's Law. The principle of it consists in comparing the relative falls of potential down the two resistances traversed by the same current through the medium of the potentiometer, employing the principle of the Clark-Poggendorff method for comparing two or more E.M.F.s. The Crompton potentiometer is a specially arranged form of comparing instrument, and the operator should, prior to commencing the test, make himself acquainted with the instrument, a detailed description of which is given on p. 510, together with the method of using it. The accuracy of the results is principally dependent on the standard known resistance, and the value of the largest current sent through this and the unknown must be such that the fall of potential down either does not exceed 1.5 volts, and that neither is warmed up by that current sufficiently to alter their resistances.

The observations may be taken in one of two ways-

(a) Suppose the potentiometer has been "set" by the Clark cell in the usual way (p. 514) for E.M.F. or current measurements, and that the standard resistance R_z=0.01 ohm. Then to avoid disturbing the "setting," balance each fall of potential down the two resistances, against that down the potentiometer, and compare the two P.D.s from the relation—

$$V_s:V_R=R_s:R_R.$$

Example.—Let the standard balance with E on stud 1 and C at 95 on the scale, the P.D. across R_s is 1000+95=1095 volts. If now the unknown balances with E on stud 2 and C at 190 on the scale, the P.D. across it = 2000+190=2190 volts,

$$R_s = \frac{VR_s}{V_s} = \frac{2190}{1005} \times 0.01 = 0.02 \text{ ohms.}$$

(β) Suppose the potentiameter has not been "set" by the Clark cell. Balance up on the standard resistance instead. Thus put K to stud 1 and C at 0 on the scale, and alter C and C_1 as described on p. 514, so as to "balance the potentiameter" for no deflection. Now with C and C_1 fixed, balance with the maknown resistance, which position of balance will give the resistance K_K in ohms directly. In the present instance this would be K on K_K or $K_K = 2 \times 01 = 0.02$.

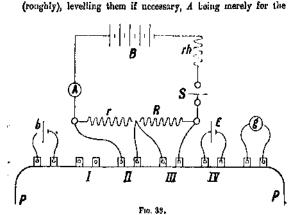
Apparatus.—Crompton potentiometer P (Fig. 208); secondary battery B capable of easily giving the largest current suitable for sending through the low resistances; switch S; one secondary cell (b) for the "working cell" of the potentiometer; accurately known low resistance R (p. 605); unknown low resistance r to be

ELECTRICAL ENGINEERING TESTING

tested; standard Clark cell E; carbon rheostat (rk) (p. 597); sensitive operiodic D'Arsonval or moving coil galvanometer (g) (p. 569), Observations.-(1) As a precaution first place the levers of ?

G and E (Fig. 208) on stude 14, and that of H on stud 1, then

connect up as in Fig. 38, in which only the row of terminals on the potentiometer PP is shown symbolically. (2) Adjust the galvanometer (g) and current indicator A to zero.



purpose of indicating roughly about what current flows in r and

 R. See that the standard resistance R chosen is of such a value as to be about the same as the estimated value of the unknown r.

Note.—The maximum current then to be used must not produce a fall of potential in either R or r exceeding 1.5 volts.

(3) "Set the potentiometer" as indicated in either . or balance on the standard resistance as in & above, the contact ' lever II referred to above being on stude IV or III respectively,

as the case may be, thus inserting E or the P.D. across R in the circuit of (g), and taking care that it opposes the P.D. due to (b). Now close S, and adjust (+h) so as to obtain some convenient current on A. N.B. This last-named operation is done before belinning P by method β .

(4) With the positions of the resistances G and G, (Fig. 207, p. 510) as found in 3, unaltered, turn H to stude H or III, according to the "setting" employed, so as to throw into circuit with (3) the P.D. across one or other of these terminals. Then adjust E and the slider C to obtain no deflection on (g) when the latter is pressed, and note the reading of each.

Note.—If it is impossible to "balance" owing to the spot of light being deflected always to one side, the P.D. down the resistance is assisting instead of opposing (as it should be) the fall due to (b) in the stretched wire; the wires from resistance to potentiometer are then to be interchanged. Lastly, turn II again to the sotting used in obs. 3 to see if balance is still obtained. If it is not, reset P and repeat.

- (5) Repeat 4 with H on the stude leading to the other resistance, if "setting a" is the one being used.
- (6) Repeat 3-5, obtaining some six or eight distinct sets of readings by suitably altering the current through R and τ, and tabulate your results as follows—

	Potentionseter reading.						Unksown	
Ammeter reading for	R	in eire	ult.	7	ի գևշդ	i t	resistance r=\frac{Vr}{R}\ \text{ohms.}	Moan r ghms.
reference only	सध्ये र्ल स	Slider C.	P.D.	Stad of R	81/der 6.	P.D.	Va	r dame.
				<u> </u>				

Inferences. -On what does the accuracy of the test depend !

(40) Measurement of Low Resistance by the Nalder Low Resistance Measurer.

This method has the advantage of boing a null or zero one, and entails the use of a specially arranged piece of apparatus or "measurer," together with a secondary cell capable of giving a current of 5 amps and a variable rheostat to adjust this current.

The general arrangement (Fig. 214) and method of use is given on p. 521, and will not be repeated here.

Insulation Resistance.

Introduction.—Probably we shall not be straying very far from the truth when we remark that Insulation Resistance is one of the most important matters that an electrical engineer has to deal with. In fact, so obvious is this that the statement hardly needs qualifying; suffice it to say that a breakdown of the insulation resistance—whether of street main, appliance fod from it, or of an ordinary electrical installation supplied off it, will either cause a temporary or prolonged stoppage of the supply owing to the mere "blowing" of a protecting fuse or out-out, or, if the circuit is over-fused, in the burning out of part of the circuit and possibly the firing of premises in which the breakdown occurs.

It is therefore of the utmost importance to be able to test the fusulation resistance of a length of cable, main, or circuit, either when no current is flowing through it or when the supply is in actual progress and the main or circuit "aliee," as it is usually termed.

A number of different methods have been devised and are in general use for measuring the insulation resistance of both "dead" and "five" cables and systems, and in the following pages devoted to this question some of the principal and common ones in use will be considered. Before, however, proceeding with actual methods of measurement it may be profitable to make some general remarks.

Electrical cables and wires are in the first place tested for their insulating qualities by the manufacturer prior to being sent out to the purchaser, but the latter should test them also himself, both before and after laying, to make sure that no faults have developed, and of course periodically during use. Such a mode of procedure is of the utmost importance if efficient working and maintenance is to be obtained, for it is quite possible for a cable to be accidentally damaged during laying and a subsequent fault to develop at this point, due to the strain of working conditions, which will finally break down the cable.

(41) Measurement of the Insulation Resist ance of Electric Light Cables by the Direct Deflection Method.

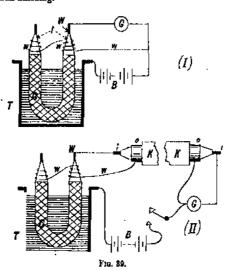
Introduction.—The ordinary Post Office form of Wheatstone Bridge will measure resistances up to 1:111 megohms, though even at this maximum limit the measurements are not very accurate, owing to the resistances of the arms of the bridge being so widely different from one another; consequently it is unsuitable for measuring insulation resistance, which almost invariably amounts to much higher values, often of the order of hundreds of megohms. The present method of direct deflections, which is also termed the "simple substitution" method, is the most accurate fit such cases and often the most convenient one to employ. The principle of it consists in comparing the deflection of a galvanometer needle caused by a given E.M.F. through a known standard high resistance in series with the galvanometer, with the deflection produced by the same E.M.F. working through the insulation of the cable to be tested substituted for the standard resistance.

Preparation of Cable for Test.—This must be carefully done and is of the utmost importance if the true insulation resistance of the dielectric is to be found, as the difference between the results obtained with properly and improperly prepared ends is very great. The method of doing this should be as follows—

- (a) For vulcanized india-rubber cables, the braiding, tapes, or other covering should be removed for at least six inches from each end down to the surface of rubber covering, care being taken in doing this not to cut or otherwise injure the rubber covering still loft.
- (b) Wash this rubber surface with naphtha and scrape with a clean knife to remove any foreign material still left on the surface, and in this way so get a clean, fresh surface.
- (c) Taper the rubber with a clean sharp knife for about 1" to 2" from the end, and then carefully dry the whole of the prepared and over a spirit flame without burning the rubber.
- (d) Paint or coat the whole of the prepared end with three or four coatings, one after another, of clean paraffin wax, melted to a temperature not exceeding that of boiling water. This can be

ELBOTRICAL ENGINEERING TESTING

done by placing the can of wax inside one of boiling water, whereas, if the wax is melted over a flame, it may be allowed to burn, and its insulating properties partially destroyed. As each coating of wax will have set before another can be got on, the whole cable end will be eventually scaled by a considerable thickness of the wax, which being much less hygroscopic than rubber, will not allow moisture to accumulate and so impair the prepared end. In lieu of wax the prepared end may be lapped with pure clean warm rubber tape well stretched, but this is not so good as the wax finishing.

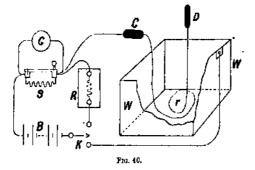


A better and much more expeditious way of eliminating errors due to surface leakage over the ends of a cable which is being tested for insulation resistance, than that just described of carefully tapering the ends and coating them with parafin wax, is to employ an ingenious device known as Price's guard-wire. This, when properly applied, gives complete protection from errors due to end leakage in the direct deflection method, where the cable

ends are close to the gulvanometer, and, consequently, the connecting wire between cable core and galvanometer is air insulated.

In the case of other methods, such as the loss of charge test, extra precautions are necessary to avoid errors (vide *Phil. Mag.* vol. xlix. pp. 343-7, April 1900).

If the cable ends are close to the galvanometer then Price's guard-wire device in its simplest form is shown in Fig. 39 (I). It is a lead-lined tank of water in which the cable C to be tested, for insulation resistance, is immersed. The ends of C are prepared with a long clean taper (t) from the core W, so as to give a long clean surface of insulation exposed to leakage. A thin copper guard-wire (w) is wound two or three times round the tapered part rather nearer the outer braiding than the core W and connected as shown to the galvanometer C and high voltage battery



B. If now the resistances of the taper surface (t) are large compared with that of G they will all be at the same potential, and we shall have no lookage, but if any leakage exists (r) will tend to keep up the potential of W, the deflection of the galvanomater G being now reduced in the ratio $\frac{a}{a+b}$, where a and b represent the conductivities of G and t respectively. Consequently the correct result will be $\frac{a+b}{a} \times$ deflection.

It will, however, be evident that in some cases the cable ends

cannot be brought up close enough to the galvanometer in order to have an air insulated wire connecting G and W.

The simplest and best way of getting over this difficulty is that, suggested by Prof. Ayrton and Mr. T. Mather and represented in Fig. 39 (II). The inner conductor (ii) of a concentric wire (K) is used to connect W and G, the outer (oo) connecting (*) with junction of G and B as before. Now if oo has a high insulation resistance compared with the internal resistance of the testing battery B, complete protection is afforded against surface leakago, even though KK is lying on the ground,

Apparatus.—Sensitive high resistance Thomson astatic reflecting galvanometer G with its box of shunts S; known standard high resistance R; unknown insulation resistance (r) of cable to be tested; well-insulated battery B of either Leclanché or secondary cells capable of giving an E.M.F. of from 100 to 500 volts; two-way highly insulated spring tapping key K (p. 586); suitable lead-lined water-tank W. If the "lead" or cable to be tested is small enough, it may be run direct from the key K into the water-tank W (clear of everything) and coiled up under water, the free end being carefully kept dry and left standing upright, about 12" out of the water, as indicated at D.

The tank should contain ordinary cold tap-water at a temperature of about 70° F., and the cable to be tested should be allowed to soak in this for 24 hours before the test, with its end trained up in mid-air above the water some 12" or so.

If the cable is too large to be taken up to G, a short well-insulated G.P. covered wire must be tisd on to it at C, and the joint insulated as at D. In all insulation tests at least the working pressure which the cable is to be subject to should be used to test it with.

The known standard high resistance may preferably consist of a metal megohm, but in lieu of this costly piece of apparatus, a carbon megohm, checked against a metal 100,000 chm coil occasionally, will do quite well, and costs only a few pounds. It must, however, be borne in mind that such a resistance slowly alters its value with time and temporature, so that the temperature abould be noted each time it is checked by the present method.

Note.—To avoid damaging the galvanometer, which is a very

¹ Or the Ayrton and Mather Universal Shunt-box.

delicate one, the shunt-box provided with it must always be used in the way indicated below.

- Tests.—(1) With the lever switch or short circuit bar of S down, thus short circuiting the galvanometer terminals, and also with the shunt-plug in the $\frac{1}{249}$ hole, connect S up to G first, and then the rest of the circuit as indicated in Fig. 40, and adjust the spot of light to zero by means of the controlling magnet.
- (2) Remove the short circuit in S, and, with the viv shunt plugged up, gently tap K for a fraction of a second so as to complete circuit through the standard known resistance R; if the deflection is inappreciable, release K to plug up the viv shunt, and again tap as before, and so on until a convenient steady deflection d_x is obtained. Note this and the shunt S_x in use at the time (if any).
- N.B.—The key K must always be released before altering the shunt S.
- (3) See that the short circuit lover of N is down so as to short circuit the galvanometer terminals, and that the with shunt is in. Now close K through the insulation resistance, and after about half-a-minute open the short circuit switch.

Note.—If this method of proceedure is not followed a sudden ballistic rush of current may ensue through G_i just at first, from the high lattery E.M.F., into the cable, owing to this latter acting as a capacity, i.e. condenser, and thus damage the galvanometer. At the end of one minute note the steady deflection d_r , and with the key K still closed, again at the end of every minute up to between five or ten, say.

If without the wire connecting K and W there is leakage from battery and galvanometer which gives a deflection d_{rr} . Then $(d_r + d_{rr})$ or $(d_r - d_{rr})$ must be used instead of d_r simply, according as to whether d_{rr} is opposite or in the same direction as d_r respectively.

(4) Repeat 2 and 3 for about 3 or 4 pairs of deflections if possible in different parts of the scale, with R and r, by altering S, and calculate the insulation resistance (r) from the formula below, and tabulate as followsNAME ... DATE ... CANA.—Insulating material ... Resistance of Galvanomoter G= ... ching G ... Rise of copper same ... S. W. Q. ... Handard R= ... G ... G ... G ... G ... G G G ..

ngth immersed L = ... Miles, no of jamersion = ... Hours. Temperature = ...

B.M.P.		darê Knor kedatanca,	4 D	Unknown Implation Resistance.				
med.	In ohma R.	Deficetion	Shunt.	Time in mon. from elosing K.	Daffeetkon dz	Shunt &.	r megobase.	Megohu per uph

(5) Plot a curve between time of electrification in minutes as abscisse and corresponding deflections d_n as ordinates.

Note.—If
$$S = \frac{1}{9}$$
 (say), then $\frac{S}{S+G} = \frac{1}{19}$, or $\left(1 + \frac{C}{S}\right) = 10$. Inferences.—Prove the formula mentioned in 4, 4.8.

$$d_{2}\left[R\left(1+\frac{G}{S_{2}}\right)+G\right]=d_{r}\left[r\left(1+\frac{G}{S_{r}}\right)+G\right]$$

and state what assumptions are made in deducing it.

Should it be found impossible to keep the deflection on the scale

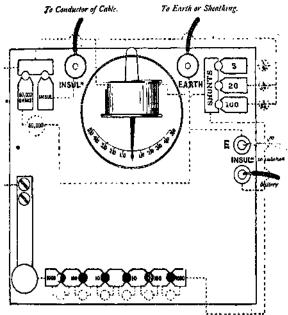
with the standard known resistance in circuit and the r_{00}^2 th shout in, using the full bettery E.M.F., then employ only a known fraction of this total E.M.F. (as measured by an electrostatic voltmeter) when taking a deflection d_2 with the standard, whence in the above formula we must use $\frac{V}{V}d_2$ instead of d_2 simply

in the above formula we must use $\frac{V}{v} \times d_{R}$ instead of d_{R} simply where V = full E.M.F. and v that used to obtain d_{R} . In testing short lengths of highly insulated cable at the least an E.M.F. of 300 or 400 volts should be used.

Referring to the ten 1-minute readings of deflection in observation 3 above, the deflection will fall rapidly at first and then more slowly. This is not due to increase in the insulation resistance, as it might appear to be, but to dielectric absorption in the cable through this acting as a condenser.

This particular test is a good one for developing a fault which would pass observation in a test of 1 minute's electrification, in which case there would oither be an irregular—or no—crawling of the deflection in the 10 minutes.

Insulation resistance is usually specified in megohns per mile at 70° F, after 24 hours' immersion and 1 minute's electrification at some definite voltage. It is necessary to record the temperature at the time of the test, as the insulation resistance decreases as temperature increases.



Connections for Testing Insulation Resistance.

(42) Measurement of Insulation Resistance by the Silvertown Portable Testing Set.

This is a measurement of the electrical resistance of the insulating material of a cable to the passage of a current from the inside conductor through the insulation to the lead sheathing, wet yarn, armour, or other outside conducting surface, and the inverse of the insulation resistance is generally termed the leakage. This measurement is effected by a method known as that of direct deflections. It consists in passing a current from a battery through a galvanometer into a conductor of a cable whose farther, end is free and disconnected, thence through the insulating material to the outside coating or earth, and so back along a temporary conductor to the other end of the battery, the deflection of the galvanometer needle produced by this current being noted. Replacing that part of the circuit which was formed by the insulating material of the cable by a standard resistance of known value, we obtain a new deflection of the galvanometer needle.

The diagram Fig. 41 shows only those parts of the apparatus and their connections that are used in this measurement; those which relate only to the measurement of conductor resistances being omitted.

The arrangement, it will be seen, is as follows:—One pole of the battery—the battery of Leclanché cells giving an E.M.F. of about 100—209 volts is normally employed—is connected by a conductor, ending in an ebonite-headed plug, to the lower of the two plug-holes marked INSULF. Thence the current passos along a connecting wire to the block marked SHUNTS, and thence through the galvanometer to the upper block on the other side. We may observe in passing that these two main blocks, one on each side, are practically the terminals of the galvanometer. If a shunt is plugged, 1th, 75th, or 105th only of the current passes through the galvanometer, the remainder finding its way through the corresponding shunt coil.

From the upper block on the left hand side the current may take two paths, according as the hole marked insula or that marked 50,000 ohms is plugged; if neither is plugged, the circuit is broken, and no current can pass. This plug forms consequently a convenient make and break key. If the hole marked insula is plugged, the current passes to the terminal marked insula is a through the insulating covering of the cable to the outside sheathing or earth, back to the terminal marked earth and the plug-hole marked E, and then along the lead to the other pole of the battery. If, however, the hole marked 50,000 ohms be plugged, the current will pass through the coil of 50,000 ohms, then along a connecting wire to the plug-hole E, and so back to the battery.

In beginning this test the conductor of the cable, or insulated wire, or a temporary lead attached to it, is connected to the terminal of the instrument marked INBUL*, and another lead, connected to the outside sheathing of the cable, or the wet soil in which it lies, is attached to the terminal marked EARTH, care being taken that these leads are separated, and that no circuit exists between them except through the insulation of the cable. It will be observed that when all the holes in the straight

commutator near the front of the box are plugged, the key on the left-hand side, which is used in the bridge test as a gulvanometer make and break key, becomes for the insulation test a short circuit key, and is useful for checking quickly the oscillations of the needle.

N.B.—Although the maximum voltage of the testing battery usually employed with this testing set is only 100 volts, the set can be used with a testing voltage of 200 volts, as required by the Board of Trade regulations. In this case, instead of using the multiplying power of 20 as described above, the multiplying power of 100 should be used in taking the constant—the deflection thus obtained will be the same as that which would be given by the unshunted galvanometer through a total resistance of five megchans, and the calculation of the resistance to be measured would then be made in exactly the same manner as described above, except that five megchum will be substituted for one megchan.

In making this test the following points may be called attention to—

- (1) Too much care cannot be taken in preparing the ends of the cable. Since we are measuring a very small current of electricity passing from the conductor to the outside sheathing, through the insulated covering, it is clear that our results will be entirely misleading if any current be allowed to pass over a dicty surface at the ends where the conductor is exposed. These ends should be looked to before testing, and in the case of india-rubher or other firm material, the section of the insulator should be pared all over with a sharp and perfectly clean knife. For methods of preparing the ends see pp. 99—100.
- (2) Care should be taken not to short circuit the battery, which may easily occur in two ways. One is by allowing the two battery plugs to touch one another, when the other ends of the loads are

attached to the battery terminals; and another is by allowing the lead attached to the earth terminal to touch that attached to the insulation terminal.

In both cases the lattery of small cells will be for a time much overworked, and in the second the needle may become bent or demagnetized.

(3) Another point that may be noticed is that in deducing the insulation resistance per statute mile from a test on any given length, the result obtained from a test on the latter is to be multiplied by the length of the piece in miles, and not divided by it.

For example, if the insulation of a cable three miles long be 15 megohms, the insulation per mile will be 15×3 or 45 megohms; or again, if the insulation of a piece of cable, whose length is 350 yards, be 7520 megohms, the insulation per statute mile will be $\frac{7520\times559}{17\,30}$ megohms = 1495 megohms.

If the galvanometer deflections are proportional to the currents producing them, and the E.M.F. employed is constant throughout the whole test, then we have current α deflection α

 $\frac{1}{\text{total resistance}}$; or if R_I = insulation resistance tested and d_I = deflection through it, and if R_S = standard known resistance and d_S = deflection through it, then

$$\frac{R_I}{R_S}\!=\!\!\frac{d_S}{d_I}$$
 whence $R_I=\!\frac{d_S}{d_I}\,R_S$ megohus,

where R_R = the standard resistance in megohns.

If however the salvanometer is shunted with

If, however, the galvanometer is shunted with, say, a $\frac{1}{4}$ shunt, for example (with the insulation), so that only $\frac{1}{4}$ of the main current goes through it, then, since without the shunt the deflection would be five times as great, we have

$$R_I = \frac{d_S}{5d_I} R_S$$
 megohms.

Thus, for example, suppose that a given battery produces on the needle of a galvanometer placed in series with the insulation of a cable in the manner described, a deflection of 10.3 divisions, and that on substituting a resistance of one megohm for the insulation we get 42 divisions, we find that the insulation resistance is $\frac{10.9}{10.9} = 4.1$ megohms approximately.

. Again, for example, suppose that the current from the battery

when passed through a constant resistance of 50,000 ohms gave a deflection of 42 divisions on a galvanometer shunted to $\frac{1}{10}$, and that when passed through the cable insulation it gave 23 divisions with the galvanometer shunted to $\frac{1}{1}$, the insulation resistance would be $\frac{49}{1000}$ megohms ≈ 37 megohms approximately.

In cable testing the battery employed should in all cases give an E.M.F. at least = the working voltage under which the cable works. The terminal marked Earth on the right of the galvanometer must be connected to earth (i.e. nearest gas or water-pipe) or to the water of the tank if the cable is being tested in such.

Tests.—(1) Connect up precisely as in Fig. 41, and adjust the galvanometer needle to zero.

- (2) Now take the "constant" of the galvanometer by plugging the 50,000 ohm hole and the $\frac{1}{20}$ shunt and note the steady deflection d_B . This is the same deflection as that which would be obtained with the same E.M.F. through $(50,000 \times 20) = 1,000,000$ ohms, or 1 megchm for no shunt at all.
- (3) Flug up holo marked INSULE. instead of that in 2, and adjust the shauts (if necessary at all) to obtain a steady deflection d_I, preferably as nearly = to d_S as possible.
- (4) Calculate the insulation resistance from one or other of the preceding formula and note for reference merely the E.M.F. used in the test.

N.B.—If the cable has been scaking in a water-tank note the time of immersion and the temperature of the water. Also the number of yards immersed.

Insulation Resistance of Electric Light Street Mains and House Installations.

Introduction.—Mains.—Seeing the extreme importance of maintaining continuously, and without any intermission of any kind, the supply of electrical energy from a central station when once commenced, it should be the ondeavour of any engineer to obtain and lay the best possible class of cables in the most efficient, thorough, and lasting manner in his power. The item of mains in the supply of electrical energy is a very serious one

hours.

at the best, and usually amounts to something like from \(\frac{1}{3} \) to \(\frac{2}{3} \) of the cost of the whole undertaking.

Notwithstanding this, however, the best possible main only should be laid if the system is to be a lasting one, free from perpetual worry to the engineer, of cables breaking down and the consequent temporary discontinuity of the supply. The insulation, jointing, and laying should be the best it is possible to obtain, for even in localizing a fault the accuracy of the test will greatly depend on the goodness of the joints.

There are roughly speaking three tests, which should be carried out on any new cable or main, namely—

(a) The insulation and copper resistances of each cable drum as soon as it arrives from the manufacturers. This can only be done satisfactorily under a pressure of at least double that which the cable will work at in practice, and with the whole cable drum wholly immersed in water at about 70° F, the ends being carefully kept dry, trained out of the water and prepared in the manner described on p. 99. Reliable results cannot be obtained from a well-wetted drum, only from one wholly immersed for 24

The insulation resistance should be obtained by the "direct deflection" method after one minute's electrification (i. e. application of the battery), and again at the end of every succeeding minute for some ten minutes.

The first reading will give, or should give, at least, the specified insulation resistance of the maker.

The second and subsequent readings are extremely useful in showing the existence of undeveloped faults in the cable insulation, which would in the usual course of events pass the specification in the one-minute test unnoticed. Should the insulation be faulty, the galvanometer deflection will hardly fall at all after the first minute's electrification, or may fall in irregular jumps. The resistance of the cupper core should be taken and noted down, as well as the length of the cable on the drum.

(b) The insulation and copper resistances during laying both before and after jointing in the following manner:—A careful test should be made on the first section of the line, one end of which we will assume is in the station when laid, but before any joint is made, and with both ends carefully prepared (see p. 99). If satisfactory, it will show that no damage has been done to it in the laying operation,

The second section is then laid and carefully but temporarily is connected to the first section by a piece of lead. These two adjacent ends and the far end of section 2 are carefully prepared and the two sections tested. If the insulation resistance per mile is up to specification, section 2 is all right and can be now jointed to 1 and the test repeated. If not the same as before the first joint is defective and should be re-made. Now lay section 3 and again test as before, and so on; thus, finally, the whole line will have been tested section by section as the laying proceeded, and, lastly, as a whole. In this way a record of all the tests will be to hand at any future date, while any damage done in laying, or any badly-made joint, will be at once detected by fall in the insulation resistance per mile, and a rise in the conver resistance per mile.

(c) Duily tests (while working or otherwise), the precise method of performing which will depend on whether the main is a high or low tension one.

A fault occurring should at once be localized and remedied. If on a "feeder" it can easily be found, but if on a distributing main, sectioning off may be necessary to localize it.

The apparatus requisite for these tests is the same as that enumerated on p. 101, and with which the testing-room of every station should be provided, in addition to other instruments.

The minimum insulation resistance for low tension cables at 100 volts is about 300 megohms per mile after 24 hours' immersion and one minute's electrification. In high tension cables at 2000 volts it is about 4000 megohms per mile under similar conditions.

Ordinary Installations.—Many of the preceding remarks apply here. For example, it is much more economical in the long run to wire a building with high-class insulated wires and leads as also with good fittings having fairly high insulation.

¹ The insulation resistance per mile = measured (total) resistance × the length in miles tested. This arises from the fact that the leakage current through two miles is twice that through one mile, assuming, of course, that no appreciable fault exists anywhere along the length of cable.

when we consider that every lamp switched on brings one or more fittings, such as a lump-holder, cut-out, switch, ceiling rose, etc., into active use, thereby adding so many additional parallel paths of surface leakage through which current can leak This in other words means a diminution in the away to earth. total insulation resistance of the whole installation, and which is considerably aggravated by damp weather, dust and dirt, etc. With respect to leakage of current, the rule given by the Institution of Electrical Engineers is that the total leakage should not exceed zooth part of the total working current, Numbers of different rules and regulations are given by the various Fire Insurance and Supply Companies. As an example of the latter we may cite the rules of the Edinburgh Corporation for installations tested at 115 volts with minimum insulation resistance.

TABLE IV.

For 12 lamps 5 0 megohms,	For 150 lamps 0:75 mogolius.
., 25 ,, 2.5 ,,	" 200 " 0·5 ",
,, 50 ,, 1·5 ,, ,, 75 ,, 1·25 ,,	,, 250 ,, 0 3 ,,
,, 75 ,, 1·25 ,, 100 1 0	,, 800 ,, 0.2 ,,
), 100 ii 10 ii	l .

The rules of the Leeds Corporation for 200 volt circuits are some 20% less than the above in the minimum insulation resistance for the same number of lamps in the respective cases.

Ordinary insulation resistance tests for installations must be taken with-all fuses "in," all lamps removed from their holders and all switches "on," with at least the working pressure for which the installation is intended, but preferably double this. It

is then advisable to make three tests as follows-

- (a) of the insulation resistance between + ** leads and earth,
- ** , ,, ,, ,, + ** and ** leads. (b) " ",
- The value in each case should not be less than that specified above or thereabouts for the particular number of lamps installed.

Usually the insulation resistance for alternating current circuits has to be greater than for direct currents, and in some regulations these are as I: 2.

The importance of testing at or even above the working pressure will be seen from the following figures by F, Uppenborn of Berlin, which show in a marked degree the way in which the so-called insulation resistance varies with different voltages.

TABLE V.

	Resistan	e por nocu	•
Terminals of sinte out-out.		Two Lwisted cotton covered wit	
Pelu. 5 10 18:6 27:9	Mryotma. 63 45	Folts. 5 10 16-9 97-9	Negokus, 281 184 184 191

This drop in the reading of insulation resistance as the volts increase will generally be found to occur with, and is due to, moisture in or on the insulation under test. The increase of voltage may either break the insulation down, or the current, due to the voltage, may partially dry the moisture out and the reading gradually rise with the time of application.

Further, in measuring insulation resistance, sudden variations will sometimes be observed, especially will such be noticeable in direct reading testing sets. This is invariably due to metallic or other conducting particles on the surface (or, very rarely, buried in the insulation) promoting surface leakage, and the rapid fluctuations are due to intermittent sparking between such particles. Thus a direct reading testing set discriminates between low-insulation due to damp, that due to dust, and that due to conducting particles, or whether the insulation is disintegrating under electric stress.

(43) Insulation Resistance of Electric Light Installations, Cables and Machinery by Evershed's Direct Reading Portable Testing Sets.

Introduction.—While there are several portable insulation testing sets on the market of both the direct and indirect reading types, we shall here consider the time-honoured form due to Mr. Sydney Evershed, which indicates the instantaneous insulation under high pressure by the direct deflection of a pointer on a scale. Thus the tests can be safely entrusted to

anyone possessing practically no technical skill who can make a report, and so enable defective work to be discovered before covering in.

The Evershed type is mule by Messrs, Evershed and Vignoles, Ltd., in two forms, namely--

- The "Mrgger" Insulation Testing Set, which is the most modern development of the early form of Evershed character and generator.
- (2) The "Bridge-Megger" Testing Set, which combines the functions of the first-named "Megger" set with those of a Wheatstone Bridge.

Both sets consist of an olummeter of the moving coil type combined in one box with a hand-driven generator for providing the necessary testing pressure and current. When the handle of the generator is not being turned, the pointer is entirely free and will rest anywhere on the scale.

The internal construction and arrangement of the chmmeter portion in both sets is the same, except for some minor additional details in the case of the Bridge-Megger set, which will be indicated later on.

We will therefore consider the use, firstly, of type (1) above, namely—

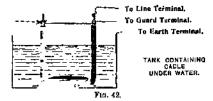
The "Megger" Insulation Testing Set.—The generator portion of this particular set may be either of the variable pressure or constant pressure kind. Unless the electrostatic capacity of the work to be tested excerds one microfarmi or so, a variable pressure instrument is suitable, which is the case for testing wiring, switch gear, dynamos and motors, are lamps, instruments and accessories. Megger insulation testing sets being ohmmeters, their readings are independent of the applied pressure. If, however, the insulation under test has a large electrostatic capacity, the reading may become unsteady, due to the capacity current, caused by the variable pressure flowing through the current roil only; but even on large capacity, once the circuit is charged, the capacity current ceases and the

For work likely to have a capacity exceeding one microfarad or so, such as the wiring in metal conduits, lead-covered cable, underground mains and a modern system of house-wiring in

reading becomes perfectly stendy.

metal conduit, which has often a considerable capacity, the constant-pressure type of set should always be used.

The type of testing set now being considered is intended primarily for the measurement of insulation resistance, and is not available for metallic resistance tests. The low-range variable pressure sets are made in three ranges of 0-10, 0-20, and 0-100 megohns with 100, 250, and 500 volts respectively (at 100 revs per min.), while the constant pressure low range



sets are made in the same three ranges together with a fourth for 0-200 megohns with 1000 volts. The high-range constant pressure sets are made in three ranges of 2-1000, 4-2000 and 4-5000 megohns with 500, 1000 and 1000 volts respectively. These last-named "Megger" Insulation Testing Sets are provided with a guard wire terminal, and, as explained on page 100, any error in tests of high insulation due to leakage internally or across the surface of the insulation under test can be eliminated, and hence the readings of the set remain unaffected, by tightly wrapping a so-called bare guard wire round the typered insulation between conductor and earth, and connecting it to the guard wire terminal as shown in Fig. 42.

To Measure Insulation Resistance by the "Megger" Insulation Set.

Observations.—(1) For both low-range-variable and -constant pressure sets, as well as for the high-range constant pressure set: place the instrument on a steady base, but not on the hedplate of, or very close to, a dynamo or notor.

(2) Connect the terminal marked LINE to the insulated copper

core of the appliance under test, and that marked EARTH to a good earth such as a water-pipe or earthplate; or for testing between, say, two insulated wires, connect one wire core to each terminal. Then—

(3) Turn the handle in a clockwise direction at a speed of at least 100 rovs, per min., at which—

In variable-pressure sets, the generator will be giving its rated or normal voltage which can be increased by increase of speed, and—

In constant-pressure sets, the clutch is felt to be slipping (for at any speed above that necessary to give slipping, the voltage will be constant). Now read the insulation resistance as given by the deflection of the pointer on the scale.

(4) High-range constant pressure sets (in addition to obs. 1-3 above) must be levelted by means of the spirit-level seen through the hole in the dial, and the index must be adjusted to infinity before connections are made to any of the terminals, by retating the handle above the clutch-slipping speed and turning the knob of the index adjuster one way or the other until the index stands exactly on the mark at infinity.

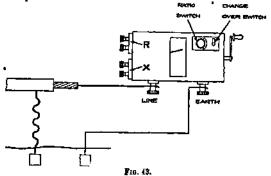
Note.—In testing circuits of considerable electrostatic capacity it is essential to maintain full speed for at least a minute before taking the reading. Further, to eliminate errors due to surface leakage, a guard wire (see p. 100) must be used.

To Measure Insulation Resistance by the "Bridge-Megger" Testing Set.

Observations.—(1) Connect up, as in Fig. 43, and turn the change-over switch to "Megger," the instrument being on a steady base and not very close to a dynamo or motor.

Note.—In all cases the LINE terminal must be connected to the insulated conductor of the circuit or appliance under test and the KARTH terminal to a good earth, such as a water-pipe or earthplate, or the equivalent. This with machines may be the framework, with conduit wiring should be the metal conduit itself, with lead-covered street main should be the lead sheathing, and for non-sheathed cable should be the water in the immersion tank, etc.

(2) The handle is then rotated clockwise just above the speed at which the clutch is felt to slip. This occurs at about 100 rova per min., while at any higher speed the voltage is constant, and the insulation resistance is then read off by the deflection of the pointer on the scale.



(44) To Measure Conductor Resistance by the "Bridge-Megger" Testing Set.

For use in this measurement, the adjustable standard known resistance box, supplied with this set, is required. Then to measure—

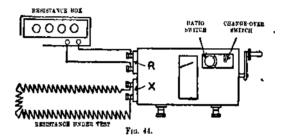
Resistances under 100 olms.—(1) Stand the instrument on a steady base and with all terminals free from any outside connections. Adjust the pointer to "infinity" on the scale by turning the knob of the index adjuster one way or the other until the pointer or index stands exactly on the infinity mark.

- (2) Connect up as in Fig. 44, set the change-over switch to "Bridge," the ratio switch to 10 or to 100, and all the resistance box dials to zero.
- (3) Rotate the handle slowly clockwise with the right hand, when the pointer will float off the scale on the side marked "increase R" above the line marked G, simultaneously with the

left hand raising the value of R by turning the resistance box switches until the pointer exactly covers the line G.

(4) Now rotate at full speed to give maximum voltage and hence sensibility, readjusting the box resistance R_i if necessary, to keep the pointer on the line C.

Then the resistance tested = the value of $R \div 10$, or by 100, whichever is in use.



Resistances from 100 to 9999 ohms.—(5) Operate tests 1-4 above, except that in (2) the ratio switch is now set to I instead of to 10 or 100 as above. Then the resistance in the box required to balance the pointer exactly on the line (f is now the value of that under test.

Note.—When measuring field coils of dynamos and motors, or other metallic resistances of large self induction, the generator must be driven above the speed at which the clutch slips to ensure the current being constant in the arms of the bridge.

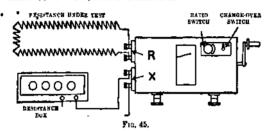
Resistances from 10,000 to 999,900 ohms (by "Bridge" method).—(6) Operate test (1) above.

(7) Connect up as in Fig. 45, set the change-over switch to "Bridge," and the ratio switch new to 10 or to 100.

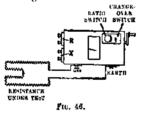
Note.—It will be observed that the connections of the unknown resistance and box to the testing set in Fig. 45 are just the reverse to those of Fig. 41.

(8) Operate tests (3 and 4) above, remembering that the directions "increase R" and "decrease R" are now also "

reversed, and that the unknown resistance now = box reading to balance × 10 or 100, whichever ratio is in use.



Resistances from 10,000 ohms and upwards (by "Megger" method).—This method is more rapid, but less accurate than the last, and is operated exactly as for Test No. 43, p. 115, the connections being as in Fig. 46.

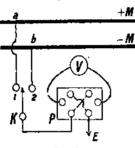


(45) Measurement of the Insulation Resistance of a Complete Electric Light Installation and plant while working.

Introduction.—The insulation resistance of any system of distribution of electrical energy when not working can be determined by one of the preceding methods. These are, however, inapplicable to systems actually running, and consequently "alive" at the full working pressure. It is most important to make frequent, if not daily, tests of the insulation resistance of any installation in order that a gradually developing fault, which

would cause the insulation resistance of the whole system to gradually fall, might be discovered in time and remedied before it perhaps burnt itself out and fired the premises.

The following method is a simple and convenient bne for making such a test on any system, whether that of a country



Fra. 47.

house, having its own generating plant or the main distributing network of a large town. The arrangement is shown in Fig. 47, where + M and - M are the positive and negative mains or wires of a two-wire system of direct current distribution.

The contact studs 1 and 2,

The contact stude I and 2, of a two-way key K (p. 586), are electrically connected (temporarily or otherwise) to

any points a and b of these mains, which might be the + and -'bus, bars on the switch-board. The common terminal of K is connected through a Pohl's commutator (p. 584) or other reversing key P to earth E (i. s. nearest gas- or water-pipe). By means of P, a voltmeter (P) connected to P has its terminals interchanged between K and E on moving P over so as to reverse. Thus a current flowing either from K to E or E to K can be made to give a deflection in the same direction on V by manipulating P. If this latter is used it can be converted into a reversing key by cross-connecting the four mercury cups, as shown by separate connectors indicated by the dotted lines; both K and P should have a good insulation resistance; V should be a + and - instrument, preferably of the moving coil D'Arsonval type. It may either be a voltmeter or ammeter, but we shall assume the former in the present case.

Observations.—(1) Connect up as shown and put K to stud 1, P being such as will allow V to deflect over the scale. Note the reading V_1 on the voltmeter.

(2) Put K to 2 and reverse at P so as to still make V read on the scale. Note the reading V_2 .

(3) Calculate the insulation resistance of the whole lighting system (including dynamos, battery, leads, out-outs, lamps, etc., etc.) from the relation—

$$R = r_r \left(\frac{V}{V_1 - V_2} - 1 \right)$$
 ohms;

where r_* = the resistance in ohms of the voltmeter, and V = the working pressure at the time across + M and - M.

The insulation resistance of the + main is

$$R_1 = \frac{r_x \left[V - \left(V_1 - V_2 \right) \right]}{-V_x}$$

and of the - main is

$$R_{2} = \frac{r_{1} \left[V - \left(V_{1} - V_{2} \right) \right]}{V_{1}}.$$

Since V_1 and V_2 are to opposite sides of zero, or on the same side by reversing at P_1 they must be added; r_* should not be too large, but its value depends on the insulation resistance tested. If this be 100 chms or so, r_* might be of the order of 1000 chms. Since the value of P_1 , P_2 and P_3 in ordinary small installations is usually high, i.e. considerably over 1000 chms, a voltmeter may be used having a resistance (r_*) of, say, 5000 to 10,000 chms.

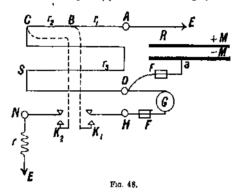
Inferences.—Why is an electrostatic voltmeter unsuitable for use in the above test?

(46) Measurement of the Insulation Resistance of Complete Electrical Installations and Distributing systems while working.

Introduction.—The following method is one of the most accurate for measuring the insulation resistance of a system taken as a whole, but it does not give any idea as to which main a fault may be developing. It is really an application of Mances' method for determining the resistance of a conductor containing an E.M.F., and entails the use of preferably an ordinary Post Office pattern Wheatstone Bridge, with its detecting moving needle galvanometer G (p. 571) and an extra-resistance (r) for eafety. Fig. 48 shows the sketch of connections for the test, where +M and -M are the mains the insulation resistance R of which it is desired to measure; E represents earth (i.e. the nearest gas- or

water-pipe); FF are protecting fuses. The P.O. Bridge is represented symbolically by the zigzag lines A, C, S, D, which indicate the rows of plugged resistance coils.

Observations.—(1) Connect up as shown, joining the bridge terminal D to some point (a) on the distributing system to be



tested; r may be a few chms or that offered by half-a-dozon or more glow lamps in parallel.

- (2) With the proportional arms r_1 and r_2 arranged so that $r_1:r_2$ is as small as possible in order to obtain the adjustable arm r_3 large, close K_1 and then bring back the galvanometer deflection, thus produced, to zero by means of the controlling magnet.
- (3) Then with K_1 closed after r_2 so that on opening and closing K_2 no motion of the galvanometer is observed. Then the insu-

lation resistance of the system as a whole is $R = \frac{r_1}{r_8} r_8$ ohms.

Note.—This method can be employed in the case of alternating current systems at work by placing a few cells of a battery in place of (r) and using a gulvanometer that will not indicate alternating currents. The mode of procedure is then the same as before.

(47) Measurement of Insulation Resistance and detection of faulty Telegraph Insulators.

Introduction. —It is of paramount importance that all insulators intended for use on telegraph or telephone lines should be tested prior to their crection in the circuits. This will at once be evident when it is remembered that the insulators, supporting a line having an "earth return," form so many parallel circuits between the line and earth, and though the resistance to leakage of current of each insulator may be very great, yet their parallel resistance to the same may be very considerably less, allowing a very appreciable current leakage to go on to earth continuously. This, especially in telephone circuits, is very troublesome, causing the lines to interfere with one another, and besides this, speaking generally now, it gradually wastes away the batteries of cells used in working the lines. Again, the insulation resistance of a "line," composed of all very good insulators except one, will be lowered by the one single faulty cup to a value less than that of the faulty insulator.

Hence the importance of preventing, by a suitable and timely test, the installation of a bad insulator, which is generally found to deteriorate rapidly with time. Insulators should be tested. profembly before the bolts are inserted in them, and with an E.M.F. of from 100 to 300 volts after from 24 to 48 hours' immersion in a suitable manner in water. The value of the results of such a test will depend, however, very greatly upon the exact method of preparing the insulators and of applying the test, and some precautions have to be attended to in order to obtain a result which is trustworthy and fair to the insulator itself. The minimum insulation resistance which each insulator ought to possess depends on the length of the line on which it is to be used. In this country, during the worst wet weather conditions, it has been found possible to maintain a minimum insulation resistance of 1 megohm per mile on air lines, which is therefore taken as the minimum maintenance standard. Now the number of poles, and therefore insulators per mile of line, varies from 20 to 30 according to whether it is a branch or trunk

line. Hence, allowing the latter number, each insulator should have a resistance of at loast 6 megohms if the line were only one

mile long, 60 if 10 miles long, and 600 if 100 miles long, and co on, in the worst wet weather. As a matter of fact the resistance

of a double shed or cup porcolain insulator, if a good one, may vary under testing conditions from 500,000 megohns to something like 4,000,000 megohus. Apparatus.—Shallow trough T lead-lined inside, to which is

attached the terminal N making contact with the lead; insulators to be tested I, Io, etc., only these two being shown; battery B capable of giving 100 to 300 volts E.M.F. and consisting of

either Daniells, secondary or other convenient cells; very sensitive high registance reflecting galvanometer G with its shunts

(S); high insulation two-way key K (p. 586); high insulation test rod t connected to K by a well-insulated length of guttapercha covered wire; standard megohm r.

N.B.—In this and all other similar high resistance tests, the connections should be in mid air as much as possible, and all insulating material quite clean and free from dust and finger-

Assuming all the insulators to be perfectly clean on the inside and outside of their sheds, there are two modes of procedure, in

each of which they are immersed in the trough T with the water up to within half-an-inch of the lips of their outside walls, Thus-(a) The whole of the inside of each insulator kept clean and

dry, the resistance then from bolt (b) to water being very approximately their insulation resistance under working line conditions. This is usually so high that the galvanometer is not sensitive enough to indicate the extremely small current passing

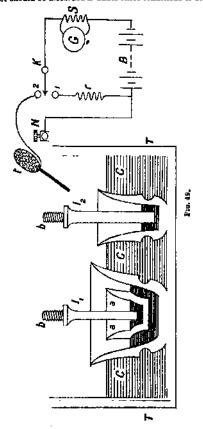
unless the insulator is actually deflective. If it is all right the

only way usually to obtain a deflection is to test from 100 to 200 in parallel at one time. (b) The inside of the shed or sheds carefully filled with water

marks.

by means of a pipette to within half-inch of the lips, the resistance now from bolt (b) to outside water showing whether the insulator is faulty through the leakage current passing through its substance, assuming the unimmersed lips to be dean and dry. The

insulator should be discarded if under these conditions it does not



show 600 megohms at least, preferably 2000, which is the minimum in some telegraph services.

In the following test we shall adopt the latter mode of testing, since the former is in most cases impracticable.

Observations.—(1) Carefully clean the perceloin or earthenware portion of each insulator, especially the lips, with clean cold water. Then dry the lips merely in a place free from dust, and place them with their helts pointing upwards (Fig. 49) in the tank T, packing up the smaller ones so that all the lips are at about the same level, but not touching one another.

- (2) Now your water into T to within half-inch of the lips and into the cups, by means of a pipotte, to the same level. Then allow the insulators to soak for about forty-eight hours (in a place free from dust), so that the water will percolate or soak into any cracks or flaws in the mass of the earthenware.
- (3) Before testing, hold a hot from close over the rims of each insulator for a short time to dry off any moisture, as it is necessary that THESE PARTS SHOULD be QUITE DRY. For this reason avoid testing on a damp day, unless the air of the room is dry.
- (4) Connect up as shown in Fig. 49. Test the insulation of the connections between t and k before each set of observations. This will be satisfactory if G does not deflect when the connecting wire is supported in mid-air when t is held in the hand.
- (5) With the galvanomotor at zero and the χ_{00}^2 th shunt in, close K1, so as to bring τ into circuit, and note the steady deflection (d), then close K2 (opening K1) and touch the bolt of each insulator successively with t, noting the deflections D in each case if any.
 - (6) Repeat 4 and 5 for the $\frac{1}{\sqrt{10}} \frac{1}{\sqrt{10}}$ and no shunt if possible.
- (7) In the case of the double-shed insulators, such as I₁ (Fig. 49), touch the water between the sheds with t, thus obtaining the resistance of the outer shed. Next connect metallically the water between the sheds, and also that outside, and touch the bolt with t, thus getting the resistance of the inner shed.
 - (8) The approximate resistance of all those insulators which show an extremely high insulation can be obtained by paralleling them or joining their bolts together metallically, and then

taking a reading (as in 6), first with the $+^{rs}$ of the battery to T, and second with the $-^{rs}$ to T, the insulators being discharged in between the two reversals. Calculate the average of each insulator from the combined or parallel resistance so obtained.

(9) Employ the formula given below, or its modification, and tabulate your results as follows—

istriction best active a Online ac C. Tutte lust issitted, stellet						. = UIIMS.		
funktator After	Distance of Water	Temp.	ЕМЕ	Shunt	Defic			inanin Remat
	from Lay		uspi.	s.	known 4.	unknown D.		
	-	 - - - - - - - - - -		_	ļ			

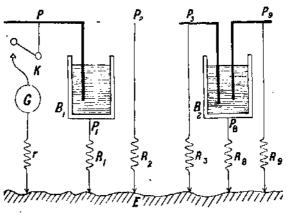
$$\begin{split} d\left\{r\left(1+\frac{G}{S_r}\right)+G\right\} &= D\left\{R\left(1+\frac{G}{S_R}\right)+G\right\}. \end{split}$$
 If $S=\frac{1}{b}$ (say), then $\frac{S}{S+G}=\frac{1}{16}$ or $\left(1+\frac{G}{S}\right)=10.$
 If no shunt is used $S=\infty$ and $\div\frac{G}{S}=0.$

(48) Measurement of the Insulation Resistance of Storage Batteries.

Introduction.—In the erection of a storage battery, provision is made for the efficient insulation of every cell composing the battery, from earth, by supporting each on suitable insulators, and keeping the cells from touching one another. Notwithstanding these precautions, leakage of current, from various causes, may go on in a greater or less degree. It may occur in different parts of the battery, or in the leads running from the battery, and the resistance opposing the leak may, and usually does, have different values at different parts of the battery; in other words, the partial "earths" at the various points are of unequal resistance, which prevents the insulation resistance being obtained by an ohumeter or other portable testing set.

The difficulties thus met with are got over by employing the present method due to Mr. E. S. Jacob, and which at once gives the joint resistance of all the earths at whatever points of the battery they may be located. Apparatus.—Sensitive high resistance galvanometer G; adjustable known resistance box (r); battery $B_1 \ldots B_s$ to be tested, there being any number of cells between the two B_1 and B_2 shown. Key K of very good insulation (p. 586), battery stands, or equivalent earth E.

N.B.—Earths or partial ones, i. s. leaks, may be assumed to



F16. 50.

occur at points $PP_1 \dots P_9$, etc., and $rR_1 \dots R_9$ to be the respective resistance of such earths.

Observations.—(1) Connect the key K, galvanometer G, and resistance box (r) to the battery system at any point P, as shown in Fig. 50, E being earth, i.e. the nearest gas- or water-pipe, and adjust the galvanometer needle to zero.

Note.—Choose the point P, so that a conveniently large defiretion is obtained on G, for it will be found that there is a certain point of minimum potential from which it increases on either side as the contact is moved one way or the other.

(2) With r=0, press K and note the current Co and, for reference only, the relative position of the point of contact P on the system.

- (3) With everything the same as in 2, adjust (r) so that on pressing K the new current C_r on G is about ½ C_G. Note the presistance r and this deflection or current C_r.
 - (4) Repeat 1-3 for two or three different values of r.
 - (5) Repeat 1-4 for two or three different points of contact P.
- (6) Calculate the insulation resistance of the whole battery from the relation—

$$R = \frac{C_r (q+r) - C_Q q}{C_Q - C_r} \text{ oloms,}$$

and tabulate as follows-

Relative position of P.	Yalue of y Oldna,	Current Co	Current G-	Institution Heart succ A Ohma
	- 			, <u>-</u>

Inference.—Prove the relation given in 6, and state any assumptions made in obtaining it. On what does the accuracy of the test depend?

(49) Insulation Resistance of Dynamos and Motors.

Introduction.—Since the total amount of leakage from a system of electrical distribution depends on the number of appliances connected to the system, which represent so many parallel paths for leakage currents to take, it is of great importance to increase the resistance in these paths, and so diminish, as much as possible, such currents. This, in other words, means that the insulation resistance of all appliances on the system should be as high as possible. Hence it becomes of importance to carefully measure the insulation resistance of motors and dynamos, both in course of manufacture and when installed before running is commenced.

The Institution of Electrical Engineers recommends that the leakage current should not be allowed to exceed $1\sqrt{3}$ th part of the maximum current in the system at full lead. As a general rule the total insulation resistance of all the insulated parts of a dynamo or motor, joined together, from the frame of the machine,

i.e. carth, should be at least equal to that of the rest of the circuit which it has to run on, but preferably much greater. The present test is a simple and convenient one for obtaining the insulation resistance of, say, a dynamo, and is as follows—

Observations.—By means of a high resistance voltmoter of resistance R_0 ohms measure the P.D. V at the terminals of the machine when running at normal voltage not connected to any circuit. Also measure the P.D.s V_1 and V_2 between the + and - brushes and the frame of the dyname. Then we shall have—

Total insulation resistance of the machine

$$R = \frac{V - (V_1 + V_2)}{V_1 + V_2} R_{\bullet}$$
 ohms.

(50) Localization of Faults in Electric Mains. (Murray's Loop Method.)

Introduction.—In the preceding pages, some of the best and most important methods of measuring the insulation resistance of electric mains have been dealt with, but the localization of the position of any prominent and serious fault in such is a matter of equal, if not greater, importance. The insulation of the cable may or may not have broken down at the fault, but obviously in either case, since the opening up of the duct in which the cables are laid is often a serious matter in a busy thoroughfare, it is important to be able to localize the position of the fault to within a very few feet.

There are two important methods or systems of localizing faults, each comprising modifications of the principles employed, viz.—

(A) "Loop" methods. (B) "Fall of Potential" methods.

The latter, though extremely simple, are less easy of application than the former, and must be applied so as to suit the conditions of the particular fault. Loop methods are much more generally applicable, and are preferable for the following reasons—

- (1) They are "null" or "zero" methods.
- (2) They are easier to work.
- (3) The accuracy is not affected by variations of the fault resistance.

(4) The test is performed in the same way for mains of any section and whatever the fault resistance.

We shall therefore restrict ourselves to one of the best of these loop methods, but before taking it is detail there are a few remarks which must be made.

Loop methods require a continuous circuit of main or cable from the place where the testing instruments are, through the faulty portion and back again, which is termed the loop. The two portions of cable between fault and instruments should have good insulation resistance, but need not have the same sectional area throughout. Referring to Fig. 51, let MSN be a cable, the two ends of which cannot be brought closer to the terminals A and C of a Wheatatone Bridge than the points M and N respectively.

Let there be a fault at some point P between the core of the cable at P and the earth E_i the resistance to earth being much less than that at any other point. This is called the fault resistance, and may be represented by r.

The fault might be on the "outer" of a concentric main, in which case the "inner" and "outer" conductors would be carefully joined at the further end S, so as to form a complete circuit or loop.

In fact, in practice we should either be dealing with this case of a concentric main or with a fault on one of a pair of separate mains.

In oither case the loop would be formed by making the best possible joint between the two ends furthest from the testing point, by disconnecting them from any terulinals to which they might be clamped. Now it is obvious that the cable ends M and N cannot be clamped under the terminals of the bridge, owing to their size and to them terminating in a position in which it would be impossible to have the testing apparatus. Smaller connections AM and CN must therefore be used and also allowed for in working out the results of observations, and this is done as follows—

Let D₁ D₂ = distances from M and N respectively to the looping point,

and $d_1 d_2$ —distances from A to M and from C to N respectively, s—sectional area of either conductor of the main MSN, s_1 and s_2 —sectional area of the connections AM and CNrespectively.

Then, since resistance is directly $\propto \frac{\text{length}}{\text{section}}$, we see that ΛM

has the same resistance as, or is equivalent to a longth of the main

$$MSN = \frac{s}{s}$$
, d_1 and CN to a length $= \frac{s}{s}$, d_2

Hence the bridge will behave as if the resistance between C and P (which = rasistance of CN+ resistance of NP) was that = to a length of the main cable = $D_2 + \frac{s}{s}$, d_3 .

The whole length of circuit L between A and C is-

...
$$L = D_1 + \frac{s}{s_1} \cdot d_1 + \frac{s}{s_1} \cdot d_2 + D_3$$
.

The expression or value for L may very greatly be simplified by making $D_1 = D_2$ and also $d_1 = d_3$, which latter can easily be done, and by choosing single wires for the connections AM and CM of the same gauges as each wire of the strand forming the main MSN. Thus if the main was $\frac{A1}{16}$ in size, uso $\frac{1}{16}$ for the connections.

If this is done and $n = N^o$, of wires in the strand of either conductor of the main,

then
$$L=2D+2$$
, $n d=2 (D+n, d)$

The lengths of AM and CN, though \Rightarrow , should be as short as possible, so that their resistance is not large compared with that of the main cable.

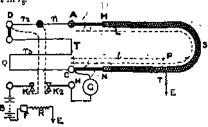
Apparatus.—Post-office or other pattern Wheatstone Bridge; somitive galvanometer G (p. 569); battery H of Leclanché cells; fuse F; resistance R; suitable connections AM and CN and main to be tested.

Note.—A few secondary or primary cells may form the hattery R_i and if the fault resistance r is anything like 1000 chms, a battery giving 100 volts might be used. The fuse F is to prevent the bridge coils being fused up should r break down unexpectedly, and it can be dispensed with if a primary battery is used. It is as well to earth the battery, if not a primary one, through a resistance R of a few ohms.

The more sensitive G is, the greater the accuracy of the test, and quite small wires may be used to connect G and B up, as their resistances do not affect the accuracy of the test.

Observations.—(1) Connect up as shown in Fig. 51, and adjust the gaivanometer G nearly to zero. See that a very fine fuse is inserted in F, if necessary at all, and make furly good earths at EE. Good soldered joints at M, N and the looping point are practically indispensable, as well as good tight clean contacts at M and M. Inattention to these points will vitiate the results.

(2) Plug up $r_1 = 0$ and unplug $r_2 = 1000$, with, say, the *Infinity* plug out in r_3 .



Fio. 51.

(3) Press K₁ first and then tap K₂ for an instant, observing which way G deflects for r₃ so great.

If on inserting "Inf." G defects the other way on manipulating K_1 and K_2 as before, then a balance can be obtained by adjusting r_3 so that G does not deflect on pressing K_1 and then K_2 . Note the value of r_2 , r_3 . If no balance can be found, the fault P is very close to M or N when the connections to A and G should be interchanged.

- (4) If the balance appears to be insensitive $r_2 = 100$ or 10 may be tried and (obs. 3) above repeated.
- (5) Calculate the equivalent distance of the fault P from the terminal C by means of the relation

$$l = \frac{r_0}{r_2 + r_3} \cdot L,$$

and tabulate your results in a convenient way.

N.B.—The distance of P from N therefore $= l - \frac{s}{s_*}, d_2$.

(6) Interchange the connections to A and C and repeat obs.
3-5, and if the result now given is close to the previous one, take

the mean of the two as the correct one. If they differ considerably, the contacts are bad and must be improved.

In this latter test the distance of P from A is given by

$$l = \frac{r_2}{r_1 + r_2} L$$

(51) Calibration of Speed Indicators.

Introduction.—There are many different forms of speed indicators or tachometers, as they are frequently termed, some of which vary in accuracy with the time for which they are in use. It thus becomes of importance to standardize such instruments at frequent intervals when accuracy is required. This can be done either by comparison with an accurately calibrated tachometer specially reserved for this purpose only, or by taking simultaneous readings on the instrument to be checked and time readings on a speed-counter. This latter method, being the more generally applicable of the two, will be the one here considered.

Apparatus.—Tachomotor to be tested; speed or revolutioncounter; stop-watch if available, or in lieu of this an ordinary watch with a "seconds-hand."

Observations.—(1) Arrange the tachometer so that it can be driven by some machine at a variety of speeds, each of which may be maintained constant for at least one minute. This driving machine must have a turned centre in one end of its shaft into which can be pressed the centre of the spindle of the revolution-counter.

(2) Drive the tachometer at the lowest convenient speed readable on its scale, and take the dial readings (D_1) of the revolution-counter. When this speed is constant (as will be observable by the instrument itself) insert the counter in the end of the driving-shaft at a noted instant of time, using a light pressure. Quickly take the counter away, the instant one minute has clapsed, and note the readings (D_2) of its dials. Then $(D_2 - D_3) =$ speed in revolutions per minute.

- (3) Repeat 2 twice or three times at the same speed, and record the mean.
- (4) Repeat 2 and 3 for some eight or ten readings on the tachometer, rising by about equal increments to the maximum.
- (5) Check some of the readings obtained in 2-4 by taking observations over two minutes.
- (6) If the tachometer is adjustable, alter it so that its indications give the correct speed in revolutions per minute. If anadjustable, plot a calibration curve having values of true speed as abscisse and tachometer readings as ordinates.

(52) Measurement of Rotational Speed by the Stroboscopic Fork.

This method has been in use for measuring the speed of generators and motors for many years. See papers by Dr. C. V. Dryskale—(1) on "Stroboscopy"; read at the Optical Society, London, in 1905, and reprinted in The Optician and Photographic Trades Review, Dec. 8 and 15, 1905. (2) "Accurate Speed, Frequency, and Acceleration Measurements," Electrical Review, London, Sept. 7 and 14, 1906. Previous to that it had been used by scientists, e.g. to measure the speed of a small driving motor to within $\frac{1}{160}$ of 1% in the Lorenz apparatus for determining the absolute value of the ohm.

The stroboscope used comprises essentially—(1) either a hand vibrated, or (preferably) an electro-magnetically vibrated tuning fork

fitted with two shutters, each containing a narrow slit, and (2) a discoidal target of observation.

The stroboscopic fork unmounted is indicated diagrammatically in Fig. 52, and that used by Dr. Drysdale consists of a steel tuning fork, the limbs LL of which are approximately 12" long $\times \frac{1}{32}$ " wide $\times \frac{1}{32}$ " thick, and are supported by a tail-rod T

clamped in a suitable frame or stand (not shown). To the extremities of LL are screwed two light and thin metal strips or flat shutters $S_1 S_2(11'' \times 15'')$ in the plane of vibration, each, containing a narrow slit $S(\frac{1}{3}'')$ long) parallel to the length of LL. These slits are exactly opposite to one another when the fork

is at rest, so that in this condition the eye can see through both slits. When hand vibrated the fork, while being held in the observer's hand, is excited into vibration at intervals by mechanical impulses derived from a light blow on the kees.

When electro-magnetically operated, the "make and break" principle used in the electric trembling bell is adopted—an iron-cored coil " being mounted between LL on a support (not shown) adjustable, for convenience, in a direction parallel to LL.

This actuating coil C is energized from one or two dry cells through a "contact breaker," formed by two platinum-tipped contacts—one on a fixed support, the other on a very light flat spring fixed to one of the limbs L. Now when the fork is excited into free vibration, the line of vision through the slits S is interrupted by the vibrating shutters S_1S_2 except during a very brief interval, once in each half cycle, or twice in each complete cycle of the vibration at the moment when the slits S

complete cycle of the vibration, at the moment when the slits S pass each other, moving rapidly in opposite directions. If, then, an object viewed through the slits S is rotating so that consecutive images conveyed to the eye are similar and symmetrical, that object will appear to the eye to be continuous and stationary, although actually rotating at a high speed.

Further, a certain cyclic departure from absolute similarity

and symmetry in the successive images seen by the eye will make the object appear as if it was rotating. If the object appears at a standstill when seen through S, its speed must be constant, and must bear a simple proportion to that of the vibration of the fork. Therefore, since the rate of vibration of a tuning fork is always very constant at all times, and almost independent of change of temperature (varying only about 0.01% per deg. cent.), it can be determined once for all with great accuracy, and hence also any speed by comparison can be measured with like accuracy

If a fork vibrates with a frequency of 50 cycles per sec., the eyo will receive 100 impressions of the object through the slik S per second, and will have 6000 peeps per minute. The geometrical form of the rotating object viewed through the slit will, in conjunction with the rate of vibration of the fork, decide the speeds at which the object will appear at a standstill. These speeds might, for example, be 100, 200, 300, etc., revs. per min., and the simple fork shown in Fig. 52 can only serve to measure speeds intermediate between these by enabling the eye to count the apparent revs, made by the object in one minute by a watch. For example, if the speed at which the objectviewed through the slit appeared stationary -was 1500 revs, per min., and afterwards the object appeared to be rotating in the direction of motion at 50 revs. per min, then the actual speed of the object would be 1550 revs. per min. If this apparent rotation of the object was in the opposite direction, the actual speed would be 1450 revs, per min.

The determination in this manner of speeds intermediate between the two nearest standstill valves, coupled with the necessity for such being constant, is a disadvantage in the stroboscopic method, for it is obviously preferable to be able to bring the object to an apparent standstill at any speed. At least two methods of doing this have been devised; one due to Dr. Drysdale employs a special arrangement of a conical roller with stroboscopic disc, as described in his paper, but which lucks pertability. In another method, designed for portability by Messrs. A. R. Kennelly and S. E. Whiting, and described by them in a paper read at the Twenty-fifth Annual Convention of the Amer. Inst. E.E., Atlantic City, N.J., June 29-July 2, 1908. the strobescopic fork is adjustable continuously in its rate of vibration through a range of about 50% above and below its mean value without sensibly disturbing its motion. This is done by a pair of sliding weights, which are moved friction tight along about 71" of the limbs of the fork, gradually from one position to another, by a pair of strings, normally slack, passing over guide-pulleys, and vibrating with the fork. The form used in this design has limbs 18" long \times 1" wide \times 36 thick, and weight by itself almost 2 lbs. The object in using so long a fork was to obtain a low frequency vibration or forkspeed comparable with the speeds ordinarily met with in rotating machinery. The fork has a mean speed giving 1900 peeps per min, and carried on its extremities a pair of thin sheet steel, shutters with slits 0.59" long × 0.008" wide. Adjustments are provided for aligning these slits, and for tuning the fork to the required normal frequency. It is operated by an electromagnet, the coil of which is wound with 525 turns of No. 27 S.W.G. enamel insulated copper wire (enamelled to No. 26 S.W.G.), having a resistance of about 3½ ohms, and requiring an average current of about 0.15 amp. to operate the fork through a form of contact breaker already referred to.

The amplitude of the vibration of the fork limbs is about $\frac{1}{3}$ at the slits, each side of their position of rest, giving a maximum cyclic velocity of about 1 foot per sec. at normal fork speed. The relative velocity of the slits is thus about 2 feet per sec., and the duration of each peep through the slits will be $\frac{1}{3000}$ of a sec. $=\frac{1}{180000}$ of a min. Hence an object rotating at 1800 revs. per min. will only move through $\frac{1}{180000} = \frac{1}{100}$ of a revolution during each peep, and if it appears at a standstill through the slits, 1 rev. per min. mure or less, i.e. a variation of $\frac{1}{16}$ of $\frac{1}{16}$ of $\frac{1}{16}$ of the speed will cause the object to make 1 rev. per min. either way.

The Target—hitherto called the rotating object, may most conveniently consist of a thin disc



F16. 53.

(between 9" and 10" in diam.) of sheet metal or thick cardboard fixed concentrically—in any convenient and satisfactory way—to the end of the shaft whose speed is to be measured. If neither end

of the shaft system is available, nor any portion of the end of the machine suitable for use as a target, it may be possible to mount the special artificial target on a subsidiary spindle with pulley, and

drive this by a light supple tape belt at a definite speed ratio from some part of the machine under test.

From many trials with different kinds of targets, it has been

of about the size above-mentioned, is quite satisfactory. The pattern (Fig. 53) comprises: a square, a pontagon, a hoxagon. a 14-point star, and an 18-point star, all concentric with one another, and with the disc and shaft, with a radial bar inside the square for enabling the apparent revolutions between intermediate standstill speeds to be counted easily.

If P = number of positions of symmetry per revolution ofany individual pattern on the target,

n = revs. per min. of the target.

N = any whole number or reciprocal of a whole number, n = number of peeps per min, given by the fork's rate ofvibration.

Then the particular pattern will stand still when viewed through the slits if

$$N = \frac{P.n}{p}$$

For example, the square or 4-pointed star has P=4 positions of symmetry per revolution.

If a given fork provides p = 3600 peeps per min, Then the square will appear to stand still for actual speeds of-

n=450 revs. per min. at which $N=\frac{P_R}{p}=\frac{4\times450}{3600}=\frac{1}{2}$ the reciprocal of a whole number,

and n = 1800 revs. per min. at which $N = \frac{Pn}{p} = \frac{4 \times 1800}{3600} = 2$ a whole number.

In the first case the square will move through half of a position of symmetry, and in the second case through two positions of symmetry between successive peops.

The useful possibilities obtainable with the above target may be conveniently seen in Table VI.

The higher the actual speed of rotation, the greater must be the rate of vibration or frequency of the slits and number of peops per min., and the narrower must the slits be, otherwise the number of positions of symmetry P must be smaller to give an increase of pitch.

The accuracy of this method of measuring speed is very high, and of the order of about 1 part in 10,000.

Table VI.—Actual speeds in race per min, at which such pattern of the Target (Fig. 55) will appear to stand still when viewed through the slite of a Fork giving 1800 peops per minute.

	Skju	are.	Pentegon.		Heragon		14-Pointed Star,	17-Pointed Bian
7	⊯ 4 ar].	P = 8 or 1	P = 5 or 1	$P = 10 \text{ or } \frac{1}{10}$	P = 6 m ⅓.	P = 12 ot 1.	P = 14.	r = 18.
450 1	lmage attorary t avery) r. p. m. = Bynchr. Bpeed.	Image appearing doubled, but less clear at latermedi- ate Speads or avery 225 r p. m., = \$ Synchr, Speed.	Tungo stationary at every 360 r.p m =- 1 Synchi. Speek.	In age approxing doubled, but less clear at [nies mediate Speed or every 180 r p m, = 18 Syrch. Speed,	image stationary at every 50 ir p ta. = i Synchr, Speed.	Image appearing doubled, but less clear at lutermediate speed or every life r p. st. = 15 Speed.	Image stationery at every 128 6 r.p.m. = 1, Synctor Spect.	Image stationary at every 100 r.p.m.: 1, Synchr, Speed.
_			·		· ·			
	- 1	215	_ !	180	- 1	150	128 6	100
	450	450	904	360	SHO .	8: H1	267.1	200
	- I	67.2		510		4.0	385-8	(2)0
	900	NiO	720	720	ero I	GUG	5114	400
		1125		3H.ID	_		614.0	1.00
	1350	1350	1044	1950	1	750	771.6	500
		1575		1260	BOD	100	44) 3	700
	1800	1500	14'6	1140		1000	10.5 8	8/10
		5015 5210	1800	1620	1200	1200	1177.1	100
	2250	2475	1500	1800 1940	1:00	1350	1260 0	1000
	2700	2710	2180	2160	1560	1500 1650	1411.6	1100
	2100	2925		2310	1800	1620 1500	1432	1930
	8150	2020 9130	2030	2520	Lova U	1950	1571:8 1800-4	1900
	0104	2375		2700	2100	2100	1929 0	1400
	8600	3600	2880	26KO		2450	21/17:6	1600 1600
	_	3425	2000	31460	2400	2 N20	로 Sing	1706
	1000	(050	3240	8410		2550	2114.0	1800
	_	1275		8121	27/0	2700	21134	19:0
	4500	4500	6493	3600		98.60	2572	2004
		_			2000	3) (d)	3010	2004

(53) Relation between Speed and E.M.F. in "Separately Excited," "Shunt," and "Compound Wound" Direct Current Dynamos.

Introduction.—The following tests are arranged with the object of investigating the way in which the terminal E.M.F. of the various types of dynamos varies with the speed when the machine is delivering no external current. The mode of procedure is exactly the same for each type of machine, and consequently this will be given in one concrete instance only, and merely referred to afterwards for the others. In all cases the terminals T_1 T_2 of the machine are the ones to which the external circuit would be directly connected. Prior to starting see that all lubricating cups in use contain oil, and feed properly

but very slowly; also that the commutators are smooth and clean, and the brushes properly trimmed.

N.B.—The performance of a "magneto" machine would be exactly similar to that of (A) below, and the "series" machine approximately the same also, providing the current through the series machine be kept constant by varying the circuit resistance as the speed varies.

Apparatus.—Dynamo D to be tested; tachometer; voltmeter (P) capable of reading sufficiently high.

(A) SEPARATELY EXCITED DYNAMO.

Observations.—(1) Connect up V to T_1 T_2 , and the exciting coils to some outside source of E.M.F. through an ammeter (a), and rheostat (R), then start D. Adjust (R) so as to obtain a current which will give $\frac{1}{2}$ max, excitation (to be kept constant).

- (2) Adjust the speed so as to obtain the lowest readable scale reading of V. Note this and the speed.
- (3) Raise the speed so as to get about ten different values of V, rising hyabout = increments to the max, and note the speed at each.
 - (4) Repeat 3 for a similar descending set of readings.
- (5) Repeat 3 and 4 for such a current through the field coils as will give max, excitation, and tabulate your results in the following general form.

		Type of Dynamo testor.	Speed in Revs. per min,	Reporte Post of United to (d. may)	Terminal Accepting V.	E.M.F.s. Descending P.
--	--	------------------------	----------------------------	---------------------------------------	-----------------------	------------------------------

(B) SHUNT DYNAMO.

Observations.—(1) Connect up V to $T_1 T_p$ and start the dynamo.

- (2) Repeat observation (2-4 A), and tabulate in the form shown above.
 - (C) Confound Wound Dynamo (Long Shunt).

Observations.—Repeat those for B above.

Flot curves for the tests on each type of machine in A, B and C above, having E.M.F. as ordinates and speed as abscisse.

Inferences.—Compare the above curves and results, and state clearly all that you can infer from them.

Characteristics of Dynamo Machines.

Introductory Remarks.—There are two great classes of electrical generators for converting mechanical into electrical energy-namely, (1) those which supply continuous current, i.e. current which flows in one direction only round the circuit, and which are otherwise styled direct current dynamos; (2) those which supply alternating current, i.e. current that reverses its direction throughout the whole circuit many times a second, and which are usually styled alternators. As therefore the supply of electrical energy to any appreciable extent invariably assumes one or other of the above forms of current, a study of the behaviour of the machines that supply it becomes of paramount necessity. Restricting our considerations first of all to the former of the above-mentioned classes, it may be remarked that it is composed of a great variety of forms, the performance of which depending practically entirely on the method employed in winding their field magnets, in other words, as to whether the whole, a fraction, or a combination of this whole and the fraction of the whole current generated by the machine is utilized in magnetizing their field magnets. Direct current dynamos in general may consequently be subdivided into the following five distinctive types according to the winding of their field magnet coils-

- (a) Magneto machine.
- (b) Separately excited machine.
- (c) Series machine.
- (d) Shunt machine.
- (e) Compound machine.
- All those types are used in practice, especially the last three, which form by far the greater proportion of direct current machines in use throughout the world. Only by a minute study of the performance and action of each type can it be seen which of them is the best suited for any particular purpose.

The current that any particular dynamo will send through a given external circuit connected to its terminals will obey Ohm's Law, and will depend on the E.M.F. of the machine, as well as on this external resistance.

If therefore the machine be run at a constant speed, and the

circuit resistance R varied by suitable steps (say), both the terminal P.D. of the machine (l') and the current A will vary. Assuming that V and A are noted simultaneously for each alteration of R we can plot a curve having values of V, measured along the ordinates, and A along the abscisse, these axes being rectangular. Such a curve is commonly called the "external Characteristic" of the dynamo, and by means of it many valuable and practical details can at once be deduced.

In fact, the function of a Characteristic in relation to a dynamo is extremely analogous to that of an "Indicator diagram" with an engine. In the former, not merely can the qualities and performance when working be seen, but also the H.P. at which it works or could most economically work at, and many defects in the design—such as the sufficiency of the field magnet field, the degree of saturation of the magnets, the demagnetizing action of the armature on the field, etc., etc. The Characteristic of a dynamo is therefore much more important to the electrical engineer than the author ventures to think is generally supposed.

(54) Determination of the "External Characteristic" of a Magneto Dynamo.

Introduction.—The present type of machine under consideration has a somewhat extensive field of use, two very important applications being for blasting purposes and use with the ohmmeter, and indeed in all kinds of work in which a portable E.M.F. and small current is desired.

Another application in the past on a heavier scale was in the production of lighthouse scarch-lights, in which kind of work heavy currents are required at a comparatively low EMF. Considering the machine more in detail, when the armature is delivering no current to the external circuit, the terminal P.D. (V) = the total E.M.F. (E) of the dynamo. When, however, a current A flows, then V is less than E by an amount depending on the armature resistance r_* ; for, by Ohm's Law.

we have $E = A(R + r_s)$

where R = the resistance of the external circuit; but since it is solely the P.D. $\{Y\}$ which drives the current through the external resistance.

, *. V = AR, and consequently $E = V + Ar_{a}$.

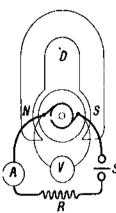


Fig. 54.

the terminals + that required to send the current A through the internal resistance r, of the armature. The permanent magnetism of the steel magnets is approximately constant.

Apparatus.—Magneto dynamo D to be tested; voltmeter V; ammeter A; switch S; rheostat R(p. 606); tachometer.

Observations.—(1) Connect up as in Fig. 54, and adjust the pointers of A and F to zero, if

necessary. See that all lubricat! ing cups in use feed slowly and properly, and that the commutator is smooth and clean, and the brushes properly trimmed. (2) Start D up to its normal

speed, and when this is constant, note the reading of V. (3) R being as large as possible, close S, and take a series of

- about ten different values of current A, rising by about equal increments from the smallest to the maximum permissible. Note the voltage V and current A for each, the speed being constant at the above value.
- (4) Repeat 2 and 3 for a similar descending set of readings of V and A at the same speed.
- (5) Repeat 2.4 for speeds 20% above and 50% below normal respectively.
- (6) Measure the armsture resistance (r_{*}) (while warm) by the Wheatstone Bridge, or if it is too low, by the "Potential Difference" method (p. 84), or by the ammeter and voltmeter method (p. 86), and tabulate your results as follows-

NAME ...

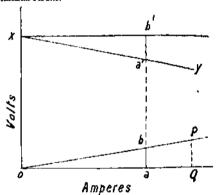
Magneto Dynamo tested ; No. . . . Type ra = . . . O mis. . . Nurmal Voltage =, , . Amps. =. . . Speed =, . .

Speed	Аьсег	ding.	Descending.		
Reva. per talp.	Terminal Volts (P).	Amja. (4).	Terminal Volta (V).	Aloye. (4).	
	<u> </u>				

(7) Plot the external Characteristic curves of the machine for both the ascending and descending readings at each speed on the same curve sheet, having values of V as ordinates and A as abscissa.

(8) Deduce from these the total Characteristics of the machine by the graphical construction given below, drawing them on the same curve shoet (vide p. 3, obs. 8).

(9) Plot the horse-power curves (see below) to the same axes. Inferences.—State clearly all that you can infer from your experimental results.



Fre. 55.

Graphical Deduction of the Total Characteristic of a Magneto Dynamo from its External Characteristic.

Referring to Fig. 55: take two co-ordinate axes having their origin in the point O. Let xy be the external Characteristia. Take any point O in the abscisse representing some definite current OO to the scale chosen, and set off on the ordinates OO = OO × r_* volts.

Join OP, which therefore represents the fall of Potential through the armature due to the currents flowing in it,

or tan. $POQ = r_e$

Now take any point a' in xy, and through it draw an ordinate entting OP and OQ in b and a respectively. Set off a'b'=ab, and y will then be a point on the total Characteristic.

Repent this construction for eight or ten points, such as a' along xy, and finally draw the total Characteristic xb' required.

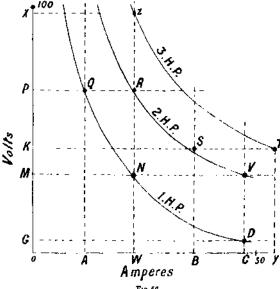


Fig. 56.

The performances of the machine, deducible from the above diagram, are roughly these-

If the curves xy and xb' are too far apart, it means that the armature resistance is excessive and is causing a large drop of terminal voltage.

Again, if the lower part of xy droops considerably, it shows that the armsture current is causing a considerable demagnetizing action for the larger currents when the angle of lead of the brushes is greater. This downward drooping occurs more markedly as the field magnets become weaker.

Horse-Power Curves.

Since the electrical power W in Watts developed by any dynamo giving a current A supps, at a P.D. of V volts is—

W = AV (Watts) and since 1 E.H.P. = 746 (Watts), ... H.P developed = $\frac{AV}{746}$.

Now manifestly, as the Characteristics of a dynamo are plotted to definite scales of volts and amperes, the power developed at any point on such a curve will be equal to the product of the co-

If, however, curves of equal II.P. are, at the onset, drawn to the axes chosen, the above calculations will be avoided, for if the 2 II.P. curve cuts the Characteristic at a given point, then the power developed by the machine corresponding to the Y and A of that point will be 2 II.P.

ordinates of that point, and can therefore at once be seen.

To determine these H.P. curves: Find several points such that the products of their co-ordinates = 716 Watts = 1 H.P. Thus, in Fig. 56 we have—

 $PQ \times QA = MN \times NW = GD \times DC = 746 \text{ Watts} = 1 \text{ H.P.}$ similarly $PR \times RW = KS \times SB = MV \times VC = 1492 \text{ Watts} = 2 \text{ H.P.}$ and $XZ \times ZW = KT \times TY = 2238 \text{ Watts} = 3 \text{ H.P.}$ Then all points on the curve QND represent $A \times B$.

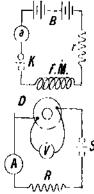
where $A \times B$ is a sum of $A \times B$ is a sum of $A \times B$.

Intermediate values of H.P., such as 1:5 H.P., can be got by halving the distances between curves QND and RSV, etc.

These H.P. curves are simply rectangular hyperbolic if equal scales are used on the axes, but are distorted hyperbolic if the scales are imequal. Instead of H.P. they can equally well be drawn to represent kilowatts.

(55) Determination of the External Characteristic of a Separately Excited Dynamo.

Introduction. — The type of machine under consideration as representing a direct current dynamo has little application in practice, but as representing an alternating current



propose to discuss at this stage. Its utility in the first-named use lies in the fact that not merely can a far more powerful field be produced than is possible with any permanent steel magnets, which is of great value and, in fact, all-important in the generation of large E.M.F.s, but such a machine can be used with perfect safety in charging secondary cells, electroplating, etc., without the least fear of its polarity being changed should the back E.M.F. of the cells exceed that of

the machine. A further advantage may

machine it has an extremely wide range of use. Such, however, we do not

Fig. 57. be mentioned, viz. that a wide variation of F.M.F. can be obtained at any speed by suitably varying the exciting current (a) by the rheastat (r). The main disadvantage lies in having to provide an independent source of E.M.F. (B) for exciting the field magnets (F, M_*) .

The total E.M.F. is, as in the case of the magneto dynamo, given by the relation $E = V + Ar_a$, where A = the current flowing in the circuit at a terminal P.D. = V and $r_a =$ the armature resistance.

The external and total Characteristics of the machine are found in exactly the same way as for the magnete dyname, but at constant excitation as well as speed, and Fig. 57 shows the requisite apparatus symbolically and the connections of the same.

(56) Determination of the Internal Characteristic or Curve of Magnetization of a Separately Excited Dynamo.

Introduction.—In any dynamo, the P.D. across the brushes, i.e. armature, when no current flows in the external circuit, gives a neasure, and is proportional to the magnetization of the field

magnets. If therefore the field magnets of any dynamo are separately excited by different currents from an independent source of E.M.F., the corresponding voltages across the brushes, for constant speed, will be approximately proportional to the inductions produced, if the machine is giving no current. The curve relating to exciting currents with E.M.F.s is termed the internal Characteristic, and it shows the region of saturation of the magnets, and also whether the eddy currents in the armature are producing any perceptible demagnetization of the field, and therefore shows the efficacy of the lamination of the armature core.

Apparatus.—Separately excited dynamo D to be tested; voltmeter V; exciting circuit comprising source of E.M.F. (B); animeter a; switch K; rhoostat (r) (p. 599); and field coils F.M.

Observations.—(1) Connect up as in Fig. 57, omitting the main current circuit there shown connected to the armature. Adjust the instruments to zero.

- (2) Start D up to normal speed and with (r) large, close S, and take about ten different values of exciting current, rising by about equal increments from 0 to the maximum, and note the corresponding voltage V at each, the speed being constant'throughout.
- (3) Ropeat 2 for a similar descending set of readings, and tabulate your results in a convenient manner.
- (1) Plot the internal Characteristic having values of terminal voltage V (x to field flux) as ordinates, and exciting currents (a) (x to magnetizing force) as abscisse.
 Thereacter State should be required of the current and the contract of the current and the current state.

Inferences.—State clearly the meaning of the curve, and any inferences which can be drawn from the experimental results.

(57) Relation between External Current and Exciting Current, at Constant Voltage, in a Separately Excited Dynamo, at Constant Speed.

Introduction.—If both the external and exciting currents are varied together in such a way that for a constant speed the terminal voltage is constant, then the curve showing the variation of one current with the other will show the increase of excitation that would be necessary to give constant voltage for varying external resistance at constant speed.

Apparatus.—Precisely that required for the preceding test, and in addition the main circuit comprising ammeter A; rheostat B (p. 606); and switch S.

Observations.—(1) Connect up as in Fig. 57, and adjust the instruments to zero. See that all lubricating caps in use feed

- (2) Start D up to the normal speed, and with a convenient excitation note the voltmeter reading V, which in future is to be kept constant as well as the speed.
- (3) With R large close S, and take about ten different load currents A, rising by about equal increments from 0 to the maximum allowable, adjusting the exciting current to keep the volts constant. Note each pair of corresponding currents.
 - (4) Repeat 3 for a similar descending set of readings.
 (5) Repeat 3 and 4 for a different speed but the same voltage
- (5) Repeat 3 and 4 for a different speed but the same voltage by suitably altering the initial excitation, and tabulate in a convenient form.
- (6) Plot curves for each speed, for both ascending readings having values of exciting current as ordinates and main currents as abscisse.

Inferences.—State clearly the practical value of the above tests, and explain the form of curve so obtained.

(58) Determination of the External Characteristic of a Series Wound Dynamo.

Introduction.—In this type of machine the whole current developed at any time is employed for magnetizing the field magnets, but these are only wound with a comparatively small number of turns of thick wire to carry this main current.

The series machine is an extremely important one in practice, and will be found throughout the world in different parts. It is essentially employed as a constant current dyname, usually developing a small current at a high E.M.F. The principal application is in the lighting of are lamps in series, and as an electro-motor in the various branches of electric traction work. Regarding it first of all from a theoretical standpoint, there is only one circuit in operation, and hence but one current, in the case of a series

dynamo running an external circuit. Thus when this is broken there is no E.M.F., and the maximum E.M.F. is only obtained when close on the full lead current is flowing.

The series dynamo possesses many peculiarities, the nature and effect of which, on practical working, it is all-important to be cognizant of. This investigation is best solved by obtaining the Characteristic of the machine and studying it.

If τ_e and r_a be the resistance of the series coils and armature respectively, and R that of the external circuit, then when the voltage across the terminals is V, the total E.M.F. generated

$$E = A \left(R + r_s + r_s \right)$$

where A = the current in the circuit; but V = AR; hence $E = V + A (r_e + r_u)$.

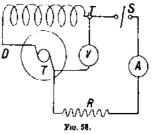
Apparatus.— Series dynamo D to be tested; voltmeter V; •ammeter A; switch S; low resistance (variable) rheostat R (p. 606); tachometer. FM represents the field imagnet (series) coils; TT represent the terminals of the dynamo.

Observations.—(1) Connect up as in Fig. 58, and adjust the instruments to zero, if necessary. See that all lubricating cups in use feed slowly and pro-

perly, and that the brushes are properly trimmed and the commutator smooth and clean.

(2) Start D up to its normal speed, and with S open note the reading on V (if any).

(3) With R large, close S, and take about ten values of current A (at constant speed), rising by about equal increments from



about equal increments from 0 to the maximum permissible, and note the corresponding voltage V at each.

Note.—In starting, care must be taken not to decrease R too quickly, as the machine might suddenly build up on its residual magnetism, and a large rush of current ensue.

(4) Ropent 2 and 3 for a similar descending set of realings of Y and A.

- (5) Repeat 2-4 for speeds 20 % above and 50 % below normal respectively.
- (6) Measure, by means of the Wheatstone Bridge, the resistance r_s of the series coils, r_s of the armature, and $r_s + r_s$ of the whole machine while warm, supposing it to be not too small, and tabulate your results as follows—

NAME . . . Date

Series Dynamo tested: No... Type ... Maker ... $(r_1+r_2)=...$ Rottes! Voltage * ... Appt * ... Spond = ... Resistance $r_1=...$... $r_2=...$

Bpeed Revu. per min.	Ascend	ling.	Descen	— -	Resistance of Baternal Carcuit
	Terminal Volta (V).	Amps. A.	Terminal Volta (P).	Amps. d.	menu V olune,
				<u> </u>	

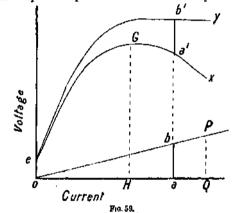
- (7) Plot the ascending and descending acternal Characteristics for each speed to the same pair of axes, having voltage (V) as' ordinates, and amps. A as abscisses in each case.
- (8) From the above curves deduce, graphically, the total Characteristics on the same curve sheet in the manner described below (vide notation, p. 3).
 - (9) Plot the H.P. curves on the same sheet.
- (10) Determine the critical revistance for this machine at each speed and also the critical current.
- (11) Determine the internal Characteristic of the machine, and plot the results, having exciting currents as abscisse and armsture
- E.M.F. as ordinates, to the same axes as the above curves.
 (12) Plot the external resistance Characteristic having values
- of V as ordinates and resistance of the external circuit $\frac{V}{A}$ in ohms as abscissor.

Inferences.—Explain the meaning of the curves very carefully. How can the effect of alteration of speed for one or more points on a Characteristic be corrected for? Why does the total Characteristic not droop so much as the external at the higher currents?

Graphical Determination of the Total Characteristic from the External One in a Series Wound Dynamo.

Take two co-ordinate axes meeting in the point O of which the ordinates represent voltage and the abscisse current in amperes. Let x be the external Characteristic curve of the series d_y^2 namo,

Take any point Q on the abscissa representing any current QQ and set off on the ordinate a line QP to represent $QQ \times (\mathbf{c}_{+} + \mathbf{r}_{a})$ volts. Join QP, which therefore gives the rate of fall of potential down the armature and series coils combined, i.e. down the whole machine, or we have $\tan PQQ = (\tau_{a} + \tau_{c})$. Now take any point a' in the curve x and through it draw an ordinate a'ba cutting QP and QQ in b and a respectively; set off a'b' as shown = ab, whence b' is a point on the total Characteristic. Repeat this operation for some ten different points along



z and finally obtain the total Characteristic y of the machine

at the particular speed in question, Fig. 59.

If the curves start at some point s other than the origin O, then Os is the E.M.F. at that speed due to residual magnetism in the field magnets when the external circuit is open, as in observation 2 above; Os will be greater the greater the hardness and retentivity of the iron in the magnets.

If the curves x and y are much separated, it shows that the resistance of the machine, i. e. tan. POQ, is too great, and therefore that it cannot be very efficient. Again, the summit G of the curve x shows for what output $(GH \times HO \text{ Watts})$ and current OH the armature is magnetically saturated, and the drooping of the part Gx gives an idea as to the demagnetizing action of the

armature on the field. It is greater in dynamos in which the magnets are relatively less powerful than the armature, and is greatest in those machines in which the armature core is more nearly saturated than those of the field magnets.

Graphical Determination of Critical Resistance at a Given Speed for a Series Wound Dynamo.

Let the curve OCs be, say, the total characteristic of the machine for a given speed. Then the total circuit resistance

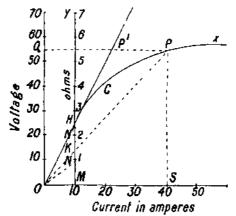


Fig. 60.

 $(R+r_a+r_s)$ corresponding to any point P can at once be found in the resistance line y is known, and which is found as follows—

Let N = point of intersection of the two axes 10, Fig. 60.

Then joining ON we have tan, $NOM = \frac{NM}{OM} = \frac{V}{A} = R = \frac{10}{10} = 1$.

Hence N is a point representing 1 ohm. Similarly N' being the point of intersection of the 20 well

similarly N being the point of the resection of the 20 voic axis and 10 ampere one, will represent $\frac{V}{A} = \frac{20}{10} = 2$ ohms, and so on.

Thus the whole resistance line yM is obtained.

Now to obtain the circuit resistance for the point P, draw its go-ordinates PQ and PS and join OP.

Then tan,
$$POS = \frac{PS}{OS} - \frac{V}{A} = \frac{55.0}{40} = 1.375$$
 ohms,

but MK = 1.375. Hence the resistance of the circuit $(R + r_n + r_n)$ is given by the point of intersection K of the join of P to O, and the resistance line My.

If then P approaches the origin O just so close that OP coincides with OP and is practically a tangent to the curve (x), then its point of intersection with My gives the critical circuit resistance, above which the series dynamo will not excite.

This point is H and corresponds to 2.60 ohms on the resistance line. Thus for this speed the machine will not work if $(R+r_a+r_a)$ is greater than 2.6 ohms. For this instance the ordinates represent *total E.M.F.* of course, but if they were terminal volts and Ox the external Characteristic, then MH would — the critical external resistance R.

(59) Determination of the Internal Characteristic or Curve of Magnetization of a Series Wound Dynamo.

This is obtained in precisely the same manner as that in the case of the separately excited machine (p. 148), and consequently the mode of procedure will not be repeated. The curve should be plotted to the same axes as the ordinary Characteristics when the relative positions will form a measure of the armature reaction on the field,

(60) Determination of the External Characteristic of a Shunt Wound Dynamo.

Introduction.—In the type of machine under consideration only a fraction of the full load current generated is employed for the purpose of magnetizing the field magnets, the winding of the coils of which consists of a large number of turns of small

· gauge wire, possessing a comparatively large resistance. This shunt winding is connected directly across the brushes of the dynamo. Shunt dynamos possess a region of approximately constant potential, the fulling off in this latter being mainly due to armature resistance.

This type of generator is an extremely important one and its sphere of application very large.

The performance and qualities of such a machine can best be investigated by means of its Characteristics. Regarding the shunt dynamo from a theoretical standpoint, suppose that A_{a} , A_{c} and A are the currents flowing through the armature, shunt, and external circuit whose resistances are respectively r_a , r_a and R_i then we have $A_a = A + A_a$, since the armature current splits up

through abunt and external circuits. Now since we are dealing with two parallel circuits and onb common potential difference, we have, that the terminal voltage $V = AR = A_1r_1$ and the parallel resistance of shunt and external

circuit is

$$E = A_n \left(r_a + \frac{R r_s}{R + r_s} \right) = A_n r_a + \Gamma,$$

Hence

or by substituting for
$$A_a$$
 its value $A + A_1$ and reducing we get
$$E = Vr_a \left\{ \frac{1}{R} + \frac{1}{r_a} + \frac{1}{r_a} \right\}.$$

Apparatus.—Shunt dynamo D to be tested, of which FM represents its field coils in sories with FM a high resistance rhoostat r (Fig. 269);

> variable rhoostat R (p. 606); switch S; tachometer. Observations.—(1) Connect up as in Fig. 61, and adjust the instru-

voltmeter V; ammeter A; main

ments to zero if necessary. See that all lubricating cups in use feed ... properly. (2) Start D up to its normal speed.

and with S open vary r so as to produce normal excitation, then note the value of V.

(3) With R large, close S and take about ten different values

of current rising by about equal increments from 0 to the maximum. Note the voltage V at each and the current A, the speed being kept constant at the above value.

- (4) Repeat 2 and 3 for a similar descending set of readings.
- (5) Repeat 2-4 for speeds 20% above and 50% below normal respectively.
- (6) Measure, by means of the Wheatstone Bridge, the resistance r, of the shunt coils (warm), and by the "Potential Difference" method, the resistance ra of the armsture if very low, and tabulate your results as follows-

N.	tu			DATI		
	tested No. , , Amps.		pe Resi		7 	
Bootd	Ascend	ling.	Descein	ling.	Resultance of Esternal Curv	
Rays, per Manute.	Terprinal Volta V.	Aluja, A.	Terminal Volta (7.)		mean / obus.	

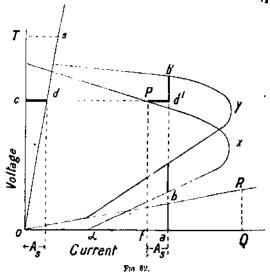
- (7) Plot the ascending and descending external Characteristics for each speed on the same curve sheet, having values of V as ordinates and A as abscirage.
- (8) From these deduce, by means of the following graphical construction, the total Characteristics on the same curve sheet.
 - (9) Plot the H.P. curves to the same axes also.
- (10) Plot the external resistance Characteristic, having values of Y as ordinates and resistance of the external circuit $\frac{V}{4}$ ohms as abscisso.
- (11) Determine the critical resistance of the machine for each speed and also the critical current,

Interences.—State clearly all that you can deduce from your experimental results, explaining carefully the meaning of the shape of the curves,

Graphical Determination of the Total Characteristic from the External Curve in a Shunt Wound Dynamo.

Referring to Fig. 62: let & be the external Characteristic. Take any point Q in the axis of abscisse representing any current OQ, and from it set off $QR = OQ \times r_a$ volts; join OR_i which therefore gives the fall of potential in the armature, we also have $\tan ROQ = \frac{RQ}{OQ} = r_a.$

Again, take any point T on the ordinates representing any voltage OT at the shunt terminals, and from T set off $TS = \frac{OT}{C}$.



amperes; join OS, which therefore gives the current taken by the shunt coils at different voltages, and we have

$$\tan, SOQ = \frac{OT}{ST} = r,$$

Now take any point P in x, and draw its co-ordinates Pc and Pf of which Pc cuts OS in d. Then $cd = \mathrm{shunt}$ current A_s and $cP = \mathrm{external}$ current A. If now cP is produced to d so that Pd' = cd, then the total armature current $A_s = A + A_s = cP + Pd'$. Now draw an ordinate through d' cutting OR and OQ in b and a respectively. Then $ab = \mathrm{loss}$ of volts in armature due to total

current $A_n = cd'$, consequently setting off d'b' = ab we get b' a point in the total Characteristic which in a shant dynamo gives the relation between total armature current $A_n = (A + A_n)$ and total E.M.F. $B = (V + A_n r_n)$. On repeating this operation for a number of points such as P on x we are finally able to draw the total Characteristic (y).

The working part of the curve is that at the top down to the sharp hend on the extreme right.

The critical external resistance $R = \tan a$ for this speed, and the machine will only work providing R is greater than $\tan a$.

The lower or straight portion of the curves is the unstable part. Thus it will be seen that a shunt dyname would give a nearly constant voltage for a given speed and variable external resistance, if it were not for the armature resistance,

(61) Determination of the Internal Characteristic or Curve of Magnetization of a Shunt Wound Dynamo.

Introduction.—The internal Characteristic of a shunt dynamo is similar in shape to the total Characteristic of a series dynamo, and is a curve showing the relation between exciting or shunt current and the E.M.F. across the brushes for open external circuit. Since, however, the shunt current is so small that its passage through the armature would not cause any appreciable reaction or demagnetization, the shunt may be excited from the brushes and the armature allowed to give this small current, instead of disconnecting the shunt and separately exciting it from an independent source. When the dimensions of the magnetic circuit of the machine are known, scales of the axes can be marked in air-gap flux density as ordinates, and amp, turns per pole as abscisses.

Apparatus.—Shunt dynamo; variable high resistance r capable of carrying the shunt current (p. 599); low reading annuetor (a); switch S; voltmetor V.

Observations.—(1) Connect the shunt rolls of the dynamo in sories with r, a and s across the brushes and V also across them, and adjust the instruments to zero.

(2) Take an ascending and also a descending set of readings

of V and a (at constant speed, say the normal) by varying r, and tabulate the results in a convenient manner.

(3) Plot the internal Characteristic having voltages V (or to magnetic field flux) as ordinates and shunt corrects (a) (or to magnetizing force) as abscisses in both ascending and descending readings.

Inferences.—Carefully point out the meaning of the curves so obtained.

(62) Determination of the External Characteristic of a Compound Wound Dynamo.

Introduction.—The type of machine under consideration is a combination of a series and shunt dyname, so far as the field arrangements go, i.e. its field magnets are would with both series and shunt coils.

The compound dynamo is a self-regulating machine for constant terminal voltage (at constant speed), independent of variations of external current. The principle of the self-regulating property is as follows:—As the external current increases in the case of a sbunt dynamo the lost volts due to armature resistance and demagnetizing reaction of the armature in the field reduces the effective magnetism of the field magnets, but this increase of main current causes an increase in the field magnetism due to the series coils, which can be made to just counteract the diminution due to the lost volts, at one definite constant speed, thereby producing constant voltage at the terminals of the machine.

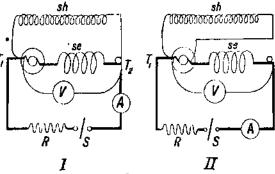
There are two possible methods of connecting the shunt coils to the machine, and which are shown in Fig. 63 symbolically, where I represents what is called "Long Shunt," and II that termed "Short Shunt." T_1T_2 are in each case the terminals of the dynamo, and as seen in the first case the shunt (sh) is across the extreme ends of armsture and series coils (se), i. s. across T_1T_2 , while in the second case it is across the brushes alone. A careful study of the dynamo with each method of connection will show which is the most desirable arrangement to use in any particular case. This, together with the investigation of the performance, etc., while working, can best be obtained by means of the Characteristics of the dynamo,

Apparatus.—Compound wound dynamo D to be tested; switch S; voltmeter V; ammeter A; rheostat R (p. 606); tachometer,

LONG SHUNT.

Observations.—(1) Connect up as in Fig. 63 (I.), and adjust the instruments to zero if necessary. See that all lubricating caps feed slowly and properly.

- (2) Start D up to its normal speed, and when excited note the reading on V.
- (3) With R large close S, and take about ten different values of current A rising by about = increments from 0 to the



Pio. 63.

maximum allowable. Note the voltage V at each, the speed being constant at the above normal value.

- (4) Repeat 2 and 3 for a similar descending set of observations,
- (5) Repeat 2-4 for speeds 20% above and 50% under normal respectively for constant excitation in each case in the shunt coils.
- (6) Measure by means of a Wheatstone Bridge the resistance r_{th} of the shunt, and by the "Potential Difference" method (p. 84) that of the armature r_{th} and series coils r_{th} .
- (7) Disconnect either coil in turn and repeat the above obs. 2-6 with the romaining coil, and so obtain the external Characteristic of the dynamo for each winding separately.

Note. - In doing this with sh connected alone, obtain the same initial voltage V as when running compound.

Tabulate all your results as follows-

NAMB				Date			
		ested; No Amps. =	Speed	Type . Resistance	Ma Carana t		
Wieding	Apred Reve,	A st etc	ding.		mhag,	Resistance of External Circuit	
named.	Reve. Por zam.	Tursusnal Volta (P)	Ampa, (A)	Termual Volts (F).	Atopor (A).	= mean / ohne.	

- (8) Plot the external Characteristics for each speed, and both ascending and descending observations, having voltages V as ordinates and currents A as abscisse.
- (9) From these deduce graphically, as described below, the total Characteristics, drawing them on the same sheet of paper, (For notation, see p. 3.)
 - (10) Plot the H.P. curves to the same axes also.
- (11) Plot the external resistance Characteristic having values of V as ordinates and resistance of the external circuit $\frac{V}{4}$ in olms as abscisso.

Inferences.—State carefully all that can be inferred from your results, and explain the meaning of the various curves.

Graphical Determination of the Total Characteristic from the External one, in a Compound Wound Dynamo.

LONG SHUNT.

Referring to Fig. 61, let x be the external Characteristic, Take any point Q in the abscisse representing any external current OQ, and set off from Q on the ordinates QR = OQ $(r_a + r_{ee})$, whence tan. $ROQ = (r_a + r_{ee})$. Again, taking any point T representing any voltage OT at the shunt terminals, set off

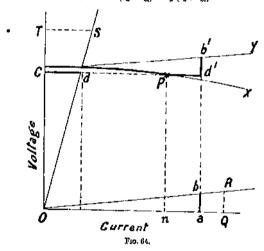
from T a line $TS = \frac{OT}{r_{sh}}$ whence $\tan SOQ = r_{sh}$.

Now take any point P in x and draw its co-ordinates PC and Pn, then the intercept Cd between OP and OS = shunt current at this voltage Pn. As in the case of the pure shunt machine make Pd' = Cd, and draw an ordinate d'a through d' cutting OR and OQ in b and a.

Then making d'b' = ab, we get b' to be a point on the total Characteristic (y). Repeating this process for several points, such as P along (x), we finally get the curve y showing the relation between total armature current A_a , which $= A + A_a$, and total E.M.F. E, which $= V + A_a$ $(v_a + v_n)$, where in Fig. 64 On = A, $ua = A_a = ad$,

$$\therefore \Omega u = \Omega u + uu = A + A_{\bullet}$$

$$\therefore ab = \Omega u \left(r_a + r_{Sc} \right) = A_u \left(r_a + r_{Sc} \right)$$



(63) Determination of the External Characteristic of a Compound Wound Dynamo.

SHORT SHUNT.

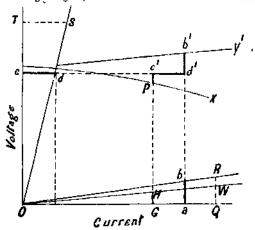
As the mode of procedure is precisely the same as in the case of the corresponding long shunt test, this latter will not be

repeated here, and must be referred to both for apparatus, which is the same in both cases, and for the diagram of connections which is shown in Fig. 63 (11.).

Graphical Determination of the Total Characteristic from the Internal one in a Compound Wound Dynamo.

SHOPT SHURT.

Referring to Fig. 65, let z be the external Characteristic. As



in the last case take any current QQ and set off $QW = QQ \times r_{\infty}$ and $QR = OQ \times r_a$ and join OR, OW.

Obtain OS as before, and let P = any point on the curve (x). From P draw Po' = GH, and from c' draw c'd' = cd; lastly, make db' = ab and b' is a point on the total Characteristic y, thus yis easily obtained. By reference to Fig. 65 it will be seen that the total E.M.F. $E = V + A_0 r_a + A r_{A_0}$, while the total current in the armature $A_a = A + A_{Sc}$, or in this Fig.—

$$ab' = PG + GH + ab = V + Ar_A + A_a r_a$$

and

$$Oa = OG + Ga = A + A_{Sh}$$

(64) Determination of the Separate Field Magnet Windings for Truly Compounding a Dynamo.

Introduction.—This is a practical method of experimentally determining the number of amptures of excitation to be supplied by both the series and the shunt coils in a compound machine without having to calculate them in the ordinary way from data pertaining to the magnetic circuit. The method forms an exceedingly instructive one for use in a laboratory, in illustrating theoretical principles, but it is essentially a works method, and has the advantages that the amptures are determined under full load working conditions, i.e. when the armature is exerting its maximum demagnetizing influence on the field, and furthermore that since the whole machine is already constructed except for these coils, any errors in the lengths and sections of the various parts of the magnetic circuit and in their

The conditions for automatic self-regulation by compound winding are, firstly, that with the external circuit open, i.e. no current through the series coils, the shunt winding must alone produce, at the given speed, the full specified voltage of the machine. Secondly, that on full lead the series or winding must supply such an extra amount of magnetization, due to the full-lead current in its roils, as will main.

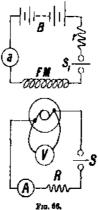
tain the same specified voltage of the dyname. There are obviously two modes of procedure differing slightly from one another and depending on circumstances at hand, namely, (1) to compound a machine given its carcase ready built up and the armature ready wound; (2) to compound a shunt

machine by finding the necessary series turns to be added. Consider the former

conditions first,

estimated permeabilities are nullified.

Apparatus. — In addition to the muchine in question—a voltmeter V; switches S and S_1 ; ammeters A and a; rheostate R (p. 606) and r (p. 599); source of E.M.F. (B) for excitation, either battery or other dynamo, etc.



Determinations.—(1) Take a mitable field frame of the type of machine specified, i.e. one that previous experience shows to be of sufficient size for the work, also a suitable ready-wound armature, wound with a suitable number of turns of a gauge sufficient to take the specified full-load current of the machine at an orthodox current density in the coils.

(2) Wind the field magnet limbs uniformly with a few temperary turns F (known) of thick wire or lead, and connect up as in Fig. 66, adjusting the instruments to zero.

(3) Run the armature at the specified speed (n) revolutions per minute, and with S open close S_1 , adjusting the exciting current (a) by means of r until V reads the specified voltage. Then aF = amp-turns to be supplied by the shunt coils alone.

(4) Now close S, and obtain the full-load current A, of specification, at the same speed (a) above; again adjust τ so that V again reads the same specified voltage as before. If a_1 now — the exciting current, then $a_1F = \text{amp.-turns}$ to be supplied by (series+shunt) together; hence $(a_1 - a)F = \text{amp.-turns}$ to be supplied by series coils alone at that voltage V and speed (a)

or number of series turns = $\frac{(a - a)F}{A}$.

Such a gauge of wire is then chosen for the shunt coils, that with a shunt current of, say, 2% of A (the main one) the shunt resistance $=\frac{V}{2A} = 50\frac{V}{A}$ ohms and the amp-turns =aP.

100

If we are dealing with case 2, in which it is desired to convert a shunt machine into a compound one, it should be remembered that such an alteration is only possible when the field numbers are not magnetically saturated.

The mode of procedure is then practically the same as before, and is as follows—

Disconnect the shunt and separately excite it, so as to reproduce the same terminal voltage (at full load) as the shunt (by itself) gave with the armature on open circuit.

If then the total number of shant coil turns = T and the shant current rose from the original value (a) to the new value (a_1) in order to keep up the same voltage at full load as on open circuit, then $(a_1-a)T=$ amp-turns to be supplied by series coils;

and if the full-lead armature current is A, then number of series turns = $\frac{(a_1 - a)T}{A}$, the speed being constant all the time.

It will be obvious that the method serves to determine the windings necessary to over compound, the exciting current at full load being raised until the excess over the normal voltage = the drop of volts in the mains at that current,

(65) Determination of the Speed and E.M.F. at which a Dynamo truly Compounds.

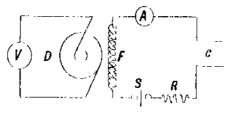
Introduction.—The present test of course relates to a compound would dynamo which is already built and finished. It has been proviously mentioned that a given machine can only compound truly and exactly to give constant voltage for wide variations of external current, at one particular definite speed. This is owing to the different alterations which a definite variation of speed produces on the series and shunt Characteristics of the machine. Thus, if after a machine is built and completely finished it is found that the compounding is not quite correct at the speed used in the calculations, which could easily be the case, then the speed would form a means of final adjustment and the mode of procedure would be as follows—

- (a) With the machine connected so as to self-excite in the usual way, place an external circuit consisting of an ammeter A, wherestat B, and switch S in series with the machine terminals and a voltmeter Y across them.
- (b) Run the dyname at the speed coupleyed in the design, and take first the open-circuit volts V and then that at some 4 or 5 leads between 0 and the maximum.
- (c) If on plotting these observations the Characteristic thus formed droops, the series coils are too weak in their effect and the speed should be raised a little, another set of readings being taken.

In this way a speed will be found by trial such that the curve is a horizontal straight line or nearly straight between 0 and full lead. The speed and volts at the terminals now are the values required for exact compounding.

(66) Variation of the E.M.F. of an Alternator with Speed at Constant Excitation.

Introduction.—The present test is an important one, as showing not merely the effect of alteration of speed on the E.M.F. developed by an alternator for constant exciting current, but also whether the demagnetizing effect of the armature on the field, due to eddy currents generated in it, is producing a perceptible effect, and if so the speed at which this effect begins to assert itself most forcibly. The eddy current loss varies as the square of the speed for constant magnetic field, so that the results of the test will give a measure of the adequacy of the lamination of the iron parts of the machine.



Fin. 67.

Apparatus.—Alternator D to be tested; alternating current voltmeter V; speed indicator and means of driving D at any suitable speed. For the exciting circuit, in addition to the field coile F of the alternator—a variable rheostat R (i. 599); switch S; ammeter A; exciting E.M.F. ϵ consisting either of the requisite E.M.F. from a secondary battery or auxiliary direct current supply, etc.

N.B.—Since in this test the speed is variable, and consequently also the periodicity of the current, the voltmeter V should be either a "hot wire" or "electrostatic" instrument, these being the only two types of meters which are unaffected by the variation of periodicity.

Observation.—(1) Connect up as in Fig. 67, and adjust the pointers of the instruments to zero. See that all lubricating cups in use feed properly and slowly, and then start the alternator.

- (2) Close S, and adjust the exciting current on A to the normal for the machine by altering R, and keep it constant; then adjust the speed so as to obtain the lowest readable voltage on V; note simultaneously the speed and voltage V.
- (3) Repeat 2 for about ten different speeds, rising by about equal increments from the above value to the highest allowable (a) at the same constant normal excitation, (b) at a constant value 50% less.
- (4) Repeat 2 and 3 for the same constant exciting currents with constant full load arouture current in each case respectively, and tabulate your results as follows—

NAME		DATE
Alternator tested: No Normal Full-Lead Volta	Typo Amperes	Maker Speed za
Specil Hovs. por min,	Yoltuga (Incressal) Ir	Exciting Current A Supp.

(5) Plot curves having E.M.F. (i.e. terminal voltage) as ordinates and speed as abseisse for each excitation both on no-load and full-load to the same pair of axes.

Inferences.—Carefully state all that can be inferred from the results of the above test, and point out their bearing on the design of alternators.

(67) Variation of the E.M.F. of an Alternator with Excitation at Constant Speed (Magnetization or Open-Circuit Characteristic).

Introduction.—This test is an important one, in that it shows the degree of approximate magnetic saturation of the field magnets at any excitation, and in conjunction with the short-

circuit characteristic will give a predetermination of the regulation of an alternator for terminal E.M.F., on load. If the magnetization of its field magnets is carried too close to the point of saturation, then manifestly it will require large variations of exciting current to produce comparatively small variation in the E.M.F. of the machine. This, it need hardly be pointed out, is undesirable, and would cause a most insensitive form of regulation. Again, it will be apparent that, if no demagnetizing action of the armsture on the field is going on, the exciting (i.e. magnetizing) current will represent the magnetizing force and form a measure of it. This in turn will create a certain magnetic field and magnetization, and in this field the armature rotates, or as in the inductor form of alternator this field is made to change from zero to full and back to zero. and in so doing cuts the stationary armature conductors. But the E.M.F. generated is c rate of change of this field, and at constant speed to the field strongth itself. Hence the E.M.F. is a measure of the magnetic field or induction excited, providing there is no armature reaction. Thus the present test will give us approximately the curve of magnetization of the alternator field magnets, but it must be carefully remembered that this is only approximate and provided there is no armature reaction on the field due to eddy currents in the armature, which should not occur when the machine is running on no load.

Apparatus.—Precisely the same as that used in the preceding test.

Observation.—(1) Connect up exactly as indicated in Fig. 67, and adjust the instruments to zero. See that all lubricating cups feed properly and slowly, and then start the alternator.

- (2) Adjust the speed of the alternator to the normal value for that machine, and keep it constant. Close S and adjust the exciting current (by varying K), so as to obtain the lowest readable voltage on V. Note this simultaneously with the exciting current and speed.
- (3) Repeat 2 for about ten different exciting currents, rising from the preceding amount to the maximum allowable, the speed being constant at the above value throughout.
 - (4) Take a similar descending set of observations as in 3.

(5) Repeat 2 and 3 for (constant) speeds 50% below, and if possible 20% above normal, and tabulate your results as follows —

Name		DATE			
Alternator tested . N Normal Voltage — . Normal Enerting Cur		Type Current	Maker Speed		
Speed	Recting Carrent A Amps.	Termosi	Voltage F.		
Heys, per mill.	Ascending Describing	Ascending	Describing		

(6) Plot curves for each speed to the same axes having volts as ordinates and exciting currents as abscisse, both for ascending and descending readings.

Inferences. -- State very clearly all that can be inferred from your results, and point out their bearing on the design of alternators.

(68) Magnetization Curve of an Alternator on Full Load—Non-Inductive and Inductive.

Introduction.—While the "no load magnetization" curve or "open circuit" Characteristic of both an alternator and D.C. dynamo take the same general form, the curve which, as we have seen, relates terminal voltage of armature with excitation current is different on full load, and in the case of an alternator depends on the nature of the external load, i.e. whether inductive or non-inductive. This difference is due to the loss of terminal voltage on load caused by the almic resistance, reactance, and reaction of the armature when delivering current; though only resistance causes loss of power. Armature reaction is responsible for distorting and either strengthening or weakening the main magnetic field in the air gap, and is due to armature current and depends on the power factor of the external circuit, while armature reactance, due to the self-induction of the armature conductors,

causes the current to lag behind the induced voltage, though in phase with the terminal voltage, and is unaffected by the power factor of the external circuit. The magnetization curve on full load, when compared with that on no load, affords valuable information needed for the design of a field regulator for the alternator to give any particular degree of sensitiveness.

Apparatus.—Precisely that given for Test No. 70.

Observations .- (1) Connect up as in Fig. 69, levelling and adjusting such instruments as need it to zero. See that the lubricating arrangements are working properly on starting up the motor alternator, which should be the same as that used in obtaining the "open circuit" Characteristic of Test No. 67.

(2) With a variable non-inductive resistance R connected for absorbing the output, and with R and r full in, adjust the speed of the alternator to its normal value and maintain this constant throughout by field regulation on the driving motor. Now close S, and S and reduce R until the alternator gives full-load current on A, then note the readings of V, A, and (a) at constant normal speed for this and a series of exciting currents (a) decreasing by about equal amounts to the lowest possible, the armature current A being kept constant by reducing R.

(3) With a variable inductive resistance for R-composed either of an adjustable choking coil in series or parallel with adjustable non-inductive resistance, or of a synchronous motor. the excitation and loading of which can be varied (vide p. 305), and the addition of a wattmeter for measuring the power absorbed in R. Fig. 69. Repeat obs. 2 for constant power factors cos & of, say, 0.9, 0.8, etc., leading and lagging if possible, and tabulate all your results as follows-

Allemator tesled ; Full lead : Volta =	-	• • [T		Maker Speed =		
Nature of load:— lad, or Non-Ind.	fipoed.	Armature Ampa,	Exciting Amps, a.	Volta V.	Watts W.	Power Vo dor con $\phi = \frac{W}{AV}$

(4) Plot (from obs. 2 and 3) curves of full-load magnetization to the same axes, having volts V as ordinates with exciting currents (a) as abscisses.

(5) For comparison replot the "no-load" magnetization curve obtained in Test No. 67 for the same alternator on the above source sheet.

Inferences.—What can you deduce from the results of the above test, and how can the range of field regulating resistance be obtained for maintaining constant voltage between 0 and full load on any particular power factor of circuit! What excitation is uncessary to send full-load short-circuit current through the armature at normal speed!

(69) Determination of the Short-Circuit Characteristic of an Alternator.

Introduction.—This characteristic, which is really the magnetization curve of the alternator on short circuit, differs from that obtained in Experiment 70, in that in conjunction with the "open" circuit characteristic of the machine, p. 169, it forms a means of predetermining the "voltage drop," i.e. the regulation of any alternator at different external loads and power factors. In this way large alternators may be tested while giving full-load current although requiring very little power to drive them.

Apparatus.—Precisely that detailed for Experiment 70, the resistance R being capable of variation and of being short circuited.

Observations.—(1) Connect up precisely as in Fig. 69, and adjust the pointers of such instruments as require it, to zero. See that all lubricators in use feed slowly and properly.

- (2) Start the alternator up to normal speed and close S, noting the readings of V and A (if any) with R cut out to short circuit.
- (3) With (r) full in, close (s), and adjust the exciting current (a) (by varying r) to some small value that will cause A to read about with the full load current of the alternator. Now read all the instruments. Next open S and again take readings, the speed being kept constant at the normal value throughout.
- (4) Close Sagnin, and increase A by about another 10th, by suitably increasing the exciting current (a). Then note the

readings of all the instruments. Next open S and again take readings, the speed being constant at normal value throughout.

- (5) Repeat (1) for a series of values of A up to 20% above, full load value.
- (6) To determine the effect of speed variation on the short-circuit current, run the alternator up to max, safe speed and raise its excitation until full load, or 20% over full load, current is obtained. Note this current, the speed, excitation and voltage and also for some ten different speeds, decreasing by about equal amounts to the lowest convenient at constant excitation, and tabulate in the following manner.

Note.—To avoid the risk of damaging the armature of the machine, especially if a large one, the series resistance R should all be cut into circuit before closing and again before opening S, and should be cut out to short circuit just before taking instrument readings.

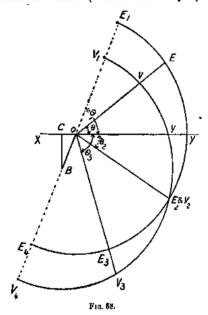
Speed (non- stant).	Torminal Acr Short Chesis B4	Open Cucut R	Blimb Coccup Armatura Current A.	Exciding Current a.	Effective Volta for Onune Resist. All r	Idlo or Inductive Voltage Drop $\sqrt{K^2 - (AR\gamma)^2}$ = $R\mu$

(7) Plot the "short-circuit characteristic" having values of (A) as ordinates and (a) as abscisse, and also the curve having A as ordinates with speed as abscisse.

Inferences.--State all that can be deduced from the results of the test.

Determination of the "Voltage Drop" of an Alternator for any given load and circuit Power Factor.

From the results of the above test and with the aid of a simple graphical construction, it is easy to find approximately the voltage drop corresponding to any load current and power factor. ThusFrom any point O in any straight line XY set off OE, to a convenient scale, to represent any desired "open circuit" voltage of the alternator and at such an angle θ to the current line XY, that the power factor (cos. θ) of the circuit has the desired value for the particular lead current (= short circuit current A) assumed.



With centre O and radius OE draw the semi-circle E_1YE_4 . Next set off along XY_1 the line $OC = AR_T$ the around red drop and allowance (K) for eddy current loss, corresponding to the same main current A.

Note.—In small, slow speed machines, the power lost due to eddy currents in armature core and pole pieces is small, and the effect of this on the voltage drop is also small compared with the term AR and can be neglected. When, however, the effect is too

large to neglect as in large machines the term AR can be increased by a certain percentage (K) depending on the form of alternator and the speed, (as dictated by experience with this type of machine or by experiment) to allow for the eddy current effect. Since the term AR_r is small compared with E, the error introduced in the value of the inductive drop E_t , through estimating the percentage increase of AR wrongly, is very small.

From C draw CB perpendicular to XY and \Rightarrow the short-circuit inductive or idle voltage drop E_t due to the self-induction of the ermuture and loss of voltage due to armsture reaction. Join OBwhich therefore = the open circuit voltage E_i which is necessary to overcome the self-induction and resistance of the armsture and leads, for the short-circuit current A assumed. OCB is therefore the right-angled triangle of E.M.F.'s on short circuit and thoungle COB - the angle of lag between current and voltage on short circuit. Now with centre B and radius OE draw the semi-circle V_1VV_2 . Then OV = terminal voltage of the machine and VE the voltage drop for the main circuit current A and sircuit power factor cos. θ . OV and I'E can similarly at once be found for any other value of power factor with the same main current A from the same diagram. A new diagram must, however, he constructed in a similar manner for a different current A in order to obtain the terminal volts such as OV and drop such as VE for this new current. Some interesting cases are now obvious, namely-

For main current lagging behind the voltage, i.e. self-induction predominating in the main circuit.

- (1) For main circuit power factors corresponding to an angle $\theta_1 = COB$, when OE takes the position OE_1 , in line with BO, the terminal voltage $OV_1 = \min \max$ and the inductive drop $V_1E_1 = \max \max$.
- (2) For a non-inductive main circuit, θ= O and the terminal voltage OY is in place, and coincides in sense, with the main current, but will differ from the resultant voltage OB by a little more than 90°.

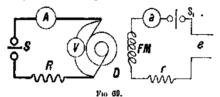
For main current leading in front of voltage, i.e. capacity pradominating in the main circuit.

(3) For the negative angle θ₂, terminal voltage OV₂ = open circuit voltage OE₂ and there is no inductive drop.

(4) For greater "leads," the terminal voltage is greater than the open circuit voltage, e.g. for a $-^{vs}$ angle θ_3 the terminal voltage $-2V_3$ and open circuit voltage OE_3 , maximum values of these quantities being reached at OV_4 and OE_4 where the maximum $-^{vs}$ inductive drop $=E_4V_4$.

(70) Determination of the External Characteristic of an Alternating Current Generator.

Introduction.—This test is for the purpose of experimentally determining, for different speeds and excitations, the relation



between external current and the terminal voltage producing it. By means of the Characteristic curve, as it is called, so obtained by plotting the observations, it can be seen at a glance whether the alternator possesses any series defects. Its performance when running on some particular circuit at some particular speed and excitation is also easily discernible therefrom.

Apparatus.—Alternator D to be tested; switch S; alternating ammeter A; and voltmeter V; non-inductive resistance R, which should preferably consist of either a bank of glow-lamps (p. 598), earbon (p. 597) or water rheostat, all of which are non-inductive; in circuit with the exciting coils F—a rheostat τ (p. 599); switch S_1 , ammeter (a); and source of direct current s from secondary cells or otherwise; speed indicator. Wattmeter W (not shown) for measuring the true watts absorbed in R when this is inductive.

Observations.—(1) Connect up as in Fig. 69, and adjust the pointers of all the instruments to zero, if necessary.

- (2) Start the alternator up, seeing that all lubricating arrangements in use feed properly. Close S_p adjusting both the speed and excitation to the normal for that machine.
- (3) With this excitation and speed constant, take, by varying R, a set of readings for about ten different values of external current between 0 and the maximum permissible, differing by about equal amounts, and note the simultaneous readings of V and A.
- (4) Repeat (3) with the same normal excitation, but for constant speed 50% below normal.
- (5) Repeat (3) and (4) for a different excitation, say, 50% lower than normal, and tabulate all results in the accompanying form.
- (6) Measure the resistance of the armature, while warm, by the "Potential Difference" method (see p. 84), or by the annucter voltmeter method, p. 86.

Alternator to	l Volts	Λ		. հիր	d	Percels p = 2x :	etk por Revol. I x Frequency. mee Worm 2	
Speed Revs, per mm.	Exerting Current (a) Amps.	Volts.	Ainps.	Walls II',	App. Walls	Power Factor on the	Inducti Residence.	E.M.F.
			 			JV.		I pd.

- (7) Plot the external Characteristic curves for each speed and excitation having terminal volts V as ordinates and current A through armature and external circuit as abscissa, in each case (see p. 3 on curve plotting) using the same pair of axes and curve sheet.
- (8) Deduce the total Characteristic curves of the machine from the "external" ones in 7 above by means of the graphical method given below.

Inferences.—Very carefully state all that you can infer from your experimental results, and show in what way the above curves indicate the performance of the alternator, and give an idea as to the goodness of the efficiency.

Graphical Determination of the Total Characteristic of an Alternator from the External Characteristic.

The total Characteristis of an electrical generator is the curve showing the relation between the total E.M.F. in volts generated by the machine and the total armature current in amperes.

ANALYTICAL TREATMENT.

Referring now to the preceding diagram (Fig. 59), let L - self-induction of the armsture in henries —

 τ_a = ohmic resistance of the armsture in ohms,

R=ohmic resistance of the external circuit, assumed to be non-inductive.

p = angular velocity of the alternating current = $2\pi n$. n = frequency or periodicity in \frown per sec.

If then a current A flows in the external circuit at a terminal voltage V and E = total E, M, E, of the generator,

then
$$A = \sqrt{L^2 p^5 + (R + r_s)^2}$$
 but $V = AR$;

hence $K = \sqrt{L^2 p^2 A^2 + (R + r_a)^2 A^2} = \sqrt{L^2 p^2 A^2 + (A r_a + V)^2}$.

Consequently we see that the total E.M.F. in volts generated by the alternator is represented by the hypothenuse of a right-angled triangle, of which the other two sides represent L_PA —the inductive E.M.F. necessary to evencome that of self-induction, and $(Ar_a + V)$ —the effective E.M.F. necessary to send the current A through the ohmic resistance $(B + r_a)$.

If K= number of periods per revolution of the armature, then $\frac{KN}{60}=(n)$, the frequency in ω per sec.; whence $p=2\pi\frac{KN}{60}$ where N= number of revolutions per minute the armature is making.

Having thus obtained an expression for the total E.M.F. of the machine analytically, we will now proceed to deduce it graphically from our external Characteristic,

GRAPHICAL TREATMENT.

Let my represent the external Characteristic plotted to the rectangular axes OT and OS, of which the former represents voltage and the latter current, respectively. (See Fig. 70.)

From the point O or origin draw the straight line OQ such that tan, $QOS = r_0$, and also draw the straight line OP such that tan, POS = Lp for the particular speed at which xy is taken.

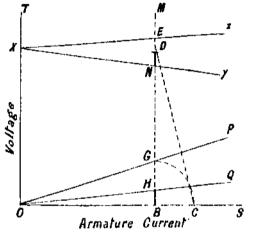


Fig. 70,

Take any point N on the external Characteristic xy and through it draw an ordinate MNB cutting OP, OQ and OS in the points G, H and B, respectively.

Set off ND = BH and BC = BG and join DC, which therefore = E. Lastly, make BE = CD.

Then E is a point on the total Characteristic required. If this construction is repeated for several more points, such as N on xy, we finally obtain a series of points such as E, and on drawing a mean curve through them all we obtain the required total Characteristic xx. In this construction it will be noticed that—BN=the terminal voltage (Y).

BG = BC = the inductive E.M.F. (LpA). BH = ND = the effective E.M.F. (Ar_s).

. DHC is consequently a right-angled triangle, and

hence $DC = E = \sqrt{BC^2 + BD^2} = \sqrt{(LpA)^2 + (Ar_a + V)^2}$. Probably a better mode of procedure and one autrequiring the

Probably a better mode of procedure and one and requiring the use of a protractor in obtaining the correct angle at which to act off OP and OQ is to first take any point N on xy, obtain the ordinate MNB and set off BG the current $OB \times L_P$, also $BH = OB \times r_a$, then joining these points H and G to O we get the required lines OHQ and O(P) respectively, after which proceed as above.

(71) Determination of the External Characteristic of an Alternator for different circuit Power Factors.

Introduction.—The circuits which have to be supplied from alternators, in ordinary commercial work, are invariably inductive, possessing either solf-induction or capacity or both. As the inductiveness of the circuit affects the terminal voltage of an alternator,—self-induction causing the characteristic to fall and capacity enusing it to rise, it is important to be able to determine the characteristic for any power factor of the circuit, whether the current lags or leads with respect to the voltage.

Lagging currents can easily be obtained with any power factor by suitable combinations of self-induction and chimic resistance, as for example by carbon rheestats and continuously variable choking cells or dimmers.

Leading currents can be obtained by inserting along with, say carbon rheostats (1) a number of condensers possessing considerable capacity, (2) a long length of concentric cable, (3) a synchronous a.c. motor with fields excited so that the back E.M.F. of the motor exceeds the voltage of the aternator. This is by far the most convenient method, for any load can easily be taken from the alternator by either braking the motor pulley or making it drives a d.c. dynamo at various loads. It can be shown that over-excited synchronous motors cause a leading current to flow in the circuit supplying them, and home produce the same offect as 1 and 2 above. By adjusting the excitation of such a motor any lead can be obtained within limits.

Where the only means available for obtaining lagging power factors is by varying combinations of self-induction and olunic resistance, or for obtaining leading P.F.s is by varying combinations of capacity and olunic resistance, it is a very tedious process t, try and take a series of readings of output current with terminal voltage at constant P.F. This is obvious since it entails varying the inductive and non-inductive sections of the load circuit so that they always bear the same ratio to one another, as only this will keep $\cos \phi$ constant in value, since the P.F. or $\cos \phi = \frac{\text{olmic resistance}}{\text{impedance}}$. In other words, trial combinations would have to be repeatedly made and the value of

impedance binations would have to be repeatedly made and the value of $\frac{V}{AV}$ worked out for each, to see if it had the desired value for cos ϕ . For this reason the following method is better, and is applicable to any appliance capable of giving an electrical output which has to be absorbed in an inductive circuit. Since the output obviously comprises (angles $A \times \text{volts } V$), both of which are variable simultaneously between 0 and full load, and $A = \frac{V}{\text{impedance}}$ or $V = A \times \text{impedance}$, it follows that A will be

constant if V and the impedance vary in the same proportion, while V will be constant if A and the impedance vary in inverse proportion. Thus if the inductive portion of the load circuit is adjusted to max. value, and the non-inductive portion in series or parallel with it (whichever is found most suitable) is varied, it is possible to obtain different values of A corresponding to different values of $\cos \phi$ at constant V, or different values of V corresponding to different values of $\cos \phi$ at constant A, and a

corresponding to different values of $\cos \phi$ at constant A, and a curve can be plotted between $\cos \phi$ as ordinates and the variable as abscisse. If, now, the inductive portion is made less inductive and the non-inductive part again varied, a now value will be obtained for the constant and a new series of values of $\cos \phi$ and the variable obtained, which will give a second curve

Repeating the process for some five or six degrees of inductiveness, giving therefore as many values of the constant and corresponding curves between $\cos \phi$ and the variable, we can utilize these auxiliary curves to obtain the same number of

with cos & sa ordinate and the variable as abscisse.

curves between V and A cach at any desired constant power factor (cos ϕ) within the limits produced by the range in degree of inductiveness used. As an example—Suppose A is the constant and V the variable with $\cos \phi$, and that six auxiliary curves, each obtained for, and marked with, the corresponding constant, are plotted on the same sheet. Now to obtain the curve between V and A at, say, 0.9 power factor: note the six points or voltages on the volt scale cut by the ordinates through the 0.9 mark on the $\cos \phi$ scale and the six curves. Then the six voltage values so found, plotted against the six constant values of A marked on the respective curves, will give the desired relation between A and V at a constant power factor $\cos \phi = 0.9$.

Similarly, a curve between A and V could be drawn for $\cos \phi = 0$ -8, 0.7, 0.6, etc.

Apparatus.—The same as that detailed for Test No. 70.

except that the load resistance R must now comprise a variable self-induction and variable non-inductive resistance, and that a wattmeter W must be inserted so as to give the true watts absorbed in the whole circuit.

Observations.—(1) Connect up as in Fig. 69 with the slight

modifications just mentioned. Level and adjust the pointers of any instruments needing it to zero, and see that the lubricating arrangements are in operation on starting up the machine. (2) With N closed and with both secitation and speed adjusted

- to the normal value and maintained constant, vary the proportions of heavy solf-induction and large olimic resistance in the main circuit, so as to obtain some six different voltmeter and corresponding wattmeter readings for each of five different but constant alternator currents A, differing by about equal amounts between 0 and full load, the same value of main current to be obtained for each of the six readings of a set.
- (3) Plot five curves one for each of the five constant values of mail current, each having the terminal voltage of the alternator as abscisse and power factor (obtained by indicator or wattmeter and volt-amperes) as ordinates. Mark on each curve the constant main current at which it was obtained.
- (4) Repeat obs. 2 and 3 so as to obtain a similar set of five curves for leading currents of the same magnitude as proviously

used by varying the load on the synchronous motor and its excitation, and tabulate as in Test No. 70.

(5) Plot the external characteristic curves having volte asordinates and currents as abscisse for power factors differing by 0-1 at a time between 1-0 and the lowest obtained in the curves between voltage and power factor (3) to (4) above, each curve in (3) and (4) supplying one point only in each of the characteristic curves corresponding to the current and voltage, and the power factor for which the particular characteristic is plotted.

Inferences.—State clearly all that you can deduce from the results of your tests.

(72) Variation of Exciting Current with the Armature Current of an Alternator to maintain Constant Terminal Voltage on Inductive and non-Inductive Loads.

Introduction.—This test is a direct measurement of the range of variation in both the resistance and current of the field regulator required to maintain constant terminal voltage for any range of load, and which can otherwise be deduced from a reference to the external and magnetization characteristics of the alternator when available.

Apparatus.—That detailed for Test No. 70, with the addition of an adjustable inductive resistance for combination with R.

Observations.—(1) Connect up, as in Fig. 69, with R non-inductives only at first and the wattmeter inserted as a check on the product $A \times V$. Level and adjust all instruments, which require it, to zero, and on starting up the motor alternator see that all lubricating arrangements are working properly.

(2) With the speed and terminal voltage each adjusted to the normal value and kept constant—the former by explation at the driving source, and the latter by field regulation of the alternator—first note the value of exciting current (a), on open main circuit, and then with S closed for each of a series of 8 or 10 armature currents, A rising by about equal increments to full load by adjusting the non-inductive resistance R, the

field regulation of the alternator being adjusted so as to keep V constant with the speed constant,

- (3) With R now inductive, and the same value of speed and voltage as in obs. 2 maintained constant, adjust the inductive part to its maximum value and vary the non-inductive part so as to maintain the main current A constant at about quarter full-load value, the field current being correspondingly varied to keep V constant. Note the readings of A, V, W, and (a).
- (i) Repeat (3) for the same speed and voltage, but for constant values of A of about half, three quarters, or full load, and tabulate as in Test No. 70.
- (5) Plot the four auxiliary carees (vide p. 183), having power factors, cos. $\phi \left(= \frac{W}{\Lambda V} \right)$, as ordinates, with exciting current (a) as abscisse, for each of the four constant values of Λ respectively.
- (6) By interpolation and transference, plot the desired relations between exciting currents (a) as ordinates, with main currents (A) as abscissa for non-inductive load (obs. 2), and for inductive load (obs. 3 and 4) at constant power factors of 0.9, 0.8, etc.

Inferences.—State clearly all that can be deduced from a study of the shape and relative dispositions of the curves in (6) above.

(73) Determination of the Efficiency of an Alternator without running it on load.

Introduction.—The proceding method, although a direct one for obtaining the efficiency of any generator by measuring the II.P. absorbed in driving it and the output in the usual way, requires some type of transmission dynamometer and has therefore a limited application on account of the difficulty of measuring the large II.P.s in the case of large generators. While small alternators can be tested in this way, the method of driving the generator by an electromotor (preferably direct coupled) having a known efficiency-load curve, is more accurate, and also has a much more extended application in range of power. The power supplied to the motor x by its efficiency at that load at the power taken to drive the generator.

Both methods are however costly of application in the case of the larger generators and an arrangement similar to Swinburne's Test No. 82 would obviously be preferable in many ways.

Further, if while absorbing (from an outside supply) only a small fraction of its rated full-load output, the armature of an alternator carries full load current at normal excitation, both the losses and temperature rise can be determined at an economical cost of energy consmand in the test.

From the fundamental principle that, in any transforming device

output = input - total internal loss

we see that if the losses can be obtained in the various portions of the alternator, the input and efficiency are at once deducible and that the method is applicable to any size of machine, however large.

The total internal loss in an alternator is made up of—

(a) The total copper loss W_c in the armature windings, thus—

If C_a = the current per phase of armature winding

and r_a = the resistance per phase , , , , the total copper loss W_C in the armature of a-single-phase alternator = $U_a^2 r_a$; of a two-phase alternator = $2U_a^2 r_a$; and of a three-phase alternator = $3U_a^2 r_a$.

- (b) The total power absorbed in excitation W_E . Thus if C_E = the exciting current employed at a pressure of V_E volts, then $W_E = C_E$, V_E .
- $W_{x} = C_{x}$, V_{x} .

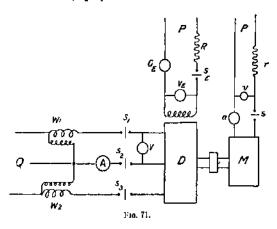
 (c) The total power absorbed in mechanical friction W_{RF} and made up of—windage, bearing friction, brush friction.
- (d) The total power spent in magnetic friction made up of—bysteresis and oddy currents in field and armature core W_{IF} . Then the total internal loss $W_L = W_C + W_E + W_{FF} + W_{FF}$

The last two losses, which may be termed the stray power, may be determined experimentally at no load by running the alternator as a synchronous motor, light and unloaded, and measuring the power absorbed by wattmeter.

Apparatus,—Alternator D to be tested, capable of being driven at no load and normal speed by some outside source of power. This might preferably be its direct-coupled exciter, if

there is one, and provided that, when used as a motor, it is powerful enough, or, in the absence of this, a direct-coupled motor M of known efficiency. The necessary switches; a watt-meter having a range up to say 5% of the full load of the alternator; an ammeter A; and a voltmeter V in the case of single-phase alternators and of two- and three-phase alternators with equally-balanced phases. Two of each type of instrument will be needed for two- and three-phase machines out of balance.

Observations,—(1) Connect up as shown in Fig. 71, adjusting such of the instruments as need it and assuming the alternator D to be a three-phase machine for instance. See that all lubricators feed properly.



(2) To run D as a synchronous motor from some a.c. supply Q of the normal voltage V and frequency developed by D. First start up D to its normal speed by means of M and adjust its exciting current U_R so that its terminal voltage V = that of the supply Q. S_D S_B , S_B being open, but S_B shorted by a wire and S_B by two synchronizing lamps (see p. 441) not shown, close this three-throw switch at the instant when the lamps are out and at

once open S. The alternator D will now continue to run as a * synchronous motor at normal speed, frequency and voltage.

(3) With D running as just mentioned, adjust its exciting correct C_k by the rheestat R so that a minimum intake current A is obtain 1 and hence maximum power factor, and note the wattmeter readings W₁ and W₂ and all the other instruments and speed.

Then $W_1 + W_2 - 3A^2r_a = W_{HP} + W_{IP}$

These losses are approximately constant for all leads, slightly increasing as the load increases due to change of induction through increase of excitation for voltage regulation, and to armature reaction in the normal operation of the alternator,

(1) With the same normal supply frequency as in obs. 2, and same excitation as found in obs. (3), increase the supply voltage V (by means of the field excitation of the supply V) so as to obtain a series of supply currents A rising by about equal increments from the value found in obs. (3) to full load, and note the readings of A V and W, W, at each.

Note.—The synchronous motor D will run throughout obs. (4) at constant normal speed but at a decreasing power factor, as was shown in Test No. 106, and since the excitation is constant at normal value, the losses $(W_c + W_{HF} + W_{LF})$ as measured by W_1 and W_2 will be the same as for the machine used as an alternator when giving the same current loads from its armature. The excitation loss W_L is also known, and the total internal loss at all loads can therefore at once be found and the efficiency Σ obtained from the relation—

$$\mathbf{Z} = \frac{\text{output}}{\text{output} + \text{losses}}$$

The accuracy of the values of efficiency (S) thus found will depend on the degree of accuracy with which the losses, in obs. 4, can be measured; this latter may not be high on account of the increasing inaccuracy of wattmeters on the lower power factors.

(5) If necessary, find the rise of temperature of the muchine after a rix hours' run on full-load or other desired condition.

Tabulate your results for the preceding test as follows-

Alternator; No Fall Load : Amps. ⇒ • Residences : Armature per Wellmeter Constants K ₁ ⇒	pheso #, = ,	Maker pred = Frequence Field =	y =
Speed of B. Bayery Frequency. Current Courters of C. Frequency. Courters of C. Frequency. Frequency. Frequency. Frequency. Frequency. Frequency. Frequency.	Watinot the distance of the Angle of the Ang		Birry Power loss W - 8.42s = War + Wyr Total loss W L

Plot the efficiency-load curve of the machine considered as an alternator having values of efficiency Σ as ordinates, and values of $\sqrt{3}AV$ (calculated for each value of A in the table but at normal voltage) as output at P.F. = 1.

The separation of the losses can be obtained in much the same way as that indicated in Test No. 77 for direct current machines by the use of the motor M in the following way—

- (4) With S_1 , S_2 , S_3 and S_B both open, run the alternator at its normal speed and note the readings (a_1v_1) of a and v. If $y_1 =$ the efficiency of M at this speed and load, then $y_1a_1v_1 = W_{HF}$ the power absorbed in mechanical frictions since with the fields of D unexcited there will be practically no iron lesses.
- (5) Next close S_x and adjust R so as to give normal full lead exciting current. Vary r so as to obtain the same speed as before and note the readings a_yv_y of a and v. If y_z = the efficiency of M at this lead, then $y_xs_1v_y = W_{RF} + W_{IF}$ and hence the iron lesses $W_{IF} = y_ya_xv_y y_ia_iv_i$.

Having now obtained the iron and friction losses the efficiency can at once be deduced for all assumed loads.

Tabulate your results for Tests 4 and 5 as follows—

Middle refer of Motor M at Speed used ; (at least $\alpha_1 v_1)y_1 = \dots$; (at least $\alpha_2 v_2)y_2 = \dots$

8	Ailon	nalar unexcile	ď	Aiu	runter Excite	ıl.	1,tr=
Alternata Speed,	-	ng of Voltageter (v)	l'riction Loss Fap = Finipp.		Voltmeter (2)	Friction + Iron Losses if ne + H're = yesters	Iron Loss II

The determination of the iron losses at any speed by the retardation method can be undertaken in alternators having sufficient inertia or momentum in their moving portion to prevent them slowing down to rest too quickly for readings of speed to be taken at intervals.

(6) With S. S. S. and S. both over now that neveral weed by

- (6) With $S_D S_D S_B$ and S_B both open, run D at normal speed by means of M. Then at a noted interval of time, the speed being at normal value, open S and note the speed by tachometer at, say, $\frac{1}{4}$ minute intervals as the alternator D slows down to rest, the motor M being of course unexcited. The retardation in this test is due to $|V_{BD}\rangle$
- (7) Repeat (6) with $\frac{1}{4}$ $\frac{1}{4}$ and full load exciting currents C_E by varying R. The more rapid slowing down in this test is due to $W_{RF} + W_{RF}$. Tabulate your results as follows—

Value of $W_1 + W_2 - 3 A^2 r_a$ (from Exp. 3).

		Tanky Dr. ,	" [F " 2 - "	21-12 fragin	to the wh		
Alternator	Uneverted.	Alt	enuntor Exe	ated	Vati	Actual	
Times 6, 4 ₁ , 4 ₃ , .	Species n, n ₁ , n ₂ , .	Exciting Current Ch	Times t, tq, tg , .	Б]н·eds п, н ₁ , н ₂ , .	N'E	Average Head N = 1 + 11	menn Power in Walts absorbed

Plot curves for 6 and 7 between speeds as ordinates and times as abscisser, and between $\frac{W_K}{I}$ as ordinates and average speeds N as abscisse.

The rationale of the retardation method is as follows-

Let I= the moment of inertia of the rotating system in C.G.S. units, or, gramme—cm.² about the axis of rotation, and let W be its angular velocity in radius per sec. Then the kinetic energy of the whole system or energy of rotation $K_x = \frac{1}{2}\omega^2 I \operatorname{crgs} = \frac{1}{2}(2\pi n)^2 I$ where $(n) = \operatorname{speed}$ in revs. per second. Hence the kinetic energy $= \frac{1}{2}(\frac{2\pi n}{161})^2 I \times 10^{-7}$

where (n) is now in revs. per min.

If now (n) = the normal speed of the alternator at the instant t of opening s and n_1, n_2, n_3, \ldots the successive speeds noted

t or opening s and n_1, n_2, n_3, \ldots the successive species noted at times t_1, t_2, t_3, \ldots , from the instant (t) when slowing down commences,

Then the energy expended or work done in the first interval of time in overcoming resistance is proportional to

ing resistance is proportional to
$$548 \times 10^{-12} I(n^2 - n_1^2)$$

and the mean power absorbed $W_K = \frac{518 \times 10^{-12} I(n^2 - n_1^2)}{t - t_1}$ watta at an average speed $N = \frac{n + n_1}{2}$ rows, per min.

By plotting a curve between values of $\frac{W_K}{I}$ for successive speeds and intervals as ordinates and the corresponding average speeds N for successive pairs of speeds as abscisse, we can get the loss at any speed, and that at normal speed by the point of intersection of the curve (produced backwards) with the full speed ordinate.

Note.—Since I is a constant but unknown quantity, the ordinates of the curve are the values of $\frac{\|f\|_{\mathcal{X}}}{I}$ and the ordinates do not therefore represent actual watts, but = watts \div a constant (I).

From Observation 3, however, we know that this normal speed ordinate = $W_1 + W_2 - 3A^2r_s$, the total friction and iron losses. Hence the value in actual watts of any other ordinate corresponding to any other speed is at once found by simple proportion.

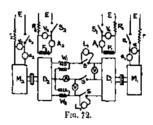
From the above data compile the following general table-

Full Let	ավ: Дա				Maker . = Fr Yield ## =	ભղποπεγ≖
atput and C.	utput FC.		Ins	MH,		7 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
March O	Watta O	Excitation $C_K V_E = W_E$.	Armatura S C_2r_= U'c.	Iron and Friction Was + Was	Total We = We + Wa + w.	Input W IFo+ i

Plot the load-efficiency curve having efficiency as ordinate and W_0 as abscisso.

(74) Efficiency and Internal Loss Test of a Pair of Alternators (by the Hopkinson Principle).

Introduction.—The following method is available when two similar alternators, as nearly alike in output as possible, are obtainable. It is analogous to the Hopkinson test of a pair of D.C. dynames, and has the double advantage that all the measurements are electrical ones; and also that while both alternators run under lead conditions, so far as field and armature current is concerned, each is running at only a fraction of its full K.W. capacity, and consequently the power taken from the necessary outside supply is small, even in the case of the testing of large alternators. The method further lends itself most conveniently to the determination of the temperature rise of each machine under the same heating conditions as would obtain if each was run for, say, six hours at full-load



output, but with far greater economy in the cost of energy consumed from the outside supply.

The test can be carried out with the two alternators under one or other of two conditions, vis. (1) when they are not mechanically coupled together, or (2) when their shafts are in accurate alignment and rigidly coupled. In each case (a) the alternator to be used as a generator (say D_1) must be either belted or (preferably) direct coupled to a small direct-current motor M_1 having a known "efficiency-load" curve at the speed to be employed; (b) the second alternator D_2 must be electrically connected to D_1 and run as a synchronous motor from its supply; (c) an

D.C. motor M_2) will be needed to run D_2 into synchronism, and afterwards to be disconnected if possible. Now, although under condition (1) above, the power factor of the circuit between D_1 and D_2 will decrease as the circulating current increases, any error that might be introduced from this cause, and referred to in test No. 73, p. 188, is eliminated in the present test, as the

losses are now measured in the D.C. circuit of M_1 instead of

being obtained from the readings of W1 and W2. Under condition (2) above, however, in which the shafts of D_1 and D_2 are rigidly coupled, the P.F. of the circulating circuit remains constant for all currents with any particular bolting of the half couplings. If this bolting can be varied, then each constant value of the P.F. can be varied from unity, when the half couplings are bolted so as to make the E.M.F.s of D₁ and D differ by 180° in phase (i.e. when in direct opposition of phase), to zero, when one half coupling is bolted with an angular difference relatively to the other half coupling equal to the angular pitch of the alternator field. Throughout this range the alternator with the greater excitation will be acting as generator,

Obviously with the rigid coupling of condition (2), the two alternators must not only be similar in output and voltage, but must also give the same frequency at the same speed, whereas in condition (1) their frequencies can be different if necessity arises. Further, the general applicability of the present method is questionable, e.g. in condition (2) the alternator D_2 must be coupled either (on the left) up to D, or (on the right) up to the other end of M_1 , so that either D_1 or M_1 must have a shaft extension each end. On the other hand, the test under condition (1) will need a second driving-motor M_2 , which for the highest accuracy should be capable of disconnection from D_{\bullet} after this is synchronized. These facilities may be obtainable in certain works, but seldom exist in a college laboratory,

Apparatus. That depicted in Fig. 72, where R_1R_2 are field regulators for adjusting the exciting currents in the fields F₁F₂

rir, are starters or main circuit adjustable rhoostats for the motors $M_1 M_2$.

 L_1L_2 are synchronizing lamps made for voltages equal that per phase of the supply.

E is a D.C. supply, and three-phase alternators are assumed for test as presenting slightly greater complication in connection and test than single or two-phase machines.

Observations.—(1) Connect up similarly to Fig. 72, but with any modifications which the facilities available in machines necessitate. Level and adjust to zero all instruments needing it, and on starting up see that all lubricating arrangements feed properly.

- (2) With D_1 running at normal voltage V and frequency, synchronize D_2 by obtaining equal voltages as V.V., and closing SSS at the moment when L_1L_2 are definitely out. M_2 (if used) being disconnected electrically and nucleating if the latter is
- possible.

 (3) Next adjust R_2 so as to make A a minimum for constant normal values of both V and the frequency,

Note the readings of all the instruments and the speeds of D_1 and D_2 .

Then the output of M_1 , or power required to drive D_1

 $= \frac{a_1 v_1}{c} = \text{the total internal running losses } (W_C + W_{MF} + W_{IF})$ (see p. 186) in D_1 and D_2 together (excluding excitation losses in $D_1 D_2$).

Where e = the efficiency of M_1 at this load and speed (from curve),

$$\frac{a_1v_1}{2a} = \text{the losses in either alternator,}$$
(4) Now reduce the excitation of D_2 by the same amount as

that of D_1 is increased, so as to obtain a series of main circulating currents A_1 , rising by about equal increments up to the full load current of the machines, and note the readings of all instruments at each value of current A_1 . Then the increased value of $\frac{a_1r_1}{2c}$ = the losses in either alternator at the respective current values A_1 , where (s) has an increasing value at each load as taken from the efficiency-load curve of M_1 . Adding half the total excitation loss, viz. $\frac{1}{2}(A_1V_1 + A_2V_2)$, to the above loss,

we get the total internal loss W_L (p. 186) corresponding to each

of the current A, and which will be practically those which would exist if either machine was supplying those currents as an alternator at the same speed and voltage. Tabulate all your results as follows:—

	T) po Maker A: Volta V. = Speed = .									
Alterestor D_d : No. —										
	Full Load : Amps = , .	Volte, = Bpeed								
Frequency (American American A		Silvey I threat to Advise = Kn + F v + F v + = Kn + A v + = Kn + A v + Total loss in P ₁ in P ₂ Total loss in P ₂ in P ₃ F v = A ₃ + kv + F v + Total loss in P ₃ or P ₃ F v = A ₃ + kv + v + Outprote as in Alternator = V A A F x = N v - Efficiency in Alternator Z = N v + N v								

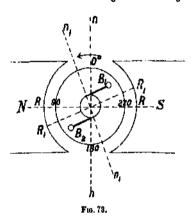
(5) Plot the efficiency-local curve of either machine considered as an alternator having values of Σ as ordinates and values of load $\sqrt{3}AV_S$ as abscisse.

Inferences.—Clearly state all that can be deduced from the results of the test.

Note.—If the wattmeters W_1 and W_1 (which are not really essential to this test, and only useful, if available, for observing and comparing certain quantities) are omitted, the eight columns in the table, necessitated by their use, can also be omitted,

Determination of the Distribution of Potential round the Commutator of a Dynamo.

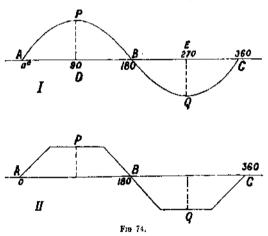
General Remarks.—On considering the action which occurs with a single turn of wire on a coreless armature as it rotates at a uniform rate through one revolution we find that, starting from a position 9°, which may be termed the zero position, when its plane is perpendicular to the direction of the lines of force due to the fixed field KS (Fig. 73), its E.M.F. is 0, because it is slipping through and not cutting these lines. When it gets to 90°, the rate at which it cuts the lines is a maximum, and this decreases round to 180° again, when the E.M.F. is 0, and after then the effect is simply repeated. The zero position m is the neutral axis or diameter of commutation for no current in the coil or armsture, while EE is the line of resultant magnetization at right angles to



nn. In fact, the E.M.F. generated in the coil at any position is approximately ∞ sine of the angle of rotation from nn, and, as we have seen, is zero at 0° and 180°, and a maximum at 90° and 270°. If the coil be wound on an iron core, carries a current, and is made to rotate, it will react on the fixed field NS, causing a distortion of this latter, so that n, n_1 will now be the neutral axis or diameter of commutation and $N_1 R_1$ the line of resultant magnetization. In other words, the resultant field produced by that due to the armature and field NS will be forced round through an angle ROR_1 in the direction of motion, and will cause the brushes to advance through an equal angle non_1 to the

position n_1n_1 , which angle is called the "angle of Lead" of the brushes.

• If now, the circular path of the coil, which we will assume for the moment not wound on an iron core, is developed out into a straight line AC, and the sine of the angular position from 0 (i.e. A), Fig. 74 I., plotted on the ordinates at each such position, the curve APHQC will be obtained, showing the variation of E.M.F. with angular position in one revolution. Thus A and C correspond to 0° or position nn (Fig. 73) when the



E.M.F. is nought, while PD and QE correspond to 90° and 270°, or position RE when E.M.F. = maximum. This curve is called a sine curve, and it possesses the uniform shape shown in Fig. 74 I.

Now in an ordinary iron core armature the E.M.F. of each coil fluctuates in a manner similar to that shown in Fig. 74 I. in a bipolar machine, and to that shown in Fig. 74 II. in a multipolar machine, but the commutator commutes such E.M.F. so as to develop an E.M.F. at the brushes perfectly continuous in direction.

Considering the approximate as which the line are expected.

Considering the armature as a whole, the line nn or n_1n_1 , i.e. the brushes of the modiline divide the aimature coils into two

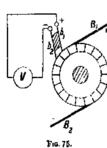
halves, which are in parallel with one another, now each half consists of separate coils in series with one another, each giving a certain but different E.M.F. depending on their position relatively to 0" or nn. These E.M.F.s being in series are added together in each half and the two summational E.M.F.s put in parallel. Thus the E.M.F. between the brushes = sum of E.M.F.s round

one half of armature between those brushes. Consequently, as we proceed from, say, the negative main brush, the E.M.F. (if we could sample it) round either half increases up to the other main brush, first slowly, then rapidly, and finally slowly again when

nearing the maximum point. From the preceding remarks it will be evident that two investigations can be made on the E.M.F. of armature coils—(a) that of any one coil in different positions of a revolution; (b) the way in which the E.M.F. varies as we proceed from one brush right round the armature.

There are many methods of performing these investigations, and amongst those most casy of application in practice may be mentioned Prof. S. P. Thompson's, Mr. Mordey's, and Mr. Swin-

barne's, and these we will now consider in detail. In Thompson's method of operating investigation (a) above, the



rangement consists of two flat metal strips or brushes b_1b_2 (Fig. 75) fixed to a piece of wood at a distance apart equal to the width between two consecutive commutator bars. A voltmeter is connected across h,b., which therefore measures the E.M.F. of a single section of the armature winding which is passing through the

particular position of the field, cor-

E.M.F. of a single section on the armature can be sampled at different points in the revolution. The ar-

responding to the position of the contacts. It is preferable that the compound brush b_1b_2 should be mounted on a brush rocker capable of swivelling round the shaft over a degree divided scale, so that angular distances from some starting-point may be accurately obtained.

The method has the advantage that only a comparatively short range accurate reading voltmeter is needed, say, to about ten volts or so in the case of a 100-volt machine. The main brushes B_1B_2 must be arranged to allow b_1b_3 to pass them on the commutator.

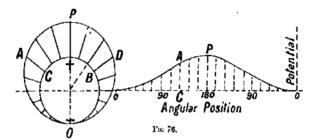
The readings of the voltmeter will be different according to whether the machine is giving no current at all or its full-load current. If the machine is shunt wound it may in the former case be self-exciting, as the shunt current will be so small compared with the load current as to not affect the distribution round the commutator,

If now the readings on F are plotted on the ordinates of a curve with the corresponding angular positions right round the commutator on the abscisse, the curve will not only show the variation of E.M.F. of the coil, but will show also the distribution of the magnetic field in the air gaps, the best position for the brushes and the "angle of Lead" which must be given to these when running on full lead due to the shifting round of the resultant magnetic field ER (Fig. 73) to E_1R_2 .

(75) Determination of the Distribution of Potential round the Commutator of a Dynamo. (Mordey's Method.)

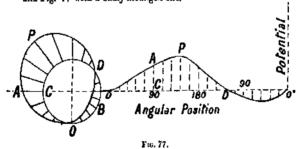
Introduction.—The following is a convenient and simple method of finding the above-named distribution, and consists in measuring the potential between one of the main brushes and a single movable or Pilot brush capable of swivelling right round the commutator. It is then found that the potential increases or decreases from that main brush (according to whether it is the negative or positive one) round each half of the armature to the other brush, and that the variation is regular in a well-designed, but irregular in a badly-designed machine.

To represent the resulting variation or distribution graphically Prof. S. P. Thompson proposes drawing a circle OBC (Figs. 76 and 77) to represent the commutator and divide it into, say, 36 equal parts of 10° each, set off radially outwards from the circle, lines ce potentials at the various angular positions of the pilot brush, thus getting the outer or potential curve OAD.



Next obtain the developed diagrams to the right of Figs. 76 and 77 by laying off a horizontal base to represent the length of the circumference of the circle OBC, then at the proper points along this angular line set up the radial lines from the left-hand Figure, due regard being paid to sign.

Fig. 76 is the result obtained with a well-arranged dynamo, and Fig. 77 with a badly-arranged one,



These curves show us several points, as, for example, the steepness of the curves in the right-hand diagrams enable an idea of the relative activity or idleness of the coils in these positions to be obtained, also the position of the brushes to give the best result and the distribution of field in the air gaps.

Fig. 77 may result from a machine in which the pole pieces are badly shaped, or the brushes badly placed.

Apparatus.—Dynamo to be tested, fitted with a third brush or pilot brush P capable of swivelling round the whole circle divided into degrees, and of making contact on the commutator at any position; a rather long range accounte reading voltmeter V, and arrangements for taking a load from the machine when required.

Observations.—(1) Calling the two main brushes B_1 and B_2 and the pilot brush P_i connect V between the negative main brush and P_i , the dynamo being shunt wound and excited off its main brushes B_iB_{ij} .

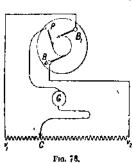
- (2) Run the inachine on open external circuit at normal speed, and adjust P in line with the negative brush, which latter has been previously adjusted to give no sparking.
- (3) Note the reading on V and the degree scale of P, and repeat every 10° right round the commutator at constant speed.
- (4) Repeat 2 and 3 for a full-load current taken from B_1B_2 , adjusting the speed (constant) to give the same voltage as before.
 - (5) Repeat obs. 1-4 with the same machine run as a motor.
- (6) Tabulate your results in a convenient form, and plot a pair of curves for each test in the way indirated above.

Inferences.—State very clearly what you can deduce from your curves of distribution, and indicate in the developed diagram the positions of the poles, brushes, and resultant magnetic field of the machine.

(76) Determination of the Distribution of Potential round the Commutator of a Dynamo. (Mordey-Swinburne's Method.)

This is a neat modification of the preceding method, and consists in connecting a high resistance wire V_1V_2 across the main brushes B_1B_2 , and finding by means of a sensitive detecting galvanometer G a position G along the resistance V_1V_2 such that G does not deflect. The point G is then at the same potential as F; hence since V_1V_2 is fixed, the distance V_1G or V_2G gives the relative potentials for various positions of F. The potential

meter V₁CV₂ can be easily calibrated by taking one single reading of the volts (V) across B_1R_2 , whence the distances V_1C_1 for



instance, in volts = $\frac{V_1C}{V_1V_2}$ of Vwhere V_1C and V_1V_2 are in olms, say, or some known units.

The speed must be constant throughout the test, so as to maintain V constant. Being a zero method it is very accurate, and has the advantage of not requiring a voltmeter which has to be equally accurato over its whole range, but only at one point.

(77) Analysis of the Total Internal Loss of Power in Direct Current Dynamos and Motors.

Introduction.—In test No. 82, p. 220, it is pointed out that the total internal loss of power in a direct current dynamo or motor is made up as follows-

(i) Copper Loss occurring in the armsture and field coils, caused by heating due to the passage of the current.

This is at once easily calculable from the relations there given for finding the copper loss in either series, shout or compound machines, when the resistances of the several coils, and the

respective currents which each carries, is known. The loss in each circuit varies as the square of the current. (ii) Mechanical Friction due to air churning or resistance, brush and bearing friction, each of which varies as the speed

simply. (iii) Eddy Current or Foucault Current loss occurring in the armature core, and also in the armature conductors, and varying as the square of the speed for the same excitation, since the eddy currents will be directly or speed at constant excitation while the watts used in producing them will vary as the square of these currents, or if WB = Watts wasted in eddy currents and n= speed in rows, per min., then loss from this cause is $W_E \propto n^2 K_E$, where K_E is a coefficient depending on the eddy loss.

(iv) Magnetic Hysteresis in the core due to reversals of magnetization in it as it rotates and \propto to its speed. If $W_H =$ the loss from this cause and K_H its co-efficient, then $W_H \propto nK_H$; hence the total iron loss $W_I = W_H + W_B = nK_H + n^2K_E$.

This equation has been made use of in several methods for separating these losses. Thus in Mr. Mordey's method, which is applicable to determining the losses in an unwound armature core as well as a wound one, the armature to be tested is driven, when in position between its own field poles, at different speeds (n), with its field (a) unexcited, (b) excited to a constant degree, (c) excited to various degrees, by an electrometer, and the power so required measured by a dynamometer or by knowing the efficiency of the motor accurately.

On plotting a curve between the speed (a) and the powers W required to drive at different speeds in a constant field, the constants K_H and K_R can be found from it.

Mr. Kapp's method is a slight modification of the preceding, and is only applicable to a ready-wound armature core. It consists in measuring the power W required to run the armature to be tested at different speeds in a constant field N, by running the armature itself as a motor "light," and noting the corresponding voltage V and current A taken at each speed (n).

If then $T_a = \text{total number of armstare turns all round we have the fundamental relation <math>Y = T_a Nn \cdot 10^{-8}$.

But
$$W = AV = AT_a Nn \cdot 10^{-8} = nK_H + n^2K_R$$

$$A = \frac{K_H}{T_0 N 10^{-8}} + n \frac{K_R}{T_0 N 10^{-8}} = (a \text{ constant} + n \times a \text{ factor}).$$

On plotting therefore the curve between A and n to the axes OY and OS with (n) along OS, we shall obtain the straight line PQ. The ordinate OP is ∞ current required to overcome friction and hysteresis, while tan. $\theta \infty$ the eddy current effect. If OP is plotted to a scale of current, then $K_H = OP$, VT_a 10⁻⁸, when $F = \frac{W - nK_H}{n^2}$ is also known.

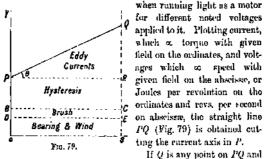
when
$$F = \frac{W - nK_H}{n^2}$$
 is also known.

We also have $\frac{OP}{QS} = \frac{Hystoresis + Friction}{(Hystoresis + Friction) + Eddies}$

Thus the three separate factors or losses are each determined.

The following graphical method of separating the various losses is a simple and convenient one, and independent of any mathematical treatment. It is due to Mr. R. H. Housman, and is as follows—

Separately excite the field magnets to the normal amount and keep this constant. Note the current and speed of the armature



QS is parallel to OP, then the total loss for that speed OS is given by $QS \times SO$. If PR is parallel to OS, then the area $PS \propto OS \propto$ power lost in hysteresis and friction together, and area $QR \times RP \propto OS^2 \propto$ power lost in eddy currents where $QP \propto RP \propto OS$. Repeating the above with a different excitation

will give a second line P'U', usually parallel to PQ, showing that the eddy currents are constant for a given voltage,

It may be noticed that the total loss corresponding to any point such as Q on PQ = product of co-ordinates = $OS \times QS$, and not the area of the Fig. POSQ. In other words, the Fig. represents the nature of a dynamo Characteristic rather than the indicator diagram of a steam-engine.

To obtain the total mechanical friction losses, run the armature with brushes down, field disconnected and unexcited by a direct coupled motor, and note the increase of current required to drive over that needed for the motor alone. Plotting this current OB on the ordinates and drawing BC parallel to OS, the area $OC \propto$ total mechanical frictions, and $\therefore BR$ must be \propto to the hysteresis loss alone. On noting this excess driving current with the brushes up, we get OD, and finally the area $OE \propto$ bearing and wind friction only. DC being \propto the brush friction alone.

The total losses for a given voltage will be a minimum for a certain induction in the armature core, usually between 15,000 and 16,000 lines per square c.m. Since the hysteresis losses increase rapidly with increase of field, while the frictional losses increase with decrease of field due to the higher speed needed to obtain the same voltage.

For high inductions up to 18,000 or 20,000 the eddy currents cause the curve to bend upwards, and also the angle θ to be greater. This is probably due to the eddies generated by the stray leakage field through the shaft, etc. If the line PQ bends, it shows that the eddy-current losses are producing perceptible demagnetization on the field. Since both the eddy and systeresis losses increase with armature current, these losses should really be measured with full-load armature current flowing by using the method of Fig. 85, which with careful adjustment of excitation will give considerable range of speed for constant armature current.

This question of the separation of the various losses is of great importance to the dynamo maker, enabling him to see in what way a machine is faulty, i.e. whether the oddy-current loss is excessive due to insufficient lamination, or the hystoresis too great due to too hard or inferior quality of iron. We will now consider a complete experimental analysis in detail.

Apparatus.—Exactly the same as that prescribed for test 95, and in addition an auxiliary motor should be available for coupling direct to the machine to be tested.

Observations. → (1) Carry out observations 1-3, test 95.

- (2) Repeat 1 for an excitation 25% above and 50% below the normal.
- (3) Disconnect all apparatus from the machine tested, and also the field from the armature. Connect the instruments up with the auxiliary motor, so as to measure the power taken to drive it. Domaguetize the field magnets of the motor to be desired by sending round the field coils a gradually diminishing (to 0) alternating current.
- (4) Measure the voltage and current needed to run the auxiliary motor at some ten different recorded speeds between 0 and the maximum allowable.

- (5) Direct couple the auxiliary motor to the armature tested, and with the brushes down, note the new power given to the auxiliary to drive the two machines at some ten different speeds, the field of the machine under test being entirely-disconnected and unexcited
- (6) Raise the brushes and repeat 5, tabulating all your results as follows-

NAME	DATE						
Motor tasked; No Basistances: Amoutore = Ohum @ °C. Normai Voltage ≈ .							
blaker ,	Blunot ⊯	P4 41	,, ,, , , , , , , , , , , , , , , , ,				
Туре "	Series ⊨ ,	P 15	, Bpeed =				
Total	conter lesses =						

Spend in Texted Muler Self- Revu. per driven (light).			M.	Auxiliery Motor close,			Motors coupled Brushes down.			ույմ ույմ ան Աթ,	ed	Friction lusses.				
Min. Soc.	Excitation.	Volta F.	Ащра. 4.	Watta (Total) A F,	Volts F1.	Aups. C.	$Q_{\Gamma_1} = \Pi_1.$, t	ئ	C2P2- FF	v,	හ්	F ₂ C ₃ = Π ₂	Total 37.2 - 17.1.	Bastrag and wind. W JF.	Brush oxly N2- H2.

- (7) Plot all your results to the same pair of axes, having in each case the speed in revolutions per second on the abscissae and the power in Watts required to be given to the shaft of the dynamo under test to produce those speeds under the various conditions mentioned in observations 1-6 on the ordinates.
- (8) Calculate the various losses at normal speed as a percentage of the total loss in the whole machine at full lead.

Inferences.—State very clearly all that can be inferred from your experimental results.

Note.—A variation of the preceding method for measuring the hysteresis and eddy current losses consists in measuring the watts absorbed by the armature in running the machine as a motor light at a series of excitatious between 0 and the normal, the speed being kept constant at normal value by adjusting the volts on the armature by means of a main circuit rheostat in series with it.

Plotting a curve with armature watts as ordinates, and excitation as abscisse, we find its lower portion to be nearly straight, and this part produced to cut the ordinates will give the watts which would be absorbed at zero excitation. Thus the difference between the watts at any given excitation, and at this zero value, will be the power lost in hysteresis, eddies, and anechanical frictions.

Again, if the curves are plotted between Joules per revolution as ordinates, and reva per see as abscisse, the friction line BC separating frictional and electro-magnetic losses has a fixed position in the diagram; whereas, with the axes denoting current and volts, a different friction line has to be drawn for each excitation, thus making it difficult to see what proportion of the whole loss is electrical and what frictional, when more than one set of curves corresponding with different excitation is drawn on the same curve-sheet.

(78) Measurement of the Coefficient of Magnetic Leakage "v," and of the Relative Distribution of the Waste Field of Dynamos and Motors. (Ballistic Method.)

Introduction.—The present test has a most important bearing on the design of the magnetic circuit of a dyname or motor, for since only a fraction of the total number of lines of magnetic force, generated by the field magnets, are usefully employed in cutting the armature conductors and so generating the requisite E.M.F., the results of the test enable the designer to allow for this discrepancy, providing he knows the coefficient of magnetic leakage "v" for the particular form and type of machine in question.

In addition to this, the relative distribution of the waste field around the machine enables defects in the design of the magnetic circuit to be seen and corrected, for at the best the magnetic circuit of a dynamo or motor is very imperfect.

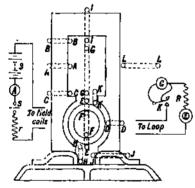
It should be remembered that leakage of magnetic lines of force will take place across any two points between which there is a difference of magnetic potential, the magnitude of which leakage will depend directly on this potential difference, and inversely on the magnetic resistance of the path.

The following is a convenient method of measuring or comparing the relative amounts of leakage in different parts of a dynamo, the term static being here used to denote the value of a obtained when the armature is at rest, for it is well known that an armature delivering current exerts a demagnetizing action on the field which directly promotes leakage. Assuming the normal excitation constant, the leakage will increase with the output, and it will largely depend on the degree of saturation of the iron and on the relative magnetic reluctances of the various parts. The method depends on the measurement of induced currents produced by moving either (1) an exploring coil so as to cut the field to be tested, or (2) the field in such a way as to cut the coil, the latter method being here adopted. Either the relative or absolute numerical values of the stray and useful flux in the various parts can be found, the relative values being obtained with reference to that part in which the flux is a maximum which can be taken as unity. Knowing these, the absolute values can be obtained by running the armature at a known speed and measuring the E.M.F. without allowing it to devolop current and thereby distort the field. The useful armature flux can now be at once calculated, and from it, that in each of the various parts, or thus:--suppose we have a circuit consisting of a ballistic galvanometer, resistance box, earth inductor of N_1 turns, mean area M_1 square c.ms. in series with an exploring coil of N_2 turns, mean area A2 square c.ms. wound round the magnetic field to be tested. If now the inductor, with its plane vertical or horizontal, is rotated rapidly through 180°, cutting the earth's field of strength F, then the total quantity of electricity set up in the transient current is $Q_1 = \frac{2N_1A_1P_1}{R_1} = K \sin \frac{1}{2} \theta_1^*$ where K = ballistic constant, $K_1 =$ total circuit resistance, $\theta_1^* =$ angular throw in degrees. If the exploring coil is now made to cut the field to be tested of strength F, by suddenly making, breaking, or reversing the exciting current, we get $Q_2 = \frac{N_2 A_2 F_2}{R_2} = K \sin \frac{1}{2} \theta_2$ where θ_2 and R_2 have the same meaning as before. . Dividing we get $F_2 = F_1 \frac{2N_1A_1R_2}{N_2A_2R_1} \times \frac{d_2}{d_1}$ lines per square c.m. in the loop or search coil (in absolute measure) where d_1 and d_2 = scale deflections corresponding to θ_1 and θ_2 .

As, however, it is the total field (A_1F_1) which we really desire to obtain, and denoting this by F_2

we have
$$F_T = F_1 \frac{2N_1 A_1 R_2}{N_2 R_1} \times \frac{d_2}{d_1}$$
 lines.

Apparatus.—Earth inductor E_i resistance box R; charge and short circuit key K_i bullistic mirror galvanometer G (p. 569), having a small log decrement and periodic time about 8 or 10 seconds, so that this may be large compared with the time of flow of Q_1 and Q_2 which can therefore pass through the coil before it begins to move. A shunt wound dynamo to be tested; ammeter A_i rheostat (r) (p. 599); quick break switch S_i and source of current B.



F10. 60.

Observations.—(1) Adjust the needle of G to zero, and wind a single complete turn of wire on the dynamo at position A, connecting it up with the other apparatus as indicated in Fig. 80. The F.M. coils must be disconnected and excited separately from B.

- (2) Close S and adjust (r), so as to get normal excitation through the F.M. coils.
- (3) Close K, open S, and adjust R by trial so as to get a convenient throw on G, then note its value (D_1) on breaking, and (D_2) on making circuit at S, the excitation being that in 2. Repeat this twice and take the mean of each, calling it (d_2) .

- (4) Repeat 1-3 for each of the positions of the exploring loop indicated by the letters H, C, D, E, F, G, H, I, J, K, and L, respectively.
- (5) Repeat 4 for excitations 50% higher and 50% lower than the normal, and in each case calculate ν from the formula,

v = Total Field Useful Field

(6) Let down the brushes and run the machine at a known speed, measuring the E.M.F. E at each of the three excitations used, and tabulate as follows—

NAME	Dare
$N_1 \simeq \dots$ turns $A_1 \sim \dots$ My cons.	$F_1 = \dots$ C.O S. units, $d_1 = \dots$ Scale days,
Galv. resistance g = oluns.	Total No. armature conductors C :=
Inductor resistance re re ohing.	sproil = , , , revs. per min.
Total revalance R ₁ = olane.	= 1044. Per sec. (a).
Pontion of loop. There on loop. Are by a me. Are by a me. Are by a me. Total residence. From residence. Ap. Ever by are are: Rear by a me. Rear by a me.	Arms theor at each for the first theory of each 10 strong for the first first the first firs

Inferences.—State clearly all the inferences which can be drawn from the results of the above experiments, and point out their bearing on the design of field magnets for dynamos and motors.

(79) Magnetic Characteristic of a Dynamo with varying Air Gaps.

Introduction .- It is of considerable importance, especially in the design of dynamos, to know the effect which the length of air gap, between the field magnet (F.M.) pole faces and armature core has on the excitation required to force a given number of magnetic lines of force through the core. For convenience the curve showing the relation between the amp.-turns (A.T.) or magneto-motive force (M.M.F.) which $=\frac{4\pi}{10}\times A.T.$ in the F.M.s and the total useful flux of lines (N) through the armsture will be called the Magnetic Characteristic for the air gap used. The flux (N) can be found in two ways; (1) by using a ballistic galvanometer in series with a "search roil" temporarily wound on the armature and noting the throws produced on the galvanometer by making, breaking, or reversing known currents in the F.M. coils; (2) by running the armature mechanically and noting its E.M.F. speed, and number of conductors round periphery, N being then calculated from the fundamental formula $E = NuC \div 10^{9}$. This is the best and more practical method to employ, because the armature will now exert a slight demagnetizing action on the F.M.s tending to increase leakage and approximate more nearly to actual working conditions. The Exp. is divided into three distinct parts, viz. the determination of the relation between-

- (a) The M.M.F. and flux (N) through armature with constant air gap.
- (8) The air gap and flux (N) through armature with constant M.M.F.
- (γ) The air gap and M.M.F. through armsture with constant flux (N) in armsture.

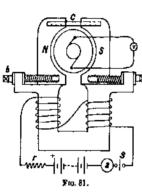
Apparatus.—The dynamo D capable of being driven mechanically; tachometer; voltmeter V; ammeter a; switch S; rheestat r (p. 599); supply of electricity.

The machine D to be tosted must be specially constructed in order to be able to operate this test. As shown in Fig. 81, the pole pieces are each capable of being made to approach or recede from the armature by turning a massive screw bolt b fitted to

each, by means of a suitable key. The distance apart of the pole tips can be read off on a scale C fixed to the body of the machine.

Note: The most tipe must given be given to the the thought to the content of the c

Note.—The pole tips must never be closer together than the two zero scale divisions which will be termed their stormal position in what follows, and must



To increase this distance turn the screw clock-wise. It will be noticed that the initial slopes of the curves in (a) are determined by the air gap, also that the air gap causes the curve to hend over.

always be left at this distance after the test is over.

All lubricators must feed properly before the machinery is started.

Observations. — a — (1)

Connect up as shown in Fig. 81, and adjust the pointers of all the instruments to zero.

- (2) Set the pole tips at exactly the normal distance apart and adjust the speed so that with the maximum excitation allowable in the F.M. coils 25% above normal, the E.M.F. can be read off
- on v.

 (3) With air gap and speed constant, adjust the excitation to about \(\frac{1}{2} \) of the maximum allowable. Note this reading \(A \) and that on (v) viz. \(E \).
- (4) Repeat 3 for about eight ascending equal increments of current to about 25% above the normal excitation.
- (5) Repeat 3 and 4 for the pole tips half-way and the farthest apart.
 - (6) Repeat 3-5 for the same current values descending.
- (7) Plot curves in each case with M.M.F. as abscisse and N as ordinates.
- β...(1) Adjust the exciting current to the normal value and the speed so that the E.M.F. can be read off on v.
- (2) With M.M.F. (i. c. A) and speed constant and the pole tips at exactly the normal distance apart, note the reading (k) on v.

- (3) Repeat 2 for eight different distances increasing by \(\frac{1}{6} \) at a time to the maximum possible.
- (4) Repeat 2 and 3 for a return set of distances to the minimum (normal).
- (5) Plot curves in each case with distances between iron of armature and pole face as abscissm and N as ordinates.
- γ —(1) Adjust the excitation to γ_0 maximum and the speed so that a suitable low reading of, say, $\frac{1}{4}$ maximum voltage is obtained on v.
- (2) With N (i.s. E) and speed constant and the pole tips at exactly the normal distance apart, note this distance (d) and the exciting current A.
- (3) Repeat 2 for eight values of (d) rising by \(\frac{1}{4} \) of the maximum at a time to the maximum, noting \(\frac{1}{4} \), at each position, which is necessary to keep \(E \) constant.
- (4) Repeat 2 and 3 for a return set of distances to the minimum (normal).
- (5) Plot curves in each case with M.M.F. as abscisse and (d) as ordinates.

Name					Dat	mi,	
No. Armstore conductors $C = 1$. Total F.M. turns $(T) = 1$.	•			Sciercal diam. Internal a Nett length	,,		. ,,
(- 	_					-,-	

1	Spec ite		Di-tance between	Distance between	Exa Current,	iling ⊿empa.		P. on E.	M M.P.	Flux
	Per Min,	Par Sec. (n).	pole t-pa (d).	iron of fare to core.	Increas- ing.	Duerona-	Increase flig.	Decreas- ing.	= 4	10 ⁸ R. C.R.

Deductions.—State very clearly all the inferences which you can draw from your results and point out their bearing on dynamo design.

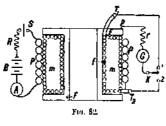
(80) Localization of Faults in Magnetizing Coils. (Induction-Ballistic Method.)

Introduction.—When a magnetizing coil of insulated wire is wound on a metallic bobbin, the latter is usually insulated on the inside by a thin strata of insulating material before winding on

the covered wire. Notwithstanding this, it may and does sometimes happer that the wire core becomes "shorted" to the metal-work of the bobbin, through the covering and insulation of the bobbin. This is particularly liable to be the case in shunt coils of dynamos which are wound on metal "formers," insulated with vulcanized fibre tissue before winding.

Such a fault, through poor contact of, in many cases, a very uncertain nature, gives trouble in the ordinary methods of testing for its position, by giving unsteady readings. Thus the ordinary resistance methods are extremely liable to be vitiated by variable contact resistance at the fault. The following method for localizing the position of the fault by means of induced currents, measured ballistically, is often a more convenient and reliable one for the purpose.

Apparatus.—Metallic bobbin or former F to be tested, wound with the magnetizing coil (m) which is "shorted" to frame at the



point (f); high resistance ballistic galvanometer G; two-way key K (p 587); battery of secondary cells B; switch S; ammeter A, and temporary primary magnetizing ceil PP wound over the autside of the magnetizing ceil mm proper, which is to

be tested; rheostat R (p. 606); known high resistance box r.

N.E.—It will be noticed that, as represented in Fig. 82, the fault (f) is on the first layer of turns next to the frame F, and we will suppose that the turn at (f) is making contact there with the metallic frame (F). Thus it will be seen that the point (f) divides the total number of turns on the whole hobbin into two parts between the leading out wires T_1T_2 of the coil, so that total turns — turns between T_1 and f + turns between T_2 and f.

Observations.—(1) Connect up as in Fig. 82, and adjust A

one of the zero, the temporary coil PI having been previously wound on and a wire soldered to any point (p) on the metallic bobbin frame F.

- (2) With R full in, close S and adjust the current on A to some convenient amount. Next also close K to stud 1 and adjust ** to such a value as will give, say, ½ or ¾ scale deflection d₁ on G when S is opened suddenly. Repeat two or three times with the same constant current, both made and broken in P.
- (3) Close K to stud 2 and repeat 2 above with the same current, noting the new resistance out in τ to give a suitable first throw on G.
- (4) Repeat 2 or 3 for about four or five current strengths A so as to obtain finally different throws on G which will check one another, and calculate the position of the fault (f), or the number of turns to be unwound, to reach it, from the relation

 $\frac{N_1}{N_2}$ turns between $\frac{T_1}{T_2}$ and $\frac{f}{f}$ mean 1st throw $\frac{d_1}{d_2} \times \frac{r_1}{r_2}$ approx. where r_1r_2 are the total resistances of r+G when obtaining d_1 and d_2 respectively, and which are assumed to be very large compared with the contact resistance at f and also the resistance of the turns between f and both T_1 and T_2 . If the resistance of the coil (m) is from 5 to 20 ohms then (r+G) should if possible be at least 10,000 ohms.

		1014 241 AIR						
Current	ist thros	as on ff.	Hox res	stimos,	Curuck	Resist	Hajle	Turns to
teferences only.	mean di.	mean dg.	r	ب	r 4 0 - (r),	r' + 11 = (12).	N _U N ₂	N ₂
·	·		- -:		<u> </u>	- 	 -	<u> </u>

N.B.—It will be noticed from the formula in 4 that if r is adjusted so that $d_1 = d_2$, then

$$N_1/N_3 = \frac{r_1}{r_2} \text{ or } N_2 = \frac{r_2}{r_1 + r_2} N_1$$

or again if r is kept constant throughout,

then
$$N_1/N_2 = d_1/d_2$$
 or $N_2 = \frac{d_2}{d_1 + d_2} N_2$

If G is insonsitive an iron core may be inserted in the coil to form a closed circuit if possible; this will increase the flux for a given current made or broken in PP, and therefore also the first throws d_1 d_2 on G.

This has the further advantage that N_1 and N_2 will now enclose the same number of lines of force, which is only approximately true if there is no iron core and the coil long.

It should be observed in passing that even a simpler method still than the one described above, for finding the position of the fault (f), would be to employ a slide wire or meter bridge or other convenient form of potential divider in the following manner. Connect the ends T_1 T_p , Fig, 82, of the faulty field coil to the extremities of a meter bridge wire and also to two or three Leckanché cells; connect the galvanometer G, which need not now be ballistic, but which must be sensitive, between the metallic former at p and the slider key of the bridge wire. Now move the key such that on tapping it G does not deflect. Then the lengths T_1f and fT_2 of the faulty coil are in the proportion of the corresponding lengths of the stretched wire either side of the K, and are therefore known if the gauge of winding and its resistance

(81) Determination of the Rise of Temperature and Increase in Resistance of Magnetwindings.

Introduction.—Since every magnet coil has some resistance, which is usually considerable in shunt or pressure coils but

(which can be meesured in the ordinary way) are known.

small in series or current coils, it follows from Joule's law that heat must be generated in them when excited. The amount of heat developed per second by a current of (I) amperes flowing through, or a pressure of (I) volts across the terminals of, a coil of R ohms resistance is $\propto I^2R$ or $\frac{V^2}{R}$. Any coil must therefore have such an external surface for radiation of heat relatively to the amount of heat developed in it, that the "steady" temperature attained when the rates of production and dissipation of heat become equal is not high enough to deteriorate the insulation of the winding. The maximum limit to this "steady" final temperature is usually fixed at about 50° C., for

it is found that the commoner insulating materials used generally begin to deteriorate with temperatures exceeding 60 to 70° C.

Admiralty specifications, however, prescribe that after a six-hours' run at full load, no accessible part of a machine may show a temperature of more than 70° F (= 38°-8 C) above the surrounding air. This would seem unnecessarily low, but from remarks to follow may not actually be so.

In the case of dynamos and motors the rise of temperature and its final steady value is required for the armature, series or shunt coils, commutator, bearings and frame. Further, it has been shown that the radiating facility of a surface in contact with iron is nearly twice as good as when it is exposed to air.

Except in special measurements and research, when perhaps thermo-couples and their equivalents may be used, the temperature rise of coils while energized is always obtained either (1) by thermometer, the bulb of which is placed on the coil and covered with a pad of cotton wool, or (2) by resistance measurement, obtained from the readings of an ammeter in series with, or a voltmeter across, the coil and the application of Ohm's law, This latter method is the one usually employed in a test room, is the most accurate of the two, and the quickest method of finding the "true mean rise" of temperature, especially with series coils. With shunt coils this resistance method can be effected by switching the supply off and then quickly measuring the resistance of the coil by the Wheatstone Bridge method, Usually the true mean rise of temperature by resistance to-ts is found to be at least I 4 to I 6 times greater than the apparent mean rise by thermometer due to the temperature of the layers of winding increasing from the outer one to that situated about three-fourths of the thickness of coil from it, and then decreasing again to the inner layer next to the iron core.

If R_0 = the resistance of the coil cold, and R_A that when hot,

then
$$R_h = R_c(1 + a(t_h - t_c))$$
 approximately,
or $\frac{R_h}{R_c} = \frac{I \times at_h}{1 + at_o}$ more accurately,

where t_0 and t_h = the temperature in deg. cent. of the coil, cold and hot respectively, and a = the temperature coefficient of the material which for copper = 0.00428 ohm per ohm per I* C.

$$= \frac{6}{8} \times 0.00428 = 0.00238$$
 per °F.

:, the rise of temp. =
$$(t_b - t_c) = \frac{R_b - R_c}{a \cdot R_b}$$

= 233 $\frac{R_b - R_c}{R_b}$ deg. cent. = 420 $\frac{R_b - R_c}{R_b}$ deg. Falir.

If now T = final temp. rise above surrounding air, $S = \text{total heat radiating surface in } \square''$ (exclusive of

end flanges and internal surface, if any),

W = total watts wasted in the coil at full load $= \text{total } I^2R$,

then $T \propto W \propto \frac{1}{S}$ or $T = \frac{W}{S} \times K$,

where $(K) = \mathbf{a}$ heating constant depending on the depth of winding, amount of faming by the armature, and whether the surrounding air is still or circulating, and may be taken as 75 for the usual shape and size of field coils of dynamos and motors, especially of multipolar types, excepting when iron clad.

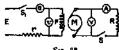
Hence $T = 75 \frac{W}{S} \text{ deg. cent.}$

and since for shunt bobbins $W = YI_{Sh} = I^2_{Sh}R_{Sh}$.

for a prescribed temp, rise (T) we have

max, shunt current $I_{Sh} = \sqrt{\frac{T_{c}N_{c}}{75R_{Sh}}}$ amperes,

Apparatus.—Magnet coil F (of, say, a dyname) to be tested; animeter (a) and voltmeter (r) each capable of dealing with the full-rated current and voltage for the coil; switch S_1 ; watch; small hulb thermometer and cotton wool; adjustable high resistance r for shunt coils, or low resistance for series coils;



F10. 83.

ammeter A, voltmeter V, switch S, and adjustable lead resistance for the main circuit to the armsture M. Separate means for driving M.

Observations.—(1) [Armature M statishary]. Connect up as shown on the left half of Fig. 83 and adjust a and v to zero, if necessary. Note the temperature of the air of the room by the

thermometer, secure the thermometer with its bulb touching the outside of the coil, and cover the bulb with a pad of cutton wool.

- (2) With r full in, close S₁ and quickly adjust r so that v or a shows the normal value for the coil, and note the readings of both v and a, the thermometer and the time.
- (3) By adjusting r maintain (a) constant in testing a series coil, or (v) constant in testing a pressure coil, either at the above normal value, and note the readings of v, a, the thermometer and time, say every 10 minutes for the first 1½ hours, and then every 15 or 20 minutes, up to the condition when the variable quantity becomes constant. Then, again, take the temperature of the room and tabulate as follows—

Nave.... Date ... Date ... Conf Tostori :—Typo ... Thuckness ... External Surface S---... —"
Temp of Resum at Stat - ... "U. at End of test - ... "U.

Trace of from Reading start (a).	Volta (r). Watis 1 - a v.	Ruce gi Corl R _h = $\frac{r}{u}$	Calculated Temp. Ruse $T = 258 \frac{R_b - R_c}{R_c}$	Thermometer Rending	Whither Motor at Rest or how Running,
----------------------------------	---------------------------------	---	---	------------------------	---

- [4] [Arimitars M driven at Full Local and at Normal Speed].— Repeat obs. I 3 after the machine has cooled down to the temperature of the air.
- (5) Plot curves to the same axes having time in "minutes from start" as abscisse with values of R_k, T, and t as ordinates; calculate the "heating constant" (K) from the relation

 $K = \frac{TS}{W}$ and the maximum value of shunt current suitable for coil tested for the value of (K) found, and for a final temperature

riso T of 50° C, above air.

Inferences.—Clearly state all that can be deduced from the results of the test, and point out their bearing on temperature testing.

(82) Efficiency of Direct Current Dynamos. (Swinburne's Electrical Method.)

Introduction.—This method, due to Mr. James Swinburne, has the advantage, firstly, in point of accuracy, of being solely an electrical one, and therefore far more accurate than a dynamometer method in which the power required to drive is measured mechanically; secondly, of not requiring another similar machine for coupling to it, in addition to the one tested. The method, which is often termed the "Stray Power" method, is consequently very suitable for employment in workshop determinations, where usually no good transmission dynamometer is available for measuring the H.P. used in driving the generator under test,

and is invariably used when Hopkinson's method cannot be

applied as, s.g., when no second similar machine is available.

The principle of the present and all similar methods is based on
the following, namely, that the total power put in = total power

given out + total power lost internally or in symbols $W_I = W_0 + W_L$

where the suffixes I, O and L denote the input, output, and total losses in Watta (IF) respectively.

Thus the commercial efficiency (7) of the dynamo is at once obtainable from the relation—

$$\gamma = \frac{W_o}{W_I} = \frac{W_o}{W_o + W_L}$$

The output in Watts W_0 developed by the dynamo is at once deducible from the product of the volts V and amperes C given out. The total loss W_L in Watts occurring internally in any dynamo is made up as follows—

(a) Copper losses L_c in armature and exciting coils due to

- (a) Copper losses L_{ϵ} in armstare and existing does due to heating by the passage of current, and which can easily be calculated when the currents and resistances are known.
- (b) Friction losses L_F due to air churning, journal and brush frictions.
- (c) Magnetic frictions or iron losses L_m due to Eldy or Foucault currents and magnetic hysteresis. Hence the total

internal loss $W_L = L_s + L_F + L_m$, and to the quantity $(L_F + L_m)$ Mr. Swinburne has given the somewhat appropriate name of "Stray Power."

The copper losses are calculable as follows-

Let C= the current given by the dynamo at its normal voltage V to some external circuit, and let R_a R_{S_b} R_{S_b} be the resistances of the armature series coils and shunt coils respectively of any dynamo to be tested, of which R_{S_b} can be measured by a Wheatstone Bridge and R_a R_{S_b} by the "Potential Difference" method (p. 84). We shall then have for a

Series dynamo $L_a = C^a \left(R_a + R_{Sa}\right)$ Shunt dynamo $L_a = \frac{V^2}{R_{Sh}} + \left(C + \frac{V}{R_{Sh}}\right)^2 R_a$

Compound dynamic (long shunt)
$$L_s = \frac{V^2}{R_{Sh}} + \left(C + \frac{V}{R_{Sh}}\right)^2 (R_a + R_{S_b})$$

Compound dynamo (short shunt)
$$L_t = C^2 R_{St} + \frac{(Y - CR_S)^2}{R_{St}} + \left(C + \frac{(Y - CR_N)}{R_{St}}\right)^2 R_{st}$$
The province leaves is a the step of the step

The remaining losses, i.e. the stray power $(L_F + L_{-})$, can readily be obtained by running the dyname as a motor, the field magnets being separately excited so that the armature has the same magnetic induction as at full load, the E.M.F. supplied to it being at least equal to the total E.M.F. which the machine would develop when running on full lead as a dynamo at normal speed. Thus the machine is running on no load other than its own friction, eddy currents, and hysteresis. If A = current flowing through the armature and V_a = the voltage across its terminals when the speed is up to normal, then we have

Stray power =
$$(L_F + L_m) = AV_a - L_a$$

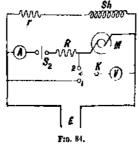
where $L_a = \text{copper loss}$ in the armsture for the current A in it.

Note.—Only a comparatively small current (A) at the proper E.M.F. mentioned above will be required to be furnished by the auxiliary source of current, and if R_a is very small, L_a can be neglected in comparison with AV_s in this last formula.

Apparatus.—Dynamo M to be tested, which for the purposes of discussion merely we will assume is shunt wound; voltmeter V; low reading long scale am-

meter A; rhecatata R (p. 606) and r (p. 590); tachomoter; complete Wheatstone Bridge set (W.B); two-way voltmeter key K (p. 587); switch S_2 ; source of current E at a sufficiently high E.M.F.

Observations.--(1) Connect up as in Fig. 84, and adjust the instruments V and A to zero if necessary. Switch on E_i when the field should be then



excited to the normal amount, as can be seen by closing K1, and observing whicher the normal voltage which the machine would

give as a dynamo at the proposed speed is indicated on V.

(2) With R at its maximum value (not less than about 10 ohms) close S₂, adjusting R so as to give the armature the full requisite E.M.F. E. It will still run under the normal speed, since with so small a current the armature produces no damagnetizing action to quicken it up. Now adjust r so as to bring it up to

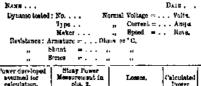
armature terminals and the current A amps. flowing through it.

(3) Repeat 2 at the same excitation for some ten different speeds in all, both below and above normal (by varying R), entering the readings in the small tabular form—

Bpred	Str	y Power	. tehrjidåi	Total intake
III r,p,m.	Volts	Amps,	Waita AVa — A'Ra,	walls 21 mning Hght ∡ Fa.
				

the normal speed, and note by closing K2 the volts V_a across the

- (4) Open E_1 S_2 and K and measure by means of W.B. the resistance R_0 of the armature and R_{SA} of the shunt, renormbering of course to disconnect one from the other while measuring their respective resistances
- (5) Calculate the power supplied and the commercial or nett efficiency of the dynamo for some ten different values of currents C (at, say, constant speed and voltage) taken from the smachine, ranging from 0 to full load by about equal increments, and tabulate as follows—



2 de 1	Power developed assumed for calculation.	Stray Fower Measurement in ols, 2,	Losses,	Calculated Comme
Revs. per	Total Output Wo-FC.	*	Copper Total Calcu- lated Lc + Ly La.	to Drive Efficience W 1 100 W 1

Note.—There will be only one value, that corresponding to normal speed, in each of the columns 1, 2, 5, 6, and 7 (counting from left to right) in the last table, but as many values in the remaining columns as there are values of amps. C assumed between 0 and full load.

- (6) Plot the following curves having -
 - (a) Efficiency as ordinates and Watts developed as abscissa.
 - (b) Stray power as ordinates and speed of armature as absciser.
 - (c) Watts developed as ordinates and Watts to drive as abscisso.

Inferences.—State clearly all that can be inferred from your experimental results.

(83) Efficiency of Direct Current Generators. (Hopkinson's Electrical Method.)

Introduction.—The earlier methods of measuring the efficiency of direct current generators, in which the electrical output of the machine was obtained by the product of the numeter and voltmeter readings, while the total mechanical input was obtained by means of some suitable form of transmission dynamometer, are more or less limited in their application from the fact that a reliable dynamometer is not always available. Even when it is, the method gives only an approximate result, for the error made in measuring the efficiency is proportional to the error made in measuring the input as given by the transmission dynamometer, and which is only too easy to make in an appliance such as this. It will therefore be evident that, given accurately calibrated instruments, any method of measuring the efficiency solely electrically will be capable of giving far more accurate results than could be obtained with any dynamometer.

The present method has this advantage, of being solely an electrical one, and requires two machines of aspearly the same output as possible, the accuracy of the test practically depending on how nearly alike in this respect the two machines are.

They must be capable of being placed in alignment with their shafts coupled mechanically together. The test can be made with either series, shunt, or compound machines, but the shunt is much the simplest.

be tested coupled both mechanically and electrically to a similar maan E.M.F. about equal

Frg. 85,

Apparatus.—Accurate ammeters A and a_1 a_2 ; voltmeter V; rhecetate R, R, for the field circuits (p. 599); change over voltmeter key K (Fig. 254); dynamo (a) to

> chine (8) which runs as a motor. An auxiliary source of current (y), such as a storage battery, or another dynamo giving

to the normal of a and B, and able to supply the losses occurring in the

muchines a and #; switch

S; rheostat Rh (p. 606, Fig. 274). Observations.-(1) Connect up as in Fig. 85, and make sure that the E.M.F. of y assists that of the dynamo a in driving the motor \$\beta\$ in the right direction for self-exciting a.

- (2) The respective fields F_a and F_{Bi} in series with rheostats R_1 and R_2 respectively, are excited from the terminals of γ_1 as shown, to the normal amount roughly, except that of β , which is weakened to enable it to run as a motor,
- (3) With Rh full in to start with, close S and adjust the auxiliary source of E.M.F. (y) and the rheostat (Rh) so that the machines get up speed, and if possible obtain the normal full load current of a through the circuit.
 - (4) Slightly re-adjust R₁ and R₂ to bring aβ up to normal speed, then in quick succession measure the volts V_1 at the terminals of the dynamo a and the volts V_{a} , at the motor by
 - means of the key K, at the same time noting the main current on A and the exciting currents a, and ag-(5) If possible obtain three or four different load currents through aff from the normal downwards, and calculate the effici-

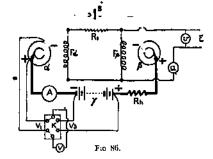
ency I from the relation $\Sigma = \sqrt{V_{V_*}}$ approximately,

and tabulate in a convenient manner.

Inferences.—Show how the above relation can be obtained, and state any assumptions made in obtaining it. What corrections would have to be applied to make it rigorously true? Obtain the true value of the efficiency S by applying the correction in question.

The test, though simple, requires a certain amount of experimental skill, especially in the case of series and compound machines. Moreover, the starting is somewhat troublesome.

By a slight modification in the connections, the test is a little easier to carry out, and this is shown in Fig. 86. Like the preceding arrangement it involves the use of an auxiliary generator or



set of secondary cells having the same current capacity as the machines under test, and a voltage of from 8 to 25% of that of the generator, according to their efficiencies. This, being, as before, in series with the generator and motor, takes the form of an added voltage to the system.

It is much better to excite the shunts from an independent supply instead of the auxiliary source.

In this arrangement the motor β must have the stronger field, and in order to start, the field F_a of the generator α must either be broken or be made comparatively weak by means of the rheestat R_1 .

Apparatus.—Similar to that for the proceding test; source of F. M. F. (E) necessary to fully excite the shunts Fa and $F\beta$, the Auxiliary Source γ being as above mentioned.

Observations.—(1) Connect up as shown in Fig. 86, and adjust the ammeters A and α , and voltmeter V to zero, etc.

- (3) With R_1 and Rh full in and the voltage (v) of the source E at the requisite value, close S, adjusting Rh to obtain full load current A through a and β , then simultaneously take the readings of a, v, A and the volts V_1 and V_3 across a and γ by means of the key K.
- (3) Calculate the efficiency of either machine from the relation—

$$\Xi = \sqrt{\frac{A.V_1}{A(V_1 + V_2) + \alpha.v.}}$$

and tabulate your results in a convenient manner.

(84) Measurement of the "Nett" or "Commercial" Efficiency of Direct Current Dynamos. (Kapp's Electrical Method.)

Introduction.—The following, being an electrical method entirely, has the advantage that all the measurements are electrical, thereby enabling the efficiency to be determined with far greater accuracy than would be possible with any mechanical transmission dynamometer.

The method consists in coupling the generator to be tested both mechanically (with their armatures in alignment) and electrically to a similar type machine of as nearly equal power as possible, and which latter is made to run as a motor, driving the other, by the weakening of its field, with a rheostat. A small auxiliary generator, giving the normal voltage of the machine to be tested, is required, and must be so connected that it can be placed in quick succession across the terminals of the two coupled machines. The auxiliary source therefore supplies the necessary exciting currents together with the difference of the currents flowing in the two coupled machines. The test, though simple, requires a certain amount of experimental skill, especially in the case of series and compound machines.

Apparatus.—Dynamo (a) to be tested, assumed to be a shunt wound machine and having its field coil- F_n across its terminals; another similar machine β to act as a motor and having a rheestat R_g in its field F_{β} ; "change over" switch C (Fig. 253);

main rheostat R₁ (p. 606); ammeter A; voltmeter V; switch S₁ and auxiliary source of E.M.F. (y), which may consist of the town mains (if the supply is continuous current), secondary battery, or small dyname giving the normal E.M.F. of the generator a to be tested.

Observations.—(1)Connect up as shown in Fig.

87, and adjust the pointers of Λ and V to zero, if necessary. Arrange the machines α and β in alignment and couple their shafts together by a suitable coupling.

- (2) Turn the "change-over" switch C to a, and with R_1 large close S_1 and gradually adjust R_1 and consequently the current until the machines start. Then when they are running at a constant speed, with V reading the normal voltage of a, note the ammeter reading A_a .
- (3) Quickly "change over" C so as to place the auxiliary source γ across β and note the ammeter reading A_{β} for the same voltage Y as before,
- (4) Repeat 2 and 3 for some four or five different speeds, current, and voltages, and calculate the efficiency from the relation—

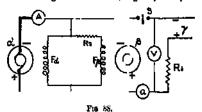
Combined officiency of the two machines = $\frac{A_a}{A_B}$

Commercial efficiency of either machine = $\sqrt{\frac{A_a}{A_{\beta}}}$ Tubulate your results as follows—

		Carrenta	in Ampa.	RAIC	icary of
Speed in Reve, per mus.	Voltage Y.	As.	Ap.	Combination A_a/A_{β} .	Ocnorator testrd or the other $100 \sqrt{A_a}/A_B$
		l	l	!	

Inferences.—Show how the expression for the efficiency can be obtained, and dilate on the advantages and disadvantages of the method.

The preceding method can be slightly simplified by the following modifications. As in the above test, the following one involves the use of an auxiliary generator or set of secondary cells, having the same voltage as the machines under test and a current output of about 8 to 25% of that in the armature of a or β . Being in parallel with the machines to be tested, it takes the form of an added current to the system at the same voltage as the combination under test. The present tests are more convenient, generally speaking, and much simpler as regards starting than those of No. 83. Fig. 88 shows the connections, and the apparatus required is much the same as in the preceding method, except that the change-over switch C, Fig. 87, is dispensed with.



The fields F_a and F_β can be connected as shown in Fig. 88 instead of as in Fig. 87 if preferred, and it will then be noticed that 87 and 88 are electrically the same when the change-over switch C is kept as shown, and an ammeter (a) inserted in one of the leads connected to it. The source of supply γ , whether power mains or a third generator, must have a voltage at least equal to that of either a or β . Further, the losses in a and β are measured directly, and are small compared with the output of a and β ; hence a small percentage error made in measuring them will be very small compared with the output of a and b, and will have but little effect on the resulting efficiencies. When two machines of the same size and type have to be tested, this method is almost always used in works for determining their efficiency and heating on a full-load time test.

- Observations.—(1) Connect up as in Fig. 88 and set all the instruments to zero.
- * (2) To start up, put R_1 full in and cut out R_2 to short circuit, so that the fields F_2 and F_3 are as nearly as possible of equal and maximum strengths. Then close S and slowly cut out R_1 , when the machines will start up as two similar motors in parallel on no load. The ammeter A will now read about half that of (a) because a will be taking about half the supply current.
- (3) Now weaken the field F_{β} of the machine β by slowly increasing R_{2} , which will cause it to run faster and act as a motor, driving α as a generator. The reading of A will simultaneously fall, while that of (n) will remain nearly constant; and when A becomes zero, the voltage of α will have reached a value just behaveing that of the supply γ , and (n) will indicate the current required to run α and β together at 0 load.

On still further increasing R_2 the current through (A) will be reversed, indicating that a is now commencing to supply, instead of receive, current.

Note.— For this reason A should be either of the moving soft iron needle type of instrument, or of the moving coil permanent magnet type connected in circuit through a reversing switch, otherwise a central zero moving coil type must be used.

(4) Take a series of load currents, as indicated on (A), differing by about equal amounts between 0 and the full-load value for either machine by still further increasing K_2 —noting the readings of all the instruments and the speed at each load, V being constant at about normal voltage.

Note.—This circulating current A between the machines a and β will increase with the difference between their field strengths; and the limit is reached when the combination of a large current in the motor armsture, and its weak field and high speed, causes excessive sparking.

Tabulate your results as follows-

Масыне			[ypa			DATE Volts =	speed	
Ī.,)enerato:		Contrat		Efficiency of		
Speci iii t.(cin.	Anips (A).	Volta (P).	Oatput in Watts W = A. F.	from Natus (a) Amps.	Motor # (4 + 4) F.	Combination Fig. A	Either Hachman $E = \sqrt{E_1}$.	

(5) Plot curves having values of E and E_1 as ordinates, with W as abscisse.

Inferences.—What errors, whether small or large, is the method liable to, and on what does the accuracy depend?

(85) Measurement of the Commercial Efficiency of a Generator by means of a Transmission Dynamometer.

Introduction .- This method of measuring the efficiency of an electrical generator, namely, by means of a transmission dynamometer, can be applied to a direct current generator equally as well as to an alternating current one. As, therefore, the application of the method to each of these two great classes of machines, to form two separate tests, was considered superfluous, preference was given to its application with an alternator, in that the output of a direct current generator is at once given by the product of the volts and amperes, while that of an alternator may present some difficulty to obtain accurately, the reasons for which are carefully explained. The actual measurement of the driving power by the dynamometer is obtained in precisely the same manner no matter what generator is being tested. There are many different methods of finding the commercial

efficiency of an alternator, depending in some cases on whether the armature rotates or is stationary, on the capacity of the machine, and on the facilities at hand for testing. In all cases the commercial efficiency—"mean" useful power developed+ total power absorbed by the alternator, the latter being—power applied to the pulley to turn it + the power used in exciting. The mean or true power developed is easily obtained if a non-inductive resistance, such as a bank of glow lamps or water rheestat, is at hand which will carry the full lead current of the machine, for then the true power = amperes × volts. This will not be true if the resistance is inductive owing to the "phase difference" between the current and voltage. For such a case the true power may be obtained by a non-inductive Wattmeter or the 3-voltmeter method (p. 379), etc. The power applied at the alternator pulley to drive it is very commonly obtained by indicating the engine, especially in large "sets." In the present ease a transmission dynamometer is used to measure this power. It is of the spring type, and the means for recording the readings of it were devised by Prof. W. Stroud. The indications,

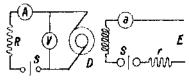


Fig. 89.

which are recorded electrically, represent the nett pull, or difference of tensions in the two sides of the belt in lbs. Then knowing the speed of the alternator and the diameter of its pulley, the H.P. can at once be deduced. For a full and detailed description of the dynamometer, see Appendix, p. 625.

Apparatus.—Alternator D to be tosted; transmission dynamometer complete with its indicating galvanometer G (p. 625); tachometer, a-c ammeter (A) and voltmeter (V); D-C ammeter (a); switch S; and non-inductive resistance or bank of lamps R (p. 598); exciting circuit containing ammeter (a), rheostat τ (p. 599), switch S_1 and exciting E.M.F. E.

Observations.—(1) Connect up as shown in Fig. 89, and see that all lubricators in use feed slowly. Adjust the secondary E.M.F. (p. 629) for use with the dynamometer, so that when placed directly across the terminals of G, a full scala deflection is produced. Then insert it in its proper place.

- (3) With the alternator belt on the loose pulley on the counter-shaft, start the motor which drives this shaft, and note the mean deflection on G for different speeds. If this is appreciable it must be deducted from each of the readings which follow.
- (3) Now throw the belt on to the fast pulley so as to start D₁ and without S being closed or the field excited, again note the mean deflection on G for different speeds.
- (4) Adjust the speed of D to give normal frequency and the excitation to give normal voltage on V. Note the reading of G, with S still open.
- (5) Close \hat{S} and repeat 4 (keeping the speed constant) for about ten different load currents on A, rising by = increments to the maximum permissible by varying (R).
- (6) Repeat 4 and 5 for frequencies of 40% and 75% of the normal respectively, and tabulate as follows —

Name			D.	A18	
licalitance of exc.	ting colle (ϵ) =	Normal output = . uhus. Dispeter of Crecumforen	aitemator:	թմի չ մ ։-	n.
Speed Reva.	Nett test Putl (T-0.1b). Evertang (4) Surbs.	Total H.F. absorbed $= \frac{R_2}{85000} + \frac{\alpha^2 r}{740}$	Cutput.	Use of H.P. developed $I_{T_1} = \frac{4F}{746}$	Commercial efficiency = 100 H_2 %.

(7) Plot curves for each speed having A and useful H.P. developed as abscisse, and V and officiencies as ordinates respectively. Also between H.P. developed as ordinates, and H.P. required to drive as abscissæ.

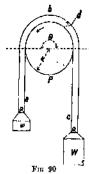
Note.—The nett pull of the belt in lbs. must be obtained from the deflection of G with reference to the latest calibration curve of the dynamometer.

The Testing of Continuous and Alternating Current Electro-Motors.

General Introduction.—Since the production of the electromotor in its more practical form within recent years, the uses to which it has been applied, for the electrical driving of workshops, haulage, electric traction, etc., etc., have assumed such proportions as to make the different forms and types of electromotor at the present day multitudinens. The systematic testing, therefore, of such machines becomes of considerable importance, in order that a comparison may be obtained and a judgment formed of the weak points of any particular type, together with its performance and qualities (whether good or bad) which it possesses.

No motor, least of all one intended for electric tram and callway work, should leave the makers' works or be installed in its proposed occupation without being first theroughly tested for the following points—(a) Resistance, or conductivity of its electrical circuits; (b) Insulation resistance between earth or framework of the machine and the copper circuits both individually and collectively; (c) Brake horse-power; (d) Efficiency; (e) Heating, or rise of temperature of the various parts of the machine after a run at full lead for a specified time. These tests we may now consider more in detail.

- (a) COPPER RESISTANCE.—That of each of the copper circuits should be separately measured, by the Wheatstone Bridge in the ordinary way (p. 81) in the case of the shunt coils or other circuit of several ohms, and by the Potential Difference Method (p. 84) or voltmeter and ammeter method (p. 86) in the case of the armature and series coils or other low resistance.
- (b) INSULATION RESISTANCE.—That of the various parts can be obtained by Tests Nos. 43 and 49 (pp. 113, 129) or other convenient method, at a pressure of something like three or four times the normal working pressure of the machine. The insulation resistance of the machine as a whole, when tested at the normal voltage, should not be less than 2000 ohms per volt, whonce, of course, that of the individual coils or circuits will be much higher. Some makers merely test the separate parts under a pressure of 2500 to 5000 volts alternating, and if they stand this they are parsed as satisfactory. This pressure can conveniently be obtained by means of a small testing transformer, stepping up from, say, 100 to 5000 volts, carefully set fuses being placed in circuit to prevent damage should the insulation break down.
 - (c) BRAKE HORSE POWER.—This may be measured in one of



three ways, depending on the facilities at hand for testing; namely, by an absorption dynamometer, in other words, a medified form of Frony brake, by the "balance" or "eraille" method, or lastly by the electrical method. The last two methods will be described in conjunction with their application to tests which follow later on, but we will now consider the principle involved in the first-named method, reserving the description of some convenient forms of brakes until later. It will be sufficient

if we consider the principle of the

simplest form of brake, consisting of a rope or band abc, of diameter or thickness (d), lapped with any arc of contact θ (in circular measure), from a fraction of n turn to more than one turn, over the face of the motor pulley P, having a radius (r) and which rotates we will suppose counter-clockwise, as indicated in Fig. 90. To one oud c is attached a large weight W, and to the other (a) a small one w. Now when the pulley P is at rest, W = tension on the right-hand or "tight" side of the rope, while w = the tension on the left-hand or "slacker" part of the rope. Then, as P rotates, the couple or torque T, due to the force of friction between the rope and surface of the pulley, tending to resist motion, and against which the motor does work, is—

$$T = (W - w)(r + \frac{1}{2}d)$$
 pound feet,

where (W and w) are in lbs. and (r and d) in foot, (W-w) being the difference in tensions or nett load on the brake in lbs., and $\{r+\frac{1}{2}d\}$ the mean effective radius in feet (of pulley and rope together) at which the nett load acts. If (n)= number of revolutions per minute made by P, then $2\pi n \div 60 = \omega$, the angular velocity of the pulley, and the work per second, or the rate at which work is done by the motor on the pulley = ωP . Hence we have—

II.P. developed = $(N-w) (r + \frac{1}{2}d) 2\pi n \div 33,000$, where I H.P. is equivalent to 33,000 foot-lbs. per minute. All the power thus measured and appearing at the pulley is wasted in heating this latter, and herein lies one of the chief difficulties in testing larger H.P.s, namely, the getting rid of the heat so generated by friction, for not only is the heat liable to burn the rope in two if the power of the motor is sufficient, but it also affects the co-efficient of friction $\langle \mu \rangle$ between the rubbing surfaces, thereby causing the brake to jork and preventing any steady readings being taken.

To obviate this trouble, either the pulley must be water-cooled (see p. 633), or readings must be taken immediately after adding a weight, and then the weight released from the rope. The trouble is further intensified by the motor running at such fast speeds, which is common to this type of driving power. By a slight modification of this form of brake, viz. substituting a spring balance for (w), the brake becomes automatically self-regulating for variations of μ , for then if μ suddenly increases, W rises, and (w), which now is the spring-balance reading, decreases, therefore W-w increases and restores the brake to its first position. The coefficient of friction μ can be calculated thus—

Let $\theta =$ are of contact (in circular measure) between cord and pulley, then $\frac{W}{a} = e^{a\theta}$

where $\epsilon = \text{base}$ of the Napierian logarithms = 2.71828,

The friction surfaces (in contact) of the brake should be as large as possible, in order to readily dissipate the heat generated. Mr. Maw gives the following rule for finding the smallest dimensions of a brake pulley: if H.P. = horse-power to be measured by the brake, and v = peripheral velocity of the pulley in feet per minute, and (l) = width of rubbing surfaces in contact, measured axially, then $\frac{vl}{H.P.}$ must not be less than 700.

(d) Efficiency.—This can at once be obtained if the electrical II.P. absorbed by the motor for a given B.H.P. is known. If A amperes as read off on the numeter is passing into the machine at a P.D. of V volts read on the voltmeter placed across the terminals of the machine, then the input of E.H.P. = $\frac{AV}{716}$ where 1 H.P. = 746 Watts.

Hence the commercial efficiency $\eta = \frac{B.H.P.}{E.H.P.} = \frac{B.H.P.}{E.H.P.} 100\%$.

(e) Heating.—This may be limited by specification or the question of safety to the conductors, and also considerations of overloading. It is not advisable that the rise of temperature of any part of the machine should exceed 40° C. above that of the external atmosphere after a six hours' run on full load. The temperature can be obtained by placing the bulk of a thermometer on the part to be tested and covering it over hy some culton wool. This can only be done to the armature at the moment of stopping, and it will here be noticed that a sudden rise of surface temperature occurs in the armature at the moment of stopping, due, of course, to the ceasing of the ventilating action which goes on while it is rotating (see p. 216).

(86) Variation of Speed with Voltage across the Armature of a D.C. Electro-Motor (at Constant Excitation).

Introduction.—This is an important test, in that it will familiarize the student with the fundamental principles underlying the regulation and control of motors. It can be carried out on a series, shunt or compound-wound motor, so long as the corresponding change in the connections and means for maintaining constant excitation are made. As, however, the same result is obtained with each type of motor, we shall operate the test with the simplest type, viz. the shunt motor.

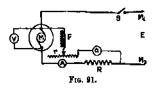
Note.—In a series motor the field regulating resistance, at least equal in value to the resistance of the series coils, must be shunted across them; whereas in shunt and compound motors it is connected in series with the shunt coils, and has a resistance and current-carrying capacity at least equal to those of the shunt coils.

Apparatus.—Shunt motor, of which M is the armature and F the field; main circuit variable rheostat R, ammeter A, and switch S, each capable of dealing with the full-lead current of M; voltmeter V and supply mains M_1M_2 of voltage E each for the rated voltage of M; field rheostat (r) and low-reading ammeter (a); tachometer.

Observations.—(1) Connect up as shown in Fig. 91 and adjust the pointers of V_i a, and A to zero if necessary.

- (2) With (r) all out and R full in, close S and gradually cut R out to short circuit as M gains speed, then adjust (r) to get normal speed (n). Note the readings of V, A, and a, which last-named must now be kept constant throughout the test by varying (r).—(See that the lubrication of M is working).
- (3) With the motor still running light as in (2) above, vary R so as to obtain some eight different speeds (n) in about equal steps between 0 and the normal, and note the corresponding readings of V, A, and a (a being kept constant throughout).
- (4) Ropeat (3) with the motor running at full load (if arrangements parmit), and for the same value of constant field current (a) as before.

Note.—The loading-up of motor can most conveniently be effected by means of an eddy-current brake or by taking any desired output from a coupled generator.



(5) Repeat (3) and (4) with, say, half the previous excitation maintained constant and tabulate all your readings as follows—

					-	
Rev	.			Dat	*	
Molor No.	Tip	0		Armainre Ro	4.7=	obina
Fall Loud:	-B.H.P. ≠	Volta	a A	трэ. —	Exciting	Amps
						Bր.ա. 🗕
Motor Hunding Light or	Supply Volta (F)	Hack K.M.F. o=V - A.r	Aimatus Aups. (A).	Constant Field Amps.	Armsture Speed in	Calculated Ration.
Loaded.	Armature.	Armsture.		Amjor	R.p m. (n).	7 7 7
			1		-	1

(6) Plot to the same pair of axes, curves having speed (n) as ordinates with values of V, A, and $\binom{supply voltage across <math>M_1M_2}{A}$ as abscisse.

Inferences.—State clearly what you can deduce from the table of results and curves, and show how they can be applied

to the design of a main circuit current rhoostat for controlling the speed of the motor.

(87) Variation of Speed with Excitation in a Direct Current Electro-Motor (with Constant Supply Voltage on Armature).

Introduction.—The reader should peruse the introduction of the last test, the remarks in which apply to the present test also. In addition, it may be pointed out that when the motor is running light the back E.M.F. will remain nearly constant, since the power required to drive is usually very small, and is α (V-v), consequently the increase of speed will be almost inversely α to decrease of field strength.

Apparatus.—That required for the present test is precisely as detailed for the last one, and need not be repeated again here.

Observations.—(1) Connect up exactly as shown in Fig. 91 of the last test, and adjust the pointers of Y, a and A to zero if necessary.

- (2) With (r) all out and R full in, close S and gradually cut R out as the motor gains speed, until F reads the normal voltage of the motor; then adjust (r) to get normal speed. Note the readings of A, a and V, which last-named must now be kept constant throughout the test by varying R (see that the lubricating arrangements of the motor M (Fig. 91) are working).
- (3) With the notor still running light, as in (2) above, vary (r) so as to obtain some 8 speeds (n), differing by about equal steps between 0 and the normal value, and note the corresponding readings of A, a and V (V being kept constant throughout).
- (4) Repeat (3) with the motor running at full lead (if arrangements permit), and for the same constant value of V as before.

Note.—The most convenient way of loading up M (Fig. 91) is by means of an eddy current brake, or by taking the required output from a coupled generator.

(5) Repeat (3) and (4) with, say, half the previously normal value of supply voltage V across the armature, maintained constant, and tabulate as follows—

	ľ	AIDS	•]	Date		
* Full lead: 11		rpe	Field	ature Res. $(r) = \dots$, ohms, I Coil Res. $(r) = \dots$ ohms. Field Amps = \dots R p.ac. = \dots			
Molor success light of loaded.	Supply Yolla F (const.)	Ampi	Specil (#).	Field Flux o. 1fm.	Eja.	i -	Descending

(6) Plot to the same pair of axes, curves having speed (a) as ordinates with values of $\langle A \rangle$, (a) and (supply voltage across M_1M_2 : a) as abscissar, and between 1/n as ordinates with (a) as abscissar.

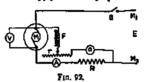
Inferences.—State clearly what can be deduced from the table of results and curves, and show how these can be applied to the design of a field regulating throstat for controlling the speed of the motor.

(88) Variation of Voltage, Current, and Speed, with position of the Brushes around the Commutator of a D.C. Machine at Constant Excitation.

Introduction.—Although the usual practice now is to design D.C. generators and motors with a fixed diameter of commutation and immovable brush-bars, special cases are met with in which provision is made for moving the brushes through considerable angular space round the commutator. As is well known, the terminal voltage of a generator and the speed of a motor is each capable of variation by moving the brushes, while a motor can even be stopped and reversed by so doing. In fact, where the variation of voltage or speed required is not large, it can be obtained by brush movement without expensive field regulators and without altering therefore the field strength -- a feature which is sometimes valuable, while most machines will admit of quite an appreciable brush movement without much sparking, when running light, such is not the case when they are running on load, so that the scope of this test may be limited by the amount of sparking. Further, it will be found easier to 240

apply the test to a motor than to a generator, and we shall therefore operate the present test on a motor.

Apparatus.—Shunt motor, of which M is the armature and F the field; main circuit variable rheestat (R); ammeter A, and switch S, each capable of dealing with the full-load current of M; voltage F at least



equal to the normal for M; field rheastat r and low reading ammeter (a); tachometer and, if possible, some scale for indicating the angular motion of the brushes round the commutator.

Observations.—(1) Connect up as in Fig. 92, adjusting (V) (A) and (a) to zero if necessary, and (R) to a value not less than the Ratio supply voltage ohms, so as to prevent the full-load motor-current being exceeded if the armsture comes to rest or its speed increasing two rapidly as the brushes are moved.

Wite.—This value of R will be given by blocking the armature and with normal excitation, noting the value necessary to give full-load current on A.

(2) Start the motor either by using the ordinary "Starter," or by (R) temporarily increased before closing S, and then gradually cutting out R until normal speed is reached—the brushes being in the normal full-load running position, and the excitation adjusted to normal full-load value.

Now note the values of V, A and (a), and the speed.

- (3) Next keeping (a) constant at the above value, adjust R
 to the minimum value allowable and found in ebs. (1), and note
 the readings of V, A and speed for normal position of brushes
 (as in obs. 2), and for a series of different positions throughout
 an angular distance = ½ the polar pitch either side of their
 normal position.
- (4) Repeat (3) at the nearest B.H.P. load to full load which it is practicable to run at, and tabulate as follows—

Name . Date . . . Motor : No. . . . Tune . . . Pull land B II,P,= . . Amps. -Yolla - . . . R p m. = . . . Amenture Resistance 7, ohni. Normal Exertation = amist. Atmalure Back B.M.F (s) Ponton of Brosh s. Field Strength Per min, (a). V - 100 Ampe, A,

(5) Plot curves on the same axes having values of brush position (normal as origin) as abscisse with values of e/n, V, A and speed respectively as ordinates.

Inferences. State clearly what can be deduced from the results of your test.

(89) Efficiency and B.H.P. of Direct Current Series Wound Electro-Motors.

Introduction.—The series motor in general possesses some characteristic features which it may be well here to note in view of the prominent place this type of motor has, and still is, taking in electric traction and power work generally. Since it can be shown that the torque T of the motor is given by the relation—

$$T = \frac{CNA_n}{2\pi} - \frac{CN}{2\pi} \cdot \frac{E - e}{r_a} = \frac{CN}{2\pi} \cdot \frac{E - CN_n}{r_a}$$

where C = number of armsture conductors all round,

N = number of lines throwling the armstore or the useful flux,

 $A_a =$ number of amperes of current through armature, E and e = impressed and back E M.F.s of the mains and motor respectively,

n = speed in rows, per second,

and $r_a = resistance$ of armature circuit.

It will be at once evident that the torque exerted is a maximum at starting, i.e. when n=o, and that it varies as the armature current A_{ai} since N also varies as A_{ai} .

Again, when the motor is "running light" at its maximum speed T=O nearly, for then the back E.M.F. generated almost = that of the mains E.

Thus a series motor tends to race directly the load is

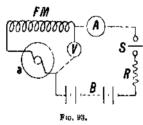
suddenly removed, which is an undesirable feature for workshop driving.

The fact that T=maximum at starting, and that the motor will start on full load, is a most valuable property for traction work on tram and railway lines.

In the following Fig. and all after it, the motor is represented symbolically, (a) denoting the armature, commutator, and brushes, and FM the field magnet coils, which in this case, being series wound, are represented by a few curly lines.

Apparatus.—Electromotor (series wound) to be tested, fitted with an absorption dynamometer or brake (Fig. 295); ammeter A; voltmeter V; variable rheostat R (p. 606); switch S; battery or dynamo B, giving the requisite voltage needed for the motor, and speed indicator and set of half-pound and one pound weights for the brake, also a lubricant if necessary.

Observations.—(1) Connect up as indicated in Fig. 93, and adjust the pointers of A, V, and the tachemeter to zero if



necessary. See that all lubricating cups in use feed slowly and properly.

(2) See that R is at its

(2) See that R is at its full, then carefully remove the brake from the pulley and close S. Take a series of gradually ascending and descending observations (by varying R) for about ten different speeds, ranging by

about equal intervals between the lowest readable on the tachometer and the maximum safe speed for the motor, noting this speed and the corresponding values of A and V at each.

(3) Replace the brake and repeat 2 for no weight in the pan. From 2 and 3 the loss in Watts in the brake can be found.

Note.—It will probably be necessary to exert a very made pressure by the finger on the brake in 3 to prevent it being carried round as the pulley rotates. No appreciable error need be introduced due to this. If a form of brake is used in which no loss of power can occur other than that incidental to its

use when actually measuring power, then omit obs. 3 and also the last seven columns in the next table, and substitute a column headed $A_1 V_1$ watts to run motor at no load.

Tabulate your results as follows-

	Without Brake,						With Brake.						
١		Velte	L	Δı	nper	164 ,		Yulli		Amperes.		es.	Less in Brike
Speed Hove. per min. (a).	Asendrag.	Descending	Mean Fi.	Ascending.	Descending.	Mests 43.	Agesuding.	Descending.	Mean Pg.	Ascending.	Descending.	April 49	10 Watta 10 Watta 11 y = $(A_2V_2 - A_1V_1)$
	-	l	Ι	-	-	ı	╌	_	ΙT	Ι			

- (4) With the brake carefully replaced on the pulley and the smallest weight in the scale pan, close S and by varying R adjust the speed to the lowest convenient. Note this and the reading of V and A simultaneously, and the weight,
- (5) Repeat 4 at the same constant speed for ten or twelve loads or weights in the pan, ranging from the smallest to that which will cause the current to rise to not more than 25% over normal.
- (6) Repeat 4 and 5 for the maximum allowable speed and an intermediate one, each constant throughout, and tabulate your results as follows—

Name... Date...

Molor tested: No... Typs... Maker... Weight ...

Besistance: Armatus r_n = ... ohms. Sories coils r_s = ... ohms.

Kireti to tailes of Brake pulley and lead r = ... R.

Normal B.H.P. - . . . Appet - . . . Yolts - . . . Speed - . . . rove per min.

Bleed Weight of Horne Terms (c). Weight of Horne Terms belance (W-v) (W-u) weight of Horne Terms (W-v) weight of H	Volts Anna	algorisal days loped	$=\frac{R_1}{R_2}100 \text{ g}$
--	------------	----------------------	---------------------------------

Note.—The true H.P. developed = H.P. calculated + H.P. lost in brake itself.

- (7) With the brake removed from the pulley and R full in, close S and obtain the maximum speed allowable. Note this and also simultaneously the amperes (A_{\bullet}) and volts (V_{\bullet}) .
- (8) Roplace the brake and add weights to the pan so as to obtain about ten different loads to the point when the largest load

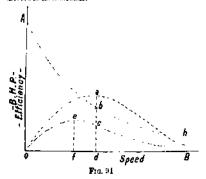
stops the motor. Note the current A_4 and speed (a) at each, the volts V_4 having been kept constant by altering R to suit the load.

Note.—The current should not exceed about 40% above the normal. Tabulate your results as above.

- (9) From observations 2 and 3 plot the following curves between
 - (a) Volts V₁ as ordinates and the corresponding speeds (a) as abscisse.
 - (b) Brake loss W_n as ordinates and the corresponding speeds (n) as abscisse.

From observations 4-6, plot for each speed curves between

(c) Efficiency and carrent as ordinates and corresponding B.H.P.s as abscisso.



From observations 7 and 8 plot the following curves between

- (d) The speed in each case and E.H.P. input, B.H.P., and efficiency.
- (e) The speed and current as ordinates and torque as abscissas
- (10) Calculate the coefficient of friction (μ) between the brake band and pulloy for various loads and for the arc of contact employed.

From the curves 9 (d) deduce the relation between the speeds that give maximum efficiency and maximum B.H.P. respectively.

Inferences.—State very clearly all the inferences deducible from your experimental observations. Explain fully the curves obtained in 9 (d) above.

Note.—The general form of the curves (d) 9 above are shown

in Fig. 94. The diagram due to Mr. Kapp is an exceedingly useful one for socing the relative H.P.s and efficiency. OaB is the B.H.P. curve, OaB is the efficiency curve, and Abh is the E.H.P. (input) curve. The shape of this last varies with the type of series motor run off constant potential majns. The ordinates, such as (ad), of the efficiency curve $OaB = \frac{cd}{bd}$, at this and similar points to any arbitrary scale of ordinates.

(90) Efficiency and B.H.P. of 500 Volt Direct Current Series-Wound Tramway Motors.

Introduction.—The particularly heavy and trying work which a tramway or railway motor has to perform renders it all important to subject the machine to the most scarching tests for defects or other faults at the outset. Such tests are twofold.—

(1) A complete test of the motor at the works of the makers

- . (1) A complete test of the motor at the works of the makers and again when fixed to the car.
- (2) A test of its performance when driving the car on some approved route on the system. With regard to this case, the worst route of the whole system is chosen, i.e. one having the steepest gradients and sharpest curves.

The car is lauled with an artificial lead, such as sand bags, for instance, equal to the full lead of passengers which it is intended to carry. It is then run as continuously as possible along that route with five-seconds stops every five minutes for say two hours.

This test is considered satisfactory, if, at the end of that time, all has gone on satisfactorily and the temperature of the armature and commutator of the motor has not risen above the prescribed limit.

Next, with regard to the "Works Tests." Besides the officiency test at various leads, the motor should be run at the average speed it will run at in practice, say that corresponding to eight or nine miles per hour of the car, for four to six hours at the maximum lead which the motor is intended for.

Except in the case of electric railways, where the car or engine axle is direct driven, single reduction gear between motor and car axles is almost universally employed of between 4 75 and 4 86 to 1.

The sizes of transcar wheels are usually either 30 inches or 33 inches in diameter. The remarks mentioned in the Introduction of Test 89 should be carefully read and remembered, when the performance of the motor on test will at once be obvious.

Cantion.—The operators of the controlling rheostat switch-gear, etc., must stand on the india-rubber mat provided, and must on no account touch any live metal work on the circuit of the 500 volt generator and tramway motor.

Great care must be taken to insure that the rheostat in the main circuit of the motor is FULL IN before closing the muin switch, and also that it is at once re-inserted before pulling out that switch on stopping.

The apparatus and connections of the preceding test are those now to be obtained, and the observations, as there given, to be carried out. In addition to curves 9, $\alpha-\epsilon$, plot two on the same curve sheet, having speed as abscisse, and both torque and amperes as ordinates.

(91) Relation between the Starting Torque and Current in a D.C. Electro-Motor.

Introduction.—It is very instructive to compare the results obtained in applying the principle of the present test to series, shunt, and compound wound motors, but it may also be applied to alternating current motors. The torque or turning effort by the armature on its shaft, measured in terms of a pull, acting at a given radius or leverage from the shaft centre, and tending to turn it, is expressed in pound-feet, usually, in this country. In a motor it results from the inter-action of the field magnets and the field of the armature as set up by the currents flowing

through it, and is α to the product of these two field strengths. If C = the number of effective conductors on the simularity;

N = the effective magnetic flux cut by them or flowing in the core;

A = the armature current:

then it can be shown that the torque (T) is given by the relation

$$T = \frac{CN}{8.52 \times 10^4} \times A.$$
 1b. ft.

an expression independent of the speed of the motor.

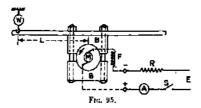
. · . T ∝ armature current × field flux ∝ AN,

In a series motor, the field flux N will vary as A varies, up to the point of magnetic saturation of the field magnets, when it will be practically constant. Any further increase in A will give the relation

$T \propto A$.

This also holds for a shunt motor, in which the field excitation is practically constant and near saturation.

In a compound or differential motor, however, the shunt and series windings oppose each other magnetically, and hence on starting it may happen that they nearly balance, thus giving practically zero starting torque.



In capstan, windless, and all traction work, maximum torque is required on starting; and since the series motor fulfils this condition and is exclusively used for the purpose in D.C. work, we will consider this type of motor to be the one used in the present test.

Apparatus.—Series motor M to be tested on a suitable D.C. supply E; brake-blocks B with yard-arm L and spring balance W; anneter A; switch S; and variable current rheostat R.

Observations.—(1) Connect up as in Fig. 95, setting A and W to zero if necessary. Clamp B B (o the pulley of the notor so as to prevent slipping (rotation), and with the yard-arm horizontal. Attach the spring balance W at a measured distance L from the pulley centre.

(2) With R full in, close S, and adjust R so as to give some ten currents through M and A differing by about equal amounts between O and the full-load current of M, noting the readings of W and A at each.

Note.—The connections of field F and armature of M must be such that the latter *tends* to turn in the direction shown. Also the yard, arm may have an equal overhang as shown, or be otherwise balanced when horizontal.

Further, as there will be a good deal of static friction at the motor bearings, the armature should be retated by hand a few revolutions before attaching B B, so as to well oil the journals; and even then the mean of several readings of W, taken for each value of A by disturbing the position at which (B) rests, by the hand.

(3) Take an ascending and descending series of value of A, and tabulate as follows—

(4) Plot a curve having values of A as ordinates, and T as abscisse.

Inferences.—Point out all that can be deduced from the table of results and shape of the curve.

(92) Efficiency and B.H.P. of Direct Current Shunt-Wound Electro-Motors.

Introduction.—If a short motor, supplied at constant potential, has a very low armature resistance, high shout coil resistance and field magnets giving a finid relatively very much more powerful than that due to the armature, the variation of "lead" of the brushes will be slight and the motor will be almost self-regulating in speed for wide variations of load, i.e. it would run at constant speed independent of the torque. The falling off of the speed in shunt motors as the torque increases will be the less as the field magnetism is the more powerful. The brushes, in two pole machines, should press at opposite ends of a diameter, and to ensure sparkless running must have a "backward lead." In all

cases the efficiency = total power given out ÷ total power put in, both being reckoned in similar units. The input is easily deduced from ammeter and voltmeter readings, but the entput is more difficult to obtain accurately. In the present test it is obtained by means of an "absorption dynamemeter," which, we will assume to be the modified form of Prony Brake introduced by Raffard. Such a brake wastes in heat all the power given out by the motor through friction, but at the same time forms a measure of this power. The arrangement is such that the brake automatically adjusts itself to variations of the coefficient of friction between the rubbing surfaces due to heat. In brake tests of this nature just sufficient lubrication (such as seep and water) and no more ensures smooth working without suddon jerks due to seizing, and this, togother with experience in manipulation, is the secret of the success of such tests.

If (r) = mean effective radius of pulley and band together in ft., n = number of revs. per min. W = weight in lbs. in scale pan, and w = weight in lbs. at the slack side of the pulley; then the angular velocity of the pulley $\omega = 2\pi n \div 60$, and the couple or torque resisting motion T = (W - w) r; then the work done per sec. = ωT , and the B.H.P. = $(W - w) 2\pi r n \div 35000$.

Apparatus.—Shunt motor (M) to be tested; voltmeter Y; ammeters A and α ; rheostats R_1 (p. 606) and R_2 (p. 599); switches S_1 and S_2 ; source of current B; speed indicator. A set of $\frac{1}{2}$ lb. and 1 lb. weights are provided with the brake, together with a pump and tank by means of which a slight dripping of lubricant may be allowed to fall into the central rotating pulley and band.

Note.—For further remarks on the testing of motors see the "General Introduction" on the subject, p. 232, et seq.

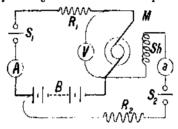
Observations.—(1) Connect up as indicated in Fig. 96 and adjust the pointers of all the instruments to zero where necessary. See that all indicating cups in use feed slowly and properly.

- (2) Uncouple the absorption dynamometer from the motor shaft. Set R₁R₂ at their maximum values, and close S₂, adjusting the exciting current (a) to the normal value by means of R₂.
- (3) Close S_1 and take a series of gradually increasing and decreasing observations (by varying R_1) for about ten different

speeds ranging by about equal intervals between the lowest readable on the tachometer and the maximum allowable for the motor in question, at constant normal excitation, noting the speed and corresponding values of A and V at each.

- (4) Repeat 2 and 3 for exciting currents (a) 50% below and 20% above normal respectively.
- (5) Re-couple the brake and motor together and repeat 2-4 for no weight in the pan. From 2-5 the loss in Watts in the brake can be found.

N.B.—It will probably be necessary to exert a very small pressure by the fluger on the brake in 5 to prevent it being



F1G. 20,

carried round as the pulley rotates. No appreciable error need be introduced due to this. Tabulato your results as follows—

	Ī	Ī	Without Dia				thout Diake. With 1						Brake,		
۱	Breiling		Volla	L .	<u> </u>	Anzpo	s		Yolte	١.	Ī	Amp	١,	Loss in	
Sperd Roya. Per init, (n)	current Ampa, (a),	Ascending.	Deresanding.	Mean P ₁ .	Ascending.	Descending.	Mean As.	Ascending.	Descending	Monn Pa	Ascending,	Descending.	Mean As.	Brake in Walte Walte $W_B = (A_2 V_2 - A_1 V_1)$	
		-	_	_		-	i-:		-	-			_		

- If a form of brake is used in which in loss of power can occur other than that inclients to it use when measuring power, then only to be, 5 and also the last 7 columns in the above table and substitute a column handed A_1Y_1 Watts to run mater at 0 load.
- (6) Adjust both the exciting current (a) and the speed (n) to the normal for the motor being tested and keep both constant, then take a series of readings of A_3 and V_3 for some ten different loads varying from the smallest weight in the pan to the one which will give an armature current not exceeding 25% over normal.

- (7) Repeat 6 for a 50% smaller excitation at the same speed.
- (8) Repeat 6 and 7 for a 50% smaller speed.
- (9) For a constant voltage across the armature maintained by means of R_i , lead the brake with different weights, and note these and the corresponding speeds and currents through the armature at constant normal excitation, and tabulate as follows—

Nama.			DATE
Motor tested: No	Tyle	Maker	Weight
Resistance - Shunt colls 7, =	գիտա	Armature r	. ohmu.
Effective rado	of brake puller	and bands =	U.
Causent to 8h	nut collu a	BUIDE	

Bpeed in Woight Lover lin pan weight per min. S' (bu.). w (bu.).	7-	Total II.P. developed $\frac{2\pi\pi}{H_b} = \frac{17\pi}{33000} + \frac{17\pi}{740}$		Total H P. absorbed 1/2= 42/3+4.3- 74b	Xefficiency = 100 × ^H k Hg
--	----	--	--	--	---

Note.—The true H.P. developed = H.P. calculated + H.P. lost in brake itself.

(10) From experiments 2-5 plot curves between, volts V_1 as ordinates, and speed (n) as abscisse, also with brake loss as ordinates and speed as abscisse.

From experiments 6-8 plot curves for each speed, having efficiences as ordinates and total H.P. developed as abscisse, also between the latter and speed as ordinates.

From experiment 9 plot the mechanical characteristic curve, having speed and current as ordinates and torque as abscissae.

Inferences.—What can you deduce from the results of your experiments, especially from observation 9?

(93) Efficiency and B.H.P. of Direct Current Compound Wound Electro-Motors.

Introduction.—The Compound Wound motor is an automatically self-regulating one for maintaining constant speed independently of the magnitude of the load.

Without considering the theory of this regulation, which is outside the province of the present work, and for which the render should refer to standard theoretical works, it may be remarked that the desired result is obtained by employing the series and shurt coils to magnetize the field magnets differentially, i.e. while the shunt magnetizes, the series coils demagnetize. This differential compounding results in the production of a nett field at any particular load sufficiently greater than what would be given by an equivalent pure shunt motor to cause the back E.M.F. to rise sufficiently to maintain the speed constant. The efficiency of such motors cannot manifestly be so high as one of the same size which is not would in this way, since an extra amount of power is used up in producing the demagnetizing force which actually destroys part of the field.

Apparatus.—Precisely similar to that required for the shunt motor test (p. 248).

Observations.—These are the same as for the above-mentioned shant motor tost, and will not consequently be repeated here.

The experimenter should refer to and carry the present test out in the same way, but in coupling up at the enset, care must be taken to connect so that the series cells oppose the shunt and tend to demagnetize the magnets. Exactly similar tabulation of results and plotting of curves must be carried out with the inferences deducible.

N.B.—The applied E.M.F. to the motor should be maintained constant.

(94) Efficiency and B.H.P. of Small Direct or Alternating Current Electro-Motors. (Cradle-Balance Method.)

Introduction.—In testing small motors, such as from $\frac{1}{40}$ to $\frac{1}{4}$ of a H.P., difficulties present themselves in measuring the power developed by them or the work which they will do, owing to the relatively large amounts of extraneous friction introduced in applying the usual brake tests. In fact, in the case of the smaller power motor, this source of friction would entirely vitiate the results and make them worthless. The following method practically gots over this difficulty entirely, and may be carried out in one of two ways—

(a) The motor to be tested is suspended freely with its armature spindle in centres, or on friction wheels, the field magnet

system with its bed-plate, etc., being carefully bilanced by counterpoise weights so as to bring the centre of gravity of the system in a line with the spindle. On the motor being supplied with electrical energy, and made to rotate and do work against the friction introduced at the face of its pulley by a stretched cord passing once round, the armature reacts on the field magnets tending to rotate them in the opposite direction with a certain force.

If then this action is resisted by a weight or force W attached to the field magnet system at a leverage L, then the moment of this force resisting the tendency, i. e. the torque, = WL.

Thus the arrangement is practically an electro-magnetic dynamometer in which the magnetic friction between armature and field magnets takes the place of mechanical friction in the ordinary dynamometer.

The preceding arrangement of the method has the disadvantage that the weight of the heaviest portion of the machine is resting on the shaft, and consequently there will be a bearing friction assisting the magnetic pull of the armature on the field.

A botter arrangement in this respect is one devised by Prof. C. F. Bracket, which is merely a slight modification of the preceding one. It consists in fixing the motor in a "cradle" supported freely by knife edges resting on steel or agate planes, on friction rollers, carried in a suitable fixed frame. The whole suspended system is very carefully balanced by means of counterpoise weights so that the centre of gravity lies in the axis of the motor shaft, this latter having been set in a line joining the knife edges of the cradle.

A horizontal balanced lever controls the cradle, the end of it either supporting weights or being attached to a spring balance. Thus it will be seen that now the weight of the armature only is on the bearings, and it is being used under ordinary conditions. The balance lever might be graduated and a sliding weight used to run along it to balance the torque, but the arrangement of the spring balance shown in Fig. 285 is the simplest and easiest to manipulate. This method has a further advantage that the friction at the journals of the motor does not affect or vitiate the measurement, but in the case of the application to a dynamo it should be remembered that it does. It should be borue in mind

direct coupled.

that a fruitful source of error may arise due to loss of power in driving the speed indicator. When small motors are being tested, care should be taken to choose an indicator that is very easily driven, and to drive it by means of a spiral or helical spring of, say, thin hard-drawn brass. Any eccentricity between the two shafts does not then matter so much as it would if they were

Apparatus.—That required for this test is precisely similar to

what is detailed under one or other of the preceding methods of testing series, shunt, or compound wound direct current motors or alternating current single phase motor, according to which of these types of motors the one being tested belongs. In addition the gradie absorption dynamometer is needed, for a complete description of which see p. 621.

Observations. -- As, with the exception of the somewhat different type of brake herein to be manipulated, the whole test will be precisely similar to one of the foregoing motor tests, depending on which kind of electromotor is to be tested, the rationale of this present test will not be repeated here. The experimenter should refer to the proper corresponding test and carry out the present one in an exactly similar manner, tabulating and plotting the results in just the same way.

Though the following expression will be found in connection with the description of the cradle dynamometer on p. 621, we may repeat that if W = weight or force applied at the end of the cradle lever in order to keep the same at zero when the motor is doing work, and if L = distance between its point of application and the fulcrum of the cradle, then the torque exerted by the motor = WL = T, and the work it does per sec. = ωT $= 2\pi nT$

Where n = speed in rows, per sec. \rightarrow $\therefore \text{H.P. doveloped} = \frac{2\pi nT}{650}$

• H.P. developed =
$$\frac{2\pi nT}{550}$$

Consequently if different tensions are applied on the cord wrapped round the motor pulley, causing it to do various amounts of work, thereby taking in different currents (A) amps. at different voltages V, the officiency of the motor at each load is-

Efficiency =
$$\frac{\text{H.P. developed}}{\text{II.P. absorbed}} = \frac{2\pi nT \times 746}{550 \times AV}$$

(95) Efficiency and B.H.P. of Direct Current Electro-Motors by Swinburne's Electrical Method.

Introduction.—In the usual brake tests it is difficult and often impossible to obtain very accurate results, owing to variation of the co-efficient of friction between the rubbing surfaces and the resulting jorky behaviour of the brake. The advantage of any method, therefore, of measuring the input and output of a motor by solely electrical means will at once be apparent, as it is possible to obtain much more accurate results with such a method.

The present method, which is purely an electrical one, is due to Mr. James Swinburne, and is sometimes termed the "Stray Power" method. The principle of it and all similar methods is based on the fact that

Total Power given out = Total Power put in - Power lest internally, or in symbols, $W_O = W_I - W_L$; where the suffixes O, I_i and L denote the output, input, and total losses in Watts (W) respectively.

We thus at once obtain the commercial efficiency of the motor to be $\frac{W_0}{W_L} = \frac{W_L - W_L}{W_L}$.

The input in Watts W_I given to the motor is at once obtained by the product of the volts and amperes of the supply. The total loss W_L in Watts we will consider now more in detail, and which in any machine is made up as follows: (a) the copper losses L_c in armature and exciting coils due to heating by the passage of current, and which can easily be calculated when the currents and resistances are known; (b) the friction losses L_F due to air churning, journal and brush friction; (c) magnetic frictions or iron losses L_m due to eddy or Foucault currents and magnetic hysteresis.

Hence total internal loss $W_L = L_G + L_F + L_{\rm so}$ and to the sum $(L_F + L_{\rm so})$ Mr. Swinburne has given the somewhat appropriate name of "Stray Power." The copper losses are calculable as follows—

Let C = total current flowing into the motor from the supply, and let R_{a_1} , R_{a_2} and R_{a_3} be the resistances of the armature, series

coils, and shunt coils respectively of any motor of which R_{ik} can be measured by a Wheatstone Bridge, and R_{ak} R_{sk} by the "Potential Difference" method (p. 84) or animeter and volumeter method, p. 86. Then we shall have for a

Series motor $L_C = C^2 (R_a + R_{sc})$, Shunt motor $L_C = \frac{V^2}{R_{sb}} + \left(C - \frac{V}{R_{sb}}\right)^2 R_a$, where V = normal

working voltage,

Compound motor (long shunt) $L_{\mathcal{C}} = \frac{V^{1}}{R_{sh}^{1}} + \left(\mathcal{C} - \frac{V}{R_{sh}}\right)^{2} (R_{s} + R_{s}),$

Compound motor (short shunt)

$$L_{\mathcal{O}} = C^2 R_{sc} + \frac{(V - CR_v)^2}{R_{sk}} + \left(C - \frac{(V - CR_v)}{R_{sk}}\right)^2 R_{sc}$$

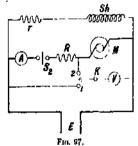
The remaining losses, i.e. the stray power $(L_F + L_m)$, can readily be obtained by running the motor at no lead, i.e. with no other load thun its own friction, eddy currents and hysteresis, at normal excitation of the field. Then we have

$$(L_F + L_m) = AV_n - A^2r_n = \text{Stray Power,}$$

where A now = current flowing into the motor armature at voltage V_a across the armature, and A^ir_a is the copper loss in the armature occurring for this current and voltage.

Note.—Only quite a small current at the normal voltage of the motor is required to be furnished by an auxiliary source of E.M.F., and if R_a is very small, $A^j r_a$ can be neglected in comparison with AV_a in this last formula.

Apparatus.—Motor M to be tested, which for purposes of discussion merely we will assume is shant wound; voltmeter V; low reading long scale ammo-



ter A; rheostat R (p. 600); tachometer; complete Wheat-stone Bridgo set (W.B.); two-way voltmeter key K (p. 587); switch S₂; source of E.M.F. (E) at least equal to that for which the motor was built; rheostat r (p. 599) in the field coil circuit.

Observations.—(1) Connect up as in Fig. 97, and adjust the instruments V and A to

zero if necessary. Insert E_1 when the field should then be excited to the normal amount, which can be seen by closing K1 and noting whether the normal voltage is read off on V.

- (2) With R at its maximum value (not less than about 10 ohms), close S_2 , adjusting R and if necessary the excitation by the rheostat r, so that the machine runs at its normal speed. Now note, by closing K 2, the volts V_4 across the armature terminals and the current A amps. flowing through it.
- (3) Repeat 2 at the same excitation for some ten different speeds in all, both below and above normal, and tubulate as shown.
- (4) Open E, S_2 and K, and measure by suitable means the resistance R_4 of the armsture and R_{4k} of the shunt, remembering of course to disconnect one from the other at the time.
- (5) Calculate the B.H.P. and commercial efficiency of the motor at normal voltage V for some ten different assumed values of current C supplied to the machine ranging from 0 to full load by about equal increments, and tabulate as shown in the larger table.¹

Speed in	fitniy Pos	eet Readings (fi	om obs. 2 and 8)	Total Intake
Řрт.	Volta Fa.	Amps. A.	Watts AVa - A'Ra.	Watts Running Light AV _p ,
•				

NAME... DATE...

Power supply awain od for calculation. Normal Speed Roya Volta Amps Total Input per min. C. F.C. F.C.	Stray Pouer Measurement in Ola. 2, Volta Ampa Lp + Lu Lp + Lu At At Ampa Watta.	Copper Total	Colouble Commercial Efficiency Wo = 100 Wo W W W W W W W W W
--	--	--------------	--

- (6) Plot the following curves having
 - (a) Efficiency as ordinates and output Wo as abscisse.
 - (b) Stray power as ,, and speed as
 - (c) Output Wo as , and input W as

Inferences.—State very clearly all that you can infer from the above experimental results.

¹ See note to larger table, p. 222-3.

(96) Efficiency of Direct Current Electro-Motors by Poole's Electrical Method.

Introduction.—This method, due to Mr. Cecil P. Poole, is an electrical one entirely, and enables the efficiency of an electromotor to be obtained without using an absorption brake. The rated B.H.P. of the machine is assumed for the purposes of calculation, and the whole essence of the test consists in obtaining the armature current at which this rated output is obtained.

Let A be this full load armature current.

V = the normal voltage which the motor should have.

W = the normal rated B.H.P. of motor, reckened in Watts, v and a = the measured quantities as detailed below.

Then the armsture core + friction losses w = (V - v)a Watts,

and the armature resistence $r = \frac{r}{a}$ ohms.

Hence
$$A = \frac{V - \sqrt{V^2 - 4(W + w)} r}{2r} = \frac{V}{r} \left(0.6 - \sqrt{\frac{1}{4} - \frac{(W - w)r}{V^2}}\right)$$

This value for A is based on the assumption that the core losses, armature friction, windage, and eddy currents in the pole pieces all remain constant from 0 to full load. While this is not strictly the case, the error introduced is practically negligible.

Apparatus.—Suitable source of supply of slightly higher voltage than the normal required for the motor to be tested; rheostat p. 599; low-reading long scale ammeter (a); voltaneter V to read the normal voltage; low-reading long-scale voltameter (v); and if the motor is shunt or compound wound, an ammeter to measure the normal shunt current a_{sh} ; switch.

N.B.—If the resistance of the shunt σ_{ik} be known, then the last-named ammeter may be dispensed with for $a_{ik} = \frac{V}{v_{i,1}}$ amperes.

Observations.—(1) Connect up the above apparatus so that the rheostat and ammeter (a) are in series with the armature alone, and the switch, so that it cuts off the supply entirely from motor and all apparatus, the voltmeter V being across the armature terminals, the shunt coils of the motor being across the mains.

¹ The rationals of the method first appeared in the American Electricies, to which the author is indebted for it.

- (2) With the rheostat fult in, close the main switch when the shart will at once be fully excited. Now gradually cut out resistance in the armature circuit, thereby running up the speed, until I reads the normal voltage across the armature, thus running light. Now note the small armature current (a) apperes flowing.
- (3) Switch off the shunt circuit and block the armsture to prevent it moving. With the rheostat full in, close the main switch and again pass the same current (a), as in observation (2) above, through the armsture while stationary, noting the corresponding fall of potential (v) volts across the armsture terminals by means of the low-reading voltmeter, and switch off.
- (4) Repeat observation (2 and 3) twice or three times and take the mean of the respective values of (a) and (v), calculating the efficiency Z of the motor on full lead from the relation —

$$\Xi = \frac{100 \text{ W}}{V \left(A + \alpha_{vh} \right)} \%$$

and tabulate your results as follows-

Naug Motor Tested: No	Ŋ.	aker	Rat	DATE .	,
Normai Volj Resistancia ; Armai			=	Catarena 86,131 &	=
Annalure Volta nerosc Currentamo- ming free. Suit (a) ninjis. (c).	Livenia (V · e) a	Armature Resistance y = #	Field Current asa	Full lead Armature Current A	Fillentey of Motor

Inferences.—State clearly any advantages or disadvantages which you consider the method possesses.

General Considerations Relative to the Testing of Asynchronous Alternating Current Induction Motors.

While it is not proposed to discuss either the construction or the theory of action of such machines, certain considerations relative to the testing of both single and polyphase induction motors may with advantage be noted. In all cases they are self-starting by reason of the rotating magnetic field set up by the supply current, whether single or polyphase, flowing in the windings of the stator or fixed portion of the motor. It is, however, only in single-phase types that after reaching fall speed the rotating field (produced only during the starting-up period) is changed by switching to a simple alternating, or reversing, or pulsating field.

The speed attained at the end of the starting period with no pulley load is called "full" or "synchronous" speed, but in all induction motors the speed of the rotor decreases as the load increases.

If (f) = the periodicity of the supply in cycles per sec.,

$$(n)$$
 = the speed of the rotor in revs. per sec.,

$$(p) \Rightarrow$$
 the number of pairs of poles in the stator,

then synchronous or full speed is the speed of the rotating

field
$$=\frac{f}{p}$$
 revs. per sec., while the difference between the speeds

of the field and rotor, called the "slip"
$$=\frac{f}{p}-n=\frac{f-np}{p}$$
 revs.

per sec., and
$$\left(\left(\frac{f-np}{p}\right) \div \frac{f}{p}\right) \times 100 = \left(\frac{f-np}{f}\right)100 = \text{the slip}$$

in percentage of full speed, which varies from about two or three in large meters to as much as twelve in very small ones. We therefore see that the slip equals the periodicity of the rotor currents.

Measurement of Slip.—The last-named fact is made use of in the following method of measuring slip, but is applicable only in the case of induction motors with slip-ring rotors. Connect preferably a moving-coil permanent magnet D.C. ammeter in one

instrument indicates for currents in one direction only, the number of impulses given to, or kicks (K) of, the pointer per min, in the same direction will directly equal the number of complete cycles per min. of the induced slow, period retor currents—in other words the slip. If (f) = periodicity of the supply to the stator, then the percentage $slip = \frac{K}{60 \times I}$ 100.

Thus, if K = 120 kicks per min., the slip $= \frac{120}{60 \times 50} \times 100$ =4% with a 50 ~ per sec. supply.

If a dead-beat moving soft iron needle A.C. ammeter is used, the number of kicks per min, would be doubled, for the game value of f and slip, and would, even if the animater was sufficiently dead beat to indicate with such rapidity, bo impossible to count. With even a very dead-beat moving coil D.C. ammeter, a 5 or 6% slip is about the maximum measurable by this method. A slight variation of the above method consists in counting the oscillations of a light pivoted compass needle placed above or below one of the leads between rotor and starter, the lead having a direction N. and S. so that the needle lies parallel to it when no current is flowing. Tho slip is then obtainable as before.

The above are direct methods of measuring slip, but if a longrange accurate tachometer is available, the slip can be obtained usually with sufficient accuracy by reading the rotor speed (n_1) running light, and (n₂) at any load when the slip is given by $\frac{n_1 - n_2}{n_1} \times 100\%$

Determination of Slip by Calculation.—If an induction motor has a three-phase wound rotor and both the rotor current (A_2) and resistance (R_2) per phase in each case are known, the slip (S) in cycles per see,, or in percentage of the supply frequency (f_{\bullet}) , or in revs. per min, or per sec., can be calculated for the corresponding load as follows-

If f_2 = frequency of the rotor currents,

 $W_2 =$ mechanical output from the rotor of the motor (in watts),

p = number of pairs of stator poles,

 $W_1 = \text{power}$ (in watts) transmitted electro-magnetically by the rotating field in the stator to the rotor,

we power (in walts) lost in the rotor
$$= 3A_2{}^2R_2$$
 approximately.

Then torque
$$\times \frac{2\pi l_2}{p} = 1 \mathbb{Z}_2$$

 $\times \frac{2\pi f_1}{a} = W_2 + w (= 3B_1A_1 \cos \phi \text{ for a 3-phase})$ and torque

stator supply)

$$\therefore \quad \frac{f_1}{f_2} = \frac{W_1}{|W_2|} = \frac{W_2 + w}{|W_2|}$$

and by a well-known rule in proportion we therefore have

and by a well-known rule in proportion we therefore
$$\frac{f_1}{f_1-f_2}=\frac{W_1}{W_1}\frac{1}{W_2}=\frac{W_1}{w}=\frac{W_2+w}{w}$$
 where $W_1=W_2=w$

$$\therefore \text{ the slip} = \frac{f_1 - f_2}{f_1} = \frac{w}{w} + \frac{1}{w} = \frac{3A_2^2 R_2}{W_2 + 3A_2^2 R_2}$$

Determination of Frequency, Slip, and Speed (Stroboscopic Method).

Introduction .- Although the measurement of such quantities as these mentioned above-by this method--is by no means common, it probably only needs the advantages and accuracy of the method to be realized in order to bring it into much more general use.

Measurement of Frequency and Slip,-The phonomenon and principles of stroboscopy can be applied in the measurement of either the frequency of an alternating current supply from an alternator, or the slip of an induction motor, as follows: A black disc having white radial lines is fixed concentrically on the shaft of an A.C. motor run from the supply, and is illuminated by an A.C. are lamp fed from the same supply. Now the illumination from the lamp will vary periodically and flicker with the supply frequency, and when the speed of the stroboscopic disc corresponds with this supply frequency, i.e. when the angular velocities of the two are equal, the white lines will always be illuminated in the same place and appear to be at rest. If the

speed of the disc is greater than that corresponding to the frequency of supply, the white lines will appear to slowly rotate in the same direction as the disc; whereas if the speed has a smaller value, the lines will appear to rotate in the opposite direction. The last condition will obtain with an induction motor and if the number of white lines equals the number of pairs of stater poles, they will rotate in the opposite direction to that of the disc with the same number of revolutions per min, as those lost by the motor, i.e. as the slips.

For example: the rotating field in a 2-pole stator on a 50 ~ supply will make one revolution in the periodic time of the current, or will rotate with a speed of $50 \times 60 = 3000$ revs. per min. If the slip between roter and field is $5\% (=5 \times 30 = 150$ revs. per min.), a single white line on the black disc will appear to tate backwards at a speed of 150 revs. per min., and will also make one complete revolution in the periodic time of the current.

With a 4-pole motor and the same slip and supply frequency, the speed of the rotating field equals 1500 rows, per min., slip equals 75 rows, per min., and each of the two white lines will appear to rotate at 75 rows, per min., which can be counted against time, and the slip thereby at once obtained. Sectors, alternately white and black, can be painted on the disc or even the pulley, and used instead of the black disc with radial white lines if so desired.

Measurement of the Resistance of Single and Polyphase Windings.—This is usually effected by the ammeter-voltmeter method with direct current (see p. 86) applied to a single phase-winding in the case of a single-phase generator or motor, and to each of the phase-windings separately of 2-phase machines.

Thus, if (r) equals resistance of each phase-winding, we see that the total copper loss in a single phase machine equals $A_1^2r_1 + A_2^2r_2$; or if in the latter case the resistances of the two windings are equal as they should be, and usually are, we have $r_1 = r_2 - r$, and if $A_1 = A_2$ then the total copper loss $W_0 = A^2 \times 2r$, where A is the current in either phase, and (2r) the so-called equivalent resistance of the machine.

In 3-phase windings, the resistance between any two terminals

is, with star connection, that of 2 phase-windings in series (as seen from Fig. 143 a), and therefore = 2r; while with mesh connection (Fig. 143 b) we see that between any two terminals there are two circuits in parallel, composed of 1 phase-winding in parallel with the other 2 phase-windings in series, or (r) in parallel with (2r), i.e. a terminal resistance of

$$\frac{1}{\frac{1}{r} + \frac{1}{2r}} = \frac{1}{\frac{2}{2r}} = \frac{2}{3}r.$$

Now, if without troubling to trace the connections in order to see whether they are star or mosh, the resistance between the three pairs of phase-terminals are measured and added together, the sum $\div 2$ will equal the equivalent resistance of the whole stator or rotor windings, and the total copper loss in the stator or rotor = (line-current)² × equivalent resistance.

(97) No-Load "Open Circuit" Test of an Induction Motor on a varying Voltage, constant Normal Frequency Supply. (Rotor running Light at No Load.)

Introduction.—Under these conditions the motor will run at its maximum possible speed, namely that corresponding almost,

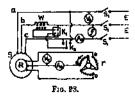
but not quite, to true synchronism, and therefore with an almost zero slip—the small difference being necessary for overcoming the small losses due to windage, mechanical and magnetic frictions, and copper loss due to the no-load running current. The test can be operated, of course, on single-, two-, or three phase motors, but we shall assume the use of a three-phase motor here on account of the connections being slightly more complex.

Such a motor may have either a squirel-cage (short circuited) rotor or a nound rotor with slip rings. If the former, it may be started up from full voltage mains either by a star-delta switch or through an auto-transformer or sectioned choker, depending on its size. If it has a wound rotor, the starting rhootat connected to this is put to "full in" and the stator then switched directly to the supply. The starter is then gradually cut out to short circuit as the speed increases. If

now, with the motor running at full speed, normal voltage, and frequency, the voltage is gradually decreased, the speed will remain practically constant until the lower voltages are reached, when it will fall off rapidly.

Both the stator and roter current will also decrease gradually, the former owing to a decrease in magnetizing and core-loss current producing the stator flux and depending on the voltage, the latter in an inverse proportion to the strongth of the rotating field and voltage,

As the voltage falls the idle or magnetizing component of the current will also decrease, while the energy component overcoming frictions will remain much the same in value, hence



the ratio of idle to energy current will decrease and the power factor will in consequence rise.

If $V_s=$ normal voltage per phase on the stater and $V_k=$ the corresponding maximum voltage per phase of the rotor indicated when this is turned through a polar pitch with slip rings open-circuited. Then $\frac{V_s}{V_s}$ is called the ratio of transformation, which is not equal to the ratio of the stater and rotor currents owing to the magnetizing current of the stater. The induced E.M.F. in the rotor circuits varies directly as the slip, and has a frequency $f_k=$ the slip. Thus the reactance of the rotor circuits (= $2\pi L_B f_z$) bears a constant ratio to the slip.

As the rotor current is not usually measured, the ratio of transformation enables it, and also the most suitable starting resistance, to be calculated, knowing the stator current at any load.

Apparatus.—Source E of three-phase alternating current, preferably a motor-driven alternator, the speed and field of

which are each variable between wide limits; three-phase switch K_1 ; voltmeters $V_K V_R$; ammeters $A_K A_R$; frequency meter f; wattmeter W; reversing key K_1 (p. 585); and two-way key K_2 (p. 587) for fine-wire circuit of W; three-phase induction motor, of which (S) is the stator and (R) the roter and (R) the starter.

Note.—By the use of only one wattmeter, with its pressure-coil connected through K_2 to the remaining two mains in rapid succession, we assume the motor to be electro-magnetically balanced, or equally leaded, in the three phases (see p. 389). On no load, such is usually the case, for the current A_n is small, and therefore any inequality in the ampere turns, resistance, or reactance of the windings is nearly negligible in effect compared with what it would be on load. With phase-windings unequally leaded or balanced, two wattmeters must be used to obtain the true power absorbed (see p. 392).

The anneter A_R in the rotor circuit should be very dead beat and of the moving needle type, and should be of low resistance so as not to throw out the balance of the rotor currents. If the rotor R is of the squirrel-rage type, $V_R A_R$ and r cannot be used.

Observations.—(1) Connect up as in Fig. 98, levelling and adjusting to zero, such instruments as need it. On starting any machine always see that its oiling arrangements are working properly before doing anything else.

(2) With R running light at no load, adjust the voltage V.

and frequency f of the supply E to the normal values for the motor, and note the readings of all the instruments under this supply condition, and also (with the same frequency kept constant) for a series of values of V_s (by field regulation) decreasing by about equal amounts to the point where the speed begins to decrease, and from this point by smaller and more gradual decrements of V_s until the speed decreases too rapidly to read.

Note.—After the speed begins to fall, sudden changes in V_s must be avoided, while the simultaneous readings of all the instruments must be taken rapidly.

W must be read, first with its volt coil across (ab) and then with it across (bc) at each voltage V_s , by using the key K_s . Further, in some cases (not all), this change of connection will be accompanied by a reversal of direction of the deflection of W depending on the magnitude of the power factor. The re-

versing key K_1 must in such cases be turned through 90°, so as to bring the deflection on to the scale again; but the reading must now be considered + ** and subtracted from the other to give the total watts (see p. 392), otherwise when the readings across ab and bc are both on the scale and therefore both + **, their sum gives the total watts.

(3) With the frequency (f) constant at normal value for the motor, raise the voltage V_8 from 0 by small and very gradual steps until the speed begins to increase too rapidly to enable readings to be taken. The simultaneous reading of all instraments at each voltage must be done rapidly. Tabulate all your results as follows—

Speed by	<u> </u>		- Տարլ-1	y .			£ !	្ត ខ	Lot	s/t	بد 5 اند 5	[]
factometer Kicks of Ag.	Frequency (one;ant)	Volts VA.	Amps As	III.	Wat	Tital Fr = 2 Ueb±Fu.	Apparent Wa	Power Every con down III/V'S A _B F'	Volta	A111116	Transformative F.	Value of

(f) Plot the following curves (from obs. 2 and 3) having values of stator volts Γ_s as abscisse with (f) speed, (2) intake watts W_s (3) stator surps. A_{ss} (4) cos ϕ_s (5) ratio $\frac{\Gamma_s}{\Gamma_R}$ as ordinates in each case,

Inferences.—From a careful study of the shapes and dispositions of the curves relatively to the axes and of the tabular results, state all that can be deduced.

(98) No Load "Short-circuit" Test of an Induction Motor on a varying Voltage, constant Normal Frequency Supply. (Rotor kept stationary and short-circuited.)

Introduction.—Under these conditions the slip will be 100 % since the speed is zero, while the power absorbed will almost

present test.

wholly consist of copper loss α to the square of the current. The only remaining source of loss is that due to hysteresis and eddy currents in the iron which will be small, owing to the low induction density reached with even the maximum voltage it is nearly to the text. Earther it will be nexted there

is possible to use in this test. Further, it will be noticed, from a reference to test No. 137, that the motor approximates to a static transformer with a stator primary and rotor secondary under the conditions for maximum magnetic leakage which the

stator windings maintain in the air gap between stator and rotor.

Under stationary conditions the ratio of stater to retercurrent is practically a constant and approximates to the ratio of transformation of the motor. Under running conditions the ratio of currents departs from constancy, due to the no-load current taken by the motor at normal voltage, and no longer

approximates to the ratio of transformation.

Apparatus.—That indicated for the preceding test (p. 265), but without K_1K_2 , an additional wattmeter now being used with its current coil in main a or c (Fig. 98), one end of each of the voit circuits of the two wattmeters, to be denoted by w_1 and w_2 being connected to the third main as indicated in Fig. 143a.

The research for now wing two wattmeters in that the language

The reason for now using two wattmeters is that the heavier stator currents to be used in this test, which will depend mostly on the resistances of the windings, will show up any slight want of symmetry, and may (or may not) result in the unequal

of symmetry, and may (or may not) result in the unequal current leading of the three phases—a condition necessitating the use of two wattmeters (p. 392). $A_s A_s w_1$ and v_2 must also now be capable of taking the heavier currents used in the

Observations.—(1) Connect up as in Fig. 98, levelling and adjusting to zero such instruments as need it. See that the lubricating arrangements of the supply set are working properly.

(2) With the rotor R short-circuited and prevented from rotating and the supply-frequency (f) constant at normal value, take the readings of all the instruments at each of a series of supply voltages V_S, increasing from zero to a value which will produce a stator current A_S of, say, 50 % in excess of that of full load, and tabulate as for the last test (p. 267).

(3) Plot curves, having values of V_3 as abscisse, with values of V, A_S , A_R and $\cos \phi$ respectively, as ordinates. Also curves between A_R as ordinates, with A_R as abscisse, for this test, and from the readings of the last test No. 97 on the same curve-sheet for comparison.

Inferences.—From a careful study of the curves state clearly all that can be deduced from the test.

(99) Efficiency and B.H.P. of Single Phase Alternating Current Electro-Motors.

Introduction.—The somewhat rapid development of the distribution of electrical energy by single phase alternating currents in recent years has brought with it the introduction of single phase alternating current motors, of which, up to comparatively recently, there has been no practical commercial instance. Now, however, there are several forms, but none of them are able to compete with the direct current motor in the matter of efficiency and powers of starting under load with the amount of electrical power absorbed in doing so. There are two classes of alternating single-phase motors, known as the Synchronous and Asynchronous types. The former cannot start themselves but have to be run up, by a separate source of power, into synchronism with the periodicity of the supply current; then, on being switched into circuit, they run perfectly synchronously with the generators, i.s. at constant speed, for wide variations of lead from 0 to considerably over full load, and are of course separately excited. The latter class are self-exciting and self-starting (on very small leads) by using suitable means, but are non-synchronous, and the difference between the speeds of rotation of the magnetic field and the rotating armature is called the "Magnetic Slip" or "Slip" simply. This generally only amounts to a small percentage at full load.

The self-starting property is obtained by producing a rotatory magnetic field at starting, caused by diphasing the current in two separate circuits by means of the suitable use of either selfinduction or capacity, one circuit being cut out when the motor gets up speed.

The fixed portion of the motor (i.e. field magnets) through the

winding of which the supply current flows is usually termed the "Stator." The rotating portion (i. s. the armsture) is termed the "Roter," and usually consists of short-circuited conductors carried on a well-aminated dram. There is no electric connection in section of the rotation of t

most cases to the rotor, or between rotor and stater. It will also often be found that the best efficiency is not at normal full lead, which is analogous to the series wound direct current motor in this respect. Speaking broadly, it may be said that single-phase motors should be self-starting, and this on a current certainly not exceeding that taken at full lead. The power factor should be high.

A motor built for a given periodicity will not give as a rule its full power when supplied with a current of a much higher periodicity, while it will take too much current with a lower periodicity.

The efficiency of any motor = the total power given out ÷ the

total "mean power" absorbed, both being reckoned in equivalent units. In the present and similar tests the true mean input caunot be obtained by the product of the amperes and volts, as in the case of direct current motors, owing to the "phase difference" between the current and pressure, but must be obtained by means of a non-inductive Wattmeter. The output, or B.H.P., is obtained by an absorption dynamometer, which is a modified form of Prony brake. Such brakes waste, in heat, all the power developed by the motor from friction, but at the same time give a measure of this power. No lubricant is usually needed, but a little black lead may be applied to the pulley if the brake is jerky.

Apparatus.—Alternating current motor M to be tested; brake

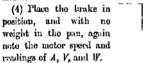
Apparatus.—Alternating current motor M to be tested; brake complete with weights; non-inductive Wattmeter W; alternating current ammeter A and voltmeter V; switch S; rheostat R (p. 597); tachometer; source of alternating current R, preferably one that can be varied.

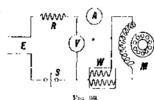
Tests.—(1) Connect up as indicated, and adjust the pointers of all the instruments to zero, levelling such as need it. See that all lubricators in use feed slowly, and that the resistance switch (S) is open.

- (2) Adjust the speed and excitation of the alternator so as to give the normal voltage and frequency required for M, and remove the brake.
 - (3) Make R a maximum; i.e. in the present case put resistance

switch S to start, and when the motor has got up speed throw S over from start to full, then, when the speed has

become steady, note it and the readings of A, V, and W.





- (5) Repeat 4 for about ten loads, rising by about equal increments of weight to the maximum, the voltage and frequency being kept constant.
- (6) Repeat 4 and 5 for a higher and lower frequency than the normal.
- (7) Determine the power required to just start M by removing the brake, turning S to start, and adjusting the speed of the alternator to give normal frequency (to be kept constant).
- (8) Carefully and gradually raise the voltage (at constant speed) by means of the excitation until M just starts, then instantly note the readings of A, V, and W. Repeat this three or four times and take the mean.
- (9) Repeat 7 and 8 for about five different frequencies, rising by about = increments to about 20% above normal.
- (10) Determine the relation between the speed of M and frequency of supply by removing the brake, and when the motor has get up speed, turning the Switch $\langle S \rangle$ to "full." Then for constant normal voltage note the speed of M and readings of A, V, and W for about ten different frequencies, rising up to about 20% above normal.
- (11) Determine the effect of variation of voltage at constant normal periodicity with the motor running light by altering R, and noting the speed and readings of all the instruments. Tubulate all your results as shown.

Name . . . Date . . .

Beerg in the state of the state	Weight in Pan Wilby, Jesser weight or balince reading to Ibs. Nett Weight in	Nett Weight in Brick (W = 0) ibs. B. H. P. doveloped Hg = vill (W - w) Hg = vill (W - w) Power Factor cos, \$\tilde{\text{a}}\$	Efficiency Eff. × 100 in % Eff. × 100 in %
--	--	---	--

Note.—The nett weight on brake = (weight of scale pan and weights) - reading of spring balance.

- (12) In experiments 1-6 plot curves having values of (a) power factor, (b) efficiency, (c) true power absorbed respectively as ordinates, and B.H.P. developed as abscisse, for each frequency.
- (13) In experiments 7-10 plot curves having (d) true power required to start, (e) speed of motor, as ordinates and frequency as abscisse, in each wase.

Inferences.—What can you deduce from your experimental results? Taking the cost of electrical energy for power purposes at 2d, per B.T.U., find the cost per B.H.P. per hour, and also when M is running on no load at normal voltage and frequency,

(100) Efficiency-Load Test of a Polyphase Induction Motor. (Absorption - Brake Method.)

Introduction. - The efficiency of any electro-motor

The internal losses in an induction motor comprise (1) copper losses in stator and rotor windings, (2) iron losses (hysteresis and oddy currents) in stator and rotor cores, (3) mechanical friction due to windage, journals, and brushes, if it possesses a slip-ring rotor.

If A_s and r_s = the current and resistance, respectively, per phase of stator winding and A_s and r_p = the current and

resistance, respectively, per phase of rotor winding; then, if this latter is of a three-phase type, the stator copper losses are—

 $A_{p''N}^2$ for single-phase; $2A_{p'N}^2$ for two-phase; and $3A_{p''N}^2$ for three-phase induction motors, while the rotor copper loss is $3A_{p'''N'}^2$.

For a given iron core, we have seen (p. 354) that the expression for the iron losses contains two variables only, namely, the frequency and the induction density a to flux, and dependent solely on the supply voltage and number of stator turns. Hence the iron loss is independent of load. Further, since the frequency of the rotor currents and consequently of the flux in the rotor core equals the slip, which is only some 5 % of the speed of the stator field, it follows that the iron loss in the rotor core will be small compared with that in the stator core and the other losses, and will increase slightly with speed. The friction losses being on to speed, will be sensibly constant at all loads in an induction motor, since the speed of such a motor has a variation of some 5 $\frac{1}{2}$ only. It will therefore be at once realized that the copper losses (increasing as the square of the current) are mostly responsible for the rapid increase of the total internal loss as the load increases.

The supply current to the stator of an induction motor is composed of two components—

(a) One which may be termed the no-load or magnetizing rempenent, producing the rotating magnetic field, and which is not only in quadrature with the supply voltage but nearly constant at all loads.

(Owing to the air-gap between stator and rotor-cores, the ampere turns of excitation, and hence the magnetizing component necessary to produce a given flux, is much higher, and the power factor much lower, than if the magnetic circuit was a closed one, and therefore an induction motor takes a considerable no-load current which may be from a quarter to one-third of full-load current. The smaller the air-gap the smaller this current, the greater the power factor and output of the motor for a given size. For this reason the air-gap of such motors is reduced to a mere clearance for rotation.)

(b) The other, which may be called the load-component, out

of phase with the voltage, but producing a field in the stator equal and opposite to that produced by the rotor currents in the stator, and hence balancing the demagnetizing effect of the rotor-induced currents on the stator field.

This load component increases directly with the B.H.P. output of the motor and $= A_A \times \frac{\text{turns on rotor}}{\text{turns on stator}}$.

Thus it will be seen that for the rotating field to have a constant strength, the stator current taken at no load will just suffice to produce this requisite field strength and provide for the iron and friction losses. As the load increases, the increase in the rotor ampere terms is balanced by an equal and opposite increase in stator ampere turns, and we have the following

Total stator amp, turns

= total rotor amp. turns + no-load amp. turns,

or Total stator current

relation, viz. that the

= (rotor current - ratio of transformation) + no load current, the line above denoting that the sum is vectorial and not algebraical.

The total power given out, i.e. the B.H.P., can be measured

either by means of an absorption dynamometer brake in the manner already clearly defined in the previous tests, or by making the motor to be tested drive a direct current dynamo, the commercial efficiency of which is accurately known at various loads. This method should be adopted whenever possible, as it

loads. This method should be adopted whenever possible, as it has the advantage, when carried out properly, of being more accurate than the ordinary brake methods. The method consists in suitably driving the dynamo from the motor to be tested either by means of a thin supple (pliable) belt or by the direct coupling of their shafts (placed accurately in alignment), through a flexible

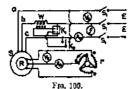
coupling or helical spring sufficiently strong for the purpose, thus avoiding the difficulty of getting their shafts exactly in true

alignment. The belt arrangement also obviates the same difficulty, but it must be very pliable, otherwise errors will be introduced due to the extra power absorbed by the slipping and bending of this belt round the pulleys.

Thus measuring the electrical power developed by the dynamo which is at once given by the current × voltage, and knowing its commercial efficiency s, the B.H.P. of the motor can easily be calculated and = $\frac{\text{D.C. output}}{740}$ \div e. Further, if n = the speed in revs. per min., the torque T of the motor is given by the relation $T = \frac{\text{B.H.P.} \times 33000}{2\pi n}$ lb. ft.

In all cases the efficiency of any motor = total power given out at its pulley ÷ total power absorbed, both being reckoned in equivalent units. A multiphase alternating current motor is saff-exciting, self-starting, but asynchronous as regards speed and the periodicity of the supply. The starting torque can be made equal to that of the best direct current motor without an excessive percentage over load in the current taken.

They can be wound to run direct on 5000 volt circuits and



over without much fear of the insulation breaking down, and their great advantage, except in the larger sizes, lies in the fact that there are no rubbing contacts of any kind to get out of order, and consequently there is no sparking. In the present case we will assume that the motor to be tested is of the threephase type, as perhaps the measurements of input are not so

obvious as in the two-phase system.

Apparatus.—Source of three-phase alternating current E; three-phase motor SR to be tested either coupled mechanically to a direct current dynamo D of known commercial efficiency, or fitted with a Peony brake, p. 634; Wattmeter W; alternating current ammeters A_S A_R and voltmeters V_A V_R ; triple pole switch S_1 S_2 S_3 ; tachometer; and if a coupled dynamo load is used, direct current ammeter A and voltmeter V; rheostat R (p. 606); switch S.

Note.—For a detailed description of power measurements in multiphase circuits, see pp. 388-400.

Observations.—(1) Connect up as in Fig. 100, and adjust all the instruments to zero, levelling such as require it. See that

all lubricating arrangements in use feed properly on starting the motor in the usual way.

- (2) With the motor quite free, take readings on all the instruments concerned when M thus runs "light" at its normal frequency and voltage, noting the speed.
- (3) If a dynamo load is used stop SR, couple the shafts of D and SR together and start the combination up again, with R at its maximum when S is closed; or if a Prony brake is used take a series of about ten different loads from D or on the brake, varying from the smallest to the largest permissible corresponding to the maximum current allowed for SR. Note simultaneously the readings of all the instruments at each load and also the speed, the supply voltage and frequency being constant throughout.
- (1) Ropeat 3 for speeds 20% above and 20% below normal respectively, if possible, by varying the speed of the generator.
- (5) Adjust the direct current load to a convenient amount, then, keeping V_{S} constant, after the speed of the three-phase generator by successive steps, and note the corresponding effect on W, W_{S} and the speed of the motor.
- (6) Keeping the speed of the three-phase generator constant, after V_s by successive steps and note the effect on W_1 W_2 and the speed of the motor, using the same load. Tabulate all your results as follows—

Dur ...

	Multipliese Motor: Ko Normal: Volta =		Maker Speed =
•	Rev. Warm per Physe Wooding Rotor (re) = ohms.	Stator = o'u	11.5 ₆ .
	Dynamo D: No Normal: Volta = , . ,	Tyj>a Atnjok.≔	Maker Speni =
	Dinineter of Brake Pulley d = .	, , , fl., if used.	
Heevs.	Watta, For Use with Dy Lord.	thrmo	Uwe nith a iny Brake.
Marakor. [Bujpit p of Bujpit Imps. 4s.	Volts Fg.	Autor 46 y 11 8800 ght Side	Pull Pull Jiba Jiba H.P. abso

NAME . . .

(7) Plot the following curves from observations 3 and 4 for each speed having efficiency, power factor, slip, speed, current, and intake Watts as ordinates and B.H.P. as abscissa, also curves having Torque as abscissa with A_B A_B and slip as ordinates.

And from observations 5 and 6, curves between voltage V_s and supply frequency as ordinates with speed of the motor as also in each case.

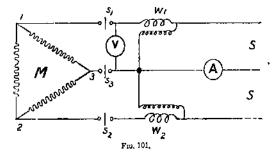
Inferences.—State very clearly all the inferences which can be drawn from your experimental results, and point out their bearing on electrical driving by multiplase current motors.

(101) Determination of the performance of an Induction Motor at all loads without loading it at all. (Heyland's Method.)

Introduction.-It sometimes happens to be inconvenient and even impossible to brake, or otherwise absorb the B.H.P. of large induction motors, and in other cases to supply the large amount of electrical power required by them at full load from a generating plant which may be already running nearly at full load. The difficulty is mot fortunately in such cases by the following method entailing the construction of the well-known "Heyland Diagram" from vory simple "no load and short circuit" readings on the motor. The intake current and power, the output, the power factor, and the slip, etc., and hence efficiency, can then be deduced for all B.H.P.s and a complete set of curves drawn showing the performance of the motor. The temperature rise at any load cannot however be obtained with this method, and the best and most economical way of determining it is to let the motor drive a generator which is capable of absorbing the required B.H.P. and simultaneously return the output of this generator to the motor supply. Thus in running a 6 hours' temperature test on, say, a 500 B.H.P. motor having an efficiency of 95%, the power wasted would only be some 10% or about 50 E.H.P. as against over 500 H.P. if, the output of the generator had been taken up in rhoostats.

Apparatus.—Three-phase induction motor M with phases equally balanced (presumably) complete with starter. A tachometer; a voltmeter; an ammeter reading up to at least full lead intake amperes, and a source of supply SS at the normal voltage and frequency for which the motor is built and capable of reduction to about $\frac{1}{2}$ full normal voltage at full normal frequency, as before, together with—

For motors with mash-connected states—2 similar wattmeters having a capacity of about 1 of the full lead output of the motor.



For motors with well-balanced star-connected stator—I wattmeter having a capacity of about 18 of the full-lead output of the motor.

The ohmic resistance of a complete stator phase (and of a rotor phase for reference later, if needed) will be required, and can be obtained from a separate measurement with a high-reading ammeter and low-reading voltmeter, by the full of potential method (vide p. 84).

Observations.—(1) Connect up as in Fig. 101 if the motor stator is mesh connected or if the stator is star connected but not well balanced, and adjust the pointers of those instruments which require it, to zero. The terminals of the stator of the motor M are 1, 2 and 3, whether it is star or mesh connected.

(2) Close the switch S1, S2, S3 and start up M, finally short-

. 14

circuiting the starter. Then with the supply at normal voltage and frequency note the speed of M on the tachemeter and the readings of all the instruments, the motor running quite light and at "no load."

N.B.—If the power factor of the system is low, one of the wattmeters will read negatively. Itererse the connections to its shout coil and take the reading which must be considered—" and subtracted from the reading of the other wattmeter to get the total true power.

(3) Open S_1 , S_2 , S_3 and when the motor comes to rest, clamp the shaft in any convenient way to prevent it retating, and place the starter at short-circuit. Now apply any convenient lower voltage, say, $\frac{1}{2}$ to $\frac{1}{4}$ of the normal value at full normal frequency, and again read all the instruments as in Test 2 above and switch off and open the starter.

Note.—A lower voltage has to be used in this test for the larger-sized motors, because the normal voltage would cause dangerously large currents to flow which would probably damage the stator winding in even their brief application. The true static current will now be the observed current x by the ratio of the two voltages, while the corresponding static watts will be those observed x by the square of this ratio (see table). The reason for this is that the static watts are nearly all copper loss and hence \(\phi \) to (current).

(4) Measure in a convenient manner (pp. 84 and 263) the resistance R_i between any two terminals of the stator and rotor, preferably while warm. Then the resistance of each complete stator phase (star connections) $r_i = \frac{R_i}{2}$; and for (mesh connections) $r_i = \frac{5}{4}R_s$. Also in the case of a slip ring rotor obtain the ratio of transformation given by the ratio of any stator voltage to the corresponding rotor voltage with rings open-circuited and rotor in the position giving max. volts,

Record your results as follows-

Remetance:—complete Stator Phase, $r_{s} = \dots$ Rotor Phase, $r_{r} = \dots$

	Amperes In		Wathurier Readings.			Power Factor			
Volta arcom Stator Phase Va.	Line As.	Each States Phase Ao.	w ₁ ,	IS ₂	= m.	Total Intako Truu Waita Ku	From #1 #2 puri curve (see	Cos. 6g Site 3.424'0	Angle of lag

Ap-	Amps. in Ide	— Stator		meter Luga.		lintako Watta at	Power	
piled Line Volta	At Volts Volts Vs At Volts Vs At Volts Vs At A	7 1112	al nă	다 다. 다 다 다	Volta Va Kw e gla	Normal Volta (V)3g1v	Factor Cos. 61 = 4/3 mg. 3VA y	Angle of Lag

Note.—With mesh-connected stators: Volts per phase = $\frac{1}{\sqrt{3}}$ line amps.; with star-connected stators: Volts per phase = $\frac{1}{\sqrt{3}}$ line volts and amps. per phase = line amps.

It will be seen that the Power Factor for the "no lead" and for the "short-circuit" tests is found from the relation--

Cos.
$$\theta = \frac{\text{True Watts absorbed per phase}}{\text{Amps. per phase} \times \text{volts per phase}}$$

but it is perhaps more convonient to calculate from the experimental readings by means of the fraction given in the above table.

From the data contained in the above tables, the Hoyland Diagram can be constructed, giving the performance of the motor. Construction of Heyland Diagram,—This will be understood more easily by working it out from tests recently made by the author on a 360 B.H.P. 500 volt three-phase induction motor, running at a speed of 300 revs. per min. with a normal frequency = 50 ~ per sec. The stater windings were star connected, the rotor windings being also star connected, and led out to three slip rings which were connected to a starting resistance. The method of procedure with this motor was as follows—

With an ammeter in one line and a watteneter connected between the neutral point and one terminal of the motor so as to measure the true watts absorbed by one phase (see Fig. 151, p. 396), the following measurements were made—

Motor running light at normal speed, frequency, and voltage with rotor short circuited.—Wattancter reading = 3600 watts per phase = $\binom{w_s}{3}$.

Line current $(A_L) = 142$ amperes.

Resistance of each phase of stator (cold) $r_* = 0.0122$ ohm., or by calculation about 0.013 ohm. (hot) on the assumption of a maximum temperature rise of 70° F, above that of the air.

Resistance of each phase of rotor (cold) $r_r = 0.0051$ ohm,

Ratio of transformation in rotor 500:325.

Bearing in mind always that the diagram is constructed with reference to one phase of the motor, and not the motor as a whole. Further that in testing motors with mesh connected stators it would be the total power absorbed that would be measured by the two line wattmeter method (Fig. 101, p. 278) instead of that per phase.

Honce the power factor of any phase, whether in star- or meshconnected stators, can be calculated best from the general relation

$$\cos \theta_2 = \frac{\sqrt{3}w_*}{3A_L \bar{y}},$$

where $w_o =$ total power in watts absorbed by motor running light with a line current A_L and line voltage V. The numeral 3 reduces w_o to watts per phase, and $\sqrt{3}$ reduces the line voltage V or line amperes A_L to the corresponding quantities per phase in the case of star- or mesh-connected stators respectively. Thus in the present case

cos.
$$\theta_2 = \frac{\sqrt{3}w_*}{3A_*V} = \frac{\sqrt{3} \cdot 10800}{3 \cdot 142 \cdot 500} = 0.0878$$

or $\theta_{\rm g}=85^{\circ}$.

Motor at standstill with retor short circuited and stator supplied at normal frequency.—With these conditions we require the line current that would flow, and also the true watts absorbed, at normal line voltage. As, however, a line voltage as great as the normal value would, in most motors, produce an abnormal current that would be inconvenient to measure and liable to damage the windings, a smaller voltage sufficient to give a convenient line current is applied. Thus in the present case the line current $A_{\mathfrak{g}}' = 104$ amps.

, pressure $V_6 = 127$ volts.

Wattmeter reading $\left(\frac{w'}{3}\right) = 8000$ watts per phase.

From which we calculate the following static standstill values—

Line current

$$A_{\rm M} = {{\rm normal \ volts} \over {\rm applied \ volts}} \times 404 = {500 \over 127} \times 404 = 1591 {\rm \ amps},$$

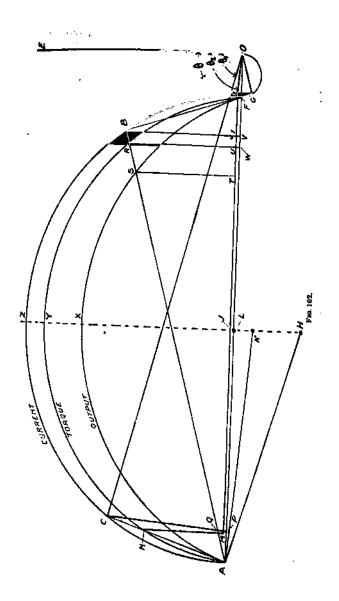
Total watts absorbed

$$w_s = \left(\frac{500}{127}\right)^s \times (3 \times 8000) = 372,000 \text{ watts}$$

whence $\cos \theta_1 = \frac{\sqrt{3} \omega_1}{3A_3 V} = \frac{\sqrt{3} \cdot 372000}{3 \cdot 1591} \cdot \frac{372000}{500} = 0.2701$ or $\theta_1 = 74.3^\circ$.

Current Circle.—Referring to Fig. 102, draw two lines OE giving the phase of the supply volts and OA perpendicular to one another, and from the point O, as origin, set off a straight line OC (:= current which would be taken by the stator if directly across normal voltage), making an angle θ_1 of 74.3° with OE and another line OD (= no-load current) making an angle θ_1 of 85° with OE. Now choose a convenient linear scale of current, e.g. in the present case, 100 amps. = 1 cm., and thus make

$$OC = 1591$$
 amps. $= \frac{1591}{100} = 1591$ cms. long.



and make OD = 142 , $= \frac{142}{100} = 1.42$ cms. long.

Then with a centre L (on OA) draw a semi-circle ACZD through the points C and D, and cutting OA in A and F, thus determining the point A. From D draw DF energy component of no-load current perpendicular to OA and cutting it in F, then DFO is the no-load triangle of currents OF = the no-load magnetizing current $\cos \theta_1$ = the no-load power factor. Roter current = $FB \times ratio$ of transformation stater intake $\propto BV$ and AZF is the current circle for the motor.

Output Circle.—Join CA, and from A draw AH perpendicular to AC, cutting the perpendicular HZ, to OA through L, in the point H. With centre H draw the output semi-circle AXF through the points A and F. Since the angle $CAH = 90^\circ$, the line CA is a tangent to the output circle, the ordinate of which at A is zero, thus satisfying the condition of no output corresponding to this point and the point C, output of motor C which has a max. value C C which has a max. value C C C

Torque circle.—The torque of an induction motor is proportional to the rotor flux $(R_F) \times$ the rotor current (R_A) and in fig. 102 the right-angled triangle ACO is a triangle of fluxes in which $AC \propto R_{F1} AO \propto$ stator flux (S_F) which is also \propto applied voltage per phase and $OC \propto$ leakage flux L_F . Consequently the actual rotor flux will be $\propto AC$ —copper drop in stator resistance, and we proceed by first finding the voltage represented by AC when the volts per phase of stator are represented by AO. Thus—

whence-volts represented by

$$AC = \frac{AC}{AO} \times \text{volts per phase} = \frac{4.55}{16.7} \left(\frac{500}{1/3}\right) = 78.66 \text{ volts.}$$

Now the copper drop for stator phase (for the short circuit current $A_S = 1591$ ampa.)

$$= A_{sF_4} = 1591 \times 0.013 = 20.68$$
 volts.

Therefore from the point C mark off along CA the length CN = 20.68 volts, which is proportional to

$$\frac{A_5r_s}{78.66}$$
, $AC = \frac{20.68 \times 4.55}{78.66} = 1.196$ cms.

Now find a centre K in ZH, such that a semi-circle ANI'RF described from it passes through the points ANF. This is the required torque circle. Since the rotor flux is represented by AN, the total torque is $\propto AN \times CF$ which is \propto to the area of the right-angled $\triangle ANF$ (the line NF not being shown in Fig. 102). But the base AF is constant. Hence the total torque is ∞ to the altitude of the triangle. For example the total torque is ∞ RW for the stator current OB. Again, in the no load triangle of currents ODF, the no lead wattless magnetising current = OFlagging 90° in phase behind the E.M.F. OE, and having a load current component in phase with OE = FD. The resultant no load stator current as read off on the ammeter = OD. Hence, since useful torque = total torque - torque spent in overcoming internal frictions for the same stater current OB, we have useful torque $\propto RW - WW \propto RU$. Starting torque would be NM at the starting current OC and a power factor $\cos \theta_1$. Slip of the Motor.-Since we know that the slip is directly

Slip of the Motor.—Since we know that the slip is directly α to the rotor current NF, and inversely α to the rotor flux AN, we see that it will have its maximum value at C and minimum value at D, for $\frac{NF}{NA}$ (which is α to slip) has its

maximum value unity at C when the motor is at standstill. From C therefore draw CP perpendicular to AK cutting AO

in P. Then the slip $\alpha = \frac{NP}{NA} \propto \frac{QP}{AP} \propto -QP$, since AP is constant and the triangles ARF and APQ are similar.

Now maximum slip corresponding to the point C and the motor at standstill is $\propto CP$, which scales 4:35 cms, and represents 100 % slip.

The slip at the output lead ST when taking a stater current OB is $\frac{\text{length }PQ}{\text{length }P^2} \times 100 \% = \frac{0.3}{4.55} \times 100 = 0.9 \%$.

Stator copper loss = (BV - RW) watts and rotor copper loss = (RU - ST) watts each to a scale of watts suitable for input BY and output ST, HR and RS = ohm drop of volts in stator and rotor respectively to same scale as OA gives stator volts per phase.

Application of Diagram. The diagram can now be employed for determining the performance of the motor at any load corresponding to any point such as B taken anywhere on the current curve AZF. Suppose that we choose the point B as

being the point of contact of the tangent OB with the current circle AZF. Join AH, cutting CP in Q, the circle AXF in S, and AVF in R, and draw the perpendiculars ST, RUW, and HIV.

Power Factor.—For any given point on AZF the power factor is given by the cosine of the angle between the join of this point with O and the line OE. At B it has the maximum value possible, since OB is a tangent to the circle, namely

 $\cos \theta = \cos 32.8^{\circ} = 8406$. Stator Current per phase = OB_i , which is also the line current

in the present case since the stator is star connected. This scales 4.95 cms. corresponding to 495 amperes (since 100 amps. = 1 cm.).

Total Apparent Watts absorbed = $\sqrt{3}$, V. line amps. = $\sqrt{3.500}$, 495 = 428,600 watts.

Total True Watts absorbed = $\sqrt{3}$. V. (component of OB in phase with and parallel to OE).

 $=\sqrt{3}$, V, BV with star connections = $\sqrt{3}$, 500, 416 = 360,200 watts.

The same result is given by $3(BV) \times \text{volts}$ per phase. Stator copper less for this load = 3 ($r_a \times component FB^2$ of

stator current) = $3.0.013.(435)^2 = 7381$ waits.

This loss is proportional to BR which = 0.43 cm., and the Rotor copper loss is & to RS which = 1.0 c.m., and this loss

therefore $=\frac{1}{49} \times 7381 = 17,165$ waits.

intake stator current OB = 10,800 + 7381 + 17,165 = 35,346watts. The output of the motor therefore = 360,200 - 35,346 =

324,854 watts = 436 B.H.P.

The total less in the motor at the load corresponding to the

The efficiency of the motor therefore = $\frac{324,854}{360,200} = 90.18$ % when giving 436 B.H.P. or 21 % overload with a power factor already found of 84 %.

The ordinate ST thus represents 436 B.H.P. or the scale of the ordinates of the output circle is $\frac{436}{ST} = \frac{436}{3 \cdot 65 \text{ cms.}} = 119 \cdot 5$

B.H.P. per 1 cm., consequently the rated full load of the motor, namely 360 B.H.P., will be given by an ordinate such as ST, but only 3014 cms. long.

The efficiency, power factor, and slip, etc., can now be worked out for this new full load point which gives another point, such as R on AZF nearer to F and a line such as AB, at a smaller angle to OA. Hence the performance at any load can be determined.

Further, if T = the torque in pound feet, d $\omega =$ the angular velocity of the rotor = $2\pi n$, here n = the roys per min of the rotor at a given B.H.P.,

where n = the rows, per min of the rotor at a given B.H.P., then B.H.P. = $\frac{\omega T}{38,000} = \frac{2\pi nT}{33,000}$ or $T = \frac{33,000 \text{ B}}{2\pi n}$ H.P.. Now since at B the B.H.P. = 436 and the slip = 5.9 % $\sim n =$

 $\frac{300 \times 93 \cdot 1}{100} = 279 \text{ r.p.m.} \qquad T = \frac{33,000 \times 436}{2\pi \cdot 279} = 8210 \text{ lb. ft.}$

and

Hence the scale of the ordinates, such as RU, of the torque circle is known from all other ordinates from the above, and $\frac{8210}{RU} = \frac{8210}{3.9} = 210.5 \text{ lb. ft. per 1 cm.}$

The maximum torque which the motor can exert before pulling up is represented by JY, and the maximum B.H.P. by JX.

The starting torque corresponding to the current CO is NM.

The Hayland diagram becomes more accurate the smaller the no load losses as compared with the copper losses, i.e. the larger the motor tested. The performance of the motor is slightly better than given by the diagram, while for motors smaller than for 4 or 5 H.P. the line MD should be drawn downwards from D at an arbitrary angle of about 25° to OA for greater accuracy, in correcting the small error (slightly affecting the accuracy of the diagram) due to the greater proportion of no-load to load losses in small motors.

¹ For higher accuracy see Theory of Induction Motors by Diagram, G. Ossanna: Zeitschr. Elektrotech. Wein, 17, pp. 223-248 (1869), and Circle Diagram, by J. L. la Cour (some journal), 21, pp. 618-645 (Nov. 1908).

Note.—If OG be drawn perpendicular to BF produced, then AB and OG will always be parallel at all loads and perpendicular to BG.

The sides OB, BG, and GO of the triangle OBC, represent the stator current, rotor current, and magnetising current respectively. Now, in any electro-magnetic circuit the total flux = the useful flux + the leakage flux, while total flux is called the leakage flux factor v, which is always greater than unity, and leakage flux is called the coefficient of magnetic dispersion σ which should be always much less than unity.

In the Heyland diagram, Fig. 102, the leakage factor O(A) = O(E), E(A) = O(E)

$$\nu = \frac{\partial A}{FA} = \frac{\partial F + FA}{FA} = \frac{\partial F}{FA} + 1$$

and the dispersion coefficient

$$\sigma = \frac{\partial F}{\partial A} = \frac{\partial A - FA}{\partial A} = 1 - \frac{FA}{\partial A} = 1 - \frac{1}{\nu}.$$

(102) Complete Test for Efficiency, Slip, Power Factor, and Temperature Rise, of Three-Phase Induction Motors. (Sumpner and Weekes Method.)

Introduction.—This method, due to Dr. W. E. Sampaer and

R. W. Weekes, is an application of the principle of the ordinary Hopkinson test of a pair of d.e. dynamos (p. 228) to the test of a pair of three-phase induction motors. The arrangement, which entirely avoids the use of a brake, is extremely convenient for obtaining the temperature rise due to a long run at any particular load, and is shown in Fig. 103. M and G are the two machines to be tested, of which M is made the motor and G the generator. Their stator terminals T are connected to the main supply SS, which is at the normal voltage and frequency required by G and M. A bolt B drives the rotor pulleys, which must be of different

diameters in order to enable the generator G to run at a higher

speed, and the motor M at a lower speed than that of synchronism.

1 Communicated by the authors to "Section G" of the British Association, August 22, 1004, at Cambridge.

If D_{μ} and D_{θ} are the diameters of these pulleys: then assuming the rotors are to remain short circuited during the test, the ratio $\frac{D_H}{n}$ must be such as to cause the right slip for the load required. For example,—if the slip of each machine M and G = 25 % at full load, and if the probable efficiency of each = 85 %, then 15 % of the load is lost in each, and the overload of the motor M = 30 % roughly, corresponding with $2.5 + \frac{90}{100} \times 2.5$ or 3.25 % roughly. The other machine G working as a generator developes full load and has a negative slip of 2.5 %. D_M and D_G must therefore differ by 2.5 + 3.25 or 5.75 %, assuming no mechanical slip of the belt B on the pulleys. If, however, 1.25 % be allowed for this, the pulleys must differ by 5.75 ± 1.25 or 7%in diameter, and the machines under test will, when switched into circuit, take a perfectly definite load which can be maintained for any length of time.

An interesting feature of the test lies in the fact that G. the machine used as the gonerator, gives current of about the same power factor as that of the current supplied to the motor M, while the current from the supply mains SS is the difference of the power components of the machine currents, together with the sum of the inductive components of these currents. Consequently, the power factor of the main current from SS is very small, and may be only gid of that of the machine current, the main current from SS may be equal to, or greater than, that through the machines, while the actual power taken from SN may be less than } of that circulating round the machines G and M.

Alteration of load with two given pulleys can be obtained by alteration of resistance in the rotor circuits between starter and slip rings, or by using a low resistance starter which can stand the full load rotor currents. The CaR losses in these rotor resistances, if appreciable, must be deducted from the power taken from SS in order to get the total loss in the two machines G and Mand in the belt drive. The machines can be run at various leads, with resistance variation such as above, if the pulleys are chosen with sufficient difference to obtain the maximum slip required.

The magnitude of the mechanical slip at the pulleys is determined by the ratio of their circumferential speeds, a quantity difficult of determination with any accuracy in ordinary belt drives, burmost easily found in the present method. Thuslet S. - frequency of the supply current, generator rotor current, $G_Y =$

 $M_t =$ motor rotor current; then ratio of the rotor speeds $R = (S_F + G_I) + (S_F - M_F)$ and

ratio of the circumferential speeds of the pulleys = $R \frac{D}{D_0^2}$ G and M_F can be very accurately determined, and are each small compared with S_P , so that although S_P cannot be so accurately

be tested: suitable pulleys and belt; four alternating current

found, the value of R is not much affected by small errors in S_R The belt losses are easily determined, as shown in the table. and are caused by (a) exten bearing friction and in bending and driving the belt, (b) heating of the pulleys due to belt slip. Apparatus.—The two similar three-phase induction motors to

ammeters a_1, a_2, A_1, A_2 ; an alternating current voltmeter V; four wattmeters we was W , W , W ; source of three-phase supply SS of normal voltage and frequency for which the machines under test have been built; three-throw switch s_1 , s_2 , s_3 . N.B.—Switches must be used with the stator connections if the

rotors are of the "short circuited" type, but are not wanted if the rotors are supplied with slip rings and starting resistance, Only two wattmeters will be needed if one is connected between neutral point and a terminal in the case of each machine, since in this case total power = $3 \times \text{power}$ of one coil, which is sufficiently accurate for commercial work. Two wattmeters to each machine,

as shown in Fig. 103, is, however, the best and most accounte arrangement, and has the additional advantage that the ratio of the readings of a pair of wattmeters gives the power factor independent of the usual method of getting the power factor from

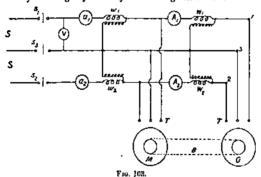
true watts + apparent watts. With two wattmeters the reading of one will be -" owing to the low power factor of the supply current, Observations.—(i) Connect up as shown in Fig. 103, and adjust those instruments to zero which require it, (2) With the supply SS at the normal voltage and frequency needed for M and G, and the belt B off, close s_1, s_2, s_3 , and start up

M and G, which must run in the same direction. If they do not, stop them, change the connections at T, and start up again. Note the readings of all the instruments, and denote those of we and we by w_{a1} and w_{na} respectively.

(3) Stop M and G, place the belt on, and start up again, with only one of the machines in circuit, and acting as a motor, but driving the other by belt with its stator excited and rotor open circuited. Note the readings of all the instruments, and denote those of w₁, w₂ by w₂, and w₃, respectively.

Thus the belt loss $W_B = (w_{B1} + i\sigma_{B2}) - (w_{01} + i\sigma_{02})$.

(4) In Tests 2 and 3 above, and in all future lead tests, the slip of each machine can most conveniently and accurately be determined by measuring the frequency of the rotor currents by suitably shunting any ordinary low reading d.c. voltmeter to the



slip rings of the rotor, and noting the number of periods made by the pointer in, say, 20 seconds, these being slow enough to be easily counted. If $M_{\pi^{\pm}}$ number of periods per second, in, say, the case of the motor rotor currents and S_{π} = frequency of the supply current in periods per second, then the slip of the motor == $\frac{M_{\pi}}{2}$ 100 $\frac{\gamma_{\pi}}{\pi}$.

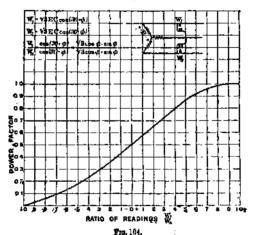
(5) Take readings at different leads, obtained by altering the resistance in the rotor circuit and tabulate as shown on page 293.

The values of the losses given in columns 31 and 32 are accurate enough for commercial purposes if the two machines are of the same make and of about the same rated full-lead output and if subjected to the same voltage. A greater degree of accuracy may be obtained, however, by subdividing these

losses. In addition to the diameters of the pulleys indicating which machine is the motor and which the generator, the latter is the one which must always run at the higher speed. If the belt is removed and the machines run light, the watematers W_1 and W_2 will read negatively if G is the generator.

Column 44 is obtained from the curve Fig. 101, which is drawn in the following manner.

The ratio of the two readings of wattmeters W_1 and W_3 connected as shown in Fig. 103, varies from +1 to -1. Hence the power factor cos. ϕ can be calculated from the readings of W_1 and W_3 by substituting different values of ϕ (the angle of lag) between current and voltage in the formula shown.



The value of $\frac{W_1}{|V_2|}$ so found plotted against the value of \cos . ϕ gives the curve, Fig. 104. As an example of the application of this curve, let $W_1 = 6800$ watts, $W_3 = 18000$, then $\frac{W_1}{|V_3|} = 0.37$ and \cos . $\phi = 0.77$. Again, let $W_1 = (-)$ 2000 watts, $W_3 = 4000$, then $\frac{W_1}{|V_3|} = (-)$ 0.50, and \cos . $\phi = 0.18$.

Holle	Pine II	_	Targ	Azoyanes.	Wattmeter Beading	,		Title watth	Power taken from Mains	Ampa
Reading	Slart.	<u>v.</u>	ď	ė	. <u>\$</u>	ţ	ij	ŝ	53. 4.4 + 1.4	र्च
-	N .	ø,				ι-	20	٥	70	п
Ambe	Wattwete	Wattweter Beading,	True	True Watts.	Output of Generator G	No. of Perio	No. of Periods of Rotor Corrents in 39 Secs.	Frequency of Rotor Currents.	of Rotor ents.	Frequency of Supply
4	₫IF ₃ ,	4 IF.	ř.	H.	F1+ F2	Me,	6.2	M. = M.	GP = GP.	Ma na ba
ęi	138	11	St.	18	1.	13	61	23	u	ន
Wachanitel	Electro Mag	Electro Magnetin 31.p of	Pall Lon	Tenperature	Teniperature in Degrees F. or C. of the	or C. of the	Natt Dower	Total Losses in	al sass	Motor
Shp of Belt Se+Ox Dr Se-Me × Dr.	Motor $\frac{M_P}{b_F} \times 100$ $= M_S \%.$	Genr. 8 × 100 Eyx 100 = 9 • X.	$(1^n x_1 + x_1 y_2)$ - $(x_1 y_1 + x_2)$ = $(y_2 y_1 + x_2)$	Air.	Motor Btalor.	Generator Stator,	### ### ##############################	Moter Mass Ma+Gi = Ma.	Generator $\frac{f_{s,s,t}}{f_{s,s,t}}$ $M_{s,t} = 0.5$	Injut Fituy+m = Mr
8	ä	£ .	265	Į;	81	63	8	31	33.	Z
, de		Moint Oat-	Ceres	Cer erator.		Power Factor of Motor.	or of Motor.		P. F. of Generator.	enerator.
Output Mr - Mr = Mo.	Efficiency 7, 100	Fraction of its Raked Full Load.	Input W+61	Efferency W	Connected Wattneters, IF ₁ + κ_2 , IF ₂ + κ_2 .	Fatincters, H2 + 12.5	$\pm \frac{17_1+49_1}{11_2+43}$	Cos. c from Curra.	# # # # .	C.4 & from
\$	8	S	li li	8	68	40	; ;	ş	3	#

(103) Relation between Efficiency, Slip, Torque, Load, etc., in an Induction Motor with Variable Rotor Circuit Resistance

Resistance.

Introduction.—The present test is obviously just an extension of, and similar in almost every way to, test No. 100, which is therefore repeated here but with different amounts of the starting resistance (r) in circuit instead of it being all cut out to short-circuit as in that test. Consequently there will be

one set of curves, such as was obtained in test No. 100, for each different value of rotor circuit resistance used in the present investigation.

Further, if, say, five different rotor circuit resistances were

used, giving five complete sets of curves as in test No. 100, then any of the variables plotted, say, against load, for the different constant rotor resistances can be transferred and replotted against rotor resistance, e. g. there would be five efficiency-load curves, then if a straight line was drawn through, say, full-load point, parallel to the axis of efficiency, and cutting the five efficiency curves; the five different efficiencies obtained by the five inter-

section points can be plotted against the five values of rotor resistance of the efficiency-load curves to give a curve of five points between efficiency and rotor resistance only.

 $K_S = E.M.F.$ induced in each stator circuit due to the rotating field, $N_dN_B =$ number of turns per phase in each stator and rotor winding respectively.

ω_{σω_σ} = angular relocities of rotating stator field and rotor respectively,

 $r_R = \text{resistance of each rotor circuit,}$

 $L_z =$ self-induction of each rotor circuit,

p = number of pairs of poles in the rotating stator field, f = frequency of the stator supply voltage and

eurrents, K =the slip.

Then we have $K = \frac{\omega_1 - \omega_2}{\omega_1}$ and the frequency of the induced

E.M.F. and currents in the rotor circuits will $=\frac{\omega_1-\omega_2}{\omega_0}\times f=$

Kf =slip in cycles per sec., and it can be shown that the running torque T is given by the relation

$$T = \frac{N_{S}^{2} K_{S}^{2} r_{g} K}{N_{S}^{2} u_{1} (K^{2} (2\pi f L_{B})^{2} + r_{g}^{2})} \stackrel{\cong}{=} \frac{N_{S}^{2} L_{S}^{2} r_{g} K}{N_{S}^{2} 2\pi f (K^{2} (2\pi f L_{E})^{2} + r_{g}^{2})}$$

where

f/p = speed of the stator rotating field in revs. per sec.,

and

 $2\pi f/p = \omega_1 = its$ angular velocity,

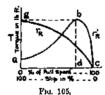
 $K2\pi f L_B =$ reactance per rotor circuit when in motion and which is ∞ to slip,

and $K^2(2\pi/L_s)^2 + r_s^2 = (\text{impedance})^2$ por rotor circuit when in motion.

Further, if $A_R =$ current per phase in the rotor, and F = leakage flux, then the coefficient of self-induction per phase of the rotor $= \frac{(X_0)^2 F}{10^9 \cdot \Gamma_R}$ henries, which can also be calculated from the shape of slots and winding in them.

The above expression for T shows us that the running torque T of the induction motor is ∞ to the square of the stator voltage, i.e. to the square of the stator flux, and increases as both the supply frequency and reacture per phase of the rotor decreases, becoming a maximum (bd) when

$${\rm K} = \frac{r_R}{2\pi f} \frac{{\rm and}}{L_R} \frac{T}{{\rm and}} = \frac{K_R^2 E_R^2}{N_S^2 2\pi f} \frac{2(2\pi f L_R^2)}{p} = \frac{N_S^2 E_R^2 p}{8N_S^2 \pi^2 f^2 L_R}$$



Thus, since the last expression for the maximum value of the running torque does not contain r_{th} we see that it is constant and independent of the rotor circuit resistance, but for different values of rotor resistance will attain the same maximum value bd at a different slip, as indicated in Fig. 105. The motor starts

at 0 with 100% slip and reaches the same maximum running torque bd = og for slips of cd% and co = 100% (i. a. full speed) respectively, with rotor circuit resistances r_s^2 and r_s ; since the stator current depends on the constant no-load current and rotor current, and the latter will always be the same for a given torque, it follows that each value of torque will have

a definite stator current which is independent of the rotor

Apparatus.—Precisely that for the preceding efficiency-load test No. 100, the starting resistance in the rotor circuit being of sufficient current-carrying capacity to enable it to carry, without overheating, the full-load rotor currents.

Observations.—Connect up as in Fig. 100, and carry out the tests precisely as directed in that test, for as many different values of starter resistance as possible.

Tabulate as shown on p. 276, adding two extra columns for values of starter resistance (r) and total rotor circuit resistance $r_x = (r_w + r)$ respectively.

Plot the following curves having torque T in lb.-ft., and rotor current A_B as ordinates with percentage of full speed (or slip), and stator current A_B respectively as absisse for each value of

rotor circuit resistance (r_s) .

Also curves having efficiency, power factor, slip and true stater watts absorbed as ordinates with B.H.P. as abcisse for two widely different values of r_s .

Inferences.—From a careful study of the numerical results and curves state clearly what can be deduced.

(104) Relation between the Starting Torque, Current, Voltage, and the Rotor Circuit Resistance of an Induction Motor. (Rotor at Standstill.)

Introduction.—Under these conditions the slip will be 100%, since the speed is zero. The power absorbed will include both iron and copper lesses, and the motor will approximate to a static transformer with a non-inductive secondary load.

Now the frequency f of the stator supply will also be that

of the rotor circuits whon at rest, and if we put K=1 in the expression for the running torque (p. 295), since the rotor is now stationary, it will be seen that the starting torque $T_{\rm c}$ is given by the relation

$$T_{\rm 0} = \frac{N_{\rm g}^{2} {\rm E}_{s}^{2} r_{\rm g}}{N_{\rm g}^{2} 2 \pi f (2 \pi f L_{\rm g})^{2} + r_{\rm g}^{2}} \quad , \label{eq:T0}$$

where $\frac{f}{p}$ = speed of the rotating field in revs. per sec. and $\frac{2\pi f}{p}$ its angular velocity, $(2\pi f L_x)^2 + r_x^2$ = the square of the impedance, and $2\pi f L_x$ = the reactance per phase of the rotation when at rest. From the above relation we see that the starting torque T_0 is \propto to the square of the stator voltage, i.e. to the square of the stator flux, and increases as both the supply frequency and reactance per phase of the rotor decreases, becoming a maximum when $2\pi f L_x = r_x$.

For this last condition-

$$T_0=\frac{N_B^2K_S^2p}{2N_S^32\pi fr_B}=\frac{N_B^2p}{4N_S^2\pi}\times\frac{E_S^3}{fr_B}, \text{i. e. inversely } \pi \ \text{to} \ r_B$$

we therefore have the following most important deductions, namely, that for a given supply frequency, the starting torque is a maximum when the resistance and reactance of the rotor circuits are equal and each as small as possible. Since the rotor currents are a maximum at starting, the present test enables the maximum value of the starting resistance to be obtained under either of two conditions: namely, (1) for maximum starting torque, or (2) for maximum safe starting retor current. In the former, by measuring the values of L_x and r_x per phase winding of the rotor we know that for maximum starting torque $2\pi f L_x$ must $= r_x + r$, whence the external starter resistance must have a maximum value $r = 2\pi f L_x - r_x$ ohns per phase.

In the latter, if V_R = the standstill slip-ring voltage at normal stator volts and frequency, then $\frac{V_R}{\sqrt{3}}$ = the standstill volts per phase winding, whence $r = \frac{V_R}{\sqrt{3}A_R}$ ohms per phase for a maximum safe starting rotor current A_R . The gradation of r

between this maximum value and 0 depends on the number of switch contacts and sections chosen.

Apparatus.—That detailed for the no-load short-circuit test No 98, using an induction motor having a slip-ring rotor connected to the usual form of three-phase equal variable starting resistance of a current-carrying capacity sufficient to allow the necessary time for taking readings without overheating. In addition, a block brake and lever, preferably similar to that shown in Fig. 95, will be needed to measure the torque exerted by the shaft.

Observations.—(1) Connect up as in Fig. 100, levelling and adjusting to zero such instruments as need it. On starting up see that all lubricating arrangements are feeding properly.

Starting Torque with Rotor Circuit Resistance for a Constant Supply Voltage and Frequency.— (2) Adjust the supply frequency f to the normal value for the motor and the supply voltage V_{σ} to some convenient value, if necessary lower than the normal value for the motor in order to avoid excessive rotor currents and keep both constant. Then read the spring balance and all other instruments as quickly as possible, when (r) is moved one contact stud at a time from its "full in" position to such a position nearer that of short circuit at which the rotor current A_{π} reaches a safe overload value. Finally measuring the resistance of each rotor circuit corresponding to each contact-stud position.

Starting Torque with Supply Frequency for Constant Rotor Circuit Resistance and Supply Voltage.—(3) With the supply voltage Vs and starter resistance r adjusted to convenient values for giving safe maximum rotor currents and kept constant, read the spring balance and all the other instruments as rapidly as possible at each of a series of supply frequencies (f) between the maximum and minimum values possible and convenient.

Starting Torque with Supply Voltage for Constant Rotor Circuit

Resistance and Frequency.—(1) With supply frequency and starter resistance r adjusted to convenient constant values, read the spring balance and all instruments as rapidly as possible at each of a series of supply voltages V₂ between maximum and minimum values giving safe maximum rotor currents, and tabulate all your results as follows—

Motor: No		Typs			MAKET .	
Pull load : Volta			ing of rotor re-	ohma.	Frequency $ ightharpoonup$.	٠.
			ico from Sheft Ci		n,	
Balance Pull if the Effecting Torque, To=M. i lb.fr. Frequency J.	Volta Fg.	True Wattr.	Apparent Waite Volds Pr. Power Factor cos \$\phi\$ \text{\$\}\$}\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\exit{\$\exitit{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{	Angle of Lag &	Santon Res. 7. Tradictor cust Res. 7.8 = 7.9 + 7. Values of 7.8	11/2

(5) Plot curves having values of A_{s} , A_{tb} and T_0 as ordinates, with values of (r_s) from obs. 2 as abscisse, also curves having T_0 as ordinates with (a) frequency (f) from obs. 3, and (b) states supply volts (V_s) from obs. 4, (c) states amps. A_s , and (d) rotor amps. A_R . An additional column for values of $T_0 = \begin{pmatrix} V_s^2 \\ fr_R \end{pmatrix}$ might be added to this table in order to see how nearly this ratio is constant, i a how nearly the starting torque is ∞ to $\frac{V_s^2}{fr_R}$.

Inferences.—From a careful study of the numerical results and curves, carefully point out all that can be deduced.

(105) Determination of the Efficiency, B.H.P., and other Characteristics of Single Phase Alternating Current Commutator Motors.

Introduction.—The comparatively small starting torque of the induction motor to that necessary for electric traction work has led in recent years to the production, improvement, and utilization on an increasing scale of the so-called alternating-current commutator motor. It is well known that any ordinary direct-current series or shunt-wound electric motor will run in one and the same direction whichever way the supply current flows through it, for with every reversal of the supply current, the magnetization of both field and armature will also be simultaneously reversed, and the motor will continue to run as if nothing had been changed. From this it follows that any ordinary D.C. machine will run as a motor when supplied with

supply.

A.C., though inefficiently owing (1) to the large eddy-current loss due to heavy eddy currents which would be set up in the solid field system by reason of the rapid reversal of the magnetization.

and (2) the demagnetizing effect of such currents on the field. If, however, the field system is well laminated, like the armature of any machine always is, the machine would run with reasonable efficiency on an A.C. supply, but will develop less power than when run with D.C., of the same mean voltage, owing to

the smaller current and flux, and to the larger internal losses due to eddy currents and hysteresis resulting from an A.C.

The field magnets of A.C. commutating motors are either hi-polar or multi-polar, whether of the projecting pole form used in D.C. machines, or of the cylindrical form with uniform air-gap as used in induction motors, and with definite polarity produced

by the windings but not otherwise so evident. The armature, however, presents the usual appearance of D.C. forms, although, along with its commutator, embodying features mentioned later and necessary for ensuring satisfactory operation.

These features will be appreciated after a brief consideration of the actions taking place in the machine, but at the outset it

should be realized that a single-phase series-wound commutator motor, built on the best possible lines for a given voltage supply, will operate in every way as well, but even more efficiently when run from a D.C. supply of the same voltage. In fact, such motors have to run on A.C. in some parts and on D.C. in other sections of certain tramway undertakings. Now, considering such a series-wound motor with (for

poles and through the armature, there will be set up a unidirectional induced potential difference (P.D.) having its maximum value between the brushes, i.e. along the "diameter of commutation" which, with the motor running light, will be coincident with the "neutral axis" and perpendicular to the direction of the fixed field. This induced P.D. (or "back E.M.F.") is set up solely by reason of the forced rotation of the armature conductors across the field, by the supply current

flowing in them, and with a given field is entirely due and

simplicity) a two-pole field, and hence with one pair of brushes, with a D.C. supply, producing a unidirectional field in the

with an A.C. supply producing an alternating field in the poles and through the armature, there will be set up two distinct alternating P.D.s: namely, (1) the induced P.D. having its maximum value between the brushes exactly as mentioned alove, and with a given field entirely due and directly a to the speed (n) of rotation; it is in phase with the field and also practically with the current, and consequently not in direct opposition of phase with the supply E.M.F., and (2) the selfinduced P.D. having its maximum value between two points in the armsture winding on a diameter perpendicular to the diameter of commutation. This self-induced P.D. is set up solely by reason of the transformer action due to the armature conductors cutting the alternating field, and will lag in phase behind the field flux by an angle of 90°. Its magnitude will depend only on the strength and rate of reversal (i.e. the frequency () of the alternating field, and in no way on whether the armature rotates or is stationary. It has no effect on the action of the motor, nor on the supply; consequently, due to the main field, in the rotating armsture of a single-phase commutator motor, there are induced two entirely distinct E.M.F.s -one caused only by and directly or to the speed of rotation, the other caused only by transformer action and directly or to the supply frequency. Now, when a current flows through the armature, the latter

becomes a powerful electro-magnet, the two halves of the winding in parallel between the brushes producing two similar semicircular electro-magnets having a consequent north and a consequent south pole situated in the diameter of commutation, and at a distance apart equal to the diameter of the armature core. The flux of this armature magnetization will be in phase with the current, and have a direction therefore perpendicular to the main field flux, or in line with the diameter of commutation, giving rise to the phenomenon commonly known as armsture reaction. It will react on the main flux in three ways: (1) by distorting and dragging it round in the direction of rotation, (2) by inducing in the armature conductors, as they rotate through it, an E.M.F. along an axis parallel to the main field, but which will not in any way affect the action of the motor,

(3) by inducing, through transformer action on the armature conductors, an E.M.F. of self-induction 90° in phase behind the current and acting along an axis joining the two brushes. The value of this self-induced or reactance voltage of the armature is $L_a 2\pi f A$ where $L_a =$ coefficient of self-induction of the armature winding carrying a current A, and f = the frequency of the current A, which in this case is that of the supply to the motor. Since the motor is series wound, the same current A will flow in the field-winding which will have a coefficient of self-induction L_F . Consequently the series field coils will introduce into the circuit a self-induced, or back, or reactance voltage $= L_F 2\pi f A$. Thus the total reactance voltage of the motor will $= 2\pi f A(L_F + L_a)$. Now the reactance of the machine has the disadvantage of reducing the power factor of the circuit,

and should therefore be minimized as far as possible.

That due to the field coils cannot be reduced, because the chief cause of its existence, viz. the flux, is also necessary for the operation of the machine as a motor.

The reactance of the armature can, and is, compensated for

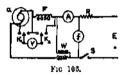
by an additional winding on the field system midway between the main field windings, and producing a flux equal and opposite to the reactance field of the armature, and which is connected either in series with the circuit or short-circuited on itself. In either case the effect is the neutralization of the armature reaction flux and reactance and an increase in power factor. Again, although the self-induced voltage in the armature coils, due to transformer action and main field has no effect on the action of the motor, it has an effect on the commutation. For example, an armature coil undergoing commutation is short-circuited by the brush while inactive, i.e. generating no E.M.F. by reason of its rotation across the field. Since, however, in an A.C. motor, the coil by transformer action has, during commutation, a self-induced E.M.F., this will produce in it, when short-circuited by the brush, a heavy current which when bruken as the segments

Now, the self-induced E.M.F. of a coil decreases with a decrease in the number of turns, and if the circuit of the coil is broken before the current has time to attain its full value the

leave the brush will cause sparking and the deterioration of the

spark will be decreased. Hence in commercial single-phase commutator motors, sparking is minimized by (a) having as few a number of turns per armature coil as possible, (b) an increased number of coils and peripherally narrower commutator segments and brushes, (c) as small a supply frequency as possible, (d) brushes of special composition. The narrower segment in (b) reduces the time during which an armature coil is short-circuited and reduces the short-circuit current in it.

The single-phase A.C. motor possesses much the same characteristics as the D.C. form, being a variable speed motor, giving maximum torque on starting which decreases with increase of speed, and is at to armature current, but independent of power factor. It will tend to race in speed on suddenly removing the load. Further, since the current is simultaneously



reversed in armstore and field, the torque will be undirectional though pulsating.

Apparatus.—An A.C. supply E, preferably a motor-driven alternator having a speed and field control independently variable between wide limits; anneter A; variable non-inductive rhoostat R; frequency numeter (F); voltmeter V with two two-way keys K_1 K_2 ; wattureter V; switch S; and single-phase commutator motor, to be tested, of which the series field windings are F and $\{a\}$ the annature.

Observations.—(1) Connect up as in Fig. 106, levelling and adjusting to zero such instruments as need it. N.B.—With a town's supply for E, the rheostat E will be needed to start up E and for regulating the current afterwards, otherwise with a motor alternator this may be done by field excitation.

(2) With R or the alternator field rheostat full in, and the armature shaft clamped to prevent it rotating, close S and adjust the frequency f to the normal value for the motor. Now "light."

gradually raise the voltage until A reads the full-lead current of the motor, and note the readings of f, A, W and V (when switched by K_1 K_2 across (a), (F), and (a + F), giving readings

value (which must not be excessive), the shaft running quite

- V_{d_1} , V_{r_2} and V respectively).

 (3) For t' is same value of V and f unclaim the armature shaft so as to see what all the instruments, including tachometer V_{d_1} , V_{r_2} and V_{r_3} will read when the speed has risen to a constant
- (4) With normal frequency, and the motor running perfectly "light," read all the instruments and speed at each of a series
- of voltages V between 0, 25% above normal value,

 (5) Repeat obs. 4 with constant normal voltage and wide variation in frequency.
- (6) With the normal frequency (f) and the motor running light, alter V so as to obtain normal speed on the tachometer,
- light, after V so as to obtain normal speed on the tachometer, and note the readings of f, A, V, V, and V.

 (7) With this same value of speed and f load up the motor to about 25% above full load in some eight or ten successive
- steps, noting the readings of all the instruments, the speed being kept constant by raising the voltage Y.

 (8) With the motor running light at constant normal frequency, obtain the maximum safe speed allowable, note this

Maker .

Warmhit ...

frequency, obtain the maximum safe speed allowable, note this and also the values of V, A and W; next apply about ten different braking loads up to about 50% above normal, noting the values of the speed V, A and W at each—V and f being kept constant.

Tabulate all your results as follows-

Motor Tested - No. es

)Szaka	e Vol	(Ages (NIM))šm	pedanco	of W	ter.	Total	H.P.
Pulls	g=	Π	,┌	\prod	_ -:	£ 2	100	Ţ *
	6 - X		2 8		. 취 또		ă le le	18 2 8

(9) Plot the following curves-

From obs. 4 between voltage V as abscisse with speed Λ and W as ordinates.

From obs. 5 between frequency f as abscisse with speed A and W as ordinates.

From obs. 6 and 7 between loads H_1 as abscisse with values of Σ , cos ϕ , H_1 and A as ordinates.

From obs. 8 between speed as abscissa with values of Σ and H_1 as ordinates.

From obs. 8 between torque as abscisse and values of speed and Λ as ordinates,

Inferences,—State clearly all that can be deduced from the tabular results and curves.

(106) Relation between the Field Excitation and Armature Current, or the "V" and other Curves, of a Synchronous Alternating-Current Motor Running Light or at Constant B.H.P.

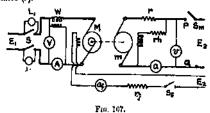
Introduction.—All alternators, whether single or polyphase, are reversible machines, and will run as motors synchronously with the periodicity of the A.C. supply to their armatures, the field system being in all cases supplied with a separate source of direct current.

Synchronous motors are, however, not self-starting, for at every succeeding rapid reversal of the A.C. supply, the armature coils receive equal impulses but in opposite direction, and hence there is no resultant torque. If, however, the motor is first started up and run by some other driving source of power, at such a speed that any armature conductor passes through the distance between the centres of two poles (i.e. the pitch) in half the periodic time of the A.C. supply, then on switching it on to the supply it will continue to run as an efficient A.C. motor in dead synchronism with the supply frequency, irrespective of load, so long as this is not sufficient to pull it out of step with the supply current.

A single-phase synchronous motor therefore develops an alter-

nating armature polarity and torque which reverses with the rapidity of reversal of the A.C. supply, thus producing unidirectional rotation. On the other hand, the currents in the phase windings of a polyphase synchronous motor combine so as to form a constant polarity of fixed position relatively to that of the field, so causing a unidirectional torque and rotation.

Apparatus.—Sources of A.C. supply E_1 to synchronous motor M, and of D.C. supply E_2 to starting motor (m) and field of M; switch S_1 lamps L_1L_2 ; A.C. anometer A, voltmeter V, watereter V; D.C. anometer a, voltmeter v. Field anometer a_n , rheostats xh and xh switches S_f and S_{20} , with starter or main variable resistance (r).



Note —The lamps L_1L_2 should be stamped for a voltage, each equal or even 10% higher than that of M, so as to avoid burning them out while synchronising.

- Observations.—(1) Connect up as shown in Fig. 107, levelling and adjusting to zero such instruments as require it. On starting the machines, see that their lubricating arrangements are working properly.
- (2) The Synchronising or starting up of the A.C. motor under test can be effected as follows: with S and S_r open and (r) off, if a starter, or "full in," if a variable rheostat, close S_m and operate (r) so as to start the machines up to about the normal speed of M; now close S_r and adjust r, rk and r_r until V indicates the same voltage as that of the supply E_r , and the lamps L_1L_2 coase to blink and go out definitely with a slow period. At this moment close S and open S_m when the A.C. machine M will continue to run as a synchronous A.C. motor at a speed entirely governed by, and directly proportional to, the supply frequency.

Note.—At the above moment of closing S_i the back E.M.F. (V) of M will be not only practically equal to, but also exactly opposite in phase with (i.e. differ by 180° from), that of the amply E_i .

The starting up may also be effected by one of the special forms of synchroniser now made for the purpose, e.g. the rotatory type or synchroscope of Mersrs. Everett, Edgcumbe & Co., the characteristics of which are as follows: with the supply and the motor connected to the respective pairs of terminals on the synchroscope, the speed and field of M are adjusted until the frequency of M = that of the supply (indicated by the rotating pointer coming to rest), and the voltage of M is equal and opposite in phase to that of the supply (indicated by the pointer taking the vertical position); under these conditions, the dial will show a white light and S can be closed. Briefly, therefore, close main switch when pointer stops vertically and white light shows. If M is running too fast, the pointer rotates clockwise and a red light shows, whereas if M is running too slow, the pointer rotates counter-clockwise and a green light shows.

Two- and three-phase machines are synchronised by the same single phase instrument with its 2 pairs of terminals connected across any one phase, either side of the main switch contacts of that particular phase. With the motor *M* under test running synchronously with the A.C. supply, the following very interesting and important investigations can be made, namely—

- (3) With S_m open and r and rh "full in," M will (unless coupled to and released from m by an electro-magnetic clutch) simply be turning it against the small windage, brush, and braving frictions, and will therefore practically be running light itself. For this no-lead condition at normal supply frequency and voltage adjust r, to obtain minimum reading on A, and note simultaneously that of V, W, a, and the speed.
- (4) Next vary r_{ρ} and hence the exciting current (a_{ρ}) , by a series of steps, above and below the value found in obs. 3, as will raise A to a value not acceeding 25% ever load, in each case noting V, W, a_{ρ} A and the speed at each excitation. The supply voltage V and frequency being kept constant throughout at the value of obs. 3.
 - (5) Repeat obs. 3 and 4 for constant B.H.P. load outputs

from M of say $\frac{1}{4}$, $\frac{1}{4}$ and full load respectively at the same constant supply volts and frequency, taking that value of a, giving minimum main current A as the starting point of the "up and down series" of $\{a_i\}$.

Note.—The brake load can most conveniently be taken up electrically in the coupled D.C. starting motor m by causing it to act as a D.C. generator and send current through a suitable current rheostat to be connected in series with a switch (neither shown in Fig. 107) across the points P and Q. In this case (r) must be short-circuited and special precaution taken to keep S_m open.

The product v.a = the power absorbed in the added rheostat, and, if the efficiency of M is known, the actual B.H.P. developed by M is at once obtainable, otherwise with constant excitation of (m), the power absorbed by it will be roughly ∞ to the currents (n) developed, and therefore to the B.H.P. given by M. Tabulate all results as follows—

, Bupply,	Armalure.	tor hase	.D.G.	M	C. Blast itus as lo	hg ad_
Frequency f Voltage F. Excline Amp	Apparent Watte AP. True Watts	Power Tart cos \$4 = 16/2 Angle of Ph Difference	Epeed in r.p	Volts v.	<u>.</u>	2 × 1 × 1

(6) Plot curves for running light and for each load on M having (1) amps A, (2) power factor (cos φ), and (3) watts W as ordinates with exciting current (a_i) as abscissue in each case.

Inferences.—From a careful study of the shapes of the curves and of the tabular results, state what can be deduced. from M of say $\frac{1}{4}$, $\frac{1}{4}$ and full load respectively at the same constant supply volts and frequency, taking that value of a_f giving minimum main current A as the starting point of the "up and down series" of $\{a_j\}$.

Note.—The brake load can most conveniently be taken up electrically in the coupled D.C. starting motor m by causing it to act as a D.C. generator and send current through a suitable current rheostate to be connected in series with a switch (neither shown in Fig. 107) across the points P and Q. In this case (r) must be short-circuited and special precaution taken to keep S_m open.

The product v, a = the power absorbed in the added rheostat, and, if the efficiency of M is known, the actual B.H.P. developed by M is at once obtainable, otherwise with constant excitation of (m), the power absorbed by it will be roughly ∞ to the currents (n) developed, and therefore to the B.H.P. given by M. Tabulate all results as follows.

Supply.	Armalure.	Factor H/A F. Phate nee \$.	12.00	J.	C. Blasting Little as load.
Frequency Voltage ? Excling	Amps. A	Powers Cos do — Angle of Different	Ppeed in	Yolts e.	Anpr. c. B.H.P. of

(6) Plot curves for running light and for each load on M having (1) amps A, (2) power factor (cos φ), and (3) watts W as ordinates with exciting current (a_i) as abscissne in each case.

Inferences.—From a careful study of the shapes of the curves and of the tabular results, state what can be deduced.

(107) Efficiency and B.H.P., with other Characteristics, of a Synchronous Motor run from a Constant Voltage and Frequency Supply at Constant Excitation.

Introduction.—In view of the peculiar relations existing between the excitation and other factors as determined in the last test, and the use of the synchronous machine for raising the average working power factor of a supply system, it is both interesting and important to see what effect load has on the same factors. This is apparent when determining the efficiency-lead curve of the machine in the present test.

Apparatus.-Precisely that for test, No. 106,

Observations.—Carry out obs. 1, 2, and 3 of test, No. 106, exactly 49 stated.

(4) With the supply voltage V and frequency f each kept constant at the normal value for the motor M, and with the creitation (a_i) kept constant at the value noted in obs. 3 (namely that giving minimum armature current A), take a series of brake loads on M rising by about equal amounts up to about 25% over load, noting the readings of V, W, a_i , A speed, and output factors at each lead.

Note.—As the heating of a machine is the factor limiting the maximum safe output, it is desirable to estimate the brake leading by roughly equal amounts of main current A up to about 25%, or even 50%, over load if kept on only a few minutes, calculating and taking the B.H.P. corresponding to such current values. The method of leading the motor M may be that indicated in the Note, obs. 5, test No. 106.

- (5) Repeat obs. 4 for two or three higher—and two or three lower—constant values of excitation (a_i) than that used in obs. 4 above, which gave minimum value of A_i and tabulate as per schedule shown on page 308, but adding one extra column for efficiency $\left(=\frac{B.H.P. \text{ output}}{E.H.P. \text{ absorbed}}\right)$ of M at each load.
- (6) Plot the following curves, namely, having in every case B.H.P. outputs as abscissae with (1) efficiency, (2) amperes A, (3) watts W, or E.H.P. absorbed, and (1) $\cos \phi_i$ as ordinates respectively.

Inferences.—From a careful study of the figures and also of the shape and relative dispositions of the curves, state what can be deduced.

Relations between the Supply Factors of an Alternating Current and the Constants of the Circuits supplied.

General Remarks.—Every electrical circuit possesses three distinct qualities, namely—

- (i) Electrical—or chanic resistance, depending on the length, sectional area and material of which it is made.
- (ii) Electrical—or electrostatic capacity, depending on the length, surface, form and the specific inductive capacity of the surrounding dielectric.
- (iii) Electrical—or self-inductance, depending on the shape, form and magnetic permeability of the surrounding conducting material.

All of these qualities are always present in every circuit whatsoever, but it may happen that one or more of them are so small as to be negligible from a practical point of view. Thus we are accustomed to speak of some special circuit as possessing only one of them, any two, or all three of them at once. It is often of the utmost importance to know the nature of a circuit, with reference to the above qualities, when alternating currents are employed, for the presence of one or more of them in such a circuit may be very troublesome or may be a necessity according to circumstances. Theory dictates that variation in the periodicity of the alternating supply causes, in some cases, a considerable change in the working results of a circuit, and it is with a view to clearly elucidating the effects of variation of frequency on circuits in which one or more of those qualities predominate that the following tests have been devised, and also of determining how such variations affect the power absorbed in the circuit, and also the corresponding variation of temperature (if any). In all cases the power is to be measured by a Wattmeter as nearly noninductive as it is possible to have it, for it will then give a true measure of the power absorbed. The results to be expected, as dictated by theoretical considerations, are as followsLet $A = \sqrt{\text{mean sq.}}$ value of current in amperes flowing in the circuit.

 $V = \sqrt{\max sq.}$,, voltage acting on the circuit.

R = ohmic resistance of the circuit.

L = its self-induction in honries.

C= its electrostatic capacity in farads or $C \times 10^6$ microfarads. p= the angular velocity of the alternating supply = $2\pi \times 10^6$

frequency.

Then we have for circuit possessing--

R only:—
$$A = \frac{V}{R}$$

and the current is in phase with the voltage.

R and L only (in series):
$$-A = \frac{V}{\sqrt{(L_F)^2 + R^2}}$$

the current now lagging in phase behind the voltage by an angle θ such that tan. $\theta = \frac{Lp}{R}$.

R and **C** only (in series) :—
$$A = \sqrt{\frac{1}{(\frac{1}{1+\alpha})^2} + R^2}$$

the current now leading in phase in advance of the voltage by an angle θ such that $\tan \theta = \frac{1}{UpR}$.

R, L, and **C** (in series)
$$c - A = \sqrt{\left(Lp - \frac{V}{Cp}\right)^2 + R^2}$$

where L predominates over C, the current now lagging in phase

behind the voltage by an angle
$$\theta$$
 such that $\tan \theta = \frac{Lp - \frac{1}{Cp}}{k}$

where C predominates over L, the current leads in phase in front of the voltage by an angle θ and the last two relations become—

$$A = \frac{V}{\sqrt{\left(\frac{1}{Cp} - Lp\right)^2 + R^2}} \quad \text{and tan } \theta = \frac{1}{\frac{Cp}{R}} - Lp.$$

$$C \text{ (only)} := A = \frac{V}{1} = C_V V_*$$

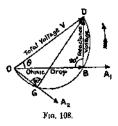
the current now being 90° in phase in advance of the voltage.

$$\mathbf{L} \text{ (only)} := A = \frac{V}{Lp},$$

the current lagging 90° in phase behind the voltage.

$$\frac{V}{A}$$
 = Impedic Resistance,

The radical denominators in the three expressions for A are termed the apparent or effective resistances of the circuit containing those particular qualities, though one of these, namely $\sqrt{L^2p^2+R^2}$, is very generally termed the impedance of the circuit. The terms Lp, $\frac{1}{Cp}$, and $\left(Lp-\frac{\eta}{Cp}\right)$ are called the reactances or reactive resistances of the circuit, and when multiplied by the current give the reactance voltage. The phase relations are shown by the vector diagram OBD, Fig. 108, and



if each voltage is \div by the current we shall get a proportionate Scalar diagram (i.e. without arrows) in which OD = apparent resistance, OB = ohmic resistance, and BD = reactance or inductive resistance, while OA = the current. It will now be obvious that if the ohmic resistance is extremely small (for it cannot be zero) the impedance becomes = the reactance, but when the ohmic resistance is large, the impedance is affected by it considerably. Again, since the term for reactance contains p=2 π × frequency, it is directly ∞ to frequency, while ohmic resistance is independent of frequency.

Further, impedance depends on the remaining component factor, namely, self-induction, which latter in most cases is due to a coiled circuit surrounding iron. Now, the self-induction of a circuit depends on the linkage of turns with magnetic field, increasing directly with the latter and with the square of the former, Thus it depends on the current, which in turn decides the degree of magnetic auturation of the core. The self-induction of the armature of an alternator is really only an average of several values obtained for different positions of the armature coils relatively to the field poles, and it affects the "wave form" of the voltage generated. Since the self-induction L is directly at to the mean permeability (μ) of the magnetic circuit, it follows that in cases where R is small compared with the Lp, the impedance will vary nearly in direct proportion to μ_i consequently a curve between impedance and current will approximate to the orthodox permeability curve of the core.

On the other hand, with a low resistance winding, the voltage absorbed in it, due to the term AR, is so small that the voltage at the terminals is practically that due to self-induction only, and hence directly α to the core flux. Thus a curve between terminal voltage and current will have the shape of that part of the magnetization curve between the origin and "knee," the higher parts of the curve being absent owing to the low degree of magnetic saturation used in the cores of A.C. plant.

Turning now to considerations relative to capacity, the fundamental definition of an electrical condenser being that of two conductors (called the coatings), separated by an insulator (called the dielectric), it follows that on connecting the coatings to a source of E M.F., positive and negative quantities of electricity will flow on to them in raising them to the same difference of potential as that of the source. The attraction between these two quantities sots up a corresponding stress in the dielectric and causes them to remain "bound" after the charging source is removed. The charge of the condenser is measured in coulombs, and is the quantity Q (which = the current in amps \times time of flow in seconds) necessary to raise the voltage between the coatings to the value V of the source. Thus, if C denotes the capacity of the condenser, we have Q = CV, or the capacity $C = \frac{Q}{V} = \mathbf{a}$ constant for any condenser and for all charging

circuit which is not constant, when containing magnetic material, but varies with the magnetic saturation of the core, and hence with the current. If the source of E.M.F. is an alternating one, the state of charge of the condenser will follow exactly the change of voltage, reaching a + " and - " maximum, each once

in every period of the supply. While, therefore, the current flowing in an A.C. circuit containing a condenser is actually a charge and discharge current alternately, and does not flow continuously through, owing to the impassable dielectric insulation, an A.C. ammeter placed in the same circuit, by its steady reading and inability to follow the rapid pulsations of current, makes it appear as if the current really passed through the condenser, though it does not do so,

Again, the internal or ohmic resistance of a self-inductance affects the corresponding impedance, while the internal resistance of a given condenser has no such effect on the corresponding impedance. From the relation already given for the current in amperes $A = C_p V + 10^6$, where C = the expacity in micro-farads and V = terminal pressure in volta it will be seen that at the smaller pressures of 100 volts or so at about 50 ~ per sec., a considerable value of (C) will be needed to give an appreciable current. Since, therefore, the capacity available is usually well under 110 mfd.s, only a small current will result. In this case, care should be taken that the voltmeter used does not affect

The tests which immediately follow are arranged to show the variation of the quantities indicated with the factors composing them, only one of which must be varied at a time in order to test its influence on the main quantity,

the voltage across the points between which it is applied, a condition fulfilled by the use of an electrostatic voltmeter.

(108) Determination of whether a Resistance is truly Non-Inductive at any Frequency and Current.

Introduction.—As in nearly all laboratories there is usually a shortage of rhoostats, more particularly those of a non-inductive nature, which are essential in the majority of A.C. tests, the present determination is both instructive and useful.

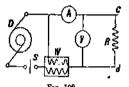
It is obvious that any inductive resistance must possess some chimic resistance, while a so-called olimic resistance usually exhibits some slight inductiveness. Carbon plate, liquid and glow-lamp rheostals are usually taken to be non-inductive for all practical purposes, which they are, especially the two first named. Since carbon filament lamps are usually employed in lamp rheostats in pure parallel combinations, the inductiveness of one lamp with its filament of one or more turns is finite though very small, and hence that of any combination is still smaller and practically nil.

Liquid rheostata usually consist of two or more metal plates dipping into a container of water, the conductivity of which is increased to any desired extent by the addition of a little common washing soda or aluminium sulphate. Such rheostats are undoubtedly less convenient than the carbon or lamp types, because, although electrolytic action with A.C. is negligible, they froth and alter in resistance considerably with rise of temperature, due to the absorption of the power in them.

Wire-wound rheostats, whether composed of wire spirals wound in a continuous spiral or non-inductively, are usually preminent in most test rooms. How far such rheostats, whether wound with high-resistance alloys (usually non-magnetic) or with iron (which is highly magnetic) are non-inductive, is the object of the present investigation. With the former, the self-induction would be constant for all current densities, but would vary with the frequency. Further, the effective or apparent resistance increases for increase of cross-sectional area of wire with alternating current, and the self-induction varies as the (number of turns) ² × sectional area of spiral — length of spiral.

Apparatus.—Alternator D, capable of being driven at a wide range of speeds, so as to obtain a corresponding range of frequency at constant voltage V by varying the exciting circuit (not shown); Siemens electro dynamometer, hot wire or other A.C. nameter A unaffected by frequency; electrostatic voltmeter V; non-inductive wattmeter W; switch S, and resistance R to be tested.

Observations.—(1) Connect as in Fig. 109, and adjust all the



instruments to zero. Then start D, seeing that the lubricating arrangements feed properly.

(2) By field regulation adjust the voltage V across the terminals of R, that a con-

venient current flows through it as indicated by A.

- (3) Obtain about ten or twelve different speeds of *D* from the smallest to the largest practicable and safe, varying the excitation so as to keep *A* constant throughout. Note simultaneously the readings of *A*, *V*, *W* and speed.
- (4) With the speed, and hence the frequency adjusted to some convenient value to be kept constant, vary the voltage by field regulation so as to obtain 8 or 10 different currents through R between 0 and maximum safe value, noting the readings of A, V, W, and speed at each, and tabulate your results as follows—

Naux . . . Alternator; Periods per Revolution K = 1

Constants: Wallmeler . . . and d . . .

Dava . . . Resistance $R=\dots$ ohne. Neture of Resistance R

Breel Frequency Rata Per sec. Vol.		Анця. Фд.	Time Writs #1 = #1 F,	Apported Walts n _A F.	d _A ² R.	<u>y</u>	Cot #	r.
--	--	--------------	----------------------------------	----------------------------------	--------------------------------	----------	-------	----

(5) Plot ourses having values of F and a_A as abscisse in each case, and V_A cos θ , and $\frac{V}{a_A}$ as ordinates.

Inferences.—State clearly all that you can deduce from your experimental results and your curves.

(109) Measurement of Power Factor in Alternating Current Circuits.

Introduction.—Alternating-current ammeters and voltmeters measure the mean or average value of the current or voltage in

Fic. 110.

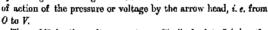
an A.C. circuit, and the product of their readings is, therefore, the product of two mean values. If the circuit is non-inductive, this product of the mean or average values is the true mean or average value of the power in watts given to the circuit. If the circuit is inductive and possesses self-induction or capacity or both, the above product does not give the true mean power, but only what is commonly called the volt-amperes of apparent power in watts. The true mean or average power in this case is given by the mean or average value of the product (amperes × volts) in the circuit, for the mean product of two periodic functions representing current and pressure is not equal to the product of their mean values.

Now, the mean value of the product, which thus represents the true power in watts, can be measured directly by a wattmeter, and the ratio

true power in watts apparent power in watts amps. X volts

is called the power factor of the circuit, which in practice can vary only between the two extreme values 0 and 1.

This limiting variation, together with the difference observed between the true and apparent power in watts in an inductive circuit, is explained by the fact that the current and voltage in such a circuit are not in phase, as will be understood by a reference to the so-called vector diagram (Fig. 110). Let the voltageter reading be represented in magnitude (on some convenient scale) by the length of a straight line OV and the direction



Thus ∂V is the voltage vector. Similarly let ∂A be the current vector for the ammeter reading, differing in phase from ∂V by an angle ϕ .

Now OA can be resolved into two component currents at right engles to one another—the one Oa in line with OV, the other (Ob) at right angles to it. Then Oa is called the useful energy or load-current, and Ob the useless, idle, or wattless-current, connected solely with the periodic charge and discharge of energy in the circuit due to its inductance OaA is therefore

a triangle of currents for the inductive circuit in which OA is the resultant (or animeter current) of two other currents, namely, an energy current Oa and an idle current aA always differing in phase by 90° . Then the product of the animeter and voltmeter readings = $OA \times OV$ = the apparent watts, the wattmeter will give a reading = $OV \times Oa$ = the true, or useful, watts, while the wattless power will be given by $OV \times Ob$ watts, which does no work in the circuit.

Thus from the geometry of the figure we have the ratio

true watts
$$\frac{\partial V \times \partial a}{\partial \Gamma \times \partial A} = \frac{\partial a}{\partial A}$$

= cos ϕ = the power factor of the circuit.

Although obtainable in other ways (vide p. 381), this ammeter, voltmeter, wattmeter method is by far the best and most direct one for measuring power factor, and is almost invariably employed.

The evaluation of the power factor $\cos \phi$ in the case of single, two, and three-phase A.C. inductive circuits, by this direct method, is given on p. 388 et seq, and in the following test we shall restrict ourselves to single-phase circuits.

Apparatus.-Precisely that detailed for test No. 111,

Observations.—(1) Connect up as in Fig. 112, levelling and adjusting to zero such instruments as need it. The extremities T_1T_2 of the combination of C and r are the terminals of the circuit of which the power factor (P.F.) is required. As, however, it is sometimes necessary in A.C. testing work to obtain either an electrical load at varying P.F. or a variable load at constant P.F. with a choker and resistance, it is both useful and instructive to determine the effect on the value of the P.F. of changing (A) the obnuc resistance, (B) the inductance (whether by change in current strength or in disposition of magnetic circuit), and (C) the frequency—one at a time.

- (2) A.—Note the readings of all the instruments, for each position of the two-way key K, for some eight different values of (r)—the frequency F and current A being kept constant throughout.
- (3) B.—Note the readings of all the instruments, for each position of the two-way key K, for some eight different values of current A, covering the range of current utility of the circuit

or appliance in use—the frequency F and resistance r being kept constant throughout.

(4) C.—Note the readings of all the instruments for each position of the two-way key K_1 for some eight different values of frequency F—the resistance r and current being kept constant throughout.

Tabulate all your results as follows-

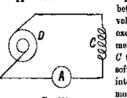
Ohmic Resistant	T	Γ	For	Induct	ive Cin	ant XZ	Por	Non-Ire	lacting (пешь ХР
Non-Industry $r = \frac{r}{A}.$ Total $RT = R + r.$	Current A.	1'requancy P	Value F.	Apparent Watta	True Watta	Power Partuif	Volta Fr.	Apparent Waits	True Watta	Power Factor

(5) Plot curves having values of power factor $\frac{n}{A}\hat{P}$ as ordinates, with values of R_T in obs. 3; current A in obs. 3; and frequency F in obs. 4—respectively as abscisso in each case.

Inferences.—State clearly all that can be deduced from the tables of results and the curves.

(110) Determination of the Effect of Frequency on the temperature of a given Circuit containing Self-Induction and Ohmic Resistance only.

Introduction.—The present test is devised with a view to ascertaining whether change of frequency materially alters the temperature of any appliance possessing self-induction and oldmic resistance, and for the success of the investigation the coils of the appliance used should have a low ohmic resistance, so that transference of heat due to the term C^2R to the core in which any alteration of temperature is to be observed, may be as small as possible.



Fra. 11).

Apparatus.—Alternator D capable of having its speed varied between wide limits, and whose

voltage can be regulated by the exciting circuit (not shown); ammeter A (Fig. 251); hollow solenoid C to test, having a bundle of fine soft iron wires, smaller than the internal hollow, to allow of a ther-

mometer being inserted as well as the bundle.

Observations.—(1) Connect up as in Fig.111, and insert the core and thermomotor in the solenoid, covering up the ends with cotton wool to prevent external cooling effects due to the air, etc. Note the temperature when steady.

- (2) Adjust the speed and excitation of D so that the frequency has the lowest value practicable, and the current A some convenient value not high enough to heat the coils much.
- (3) The speed and current A being kept constant, take the temperature T on the thermometer at successive noted intervals of time (t) from switching on until it remains constant, and note also the temperature of the room at intervals.
- (4) Repeat 2 and 3 for the maximum speed allowable, and for one intermediate between this and the first-named, the core having been allowed to cool down in between each distinct set of observations, and the current A being the same. Tabulate your results as follows—

NAME	Date
Nature of Call lesion Periods of alternator per Royal, K =	Form of Cure
Portous di atternator per 10000. A	

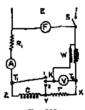
Temperature of Rooms of Curv for blatt Time from start Bleed Roys, per son. Temperature of Curv for blatt Time from start Leg min. Temperature of Curv for blatt Time from start Leg min. Temperature of Curv for blatt Time from start Leg min.		COLA TOL DIVER	Time from start	Bjited Rova, per min, H.	
---	--	----------------	-----------------	--------------------------------	--

(5) Plot a curve for each frequency on the same sheet, having temperatures T C. as ordinates, and (t) minutes as abscissæ.

Inferences.—What can you infer from your experimental results and the curves?

(111) Variation of Impedance with (a) Self-Induction, (b) Frequency, and (c) Ohmic Resistance in Circuits having Self-Induction and Ohmic Resistance only in Series.

Introduction.—In this test it will be necessary to vary one factor only at a time, keeping the remaining two constant. It should also be remembered that, as the coefficient of self-induction of any coiled circuit is the number of lines of force linked with it when unit current flows through it, any change in the current will alter the permeability of the magnetic path when this is composed partly or wholly of magnetic material, and hence also the self-induction. With an air-core the self-



Fic. 112.

induction will be constant for all values of current. The variation of impedance and solf-induction of an iron-cored solenoid with the position of the core has already been investigated in test No. 118, and the present determination can be conveniently made for fixed positions of the core P (Fig. 123).

Apparatus.—Source of A.C. supply E, preferably a motor-driven alternator, the excitation and speed of which are independently variable within wide limits; switch S; frequency meter F; ammeter A; voltmeter V; wattmeter W; two-way key K; two non-inductive variable rheostats R_1 and r (e.g. banks of lamps or carbon-plate rheostats); solenoidal choker C with movable iron core.

Note.— R_1 is needed (only if the supply E is from town mains) for keeping the current A constant, as r is varied. T_1T_2 are to be taken as the terminals of the impedance.

Observations.—(a) Impedance with Self-induction at Constant Frequency and Ohmic Resistance.

(1) Connect up as in Fig. 112, levelling and adjusting such instruments to zero as need it. Start the alternator with field regulator "full in," and see that the lubricating arrangements are working properly.

Note.—The following tests, Nos. 2 and 3, can be made on a public A.C. supply instead, if desired.

- (2) With the core P clamped centrally in the coil C, and the speed adjusted to give a frequency F (= no. pairs of poles \times revs. per min. \div 60) of 50 \sim per sec., close S, and by field regulation obtain some eight different currents on A, rising by about equal increments from 0 to the maximum safe value for
- frequency F and resistance r being constant throughout.

 (3) Readjust the field regulator to "full in," and with the core P removed altogether, repeat 2 for the same constant frequency and range of currents

the coil C, and note the readings of F, A, IV and V at each, the

- frequency and range of currents.

 (b) Impedance with Frequency for Constant Self-induction and Ohmic Resistance.
- (4) Fulfil obs. 1 above; a variable speed alternator now being a necessity.
 (5) With P clamped contraity, adjust the speed and conse-
- quently the frequency F to the lowest convenient value, and the current A (by field regulation) to, say, half the maximum value for the coil, to avoid much change of chinic resistance by heating. Note the readings of F, A, W and V at each of some eight different values of F between the lowest and highest convenient, obtained by speed regulations, the above value of current A being kept constant throughout by field regulation.
- (6) Repeat 5 with the core removed altogether, and for the same constant current, and tabulate all the results of obs 2 to 6, as shown.
- (c) Impedance with Ohmic Resistance for constant Self-induction and Frequency.
- (7) With the core of C clamped centrally and a constant frequency F of, say, 50 ~ per sec. adjust the current A to about half the maximum safe value for C (to minimize heating) and keep it constant throughout (by varying R₂ with town.

supply for E or by field regulation with an experimental alternator for E) for some eight different values of r between 0 and the highest convenient, noting at each the readings of F, A, W and V, when the latter is connected by K across T_1 , T_2 and r respectively.

(8) Repeat (7) with the core of C removed altogether for the same current and frequency, and tabulate as follows.—

Cort (C): Longth = Secti	No. of turns =	Resistance (#) =	obme.
Non-inductive Resistance (r)		p = 2xF =	

Yultage across	Ohnic Restance	
Core C. Core Care Core C. Core C. Core C. Core Core Core Core Core Core Core Core	इ	MALE MALE MALE MALE MALE MALE MALE MALE
Choke Choke	1 85 2 4	Ower Colors
E SE SE SE	, A	William Kari

(9) From obs. 2 and 3 plot curves having values of impedance, as ordinates, with values of A, L, and Lp as abscisse in each case; also between V and L as ordinates and A as abscisse.

From obs. 5 and 6 plot curves having values of impedance, as ordinates, with values of F and (Lp) as abscisse.

From obs. 7 and 8 plot curves between impedance as ordinates and R_x as abscisse,

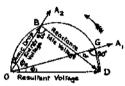
Inferences.—From a careful study of the tables of results and forms of curves state clearly all that can be inferred therefrom,

(112) Numerical and Phase Relations between the Voltages and between Voltage and Current in Circuits containing Capacity only and when in Series with Ohmic Resistance.

Introduction.—The numerical relations between the various voltages in a circuit such as is now under consideration, seem at first sight to be so impossible that it is necessary to consider them in relation to phase. This can be done by a reference to the vector diagram (Fig. 113). In this, the total or resultant

voltage, as indicated on the animeter A_i is set off in magnitude and direction = OD. The energy voltage or olimic drop OG is set off at an angle ϕ_i in advance of OD, while GD will be the condenser, idle, or reactive voltage in magnitude and direction.

Comparing this with Fig. 108 for a self-inductive circuit, we see that capacity causes the current and its vector OA_1 to lead in front of the voltage OD by an angle ϕ_D instead of to lag behind as shown in Fig. 108 for self-inductive circuits, both diagrams being supposed to rotate about O in the $+^*$ -direction (counter-clockwise). The angles B and G being right angles, lie (by geometry) on a semicircle, which is consequently the loci of the point of intersection of the energy and reactive voltages (which always differ by 90° in phase) between their limiting



F16. 118.

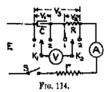
values of resistance R and capacity C respectively, namely, that of $R=\max$ namely with C=0, for which $\phi_1=0$, OG=OD, and GD=O; and that of R=O with $C=\max$ namely, for which $\phi_1=90^\circ$, GD=OD, and OG=O. If for the triangle of voltages OCD we divide each of the voltages by the current A_1 , the sides will represent the corresponding resistances in circuit while the voltage vectors, as given if divided by these resistances respectively, will give the triangle of currents. The idle or wattless current equals A_1 sin ϕ_D and the energy current equals A_1 cos ϕ_D .

Apparatus.—Source of A.C. supply E of, say, constant frequency, such as town mains; switch S; variable non-inductive resistances r and R; ammeter A; electrostatic voltmeter V; two two-way keys K_1K_4 ; condenser C.

Observations.—(i) Connect up as in Fig. 114, levelling and adjusting to zero A and V, if necessary.

(2) With R adjusted to O close S, and by varying R obtain

some six or eight values of current A, rising by about equal increments from O to the maximum possible, noting the values of V_1 , V_2 , and V_3 on V by means of K_1 and K_2 .



Note.—A convenient form of non-inductive resistance to use for R would be an 8 C.P., 16 C.P., and 33 C.P. glow-lump, each of the same voltage as that of the supply, and arranged so as to be paralleled in any combination, thus giving seven possible different resistances of wide range. Tabulate your results as follows—

Capacity used Non-Ind Res				Presp ancy (c	mfds. √ per acc.		
Supply Fa	Condenser we lide voits (AjugC) w	Non-Inductive Resistance = changy volts (AB)	Ainje.	Ohmic Resistance $R = \frac{V_2}{A}$.	Impudance Pa	Power Rector cos $\phi = V_{2}/V_{2}$	Angle of Lead \$.

(3) Plot curves having values of V_2 , as ordinates, with V_2 and C as abscissæ respectively. Also between $\cos \phi$ and impedance, as ordinates, with values of R as abscissæ. Compare V_3 with the algebraical sum $(V_1 + V_2)$.

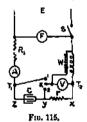
Inferences.—State clearly all that can be deduced from your results.

(113) Variation of Impedance with (a) Capacity, (b) Frequency, and (c) Ohmic Resistance in Circuits having Capacity and Ohmic Resistance only in Series.

Introduction.—While the term impedance is applied almost universally to denote the apparent resistance of an alternating current circuit containing self-induction and ohmic resistance only, it is also used here to denote the expression $\sqrt{1/C^2p^2+R^2}$ for the apparent resistance of an A.C. circuit having capacity (C) and ohmic resistance (R) only, the angular velocity p of the current being $= 2\pi \times \text{frequency}$. As therefore it contains three variable factors, it will be necessary to vary one only at a time, keeping the remaining two constant.

When C and p are respectively the variables, we may make R=0 and determine the effect of each on the remaining term, $\sqrt{\frac{1}{C^2p^2}}=\frac{1}{Cp}$, called the reactance or reactive resistance of the circuit.

Apparatus.—Source E of A.C. supply, preferably a motordriven alternator, the speed and voltage of which can be varied



within wide limits; animeter A; voltmeter V; wattmeter V; frequency meter F; switch S; variable capacity C; variable non-inductive resistance r; two-way key K; variable non-inductive rheostat R_1 (only needed if E is town mains).

Observations.—(a) Impedance with Capacity at Constant Frequency and Ohmic Resistance.

- (1) Connect up as in Fig. 115, levelling and adjusting to zero such instruments as need it. Start the alternator with field regulator "full in," and see that all lubricating arrangements in use are working properly.
- (2) With the alternator up to maximum speed, and therefore giving maximum frequency $F' (= \text{No. of pairs of poles} \times \text{rev. per min.} + 60)$, close S, and adjust C to some six or eight different capacities, rising by about equal increments from the smallest to largest available, noting the reading of F, A, C and of W and V
- on K_1K_2 at constant frequency F and resistance (r).

 (3) With r = 0 repeat obs. 2 for the same values of C, noting W and V on K_1 , in addition to F, A, C, for the same constant frequency.
- (b) Impedance with Frequency for Constant Capacity and Ohmic Resistance.
- (4) A variable speed alternator being available, make C a maximum and give r some convenient fixed value. Now read all the instruments for both positions of K at each of some six or eight frequencies differing by about equal amounts between the maximum and minimum values obtainable by speed regulation.
- (5) With r = 0 repeat obs. 4 for the same constant value of C and range of frequencies.
- (c) Impedance with Ohmic Resistance for Constant Capacity and Frequency.
- (6) Give C and the frequency their maximum possible values, and take the readings of all the instruments with K on study 1 and 2 for some six or eight values of r, differing by about equal amounts between maximum and zero values.

Tabulate all your results as follows (where $p = 2\pi f$)—

Amps. A. Amps. A. Capacity C. Capacity C. Volta serves Tulys arryst Noll's	Westenson Westenson Type olive Type olive Westenson Westenson Westenson Westenson Westenson Westenson Westenson Appearance Appearance Zower Factor Con 4 = Wydey Angle of Jag 6.
---	---

(7) From obs. 2 and 3 plot curves having values of impedance $\left(\frac{V_I}{A}\right)$, reactance $\frac{1}{Cp}$ and amps. A as ordinates with values of capacity C as abscissa,

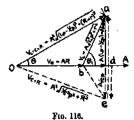
From obs. 4 and 5 plot $\frac{V_{\ell}}{A}$, $\frac{1}{C_P}$ and A as ordinates with

frequency (f) as abscisse, and from obs. 6 plot $\frac{V_I}{A}$ as ordinates with olimic resistance (r) as abscisse.

Inferences.—State clearly all that can be deduced from the above results.

(114) Variation of Impedance with (a) Selfinduction, (b) Capacity, (c) Ohmic Resistance, (d) Frequency in Circuits having Characteristics a, b and c in Series.

Introduction.—It has been stated that self-induction L causes the current to lag behind the voltage, while capacity C causes it to lead in front of the voltage. A circuit possessing both L and C may therefore cause the current to lag behind, lead in front of, or be in phase with, the voltage, depending on the relative mag-

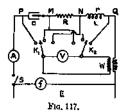


nitudes of L and C for a given olimic resistance and frequency. Each of the two last named will in turn affect such phase relations, and hence in the present investigation we have four possible variables composing the *impedance* or "apparent" resistance of the circuit, only one of which must be varied at a time with the remaining three kept constant.

The phase difference between current and voltage will be less than that which would be caused by the same value of either L or C alone, and, as stated above, may even be zero. The above remarks will be better understood by a reference to Figs. 116 and 117.

Let OA be a vector representing, in magnitude and direction, the current A. Set off Ob = the voltage $V_R (= AR)$, which is an energy or useful voltage in phase with A, along OA.

With centre (b) and radius $ba = V_L$ describe an arc of a circle, and with centre (O) and radius $Oa = V_{L+R}$ describe an arc



of a circle (Fig. 116), intersecting the other are in the point (a). From (a) drop a perpendicular to OA meeting it in (d) and produce it to (s) so that $de = V_e = \frac{A}{Up}$ the condenser voltage. This will be 180° out of phase, i.e. in direct opposition to the voltage overcoming the self-induced idle voltage (ea) = LpA. Consequently the nett or effective idle voltage of the circuit $da = A\left(Lp - \frac{1}{Up}\right) = AL_1p$, where L_1 = the effective or nett inductance of the whole circuit PQ, and is of a self-inductive nature causing an effective angle of lag θ in the circuit. In the triangle Ode, Ar = O, since the condenser C is not considered to have any ohmic resistance r like the self-inductance L has. Therefore Od = the energy voltage AR for the portion PN, Od is therefore also the useful or load component of the total voltage of the circuit PQ.

A most important deduction, affecting the calculation of the

A most important deduction, affecting the calculation of the ries of pressure in cables and sometimes the breakdown of their insulation, now follows, namely, if the reactances of the selfinductive and capacity portions are equal, i.e. if $Lp = \frac{1}{Cp}$ where $p = 2\pi f$ and f = the supply frequency, the idle voltages of L and C will be equal and opposite in sign, and each may have much greater values than that of the supply. This condition in such a

series combination, shown in Fig. 117, is called pressure resonance. The above condition may be written $2\pi f L = \frac{1}{2\pi f \bar{U}}$, from which we get $f = \frac{1}{2\pi \sqrt{L\bar{U}}} \sim$ per sec., but only when the ohmic resistance of the circuit is negligible is the periodicity of the supply equal to the natural periodicity of oscillation. The natural period of the

circuit $\frac{1}{f} = 2\pi\sqrt{LU}$ seconds. The periodicity giving maximum resonance in a circuit of appreciable ohmic resistance R is $f = \frac{1}{2\pi}\sqrt{\frac{1}{LU} - \frac{r^2}{4U^2}}$ which is not the natural periodicity of

oscillation of the circuit.

Either of the above values of the critical frequency (f) giving maximum resonance is usually much greater than that of the supply voltage.

Apparatus.—Source of A.C. supply E, preferably a motor-

driven alternator having a wide range of speed and excitation; ammeter A; wattmeter W; switch S; voltmeter V; and two three-way keys; a capacity C, self-induction L, and ohmic resistance R, each capable of variation; frequency meter (f).

Observations.—(a) Impedance with Self-induction at Constant Frequency, Capacity and Resistance.

(1) Connect up as in Fig. 117, levelling and adjusting to zero such instruments as need it. Start the alternator with field regulator "full in," and see that the lubricating arrangements are working properly.
(2) With the self-induction L, resistance R, and capacity C

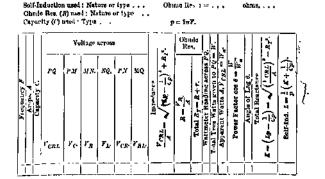
adjusted to convenient values, and the speed to give a frequency F := No. of pairs of poles \times rev. per min. \div 60) of 50 \sim per sec., close S and by field regulation obtain some eight different currents on A (and hence values of L) rising by about equal increments

from 0 to the maximum safe value, noting the values of F, A, W, V and C at each, F, R and C being constant throughout

- (b) Impedance with Capacity at Constant Frequency, Selfinduction and Resistance.
- (3) Repeat obs. 2 for some eight different values of capacity C between 0 and the maximum possible, F, R and A (i. e. L) being constant throughout.
- (c) Impedance with Ohmic Resistance at Constant Frequency, Capacity and Self-induction.
- (i) Repeat obs. 2 for some eight different values of resistance R between 0 and the maximum possible, F, C and A
- (i. e. L) being constant throughout. (d) Impedance with Frequency at Constant Self-induction. Capacity and Resistance,
- (5) Repeat obs. 2 for some eight different frequencies between the minimum and maximum values possible, C_1R and A (i. e, L) being kept constant.

Ohnus Res 1 -- . . .

Tabulate all your results as follows-



(6) Plot curves having values of impedance as ordinates with each of the variables A (or L), C_1 R_{T_2} and F in obs. 2-5 as abscisse on the same curve-sheet,

Inferences .- State clearly all that can be deduced from the results of the test.

Note.-The numerical and phase relations between the voltages across C, R and L, and the combinations of these can

be studied in the above table with advantage and are highly instructive. From them the student should draw to scale the diagram shown in Fig. 116 above, for, say, two extreme values of the overall voltage $V_{\rm CRO}$ and see how the angle of phase difference θ compares with that calculated in the above table.

(115) Numerical and Phase Relations between Main and Branch Currents in Circuits containing Ohmic Resistance in Parallel with either Self-induction or Capacity.

Introduction.—The determination of the above relations between the main and branch currents in a circuit comprising camic resistance and self-induction in parallel is effected in detail in test No. 131, which should be done for the present test.

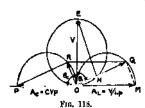
The numerical relations are at once seen in the table of results, while the phase relations are best seen from the diagram (Fig. 142) constructed for any particular set of simultaneous currents. It will be obvious that the relations will differ according to whether the self-induction branch PQ possesses appreciable ohmic resistanceor practically none. Fig. 111 presumes the former condition, but if the latter obtains, then the current A_1 in the non-inductive branch, being in phase with the voltage, will be given by OC, while that in the inductive branch A_2 (having no resistance) lags just 90° behint the voltage, and will now be given by Ca (perpendicular to OC), instead of by ba as in Fig. 112.

The present test should also be operated with capacity C substituted for the self-induction shown, when the student should have no difficulty in modifying both the tabular form of entry and the vector diagram to suit the new condition of capacity in parallel with ohmic resistance. If no resistance is purposely added to the condenser branch, the current in this will lead just 90° in advance of the voltage. Thus, the main or resultant current will be given by the diagonal of a parallelogram, the

sides of which will be at right angles and represent the branch currents.

(116) Variation of Impedance and Phase Relations between the Currents in a Circuit containing Capacity and Self-Induction in Parallel.

Introduction.—The combination of self-induction in parallel with capacity is an extremely important one, and has some interesting and highly useful applications in electrical engineering which will be mentioned later. Referring to Figs. 118



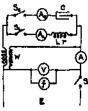
and 119. Let OE = the supply voltage V_i and if the ammeter A_c and switch S_c add a negligibly small resistance to the condenser branch, the current A_o in this branch will = CVp and $\tan \theta_0 = \frac{1}{C \rho r_0} = \infty$, whence A_0 will make an angle of phase difference $POE = \theta_0 = 90^{\circ}$ in advance of Γ .

Similarly, if the chair resistance of the self-inductive branch is negligibly small, the max, current A_L in this branch will $\Rightarrow \frac{V}{Ln}$ and $\tan \theta_L = \frac{Lp}{r} = \infty$, whence A_L will lag behind V by an angle $MOE \Rightarrow \theta_L \Rightarrow 90^\circ$. OP and OM are therefore the max. values of the respective branch currents. If, however, the selfind, branch possesses a resistance (r) ohms in addition to selfind. L, its current will be given by $A_L = \frac{V}{\sqrt{L^2 \mu^2 + r^2}} = 0Q$

lagging behind V by an angle $\theta_L = QOE$, such that tan $\theta_L = \frac{L\rho}{n}$

(less than before). The total current A being the resultant OR of OP and OQ and making an angle $ROE = \theta$ (seen to be one of advance in this case) with the voltage V.

The semi-circles ORP and OQM are the loci of the vectors representing the branch currents A_G and A_D and it will be seen that the smaller the resistance (r), the nearer will Q approach M, and the smaller will be the resultant or main current OR (= A) from the supply and the more nearly will it be in phase with OE (= V).



10, 119,

Thus at the practical limit, r will be very small, Q very close to M, A_L nearly $= A_0$ and nearly 180° out of phase with it, and OR very small and nearly in phase with V. Under these conditions current resonance is said to prevail in distinction to pressure resonance explained on p. 330 for series circuits. With current resonance in such a parallel circuit, the local current circulating in the loop may be many times greater than the main supply current A—a condition obtained when the idle or wattless components of the branch currents are practically equal, but of opposite sign when the wattless or idle component of the main current A will be less than that of either branch. Equal and apposite wattless currents in the branches will be obtained when

$$\frac{1/Cp}{1/C^2p^2 + r_c^2} = \frac{Lp}{L^2p^3 + r^2}$$

but as explained for series circuits this condition can only truly be called resonance when both r_0 and r are negligibly small.

In practice we see capacity used for starting up alternating current motors; for nullifying the effects of the idle currents in a distributing system, thereby mising the power factor, and so increasing both the efficiency and economy of operation. The capacity effect in this case is produced by an over-excited synchronous motor connected to the same supply.

: Apparatus.—Source E of A.C. supply preferably a motor-driven

alternator variable in speed and excitation within wide limits; frequency meter (f); voltmeter V; wattmeter W; ammeters A, A_0 and A_L ; switches S, S_C and S_L ; variable capacity C; variable

self-induction L of ohmic resistance (r).

Observations.—(a) Impedance with Self-induction at Constant
f, C and r.

- (1) Connect up as in Fig. 119, levelling and adjusting to zero such instruments as need it. Start the alternator with field regulator "full in," and see that the lubricating arrangements are working properly.
- (2) With f_i G and r (if alterable) adjusted to convenient values, close S_i and then N_0 only, taking the readings of all the instruments.
- (3) With f, C and r as in obs. 2, close S, and then S_k only and take the readings again.
- (1) With f, C and r again the same, close all 3 switches and by field regulations obtain some 8 different currents on A_L (and hence values of L) rising by about equal increments up to a safe max. value, noting the readings of all instruments.
 - (b) Impedance with Capacity at Constant f, A_L (i. c. L) and r.
 (5) Repeat obs. 4 for some 8 different values of supacity C at a start f a and A_L (i. c. L).
- constant f_i r and A_Z (i. e. L). (r) Impedance with Ohmic Resistance (r) at Constant f_i A_Z (i. o.
- and C.
 (6) Repeat obs. 4 for several values of (r) if this is variable at
- constant f, L and C.
 (d) Impedance with Frequency (f) at Constant A, (i.e. L), C
- (a) Impainted with Frequency (f) in Constant M₂ (i.e. I.), 6 and r.

 (7) Repeat obs. 4 for some 8 different values of frequency (f)
- (1) Repeat one. 4 for some 6 americal values of requency (1) at constant A_L (i. c. L), C and r.
- (8) By varying C, I_n f, find the minimum value of A obtainable, noting the readings of all instruments at this, and tabulate all your results as follows—

Valtage F. Valtage F. Valtage F. Watturker Riesing. True Watta if. Ample: A.c. Cos 6_L = V_L
--

Inferences.—State clearly all the inferences which can be deduced from the above results.

(117) Determination of the Load and Wattless Currents in an Inductive Alternating Current Circuit.

Introduction.—While the present investigation is bound up with that of power factor, considered in tost No. 109, p. 316, the whole subject has such a vastly important bearing on the economical and efficient generation, transformation, and distribution of electrical energy, that a further consideration of it will be an advantage.



Fin. 120.

It is well known that of the power in watts, given by the product (amperes × volts) "apparently" supplied to an inductive A.C. circuit or one containing self-inductance, or capacity, or both, only a portion constitutes an actual or useful load or power and does useful work in the circuit, while the other portion represents no load at all, and is said to be wattless or idle power, doing no work in the circuit.

The useful power is given by the product of that portion of the current and voltage in phase with each other, and is usually called the true power, while the wattless or idle power is given by the product of those portions of the current and voltage which are in quadrature, as it is termed, i.e. differ in phase by 90° or a quarter period, the average value of the latter product being always zero. The useful and wattless powers are each given by a product of amperss × volts, and may be arrived at in either of two ways as follows: let a voltage OE and a current OA differ in phase by an angle ϕ . Resolve OA into two components, one Oa along and in phase with OE, the other Oa_I perpendicular to it. Then $OaAa_I$ is a rectangle, and the corner



Fra. 121.

 a_I will lie on a semi-circle Ua_IA drawn on OA as diameter. We now have the true power = $OE \times Oa$, the wattless power = $OE \times Oa_I$, and the apparent power = $OE \times OA$. Oa_IA is, therefore, the triangle of currents of which OA is the total or resultant or animeter current, a_IA the load or useful current, and Oa_I the idle or wattless current, always perpendicular to a_IA .

The power factor
$$\cos \phi = \frac{\partial E \times \partial a}{\partial E \times \partial A} = \frac{a_t A}{\partial A} = \cos \theta A a_t$$

Again, resolve ∂E into two components—one ∂A along and in phase with the current vector ∂A , the other ∂E_I perpendicular to it. Then $\partial E_I EA$ is a rectangle and the corner A will lie in a semi-circle ∂AE drawn on ∂E as diameter. We now have the true power $= \partial A \times \partial A$, the wattless power $= \partial A \times \partial E_I$. ∂AE is therefore the triangle of voltages of which ∂E is the total or resultant or voltmeter voltage, ∂A in phase with the current, the load or useful or energy voltage, and ∂E_I the idle or wattless voltage always perpendicular to ∂A . The power factor $\cos \phi =$

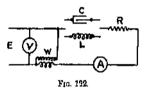
$$\frac{\partial A \times \partial A}{\partial A \times \partial E} = \cos A \partial E.$$

Now, the wattless powers in the two cases are $OE \times Oa_I$ and $OA \times OE_I$ respectively, which are equal, since the areas of the rectangles $(OE \times Oa_I)$ and $(OA \times OE_I)$ are equal. Mathematically, therefore, it is immaterial from which point of view the matter is treated, as both lead to the same result, namely—

True power = total voltage \times useful current = $V \times A \cos \phi$, , , = total current \times , voltage = $A \times V \cos \phi$.

In practice, however, it is more convenient and general to consider the total current A to be made up of two components, respectively A cos ϕ in phase with, and A sin ϕ in quadrature with, the voltage, and termed the energy, useful, or load current and the idle or wattless current. These are related geometrically, as seen in Fig. 121, by the equation

(Total current)2 = (useful current)2 + (wattless current)2,



from which the wattless current measurement of the present test is deduced. This can be made with the two possible circuit conditions, namely, self-induction with ohmic resistance, for which the total current lags in phase behind the load current by an angle ϕ , and capacity with ohmic resistance, for which the load current lags in phase behind the total current by an angle ϕ , i. e. the total current leads in front of the load current. This is shown in the single diagram, Fig. 121, though more commonly by two separate ones split along the line OA.

Apparatus.—Source E of alternating current; voltmeter V; ammeter A; wattracter W; variable non-ind. resistance R; capacity C; self-induction L.

Observations.—(1) Connect up as in Fig. 122, levelling and adjusting to zero such instruments as need it.

(2) With C only connected in circuit, note the readings of V, W, and A for some five or six values of current A between O and the maximum possible by varying R. (3) With L only connected in circuit, repeat obs. 2 and atabulate as follows.—

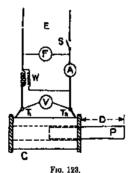
Nature	Voltane	Watte		Curre	ılə.	Power Factor	Angle of
Circuit	Y.	ΪŸ.	Total (04)	1,00d → 11/17.	Wattless $= \sqrt{A^4} - (H/V)^4$.	- 11/AF.	Phase Diff.

(4) Check one or more of the tabular readings by diagram, such as Fig. 121.

Inferences.—State all that can be deduced from the results of the test.

(118) Variation of Impedance, Reactance and Self-Induction with Position of Movable Core in Solenoidal Choker.

Introduction.—This test is intended to show the principle underlying the action of the so-called dimmer, which is so commonly used now in theatres and picture-halls for raising and



F10. 128,

lowering the lighting when the supply thereto is alternating current, also the range of regulation of a choking coil for working on arc lamp circuits of different voltages. It has the great advantage over a variable "line" resistance of preserving completely the electrical continuity of the circuit, while introducing a back E.M.F. of self-induction to the supply depending on the position of the movable core.

Apparatus.—Source of A.C. supply K, preferably an experimental motor-driven alternator, the excitation and speed of which are independently variable within wide limits; switch S; frequency meter F; ammeter A; voltmeter V; wattmeter W; and the movable core solenoidal choker ℓ .

Observations.—(1) Connect up as shown in Fig. 123, levelling and adjusting such instruments to zero as need it. Ensure that the labricating arrangements are working properly on starting up.

- (2) With the field regulator of E full in and the machine supplying constant frequency F, close E and adjust the alternator field excitation so as to give the max, safe current A through C with the centres of P and C coinciding (i. e. D=O), then note the readings of F, A, W and V.
- (3) Take the readings of F, A, W, V and D with the same constant values of F and A for each of a series of clamped positions of P between D=O and D= full length of P, with P finally removed to a distance.
- (4) Repeat obs. 2 and 3 for the same constant frequency F, but with V now maintained constant, at such a value as will prevent the current rising above the max, safe value when P is removed to a distance, and tabulate all your results as follows—

Choker coil . Length	No. of turns	Bos. R =
Care Length	. Cross Section = ,	

				. —					1			1 (10)
	N.	·). <u>.</u>	ų	Beadio	<u>.</u>	Wates	100 ± (2)		9 ± 14 ± 1	ر ا	1.11.1 4
	Frequency	E Par	Volta	Lience	netor I	Watt	AP.	A PER FE	le of I	nrodn V.	(+ / 4)	
i	Fre		ĺ	Ā	Watt	Ē	ą.	Pon	Angl	id 1.7.4 ■ 1.7.4	H 1 - 47	8 TIA
		_	<u> </u>	<u>'</u>		<u> </u>	<u> </u>	<u> </u>			<u>`</u>	

(5) Plot curves for obs. 2 and 3 having values of D as abscisse with values of Y, W, $\cos \theta$, V/A, Lp and L as ordinates respectively, and for obs. 4 having values of D as abscisse with values of A, W, $\cos \theta$, V/A, Lp and L as ordinates respectively.

Inferences.—State all you can deduce from the table of results and curves.

(119) Effect of Length of Air Gap in a Closed Magnetic Circuit on Impedance, Reactance, Self-Induction, Current and Power.

Introduction.—The present test is a very important one, inasmuch that it is a direct proof of fundamental theory, and has an important bearing on the use and range of regulation of all kinds of choking or reactance coils for adjusting the current in are lamp circuits at different voltages, while at the same time emphasizing the relative merits of "closed" and "open" magnetic circuits. The factors of an alternating current supply being voltage, current, and frequency, with the last named usually

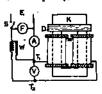


Fig. 124.

constant, it follows that the present investigation can be carried out in at least two ways, namely-

- (a) With constant current and varying voltage at constant frequency.
- (b) With constant voltage and varying current at constant frequency.

In the former method of supply, and with a series wound and connected choker, any offects observed by varying air-gap must be due to this alone. In the latter method, owing to change of current strength (in all but saturated magnetic circuits) causing a change of magnetic flux and induction density, any effects otherwise due to change in length of air-gap may be seriously vitiated.

Apparatus.-Experimental magnetic circuit with adjustable

air-gap; switch S; frequency meter F; ammeter A; voltmeter V; wattmeter W; source of A.C. supply E, preferably from an experimental motor-driven alternator, the voltage and speed (i.e. frequency) of which are independently variable within wide

limits.

Observations.—(1) Connect up as in Fig. 124, levelling and adjusting to zero such instruments as need it. Now start the motor-alternator, observing that the lubricating arrangements

are working properly.

Note.—If a constant voltage and frequency town supply is used, a suitable non-inductive resistance must be connected in series with one of the mains on the supply side of IV for regulating the current.

- (2) Remove all the non-magnetic distancing strips D and clamp the laminated iron keeper K down on to the poles by means of the wing-aut clamp (not shown in Fig. 124). With the field-regulating resistance of the alternator full in, close S and obtain a frequency of 50 or 60 \sim per sec. on F, to be kept constant by driving the alternator at the requisite constant speed,
- where the frequency (f) = No. of pairs of poles x revs. per min. ÷ 60.

 (3) Raise the A.C. voltage by field regulation to the maximum value possible, so long as the current produced does not exceed
- the safe maximum for the choker winding. Then note the readings of F, A, W, V, and that the air-gap is zero.

 (4) Unolamp K, and carefully raise it just sufficiently only to slide one distance strip D in between it and the poles, and

re-clamp K.

Now, lower the voltage (by field regulation) until A has the

- same value as before—the frequency being also the same. Then read F, A, W and V.

 (5) Repeat (4) for about ten different air-gaps, increasing by
- one distance strip at a time, and finally with K removed altogether, i.e. air-gap = max.

 (6) Employing supply condition (b), mentioned in the introduction above, with K removed altogether, adjust the field
- regulator of the alternator so as to give such a voltage as will send the max, safe current through the choker winding at the same frequency as before. Now note the values of F. A, W and

V, and that the air-gap = max. This voltage and frequency is to be kept constant in future.

(7) Next take the readings of F. A, W and V for each of a series of air-gaps, ranging from that given by all the distance strips clamped together between K and the poles to none in at all, by one at a time, and tabulate all your results as follows—

Form of Inductive Oracit tested												
Frequency F.	Amps 4.	Volts F.	No of Strips in use,	Leagth of Air Gap	Wattneber Reading.	True Watts W.	Apparent Wates	Power Factor ons 8 — IF	Angle of Lag #".	Impedence $\Gamma/A = \sqrt{L^2 \mu^2 + R^2}$.	Resctance $Lp \Rightarrow \sqrt{(P/A)^2 - h^2}.$	Coeff, of Self-Ind. $I = \frac{1}{p} \checkmark \left(\frac{p}{A}\right)^{2} - R.$

(8) Plot curves from obs. 3-5 having values of D as abscisse with V, W, cos θ , V/A and L as ordinates respectively. Also from obs. 6 and 7 plot curves having D as abscisse with A, W, cos θ , V/A and L as ordinates respectively.

Inferences.—From a careful study of the above table and curves state clearly all that can be deduced.

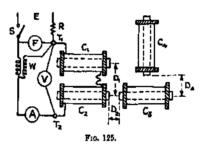
(120) Investigation of Mutual Inductive Effects due to the Relative Positions of Two Coiled Circuits.

Introduction.—The object of this investigation is to find out to what extent, and in what way, two neighbouring electromagnetic fields may react on one another when in different relative positions.

Qualitative and quantitative results are obtainable which are both interesting and instructive, in view of how little the average student realizes the possibilities of interaction between neighbouring magnetic fields and apparatus with the prejudicial effects often resulting. For the investigation, two solenoidal movable iron coro choking coils (preferably similar in all respects) may be used, connected in series.

Apparatus.—Two similar chokers; ammeter A; voltmeter V; watteneter W; frequency moter F; switch S; non-inductive resistance R (such as a bank of lamps) for regulating the current, if the supply E is from the town. If from m experimental motor-driven alternator, R can be omitted and A adjusted by field regulation on the alternator.

Observations.—(1) Connect up as in Fig. 125, where T_1T_2 are the terminal extremities of the two coils connected permanently in series. Level and adjust to zero such instruments as need it.



- (2) With coils touching side by side in arrangment C_1C_2 (i.e. $D_1 = \text{minimum}$) and cores clamped controlly, take the readings of F, W, Y, A and D_1 for constant full-load current A and frequency F = 50 for each of a series of values of distance D_1 up to a convenient maximum, the coils being parallel at each.
- (3) Take a copy of an iron filing diagram for the position $D_1 = a \text{ min.}$
- (i) Repeat obs. 2 and 3 with one coil reversed or turned through 180°.
- (5) Repeat obs. 2 to 4 for the position of coils shown at C_2C_4 (i.e. with magnetic axes of cores perpendicular) at different distances D_a .
- (6) Repeat obs. 2 to 4 for the position of coils shown at C₂C₃ (i.e. axes in line) at different distances D₂₁ and tabulate as follows—

articular and To (Constant) (Constant) 12 4 \cup	Relative Positions of Code,	Distances D ₁ , D ₂ and D ₃ .	Frequency P (Consist)	Current A (Constant)	Volta V.	Tine Walts W.		Impedance V/A,	Power Factor rest = B7AY.
---	-----------------------------------	---	-----------------------------	----------------------------	-------------	---------------------	--	-------------------	------------------------------------

(7) In addition to the copies of the respective iron filing diagrams, plot the following curves having values of distance D as abscisse, with volts V and impedance $\frac{V}{A}$ respectively, as ordinates in each case.

Inferences.—From the table of results, diagrams and curves state all that can be deduced.

(121) Measurement of Magnetic Permeability by the Permeameter.

Preliminary.—The following method, devised by Prof. S. P. Thompson, is a simple and convenient workshop one for rapidly measuring the magnetic permeability (μ) of any material. It is quite distinct from the ballistic, direct magnetemetric, or optical methods of measuring (μ) , and is based upon the law of magnetic traction, viz. that the tractive force over a given area of contact is proportional to the square of the magnetic flux through the junction. This and all other traction methods are not capable of giving very accurate measurements of (μ) , for both the tensile stress and the place chosen for contact between specimen and block may affect the results somewhat, as in the latter case the distribution of the induction is not very uniform at this point. Now, since in the permeameter the magnetizing coils remain fixed, the pull on the specimen core will be due to (B-H) lines, where B= induction per sq. cm. through the junction, and H =magnetizing force producing it. sectional area of the junction in sq. cms. the force of attraction between core and block, i. c. Pull $(P) = (B - H)^2 S + 8\pi$ dynes = $(B-H)^2S \div (8\pi \times 453.6 \times 981)$ lbs. $B = 1317 \times \sqrt{\frac{P}{S(\epsilon_0, \text{ in.})}} + H$ C.G.S. lines. Where P = pull in lbs, to detach.

If the magnetizing coil consists of T turns, carrying a current A amps., and its length between ends = L. Then $H = \frac{4\pi AT}{10 L} = KA$,

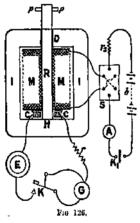
A amps., and its length between ends = t. Then $H = \frac{1}{10t} = K$ in C.G.S. measure. (The constant $K = 4\pi T + 10 k$)

An advantage with this method of measuring permoability is that the specimen of the material to be tested is in the form of a simple straight rod of circular cross section, and in this form it can generally be very easily obtained. Further, owing to no delicate ballistic galvanometer being used in the method, the test can be performed even in fairly close proximity to dynamos

or near other magnetic fields without especially vitinting the results. The permeameter illustrated is fitted with a slip coil CC for measuring μ ballistically if desired. For a more detailed description of the instrument vids p. 615,

description of the instrument vide p. 615.

Apparatus.—Permeameter (Fig. 280); Salter's spring balance; ammeter A; rheostat r₂ (p. 599); battery b; awitch K₁; Pohl's commutator or reversing



switch S (p. 584); specimen or rod R to be tested.

Tests.—(1) Connect up as

indicated in Fig. 126, omitting

the ballistic circuit shown at the lower part of the Fig. Insert a specimen in the coil after having cleaned the end and demagnetized it. Then attach the spring balance by means of its double hook to the pin pp in the present case.

(2) With r₂ full in, adjust the current to a small value (say 0.02 amp.), and note the force P lbs. required to de-

(say 0.02 amp.), and note the force P lbs. required to detach. This should be repeated two or three times, and the mean noted.

(3) Repeat 2 for about fifteen different currents up to the maximum (about 7 amps.), rising by such amounts as will give about equal increments of pull on the balance.

(4) Repeat 2 and 3 for different specimens, and (abulate as follows-

		M.	AMB		DATE							
I	_	-	cimen tests			etleing.			Permeability			
Į	Nª	Nature.	Diameter d (ins.)	Berlien (8) = $\frac{\pi d^2}{4}$ 8q. in.	Current 4 amp.	Force	Pall Fibe,	Induction B.	# #]/			
	. !	ļ		١	1 '	1			1			

(5) Plot two curves, one having H as abscisse and B as ordinates, the other having B as abscisse and μ as ordinates.

(122) Measurement of Magnetic Permeability (by Hopkinson Permeameter).

Introduction.—The present test is very similar to the preceding one (No. 121), except that a slightly different form of



Fig. 127.

permeaneter, devised by Professor Hopkinson, is provided. This instrument consists (as seen in Fig. 127) of a heavy wroughtiren yoke with two magnetizing coils, one having a fixed core and the other a movable one. On the movable core is a small coil of wire which, when the core is withdrawn, is jerked up by a spring; this coil is connected to a ballistic galvanometer, and the throw is proportional to the lines in the core; by this means cores made of various samples may be compared for permeability. The apparatus and connections, except for the differ-

ence in the actual form of permeameter, and the addition of a ballistic galvanometer C, key K, adjustable standard known resistance (\cdot) , and earth inductor E, or preferably a standard solenoid, are precisely those indicated in Fig. 126, and the student should read the introductory remarks of test No. 121.

The evaluation of the throws on the bullistic galvanometer G is exactly as given in the introduction to test No. 78, and therefore need not here be repeated.

Observations.—These consist in taking the galvanometer first throw at the moment when the small slip-coil springs out, for each of a series of exciting currents ranging from 0 to the safe maximum permissible, and tabulating all the readings and evaluated results in a convenient form.

Note.—The first throw should be repeated, for each excitation, by replacing the slip-coil two or three times, when the mean throw only at each current should be tabulated. Further, a preliminary trial must be made, before taking the above series of observations, by adjusting the resistance (r) until maximum permissible exciting current gives a mean first throw, not exceeding full-scale deflection. Lastly, the increments of current in the series must be smaller during that part of the range where the magnitude of the mean throws appears to be differing considerably.

A curve should be plotted between values of induction density B found, as ordinates, with values of magnetizing force H as abscissa, and also one between permeability μ as ordinates, and values of B as abscissa.

(123) Measurement of Magnetic Hysteresis and Eddy or Foucault Currents in Samples of Magnetic Material. (By Single Phase Alternating Currents.)

Introduction.—The determination of magnetic hysteresis in magnetic materials by some of the most important methods is given in considerable detail in Practical Electrical Testing by the author, and the reader is referred to this book for further particulars of these tests. It is of course well known that an iron

core, magnetized by an alternating current of electricity, is the seat of two distinct losses of power, (1) from hysteresis, and (2) from eddy currents generated in the transverse section of the conductor.

The former depends on the induction density in the iron, the frequency of the alternating current, and on the volume and nature of the magnetic material in question. No amount of lamination will get over this loss.

The latter source of power loss is dependent on the extent of lamination of the iron and on the transverse section of each individual portion of the core.

Now by employing sufficient iron in a test specimen, well laminated, the eddy current loss can be made small compared with the hysteresis loss, whence any measurement now made of the total core or iron loss will for all practical purposes represent the hysteresis loss simply. This is the principle upon which the present method is based, but if greater accuracy be desired the results so obtained can easily be checked by one of the methods

It will thus be at once evident from the foregoing remarks that the iron employed in all electrical engineering appliances, but more particularly in alternating current ones, should be tested for hystoresis loss prior to being used in the construction of such appliances. The present method is one of the simplest and most expeditious ways of measuring the hysteresis loss in different samples of iron which may be to hand, and it is accurate enough for most practical purposes.

given in the above-mentioned work,

Probably the most important direction in which the preceding remarks find an application is in transformer, alternator, and alternating current motor work. As the magnetic circuits of such appliances are built up of stampings-out of thin soft sheet iron, this latter is the form in which samples to be tested usually come to hand. Assuming therefore that a few large sheets of the material to be tested, the thickness of which usually varies from 0.25 m.m. to 0.5 m.m. for transformers and up to about 1 m.m. for alternators, etc., is at hand, the first thing to do is to prepare the material for testing by constructing a small transformer out of it thus—

PREPARATION OF IRON SAMPLES FOR TEST.

Cut such a number of strips out of the sheet, each about $12'' \times 2''$ as will make four equally thick piles; each containing the same rumber of strips, placed on the top of one another like the leaves of a book, to a thickness of, say, $\frac{1}{2}''$ and each weighing about 2 lbs.

Now remove any burr from the edges of each by means of a file, and weigh all the strips, noting the total weight of iron W which should preferably be 8 or 10 lbs.

Next varnish one side of each strip with thin shellae varnish, and when dry assemble into four equal piles with varnished faces all pointing one way. Bind each pile, to within 11 of each end, with a layer of thin prepared tape, when each will be ready to receive the magnetizing coils. It will be noticed that each strip is insulated from the next by the equivalent of one layer of thin varnish, which is all that is needed. Next make a thin rectangular cardboard tube about 4" to 41" long for each pile and capable of just slipping easily over it. Wind each of these with two distinct coils of, say, No. 18 double cotton-covered copper wire, each coil consisting of two layers and the two coils wound one over the other. Place the four hundles of strips with their coils in position so as to form a rectangular frame of iron with adjacent ends interleaved, so to speak, and clamped together so as to form a compact joint of low resistance. Join the four coils of each set together so that they would help one another in magnetizing the ring and the specimen is then rendy for test. Note the total number of turns N_P and N_B on both primary and accordary coils respectively, also the cross section S sq. c.ms. of iron in the frame, i.e. thickness of strip x by number side by side x width of strip, and the mean length of the path of a line of force right round.

Apparatus.—Iron core on frame I to be tested and wound with the two distinct (closely-wound) primary and secondary coils P and S. Siemens electro-dynamometer or Parr direct reading dynamometer ammeter A (Fig. 577); non-inductive Wattmeter W; non-inductive rheostat R (p. 597); switch K; electrostatic voltmeter V; Pohl's commutator D (p. 584), or other suitable change-

over switch for throwing V in quick succession across P or S. Source of alternating current supply E, preferably one the frequency of which is under control; a tachometer will be required in this latter case.

Observations.—(1) Connect up as indicated in Fig. 128, and adjust the pointers of A, V and W to zero if they require it and levelling them where necessary. If the alternator is under control see that all the lubricating cups in use feed slowly and properly.

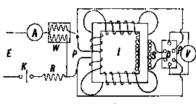


Fig. 128,

- (2) Start the alternator up to its highest desirable speed, which is to be kept constant, then with R at its full close K and alter R and the excitation to give the smallest readable current on A. Note simultaneously the readings on A, W and V in quick succession when across P and S by turning D to P or S as the case may be, and the speed.
- (3) Repeat 2 at the same speed for eight or ten different currents A, rising by about = increments to the highest desirable.
- (4) Adjust the current A to some convenient value, preferably one that will produce an induction of B-about 4000 lines per sq. cm. in I and keep this constant.
- (5) Now take a series of readings of W and V for about eight or ten different speeds, ranging from the greatest down to the smallest, noting the value at each.
- (6) Measure the resistances of the primary and secondary windings by means of a Wheatstone Bridge set, and tabulate all your results as follows—

NAME... DATE...

Alternator: Periods per Revola. $K=\dots$ $p=2\pi s=\frac{2\pi R}{60}$ — per sec. Restincts (lof) Primary $R_p=\dots$ olund. Restinct from Core $S=\dots$ eq. cms. $N_p=1$. Secondary $N_p=1$. Secondary $N_p=1$. Thickness of Strips = . . Thickness of Strips = . .

R	ā l	8	Cur	rent,	B.I	ι γ.	. For	a er.	투자		a	8 s	a . 1812	ĺ
peed of arnator	5	(Demoy.)	ection .	4 4	Past 7	ndary Fe	co Buc	Watte F.	rox. loss	Core I	e appro	15. of 18 18. of 18	duction	
	5		A	1	Ĕ	8	Read	감	P. P.	X X	•	H H	ğ # Eğ	

- (7) Plot the following curves-
 - (a) Between H and B having B as ordinates and hysteresis loss H as abscisse.
 - (b) Between H and n having n as ordinates and hysteresis loss H as abscisse.
 - (c) Between H and A having A as ordinates and hystoresis loss H as abscisse.

Note, \overline{B} varies from 3000 to 5000 C.G.S. lines in ordinary transformers. With good iron H/W should not exceed $\frac{1}{2}$.

Inferences.—State very clearly what you can infer from the

Inferences.—State very clearly what you can infer from the results of your tests.

(124) Separation and Measurement of Iron Losses in the Cores of Alternators, Transformers, Motors and other Electro-magnetic Appliances. (Alternating Current Frequency Method.)

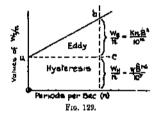
Introduction.—The iron losses taking place in the cores of alternating current plant (e.g. alternators, tronsformers, motors, etc.) consist of those due to magnetic hysteresis and eddy or Foucault currents respectively.

The Hysteresis Loss depends on the induction density in the iron core, the periodicity of the supply current, and on the volume and quality of the iron used, but in no way on the extent to which the lamination of the core is carried and increases with, but more rapidly than, the induction.

Steinmotz gives the empirical equation for the work done on account of hystoresis as $w = \eta \hat{B}^{t\, c}$ ergs per cycle of current and magnetization where η equal the hystoretic constant which may vary from 0.001 to 0.003 for soft, annealed core plates, and $\hat{B} = \max \max$ value of induction density in lines per sq. cm.

If (n) = periodicity of the supply or number of complete periods per second, the effective loss W_B due to hyteresis (per cub. cm. of core) will be

 $W_d = \eta n B^{*4}$ ergs per sec. = $\eta n B^{*1} 10^{-\eta}$ waits, on the assumption that the hysteresis loss per cycle is independent of the rate of cycle which the latest research shows to



be not quite the case, though sufficiently so for practical purposes. Actually the hysteresis loss per cycle increases slightly with increase of periodicity, and from the above relation we see that for a given core, run at constant induction density $|F_n|$ is ∞n .

The Eddy Current Loss depends on the strength of the induced eddy currents set up in the thickness of each lamina composing the core, and hence, by Ohm's law, will vary as the square of such strength. The eddy currents are due to the varying flux through the core, and will depend on the rate of variation of this flux, i.s. on the periodicity (n). Thus the eddy current loss will vary in proportion to n, and the effective loss II', due to eddy currents (per cub, cm. of core) will be

$$W_{\mu} = K n^2 B^2 10^{-16}$$
 watts,

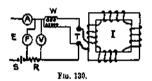
where K = a constant taking into account the specific electrical resistance of the iron and the thickness of plate lamina.

Eddy currents tend to reduce the flux in a core due to their demagnetizing action and also cause a non-uniform distribution over the sections of the lamina. Due to this, the hysteresis loss will be further increased with increasing values of (n), and will appear as an increase in the eddy current constant (K) in the present method over and above the calculated value. Especially will this be the case if the insulation between core lamina is not all effective.

If W = the total power in watte absorbed by any electromagnetic appliances

and W_{σ} = the watts absorbed or expended in the exciting coil,

then the nett iron losses
$$= W_{I} = W - W_{G} = W_{H} + W_{S} = \eta n \dot{B}^{1/4} 10^{-7} + Kn^{2} \dot{B}^{2} 10^{-16}$$
watta



Now the coefficients η and K can be found experimentally by testing the appliance at constant induction density \hat{B} with alternating current at variable periodicity (n). This can be done by varying the speed of an alternator running at constant excitation, for then the voltage V varies α to the periodicity (n), so that V/n, and hence the flux, remains constant. On plotting the values $\frac{W}{n}$ as a function of the induction \hat{B} , the straight line ab is obtained corresponding to one particular value of \hat{B} and of V/n. From the curve ab and this value of \hat{B} the coefficients η and K can be calculated, and hence the hysteresis and eddy current losses respectively.

Apparatus.—Electro-magnetic core I to be tested; low-reading alternating current sometor A; wattmeter W_1 and voltmeter V_2 , each independent of periodicity; frequency meter F_2 , or, failing this, a tachometer for measuring the speed of the supply alternator F_2 ; switch F_2 and non-inductive variable resistance F_2 .

Observations.—(1) Connect up as shown in Fig., 130, levelling and adjusting to zero such instruments as require it. Start up the experimental alternator and see that the lubricating arrangements are working properly.

- (2) With a suitable ammeter, variable regulator, and switch in series with the alternator field across the D.C. supply, close the field switch TS, and adjust the speed to give the lowest readable value of periodicity (n) on F (or smaller value by tachometer), and adjust the field regulator to give some suitable reading on V. Now note the readings of all the instruments, and particularly the value of V/n for future use.
- (3) Note the readings of all instruments for each of a series of periodicities (n) up to the highest permissible, taking care that the value of V/n (and therefore the value of the induction \hat{B} in I) is the same at each periodicity.
- (4) Repeat the above for the same range of periodicity, but for each of two other widely different values of V, giving corresponding values of the ratio V/n (and hence inductions B) kept constant throughout each range of \sim variation.

Note.—If the appliance tested will safely stand, say, 150 volts, then three values of the constant 1/n might be used, viz.—150 $\frac{100}{50}$ and $\frac{50}{50}$ or 3, 2 and 1 by suitable variation of field excitation, thus giving three corresponding values of \hat{B} in the core. Further, since $\frac{1V_I}{to}$ is not likely to exceed 1.5 or 2.0 watts per 1b, in modern iron cores, a low-reading wattmeter will be required, unless the core is a heavy one.

Tabulate as follows-

Supply After after; Periods per ter, P = ...Material . . . Core tented : Form or type . . . No, of magnetizing turns T -Monn length of magnetic circuit ? -CBI4, Net cross section of gan Acs. of magneticing turns r = MJ. CEP. Not weight of Iron Пa. Thickness of core luminations -Net volume of mon e,r, Width of core lamination -Literatur Rose in F p.m. A. Fotal Iron 1042 Calculated Constant 1/2, T Total ŧ Amps, Yer, Jed.

- (5) Plot curves having values of (n), as abecisse, with values of V, A and W_I respectively, as ordinates, for each constant V/n taken.
- (6) Determine the hystoresis and oddy current coefficients, and from 2 draw a straight line, tangent to the curve relating W_I and u, separating the hysteresis and eddy losses, when ordinates of this line will represent losses due to hysteresis $\propto u$, while the ordinate intercepts between it and the watt curve will represent losses due to eddy currents $\propto u^2$.

Inferences.—State clearly what you can infer from the above results.

(125) Measurement of Magnetic Hysteresis by Ewing's Hysteresis Tester.

This instrument, a general view of which is seen in Fig. 131, and for a full description of which see Professor Ewing's Paper in the Journal of the Institution of Electrical Engineers, April 25, 1805, has been designed to meet the want which has been felt of a means of testing the magnetic hystoresis of sheet-iron or steel in a simple and expeditious way suitable for workshop as well as laboratory use. A few strips of the sheet motal to be tested are cut or stamped, five-eighths of an inch wide and three inches long. They are filed to the exact length when clamped in a gauge, which is provided with the instrument, and are then inserted in a carrier which is made to revolve by turning a handle. The carrier turns between the poles of a permanent magnut, which is suspended on a knife-edge. In consequence of the hysteresis of the specimen the magnet is deflected and the amount of its deflection is observed by means of a pointer and scale. From this deflection the hysteresis of the specimen is determined. The magnetic induction is practically the same in all specimens, notwithstanding differences in the permeability of the iron, on account of the comparatively large air-gap between the specimen and the magnet poles.

Two standard samples are provided with the instrument,

having stated amounts of hystoresis. The test of any other specimen is made simply by comparing the deflection produced by it with the deflections produced by the standard samples. This serves to determine the hystoresis of any specimen in absolute measure.

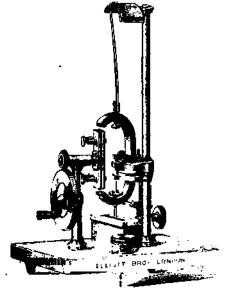


Fig 131,

The operation of the instrument is entirely mechanical, and requires no knowledge of electrical testing.

(126) Measurement of the Impedance, Reactance, and Self-Induction of Alternator Armatures, Motor Stators, Transformer and other windings (by Alternating Currents).

Introduction.—The following is a simple and an approximate method of finding the self-induction L of an inductive circuit. It depends on the fundamental relation subsisting between current (A) and impressed E.M.F. (V) in such a circuit, namely—

V

$$A = \sqrt{\frac{\gamma}{L^2 p^2 + R^2}}$$

or, as it may otherwise be written,

Impedance =
$$\sqrt{L^2p^2+K^2} = V/A_1$$

where the angular velocity of the current $p=2\pi n$, a being its frequency in per sec.

Since by definition, the coefficient of self-induction L of any coiled circuit is $=\frac{N}{A}$ where N is the total magnetic flux threading the coil and produced by a current A, it follows that if the inductive circuit encloses, and is surrounded by, a non-magnetic mealium, the value of L calculated will be the same for all values of A. If, however, it encloses an iron core, any variation of A will produce variations in the permeability of, and consequently the flux in, the core, and the value of L-will vary with A.

Thus the impedance and self-induction of the primary of a static transformer, and of the stator winding of an induction motor will decrease as the secondary load of the former and B.H.P. developed by the latter increases, owing in each case to alteration of current and core flux. The same effect occurs with the armature of an alternator or of a synchronous motor, the impedance and self-induction of which will vary with—

- The armature current, since the core flux and permeability will vary inversely together as the current changes.
- (2) The magnetization of the core due to any variation of the field-magnet strength.
 - (3) The type of winding used, i.e. whether "distributed" or

"concentrated," the former having small self-induction owing to the circuits being partly in both favourable and unfavourable positions for linking with the flux, the latter having a large self-induction, due to all the circuits in certain positions in the

- revolution linking up simultaneously with the flux.

 (4) The reciprocal of the length of air-gap between armature eore and field poles.
- (5) The exact position of the armature relatively to the field poles, especially with windings concentrated into single slots.

 (6) The induced currents in the pole pieces and field windings
- (6) The induced currents in the pole pieces and field windings due to the armature current.

 In view of the above considerations, it will therefore be

obvious that the value of the impolance or self-induction of the armature of an alternator available for calculation can only be a mean value as obtained in the manner indicated in the present list,

Two methods of procedure are possible, according as to the mode of obtaining the Ohmic resistance R.

- (a) R may be measured in the usual way on a Wheatstone Bridge either before or after the test, in which case a measurement of the current at a known voltage, or vice versa together with (n), at once gives the self-induction L.
 (b) R may be obtained by Ohn's Law in terms of a continuous
- current and pressure when this latter is available, and therefore no Wheatstone Bridge is necessary. This method of procedure, which is the one adopted in the prescut instance, has the further advantage that in cases where R is liable to heat up, due to the current, its value will be obtained correctly, which would not be so if obtained by the bridge.

The following precautions should, however, be carefully observed, and are practically the same as appear in the measurement of the resistance of an electric glow lamp while running (vide p. 47). If the voltmeter is shunted across the terminals of L, then its

If the voltmeter is saunted across the terminals of L, then its reading is correct, but the true current through L which is required = ammeter reading - voltmeter current. If, therefore, an electrostatic voltmeter is employed this correction does not occur, but if a hot wire voltmeter is used, the correction should be made, as the voltmeter current is not usually negligibly small compared with the main current.

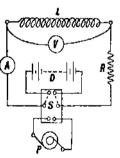
If the voltmeter is across the ammeter and L combined, then the true voltage across L=voltmeter reading - voltage absorbed in ammeter. Owing to the low resistance of the last-named usually, this correction is negligible, but must be made if the ammeter resistance is considerable. In this arrangement we also have—

True self-induction of call=calculated L-self-induction of ammeter.

The test can be performed either using the same voltage from the direct and alternating sources and noting the relative currents, or employing the same current and observing the relative direct and alternating volts necessary to send this current through the circuit, the frequency in either case remaining the same.

In the present instance the latter way will be adopted as being more readily applied.

Apparatus.—Inductive circuit L to be tested; alternating current voltmeter V, preferably electrostatic; Siemens electro-



Ftg. 132.

dynamometer or A, C, ammeter A (Fig. 251); variable non-inductive resistance R (p. 598); change-over switch S (p. 582); alternator P, with its tachemeter; direct current dynamo or secondary battery D.

Observations.—(1) Connect up as indicated and adjust the pointers of A and V to zero. Before starting see that all lubricators in use feed slowly.

(2) Make R as large as possible and switch S over to D, adjusting A to the maximum current which

L will carry. Note the current A amps. and the volts V_D across L.

(3) Turn S over to P and adjust R and the speed of P so as to

- (3) Turn S over to P and adjust R and the speed of P so as to again obtain the same current A amps. Note the volts (V_s) and the speed of alternator.
- (4) Open S and make R as large as possible again. Repeat 2 and 3 for about ten different decreasing values of current to the smallest convenient, and keep the speed of P constant throughout, its excitation being varied, if necessary.

Note.—If the double pole change-over switch S is not available, the common circuit containing A, L and R can be closed to D through a single pole switch, and a series of pairs of values of A and V first taken in order to obtain the olunic resistance $\binom{V}{A}$ of L. P can then be substituted for D, and a similar series taken with alternating currents of the same scale values on A as before between 0 and the maximum L will carry at constant frequency.

- (5) If the inductive circuit has a removable magnetic core, as, e g., in the contral movable core open-magnetic-circuit type of choking coil. Then operate obs. 2-4 above, or the alternating current series only of observations mentioned in the Note above, with the core (a) central in the coil, (b) removed altogether away from the coil.
- (6) If the inductive circuit L (Fig. 132) consists of the armature of an alternator the impedance and self-induction of which is required, the A.C. supply should have the same periodicity as the normal value for the machine under test. Then, with the field magnets of the machine under test, vary R so as to obtain about a quarter, half, three-quarters and full-load currents (A) through the armature, noting the corresponding readings of V at each of a series of positions of the armature throughout a fraction of a revolution equal to half the polar pitch.
- (7) Repeat (6) with normal field excitation and tabulate as indicated.
- (8) Plot curves for each fraction of full-load current having impedance and self-induction respectively as ordinates with positions of armsture throughout the half polar pitch as abscisse.

Inferences.—State clearly all that can be deduced from the results of the test, and find the average value of the impedance and self-induction, and tabulate as follows—

Alternator; Speed $K=1,\ldots K$ p.m. Periods per Revolution K=1.

Frequency $n = \frac{KH}{60} = \dots = 0$ per s.c. $p = 2\pi n = \dots$ Nature and form of cold test of . . .

Position of Core of Armature. Field Amps. Field Amps. Armature. Armature. Aftre.	Direct Constitution of Constit	Impedance myledance myl	$\frac{1}{pA} \sqrt{P_a^a - V_D}.$
--	--	--	------------------------------------

(6) Plot curves having values of L and V₄ as ordinates and the corresponding currents A as abscisses in each series.

Inferences.—What can you infer from your experimental results? On what does the self-induction of an alternating current circuit depend? Show how the formula given for L can be obtained.

Self-induction by Rowland's Alternating Current Method.

General Remarks.—Every electrical conductor possesses three qualities, namely, (1) Electrical resistance, which depends on the size and material of the conductor.

- (2) Electrical capacity, depending on its surface and form, and on the specific inductive capacity of the surrounding media (i.e. dielectric).
- (3) Electrical inductance, which depends on the shape and form of the conductor and on the magnetic permeability of the surrounding media.

This last-named property may be of one or other of two kinds, namely, either the self-induction of the conductor on itself, or the mutual induction of the conductor and a neighbouring circuit on one another.

The quality (1) above is usually easily obtained, except perhaps in the case of electrolytic liquids, and this only in one or two methods; the other qualities are much more difficult of determination, and almost numberless methods have been devised for obtaining them.

In general it may be remarked that relative or comparative measurements are more accurate than absolute ones, though the final results might be completely vitiated by comparing with an inaccurate standard. The former remark results in the difficulty experienced in accurately measuring an alternating current, and from the fact that its E.M.F. wave may differ considerably from that of a sine curve.

In employing condensers in methods of measuring self and mutual induction, considerable difficulty is usually met with in the phenomena of electric absorption. Professor II. H. Rowland has found that this can be represented by a resistance placed in series with the condenser, which resistance is a function of the square of the current period.

(127) Absolute Measurement of Self-induction (by Alternating Currents).

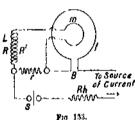
Introduction.—The following method of measuring the self-induction of a coil, due to Professor Rowland, necessitates the employment of ordinary single phase alternating currents of electricity with an electro-dynamonucter specially constructed, so as to be as sensitive as possible. It is possible to make such an instrument, having its fixed and moving coils connected up to two distinct pairs of terminals, that it will detect 0.0001 of an ampere with a self-induction in the suspended coil not exceeding 0.00075 henries, and in the fixed coil of not more than 0.0006 henries, capable of carrying about 0.1 ampere comfortably.

Such an instrument obviates the necessity for using large currents in order to obtain accuracy and sensibility. If (d) = the deflection of the swing coil from zero when its plane was perpendicular to that of the fixed coil, C_1 and C_2 = strengths of the alternating currents flowing through the movable and fixed coils and having an angle of phase difference θ . Then $d \propto C_1 C_2$ cas. θ .

The principle of the present method consists in adjusting C_1 and C_o to a phase difference of 90°.

In deflection methods cos, & is greater than 0, while for zero methods cos. $\theta = 0$. In the former the self-induction is obtained in terms of resistance and the angular velocity of the current $p = 2\pi \times$ frequency, which consequently require that (n) the frequency should be constant and accurately known to at least 1%, in which case the results will probably agree to within about

the same amount. Apparatus.—The electro-dynamometer, of which (f) is the fixed, and (m) the moving coil; non-inductive resistance r;



source of alternating current; and the self-induction L to be measured; switch \$; rheostat Rh (non-inductive). Observations, -- (1) Conneet up as indicated in Fig. 133, placing L and a noninductive resistance R in series with the moving coil

(m), and the combination

across the terminals of a re-

sistance (r) in the main circuit in which the fixed coils are also placed.

(2) With the moving cail adjusted to zero, Rh at a maximum, close S, and obtain a convenient deflection d by adjusting Rh and the non-inductive resistance R in the moving coil circuit. Note this deflection (d) and the speed (N) or periodicity (n) of the alternator and the added resistance R in circuit with L. (3) Remove the self-induction (L) which is being tested, and

add a non-inductive resistance to the swing coil circuit such that the same deflection (d) as before is reproduced. Note the new resistance R' in the circuit, the frequency (n) ___per sec. being the same as before.

(4) Calculate the self-induction L tested from the relation

$$L = \sqrt{\frac{(R'-R)(R+r)}{p^i}} = \frac{1}{2\pi n} \sqrt{(R'-R)(R+r)} \text{ secohras,}$$

and tabulate as follows-

MANE .. Daze . . . Alternator: Feriods per revolution $\mathcal{L} = \dots$ Self-induction tested : Nature . . .

			_				
Speed at Albernator	f'requency F N	Resistan	DEG.	Deflection	Self-Induction		
N 1070. per. man.	* = ^{RN} ~ per. see	r. B.	₩.	(v).	L.	Moen L.	
		' 	┢		_		

(5) Repeat 2-4 for different deflections (d) at constant frequency. Also for different frequencies with the same deflection. N.B.—Great care must be taken to keep the frequency constant throughout any pair of readings.

(128) Comparison of Two Coefficients of Selfinduction (by Alternating Currents).

Introduction.-When an accurate standard known self-induction is available the value of an unknown induction can be more accurately determined by comparison, for in this case the measurement is independent of frequency. The following method due to Professor Rowland is a zero one, and is similar in many respects to the preceding method, though this was a deflection method. The effects of induction and electrostatic action of the various parts of the circuit on one another must be carefully avoided as much as possible, and in this connection it should be remembered that a twisted twin lead possesses the latter quality.

Apparatus.—The unknown self-inductions L_i to be compared, with a standard L (known); non-inductive resistances r, R, Kand rhoostat RA; switch S; source of alternating current K; electro-dynamometer of which (f) is the fixed and (m) the moving coil.

Observations. — (1) Connect up as in Fig.134, the coils L_1 L_2 being together, and adjust the moving coil to zero.

Fig. 124.

(2) With Rh large close S, and adjust the current to a

convenient value, and adjust R, R' and r so as to get no deflection of the moving coil for the currents in f and m.

(3) Calculate the self-induction in terms of the standard from the relation $\frac{L}{L_i} = \frac{R + R'}{r}$, and tabulate as follows—

Speed of	Fraquency KN	Known	lles	ptano	6 B.		Duknown Belf-ind,		
Alternator (N) reval per min.	~ 1/6r edc.	Self-nd.	R.	В.	r.	liatio L/L ₁ .	L ₁ secohms.	Mean L ₁ .	

(4) Repeat 2 and 3 for different values of L, R, K' and r at constant frequency (n). Also for the former constant at different frequencies.

Motes.—When equal self-inductions are being compared it is found that the accuracy depends only on the sensitiveness of D to changes in (R + R), and this instrument may be such that it detects differences or changes of 0.01%.

If it is noticed that increase of frequency causes a diminition of the resulting value of L_1 , then the electrostatic capacity of the turns of the coils on one another is asserting itself and cannot be avoided. Considerable care should be taken to avoid this source of vitiation as much as possible, and also that due to heating of the conductors, etc. To minimize the former error, use short small wire leads, some distance apart, and not twisted twin lead.

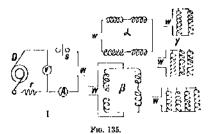
(129) Self-Inductions in Series and Parallel. Experimental Determination of Laws of Combination.

Introduction.—An electrical circuit may contain any or all of the three qualities—self-induction, capacity, and ohmic resistance. The last-named is always present, and may be combined with one or both of the former.

Let us suppose that no capacity is present, then the circuit, whether consisting of several distinct portions either in series or parallel, or a combination of these, each having its own particular self-induction and chmic resistance, possesses on the whole one definite effective value of induction and resistance, which may be termed the "combined, equivalent, or effective" self-induction and chmic resistance of that circuit composed of such detailed portions.

In alternating current work it is of great importance to know the way in which various combinations of self-inductions and chmic resistances will affect the working conditions of a circuit. The present test is devised with a view to clacidating these points for the three different forms of circuits or combinations, as follows—

(a) The self-inductions and ohmic resistances in simple series only.



(B) Self-inductions and resistances partly in parallel and in series.

(γ) ,, , , , in parallels only.

Apparatus.—Source of alternating current, preferably an independently driven alternator D, the exciting circuit (not shown) and the speed of which are under control; Siemens electrodynamometer (Fig. 251) or Parr direct-reading alternating current ammeter A (p. 572); hot wire or electrostatic voltmeter V; non-inductive rhoostat r (p. 598); switch S; speed indicator; four coils A-D to be experimented upon, as nearly alike as possible, and capable of being used with or without iron cores, which latter are also similar in all respects.

Observations.—(1) Connect up us in Fig. 1351., and adjust the pointers of all the instruments to zero, levelling such as require it.

(2) Connect coil A (only) to W (I.) and remove its iron core.

See that all lubricating cups are feeding slowly, then S being open, start D up to a convenient speed, N revolutions per minute, which must be kept constant throughout all the tests.

- (3) With (r) at its maximum, and the excitation low to start with as a precaution, close S, and adjust r and the excitation so as to give $\frac{1}{4}$, $\frac{1}{4}$, $\frac{3}{4}$, and full or maximum safe current through coil A successively at constant speed. Note the reading of the voltmeter V and ammeter A simultaneously at each, then open S.
- (4) Repeat 3 for each of the coils B, C and D singly without their cores.
- (5) Repeat 3 for the coils connected 2, 3 and 4 in series respectively, i.e. as in a.
- (6) Repeat 3 for the coils connected 2 in series and 2 in parallel, i. c. as in B.
- (7) Repeat 3 for the coils connected 2, 3 and 4 in parallel respectively, no iron cores being used in any of the cases above.
 - (8) Repeat 2-7 with iron cores in all cases, if possible.
 (9) Repeat 2-8 with an entirely different speed, and therefore
- frequency of alternating current.

 (10) Measure the ohmic resistance of each of the coils A-D by
- a Wheatstone Bridge in the usual way, and calculate the self-induction (L_0) of the coil or combination of coils from the relation

$$A = \frac{V}{\sqrt{L_o^2 p^2 + R_o^2}} \text{ amperes,}$$

where R_{\bullet} —combined or effective ohmic resistance of the coil or combination of coils obtained by employing the ordinary rules for the combined resistance of coils in series and parallel. Tabulate your results as follows—

						· · ·				
Ιđ	Ource	nt.	1 1		'	_	Impede	ner.	Belf-indi ela	ion.
Arrangement of Cu	Dynamometer	7 May	Effective ohmer Resistance of Cree	Inductance Lo P.	tan. 8 = Er. 9.	Angle of Lag F.	Meanwood 17.4 = $V(L_c, p)^2 + J_c^2$.	Calculated	Measured 2, (7/4/3-K, 5)	Calculated.

I. For pure series combinations such as (a) Fig. 135, show that $\frac{V}{A} = \sqrt{L_o^3 p^2 + R_o^2} = \sqrt{(L_1 + L_2 + L_3 + \dots)^2 p^3 + (R_1 + R_2 + R_3 + \dots)^2}$ or generally that $\frac{V}{A} = \sqrt{(2L)^2 p^2 + (2R)^2}$, and therefore that the

total effective self-induction L_{\bullet} =sum of the individual self-inductions composing the circuit,

II. For series-parallel combinations such as (β) Fig. 135, show that

$$= \frac{\frac{V}{A} = \sqrt{(L_1 + L_2)^2 p^2 + (R_1 + R_2)^2} \sqrt{(L_2 + L_4)^2 p^2 + (R_3 + R_4)^2}}{\sqrt{(2L)^2 p^2 + (2R)^2}}$$

III. For pure parallel combinations such as (γ) Fig. 135, show that

$$\frac{V}{A} = \sqrt{L_{s^{2}} p^{2} + R_{s^{2}}} = \sqrt{\frac{1}{\left(2 \frac{L}{I^{2}}\right)^{2} p^{2} + \left(2 \frac{R}{I^{2}}\right)^{4}}}$$

where I is the impedence of each parallel branch.

N.B.—In the present test it is assumed that the coils are incapable of having any mutually inductive action on one another, and consequently they must be arranged not to have such when making the test.

The Electrostatic Capacity of Electrical Wires and Cables,

General Remarks.—The condition for obtaining an electrostatic capacity is the passage of a quantity of electricity into one of two conducting bodies which are separated by an insulator. Such an arrangement constitutes what is commonly termed an electrical condenser, the two conducting bodies being called the "coatings," and the separating insulator the "dielectric" of the condenser. Now it will be obvious that any insulated electrical wire or cable in contact with earth or its equivalent will form a condenser, the inner conductor or wire and earth being the two coatings, and the insulation of the cable the dielectric. In the case of an insulated cable possessing only one core, whether

consisting of one wire or a strand of wires, we shall obtain one particular definite capacity with a definite position of the cable. In other words, the capacity will depend on the geometrical form of the wire, so that if it was coiled up in a tank of water the capacity world not be the same as if it was laid out straight on

capacity we ild not be the same as if it was laid out straight on the ground.

The actual value will depend in addition on the length and size of cable, and on the thickness of the insulation and its specific inductive capacity. The latest forms taken by cables, in which one conductor completely envelops another, but is insulated from it by a fairly uniform stratum of insulating material between the two, possess this property of having an electrostatic capacity in

a more marked degree than the simple form mentioned above. Such a concentric cable, as it is termed, possesses a definite

capacity per unit of length, and which is independent of how the cable is placed, i.e. whether coiled or straight. For continuous currents the capacity of cables or wires is of no practical importance, but for intermittent or alternating currents the case is otherwise. In submarine telegraphy the cable has naturally a very considerable capacity, while the current is intermittent; consequently when the circuit is closed so as to send a message. the cable has first to be charged by the sending battery before any current arrives at the receiving end for actuating the receiving appliances. This may take some accords, depending on the length of cable, i. s. on its expacity. Thus the effect of capacity in such an instance is a detrimental one, giving rise to what is called "inductive retardation," and diminishing the speed of signalling. Here, in the above instance, we have the case of a single cable stranded conductor of which the copper core forms one coating, the iron sheathing and water the other.

With concentric cables, it has already been remarked that their capacity is greater than with single cables for equal lengths and section of conductors in the two cases; but the former possess the advantage that whereas the "outward" and "return" leads are very close together, in fact one encircling the other, their inductive action on telegraph and telephone wires in the vicinity is practically nst, as the external magnetic field produced is very small. This is, as the external magnetic field produced is very small. This magnetic field produced by such currents alternator rapidly in

direction with the alternations of current, the inductive action of alternate current cables on such wires would otherwise be great. The capacity of a concentric cable can at once be calculated from the analogy to a cylindrical condenser as follows—

Assuming the two conductors to be both concentric and cylindrical, let R=radius of the inner surface of the outer conductor and r=radius of the outer surface of the inner one, and also let L=length of cable in continueres. Then its capacity in farads—

$$C_{F} = \frac{2 \cdot 413}{10^{13}} \times \frac{KL}{R - \log_{10} r}$$

where K=specific inductive capacity of the dielectric or insulating material, which for paper=1.86 about, for india-rubber (pure) 2.34, vulcanized 2.94, for gutta-percha 4.2, and resin 2.55 about.

It may be noticed that since $(\log_{10}R - \log_{10}r) = \log_{10}\frac{R}{r}$ the units in which the radii are measured is quite immaterial, so long as the same is employed for each; the diameters P and d corresponding to R and r, may be used instead if we like, whence we shall have the

 $\begin{array}{l} \text{Capacity} = \frac{2\cdot 413}{10^{13}} \times \frac{KL}{\log_{10}^{M_f}} \text{ Farads} = \frac{2\cdot 413}{10^{7}} \times \frac{LK}{\log_{10}^{M_f}/s} \text{ Microfarads} \\ \text{roducing this to Mfds. per mile (statute) which } = 160,933 \text{ cms.} \\ \therefore \text{ Capacity} = \frac{2\cdot 413 \times 160,933}{10^{7}} \times \frac{K}{\log_{10}^{M_f}/s} \cong \overline{5} \times \frac{K}{75 \log^{M_f}s} \right) \text{ Mfds.} \\ \text{per mile.} \end{array}$

The capacity can roudily be measured by means of the "method of mixtures" due to Lord Kolvin, and which is one of the best for the purpose. A complete digost of this and other kindred methods will be found in *Practical Electrical Testing*, p. 182, by the author, and they will not therefore be repeated here.

It may, however, be remarked that in testing the capacity of electric light and other cables by this method of mixtures the E.M.F. employed may conveniently be about 100 volts, and referring to Fig. 82, p. 184, of the above-mentioned work, the resistance ADH might be 100,000 ohms, and D connected to earth or tank if a single conductor cable is being tested. If it is a concentric cable this will not be immersed, and its two conductors at one end must be carefully insulated, while their other ends will form the two terminals of the capacity to be tested.

(130) Measurement of the Electrostatic Capacity of Concentric—or Ordinary— Catles and Condensers. (Alternating Current Method.)

Introduction .- When an alternating-current E.M.F. is placed across a condensor or, say, a concentric cable, a cortain measurable alternating current flows into the condenser or cable, even though in the latter the two conductors are quite free of all connections to lamps or any other appliance throughout their entire length. Moreover this current, which is called the "capacity current" of the cable, is not in phase or step with the periodic impressed E.M.F., but leads in advance of it, and constitutes what is called a Wattless or alls current, to distinguish it from the load or useful current which would flow in the cable when lamps or other appliances were switched on. In other words, it represents waste energy in the copper of the mains so far us the utility of the current is concerned, and the effect is always present with alternating currents. Thus it becomes of importance to know this idle or capacity current in order that its flow in the cable may not be mistaken for leakage current when no apparatus is connected to the cable.

It should also be noted that this current is out of step or phase with the main current.

The value of the capacity current in any cable can be deduced when certain constants are known. Thus--

Let A =virtual or $\sqrt{\text{mean square value of the capacity current}}$ in amperes,

 V = virtual or √mean square value of the E.M.F. impressed in volts,

between the two conductors.

C = capacity of the cable in farads,

and $p = 2\pi n$ where n = frequency of the alternating current in periods (\longrightarrow) per second,

then
$$A = \frac{V}{1} = CpV$$
 amperes, $C\overline{p}$

 $\frac{1}{U_D}$ being the effective resistance to the passage of the current or reactance of the cuble or condenser.

If C is in microfarads per mile and L = length of cable in miles,

then
$$A = \frac{CLVp}{10^6} = \frac{2\pi n CLV}{10^6}$$
 amperes, whence $C = \frac{10^6A}{LV2\pi n}$ mfds, per mile,

The present test is a very practical one and can nearly always be applied if the working pressure V is available.

Apparatus.—Cable or condenser to be tested (C); either a Siemens electro-dynamometer, hot wire or Patr anuncter A (p. 577), each of which will correct-

ly measure the $\sqrt{(\text{mean})^2}$ value of the current; an electrostatio or hot wire voltmeter (V), preferably the former; tuchomoter

for measuring the speed of the alternator D, and



from it deducing the value of (n); switch S.

Observations. -- (1) Connect up as shown in Fig. 136, and adjust the pointers of V and A to zero, carefully levelling them if necessary,

(2) Carefully "free" and insulate the far end of the cable, and prepare the near end so as to make contact with the two conductors I and II.

Note.—If a condenser is being tested I and II will now be its terminala

- (3) Close S, and with D running at constant speed take some six or eight widely different values of V by altering the excitation of D, and note the corresponding values of A simultaneously with Y.
- (4) Next run D at six or eight different speeds, keeping V constant by altering the excitation, and note the corresponding reading on A for each speed,
 - (5) Calculate the capacity tested from the relations---

$$C = \frac{10^{s} \Lambda}{V 3\pi n} \text{ mfds. for a condenser,}$$

value.

 $C = \frac{10^0 A}{LV^2 - n}$ mfds, per mile for a cable,

and tabulate as follows-

	NAME.				Darm						
Cable to Conden	ntod:Ty ker: Ty	₽6 pr		COT	Size Unelectri	Insulation					
					Сит	rnt.	Cnpec	nty of			
Length of Cable	Speed of Alter-	quency (F) per nec.	Volts F.	luctive cranos	libe ment	, pr	enser Itda,	able Mfds. per man.			
(L) unice.	anter.	£ }	Þ	i i i i i i i i i i i i i i i i i i i	Read Tottur	३`	Com	Cable			
	<u> </u>				i '-	<u> </u>	1				

(131) Measurement of the Electrostatic Capacity of Short Lengths of Submarine

and Electric Light Cables. (Kelvin Dead Beat Multicellular Voltmeter Method.)

Introduction.—The effects of electrostatic capacity in a cable on the intermittent or alternating currents flowing in it have already been mentioned (vide p. 370), consequently it is desirable to obtain the value of its capacity. The following is a convenient and accurate method of measuring the capacity of any insulated conductor comprising a short length of submarine, telephone, teleparaph, or electric light cable, and its great advantage lies in

the fact that it is applicable to short lengths.

The method, which is very analogous to the "Siemens subtraction method," except that only one deduction is made, consists in charging a standard known condenses to a measured potential and observing the fall of this on connecting the cable as a condenser in parallel with it. The condition for maximum accuracy, i.e. when a slight error in reading the diminished value of potential has least effect on the final result, has been shown to be when the standard capacity is equal to that of the unknown, or when the diminished potential = half the original

For accurate work it is necessary to employ two or three small corrections—one arising from the multicelinlar voltmeter possessing a small capacity itself which varies with the deflection of the suspended needle vanes, being less for smaller deflections. It is of the order of about 10⁻⁶ mfd, and in most cases can be neglected in comparison with the capacity of the standard and cable to be tested, at least when these are of the order of 0-01 mfd, or greater. When, however, extreme accuracy is required, the potential-capacity curve of the voltmeter, which is supplied by the makers, must be referred to, and the capacities of it, for the deflections obtained, taken into account.

Another correction is for loss of charge due to leakage occurring in the voltmeter, condenser, and cable; since during the time taken for the needle of the multicellular to come to rest after entting off the battery or charging E.M.F. and putting the cable in parallel, the potential may have fallen owing to leakage.

It may therefore be necessary to determine the leakage of the voltmeter, cable, and condenser, which can be done as follows—

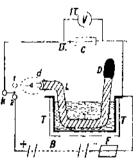
- (a) Chargo the voltmeter to some conveniently large potential, and take readings of potential and time after disconnecting the charging source. Then the curve plotted with potential as ordinates and time as abscisse shows the rate of fall of potential at any time after the disconnection of the charging source.
- (b) Join the voltmeter and standard condenser in parallel, and repeat the preceding operations. Then the leakage from the condenser will be given at any time by the difference of the ordinates of the curves in a and δ.
- (c) Join the voltmeter and cable in parallel and again repeat.

 From these results leakage of the cable can be found at any time
 by subtracting the ordinates of the curves in a and c.

Preparation of Cable Ends.—The free ends of the cable should be bared of the outer insulation down to the pure rubber for a space of some $2\frac{1}{2}$, and the rubber itself pared or tapered with a clean sharp knife for a length of about $1\frac{1}{2}$ " from the end; the ends should be carefully dried over a spirit lamp. One end should then be repeatedly painted with melted paraffinwax (for some $3\frac{1}{2}$ " from the end) heated to a temperature not exceeding 100° C. by means of boiling water. The other end of the cable after having a short well-insulated gutta-percha wire soldered to the copper core should be treated in a similar manner.

This method of preparation if carried out carefully will prevent all end leakage.

Apparatus.—Kelvin dead beat multicellular electrostatic voltmeter V (Fig. 240); Kelvin standard air leydeu or condenser C



F10. 133

(p. 616); cable L to be tested immersed in a metal-lined water-tank T; highly insulated two-way key K(p. 586);

battery B giving an E.M.F. of something like 100 volts;

and a fine fuse F to act as a safeguard in case of accidental short circuit in the condenser

Observations. — (1) Carefully prepare the ends of the cable as indicated above and immerse the cable in the tank

T, taking care not to allow the

or voltmeter.

prepared ends D and d to get wet; these must be trained up out of the water.

- (2) Connect up as in Fig. 137, taking care that the insulated terminal I.T. of both V and C are joined as shown. Adjust the pointer of V to zero if necessary and see that a fine fuse is in F.
- (3) Press K to 2 to charge V and U, and note the reading V_1 on the voltmeter when steady and then release K. Now observe the reading for one or two minutes to see if there is any sensible less due to imported insulation in V or C, and if so, whether it is
- small enough to neglect.

 (4) Close K to 1, and in fifteen to twenty seconds, which is usually long enough, note the steady diminished reading V_2 on
 - the voltmeter.

 (5) Repeat 3 and 4 with different charging E.M.F.s, and calculate the capacity of the cable L from the relation—

$$C_L = \frac{C_a (V_1 - V_3) + V_1 K_1 - V_2 K_2}{V_2}$$
 mfds.

where $C_e = \text{standard capacity, in this case 0.0025 mfd., and } K_1K_3$ the capacities of the voltmeter at potentials V_1 and V_2

ELECTRICAL ENGINEERING TESTING

377

Names...

Bitandard Capocity: Type ... Capacity = ... mt/4.
Cable tested: Type ... Leugth (/) ... Insulation ...

	Volt	gus.	Capacity of	Voltmeter.	Capacity of Cable,			
R.M.F. nvel to Charge.	Instal Y _I ,	Final F ₂ ,	# ₁ at 1' ₁ ,	Kg at Fg.	\mathcal{O}_L Nide.	$\frac{C_L}{l}$ MAI.		
					ļ			

.

(132) Measurement of the Electrostatic Capacity of a Concentric Cable Ballistically. (Standard Magneto Inductor Method.)

Introduction.—When some standard form of magneto inductor is available, the form devised by Dr. W. Hibbert being a very convenient and casily manipulated one, the capacity of a concentaic or other electric light cable can be readily determined, providing a few other additional pieces of apparatus are available. The reader should note the general introductory remarks on p. 369 concerning the capacity of cables in general, and also those of the alternating current method of measuring the capacity of cables.

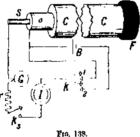
The research test can be employed for finding the capacity of

The present test can be employed for finding the capacity of cables in tanks and of ordinary and concentric mains. As, however, the former are best

tosted by the "method of mixtures" (p. 371), we shall here only consider the test of a concentric cable by this inductor method.

Apparatus. — Standard inductor to be tested *I* (Fig. 138); scusitive ballistic galvanometer *G*; concentric cable to be tested *G*, of which *F* is the free

and well-insulated end, S the inner conductor, and O the other; box of known resistances r; battery B, of known E.M.F., or, if this is unknown, a standard rollmeter to measure the P.D.; two-way spring



tapping-key K (p. 586); ordinary spring tapping-key K,; damping-coil with its cell and key.

Observations.—(1) Connect up as in Fig. 138, and adjust the galvanometer needle to zero, carefully prepare the free (far) end

- of the cable, viz. F, in the manner described on p. 375, and also the (near) end as well; by so doing the vitiation of the results from leakage across the cable ends will be avoided.
- (2) K1 and K2 being open, adjust r to a low value, such that pressing K_3 nearly a full-scale throw d_1 is obtained on slipping down I. Note this value of d_1 and the bex resistance r ohms.
- (3) K, being open, adjust the voltage of the battery B to such a value that on closing K2 for two or three seconds, then opening it, and immediately closing K1, a first throw d_{c} is obtained

on discharging C_i as nearly as possible equal to the former. N.B.—Two or three throws should be taken in both 2 and 3, and the means noted as being more accurate.

(4) Obtain the mean throw on the charge in a similar way by first closing K1 for a few seconds so as to completely discharge C, and then opening it and closing K2 afterwards.

Note.—Care must be taken that C is each time discharged before taking the charge throw.

- (6) If possible employ three or four different voltages and repeat 2 and 3 with each of them, keeping the deflections di and $d_{\mathcal{C}}$ about equal to one another, preferably by varying r to suit.
 - (6) Calculate the capacity of the cable tested from the relation $C = \frac{FN}{100 \ VR} \cdot \frac{d\sigma}{dx} \text{ microfarads,}$

where
$$F = \text{total magnetic flux in the air-gap of the inductor and}$$

R =total resistance in ohms of the inductor circuit,

Tabulate as follows—

NAME . . . Standard inductor . . . ; turns H=0 , . . ; resistance $r_{K}=0$, . ohum. Galvanometer resistance $G = \dots$ olumns; Total Flux $F = \dots$ C.G.S. lines Cable tested : Type . . . Maker . Heation (for reference only) = . . , eq. ins, Length of Cable & a . . . miles.

Mest thre		Reels	tance in Ohnu.	P.D. Sf variable V.	Capacity to Microfarada	Kean Consulta	Capacity of Cable in Mids.		
d _i .	ě,	In box	Total $R = \tau + \tau_R + G$.		C.	C.	per ipile		

Inferences.—Show how the relation given in 6 can be obtained, and state any assumptions made in obtaining it. Is any correction required for greater accuracy in the relation for C?

(133) Measurement of the Electrical Power absorbed in Alternating Current Inductive Circuits. (Three-voltmeter Method.)

Introduction.—The measurement of alternating current power depends on the nature of the external circuit. Thus, if this circuit is non-inductive, then the true power W = amps. $(A) \times \text{volts } (V)$, the former flowing in the external circuit at a terminal potential difference (V).

If the circuit is inductive, and every circuit is to some slight degree, then $W = AY \cos \theta$, where $\theta =$ angle of phase difference of the current A behind the voltage Y and the product $(A \times Y)$ is called the apparent power absorbed.

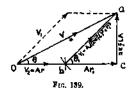
The measurement, therefore, of this electrical power accurately is more difficult than that in the case of a direct current circuit, using to the effects of self and mutual induction and capacity which appear in alternate-current (A-C.) working. In such a case a Wattmeter may be used, but it must be practically non-inductive to give accurate results. Another method to employ, which will give accurate results even though most of the circuit is highly inductive, is that known as the "three-voluncter method," and it has the advantage that only one A.-C. voltmeter is required, though three similar ones may be used if available. By it the true power absorbed by the circuit may be obtained with any degree of accuracy desired by using an accurately graduated voltmeter, and by carefully repeating the readings two or three times and noting the mean in each case.

The three-voltmeter method, which was simultaneously suggested by Prof. Ayrton, Dr. Sampner and Mr. Swinburne, gives a true measure of the power given by any current, whether harmonic or otherwise, to any circuit, inductive or not. It has the disadvantage that, as the differences of squares of quantities is being taken, a small error in the quantities themselves may make a considerable error in the final result, especially if the angle of lag θ is large.

The voltmeter used must be such as will not after the voltage across the points to which it is applied. In other words, it must have a high resistance compared with that between these points,

An electrostatic voltmeter most accurately fulfils this condition, but if a hot-wire voltmeter is used (of relatively low resistance), the main current must be *large* compared with its own current, or an error will thus be introduced.

With this apparatus we are in a position to investigate the following important characteristics of an inductive circuit formed



by, say, a choking coil or the primary of a static transformer, etc., namely—

- (1) The true power absorbed in the whole and each part of the circuit.
- (2) The angle of phase difference between the current and both the supply and choker voltages,
- (3) The impedance, ohmic, and inductive resistances, and self-induction of the choker.

The vector diagram for the circuit PR is that shown in Vig. 139, and is constructed as follows: set off a vector on equal to the total voltage V across PR to any convenient scale. With radii $ob = V_1$ and $ba = V_1$ and centres o and a respectively, draw area intersecting at b, join b to o and a and produce ob to meet a perpendicular from a in the point c. Then oba is the triangle of E.M.F.s for PR, and bca that for PQ where r_1 and L are the ohmic resistance and self-induction of the inductive portion PQ. Since QR is non-inductive, the current A and voltage V_2 are always in phase, and hence by Ohm's law $V_3 = Ar$ where (r) is the ohmic resistance of QR, and co will be coincident with the current vector. Thus θ will be the angle of phase difference

between the current (A) and total voltage V_1 , while θ_1 will be that between A and the voltage V_1 .

Note,—Errors in V, V_1 or V_2 or in the graduation of the voltmeter scale, will have least effect on the result when $V_1=V_2$ which is the condition for maximum accuracy, and the resistance r of QR should first be adjusted if possible to obtain this condition.

Should the non-inductive resistance QR not be accurately known, or be likely to alter in value through heating due to the passage of the current A, then its equivalent in terms of V_2 and A can be substituted in the formula. Hence, if A is the $\sqrt{\text{mean equare current in amps as given by a Siemens dynamometer or other direct reading alternating current ammeter, we shall have$

$$W = \frac{A}{2V_g} \left\{ V^2 - V_1^2 + V_2^2 \right\}$$
 Watts,

for the true mean power given to the whole circuit PR, QR may consist of a bank of electric glow-lamps, as the resistance r of QR can vary if it likes with the different mean currents.

It can easily be shown, in like manner, that the true mean power given to the inductive portion PQ of the circuit is

$$W = \frac{1}{2r} \left\{ V^2 - V_1^2 - V_2^2 \right\} = \frac{A}{2V_2} \left\{ V^2 - V_1^2 - V_2^2 \right\}$$

The method is not based on any assumptions as to the nature of the current (whether periodic or otherwise) or of the circuit, which may contain either self or mutual induction, and capacity, or all three. It is based solely on the difference in phase between the current and voltage.

If θ = angle of phase difference or lag of the current behind the voltage, then if both are sine functions

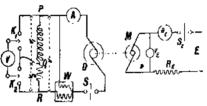
cos.
$$\theta \simeq \frac{V^2 - V_1^2 - V_2^2}{2V_1V_2}$$

Apparatus.—Alternator D and its exciting circuit; inductive portion PQ of the circuit in series with a strictly non-inductive portion QR; two 2-way keys $(K_1$ and K_2) $\{p. 587\}$; an A,C, voltmeter (V); main switch (S); A,C, ammeter (A). For comparison of methods, A may be used, and also a non-inductive Wattmeter W for measuring directly the power used up in PR. Fraquency water f connected across the supply D.

In the electrical circuit of the motor M may be used a voltmeter V_B ; animeter a_B ; switch S_B ; rheostat R_B ; source of continuous current E.

Experiments.—(1) Connect op as shown in Fig. 140. Adjust the pointer of all the instruments to zero, levelling such as need it.

- (2) See that all lubricators in use feed properly, then start D, running slowly.
- (3) Adjust its speed so as to get \(\frac{1}{2}\) of the max. \(\sime\) per sec., at the same time varying the excitation of \(D\) to alter its voltage \((V)\), so

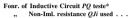


Frg. 140.

as to send a convenient current (A) through PQ. Note A, and in quick succession (the speed being constant) the voltages V, V_1 and V_2 , across PR, PQ, and QR. (See Note above.)

- (4) Repeat 3 for about 5 frequencies between the max, and min. values possible, using the same current A in each case by suitably altering the excitation.
- (5) Repeat 3 at a constant frequency of about normal for five different current values, rising by equal increments up to the maximum allowed, by varying the excitation.

Tabulate your results as follows-



		Vo	ltflgC	В.	Pov	wer in	Wat		orbed	Pov Fact			From li.Tul		Ohi lie					
c	1 4				PR.	PQ	QR	Bv (PR. EV epi- tion.	PR.	PQ.	_	le of		PQ.	QR.		* 5	a, 1	Л
Frequency	l ≺	v. ~~	VI	V-i	а	£ I I	•	*] * s * s 3 3	*	>\ y 8 V	I 1	0 °	0 _L *.	3	r0>0 X	1	.5 a ¥ ∓	5	P b- a 3>	71

(G) Plot curves having values of A as abscissas with values of \mathbf{r}_{it} cos $\mathbf{0}_{X}$, \mathbf{X} , $\frac{\mathbf{y}}{A}^{-1}$ and \mathbf{w}_{lt} respectively, for the inductive purtion

PQ as ordinates.

- (7) Draw the vector diagram (Fig. 139) for the maximum current used.
- (8) Compare V with the algebraical sum (|| \mathbf{f} V_2), also W with w.

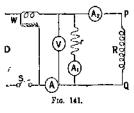
Inferences.—Prove the formula in column 7, and state any assumptions made in deducing it. What can be inferred from the results of the test and from the curves?

(134) Measurement of the Electrical Power absorbed in Alternating Current Inductive Circuits. (Three-Ammeter Method.)

Introduction.—This method, though inferior to that of the Wattmeter, is nevertheless instructive, and therefore a brief remmt of it will be given here. As will be seen, it is very similar to the 3-voltmeter method of measuring power, the formulae in the two cases being strikingly similar. There is, however, one chief difference between the methods, namely, that practically three ammeters are, necessary for a satisfactory test, as large errors

may occur if only one ammeter is employed and interchanged between the circuits, while in the case of the allied method one voltmeter can easily be made to do and no appreciable error need be introduced. The actual arrangement is shown in Fig. 141, in which PQ represents the circuit in which it is desired to measure the power taken up, A, A, and A, are three non-inductive ammeters, at least A, should be of this nature, while (r) is a noninductive resistance connected as shown, and which is large compared with that of A,

> Greatest accuracy will be obtained when $A_1 = A_2$, and under these conditions it will be seen that (r) consumes about as much power as Q. Henco twice as much power has to be available at the source for operating this



method as is taken up in PQ, but practically no excess voltage is needed in this case as it was in the 3-voltmeter method. If $w_2 =$ the power in Watts absorbed by PQ, then

$$w_1 = \frac{1}{2}r\{A^2 - A_1^2 - A_2^2\}$$

$$\cos \theta_1 = \frac{A^2 - A_1^2 - A_2^3}{2A_1A_2}$$

and

where $\theta_1 =$ angle of lag of the current A_2 in the inductive circuit PQ behind the terminal voltage.

It will thus be seen that the method is based on the difference of phase of the various currents, and, as in the 3-voltmeter method, a small error in observing the currents introduces large errors in the answer. The possibility of such occurring can be minimized by using accurately calibrated non-inductive ammeters and taking the mean of three or four similar readings at each value of, say, A. If the value of non-inductive resistance (r) is not occurately known, or if it is liable to alter through heating due to the passage of the current, then its equivalent value $\frac{V}{A_1}$ may be used instead in the formula, which will therefore become - $W = \frac{V}{2A_1} \left(A^2 - A_1^2 - A_2^2\right) \text{ Watts,}$

$$W = \frac{V}{2\overline{A_1}} \left(A^2 - A_1^2 - A_2^2 \right)$$
 Watts,

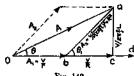
Ab > 2

where V= the voltage across the extremities of PQ. There is no objection to using a bank of incandescent lamps for (r), since the resistance may vary if it likes with the different mean current strengths. It will be observed that if the resistance of A_2 is appreciable, an amount of power may be absorbed in it which is comparable with that in PQ. In such cases the former must be deducted from the result as given by the above relation in order to obtain the true power absorbed in PQ alone.

If (r) is accurately known we may dispense with A_1 and put (r) directly across the mains, then on placing a voltmeter (preferably an electrostatic one) across the mains as in the last instance, we may substitute the value of A_1 in the first formula, when we shall have

$$W = \frac{1}{2}r\left\{A^2 - \left(\frac{V}{r}\right)^2 - A_2^2\right\}$$

The preceding remarks will be understood more clearly from the vector diagram, Fig. 112, for the circuit of Fig. 141, constructed



F10. 142.

as follows: set off a vector oa equal to the total current A in the main line to any convenient scale with radii $ob = A_1$ and $ba = A_2$ and centres o and a respectively, draw area intersecting at b. Join b to o and a and produce ob to meet a perpendicular from a in the point c. Then oba is the vector triangle of currents for the main and both branches altogether, while bca is that for the inductive branch only. Since r is non-inductive, its current A_1 and voltage are always in phase, and hence by Ohm's law $A_1 = \frac{V}{r}$. If R equals the ohmic resistance of PQ and L the self-induction, then the energy or magnetizing component of the current A_2 in PQ while is in phase with the voltage od across it, is $bc = \frac{V}{R'}$ while the idle or wattless component of the current A_2 in quadrature with the

" voltage V is ca. The angle of phase difference between the main current A and V will be θ , and that between A_2 and the same voltage I across PQ will be θ_1 .

$$A_2{}^2=A^2+A_1{}^2-2AA_1\cos\theta,$$
 but $A_1=\frac{V}{r}$ by Ohm's law, and

$$A_2^2 = A^2 + A_1^2 - 2A \frac{V}{T} \cos \theta,$$

and $AV\cos\theta =$ total power given to the whole parallel circuit.

 $10 = V \times 0c = \frac{9}{10}(A^2 + A_1^2 - A_2^2)$ watts,

the power absorbed in the non-inductive branch
$$w_1 = A_1^2 r = A_1 l'$$
 watts,

and the power absorbed in the inductive branch

$$w_2 = V \times bc = \frac{r}{5}(A^2 - A_1^2 - A_2^2)$$
 walts,

where the power factor for the whole circuit =

$$\cos \theta = \frac{A^2 + A_1^2 - A_2^2}{2AA_1} = \frac{r(A^2 + A_1^2 - A_2^2)}{2AA^2},$$

and the power factor for the inductive circuit
$$PQ = \cos \theta_1 = \frac{A^2 - A_1^2 - A_2^2}{2A_1A_2} = \frac{r(A^2 - A_1^2 - A_2^2)}{2\sqrt{1}A_2}$$
.

In this three-ammeter method the non-inductive parallel branch is equivalent to an added current, while in the threevoltmeter method the non-inductive series resistance means an added voltage. Both methods, therefore, require the supply of practically twice as much power as that needed for the circuit under test. Further, the losses in the ammeters, voltmeter, and wattmeter may cause serious errors in the results if the currents

method for measuring power if a waltmeter was available, except from a purely scientific interest. While the power absorbed and phase difference may be calculated in each method from the vector diagram, constructed for each set of readings, it would usually be obtained from the respective formulae. **Apparatus.**—That indicated in Fig. 141, where D is an adjust-

are small. For the above reasons, no one would use either

able source of alternating current, preferably a motor-driven alternator, the frequency, current and voltage of which can be varied independently. A voltmeter V is connected across the parallel combination, and a wattmeter inserted so as to measure the total watts absorbed in the parallel combination merely for the comparison of the three-ammeter and wattmeter methods.

Observations —(1) Connect up as in Fig. 141, levelling and adjusting to zero such of the instruments as need it.

(2) See that all lubricating arrangements are in operation

on starting up.

(3) Adjust the speed to get maximum frequency, and also the voltage V of the alternator (by varying its excitation) so as to send the maximum safe current A_2 through PQ_1 and note in rapid succession the readings of A, A_3, A_4, W and V.

Note.—If possible adjust the non-inductive resistance r so as to obtain the conditions for maximum accuracy (other things being the same) of $A_1 = A_2$.

- (4) Repeat (3) for about six different frequencies between the maximum and minimum values possible, using the same current A₁ in each case by suitably adjusting the speed and excitation of the alternator.
- (5) Repeat (3) at constant maximum frequency for about six different values of current A_2 between the maximum and minimum values possible by varying the excitation, and tabulate your results as follows—

	Cui	rrenta	Po	mer.	In Wa		beo:	rbed	Par Fact	wer bej (n	Mat	Front L T41	ly'ere	Res	of		
	Ī		Pt + 1	?	PŲ	Hy	Cal Cal	;} leu-	PQ +1,	PQ.	A TIL	le of g an		۴.	rq	of (PQ)	ou British
Toltage V.	л.	41.	Wattmeter 1F,		$V_2 = \frac{V}{2A_1}(A^2 - A_1^2 - A_2^3)$	ón + in = a	* - AV coa 6.	$w = \frac{V}{2A_1}(A^4 + A_1 - A_2)$	Con 9 = 4" + 41" - 42"	Cos $\theta_1 = \frac{A^2 - A_1^2 - A_2^2}{2A_1 A_2}$	6 °.	θ _ι »,	Tan 6,	<u>.</u> [₹	R .	Cost, of Self-Ind o	201

- (6) Plot curves having values of A_2 as abscisse with values of $V_1 \cos \theta_1$, $L_1 \frac{V}{A_2}$ and w_2 , respectively, for the inductive portion PQ as ordinates.
- (7) Dray the vector diagram (Fig. 143), for the maximum current used.
- (8) Compare the value of A with the algebraical sum A₂ + A₃; also W with w.

Inferences.—What can you infer from the results of the test and from the curves?

(135) Measurement of Power in Three-Phase Alternating Current Circuits.

Introduction.—The measurement of the electrical power absorbed in a 3-phase alternating current circuit might well at first sight appear somewhat complicated. In reality, however, it is very little more so than in the case of single-phase circuits and the actual extent to which it is, depends mainly on the nature of the circuit in which the measurement is being made. It has already been seen that the non-inductive Wattmeter forms the best means of obtaining the true power absorbed in a single-phase circuit, but with multiphase circuits usually, though not always, two such instruments are necessary.

The object consequently of the present investigation is not only to state the methods of measuring, but also to prove the truth of them under the several distinctive conditions met with in practice.

The circuit in which the power has to be measured may be of the type shown at (a) Fig. 113, which is known as the star or open form, or of the type shown at (b) Fig. 143, known as the mask or closed form. (c) represents the circuit containing the measuring instruments, which may be connected to either (a) or (b) arrangements at will, E being the source of polyphase supply.

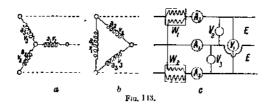
Now let $A_1 A_2 A_3$ and $a_1 a_2 a_3$ be the $\sqrt{\text{mean square values of }}$ the currents flowing in the mains and branches respectively for Fig. 143(b and c), also $V_1 V_2 V_3$ and $v_1 v_2 v_3$ the same values of voltages across the mains and branches respectively for Fig. 143(b and c); then if the mains are equally leaded we have—

$$A_1 = A_2 = A_3$$
, and $A_1 = a_2 = a_3$, and $V_1 = V_2 = V_3$,

whence $A_1 = 2a_2 \sin 60^{\circ} = \sqrt{3}a_3$, and $\therefore A = \sqrt{3}a_3$ since the mains are equally leaded and the load non-inductive.

For Fig. 143 (a and c) we have, if $A_1 = A_2 = A_3$ and $E_1 = E_2 = E_3$, that $A_1 = a_1$, $A_2 = a_2$ and $A_3 = a_3$, and since V will now key 30° in phase behind r, in each main and the corresponding branch circuit, we have $V = 2v \sin$. $60^\circ = \sqrt{3}v$, providing the load is non-inductive.

CHOURTS EQUALLY COADED AND NON-INDUCTIVE.—Here if each main carries the same current A, and if the pressure between



each pair of mains = V, then the True Power absorbed in a non-inductive load, Fig. (b)

$$W = 3av = 3V \frac{A}{\sqrt{3}} = \sqrt{3}AV \text{ Watts,}$$

True Power absorbed in a non-inductive load, Fig. (a)

$$W = 3av = 3A \frac{V}{\sqrt{3}} = \sqrt{3}AV \text{ Watts.}$$

If, however, the load is inductive, then if θ =angle of phase difference between voltage and current, we have, as in the case of single-phase work, that for equal load the True Power absorbed in the inductive load, Figs. (a) or (b)

inductive load, Figs. (a) or (b) $W = \sqrt{3}AV \cos \theta \text{ Watts}.$

This latter can best be obtained by means of the non-inductive Wattmeter for each of the two following conditions met with is practice.

CIRCUITS EQUALLY LOADED AND INDUCTIVE—ONE WATTHETER ONLY needed to obtain the true power. Assuming this to be W_1 , Fig. 143(ca) or (cb), then with the thick coil in any main (A_2 say, as shown) note the Wattmeter reading (w_1) with its fine coil on

to main A_1 , and the reading (w_2) with it on to main A_2 immediately after, then the True Power absorbed in the equally loaded inductive circuit $W = w_1 \pm w_2$, where both w_1 and w_2 will vary with load and power factor.

The region why w_1 or w_2 alone does not give the power of the circuit is because A_3 and V_2 are not in phase, even in a non-inductive circuit, but differ in phase by an angle $= 30^\circ \pm \phi$, for both star and mesh connections. Therefore W_1 will read the product A_3V_2 , $\cos 30 = \frac{\sqrt{3}}{2} A_3V_2$ for unity power factor. Thus we see that $w_1 = A_3V_2$ cos $(30^\circ + \phi)$, and $w_2 = A_2V_3$ cos $(30^\circ + \phi)$, and the sum of these after expansion $= 2A_3V_2$ (cos $30^\circ + \phi$) and the sum of these after expansion $= 2A_3V_2$ (cos $30^\circ + \phi$) $= \sqrt{3}A_3V_2$ cos $\phi = w_1 + w_2$, which is the true power in the circuit. If now the lead is so highly inductive that ϕ exceeds 60° , i.e. the power factor $\cos \phi$ is less than 0.5, then $\cos (30 + \phi)$ becomes - w, and the wattmeter will reverse for one of its readings w_1 or w_2 , which must therefore be considered as - w since the volt-coil connection must be reversed to get a

- scale reading. ... the total power $B' = w_1 - w_2 = 2A_1V_1 \sin 30^\circ \sin \phi$ $= 24 \text{ ff.} \times 4 \sin \phi = V_1 \times 4 \sin \phi$, and $\frac{V_2}{2} \times \frac{A_3}{2} \sin \phi$
- = $2A_3I_2 \times \frac{1}{2}$ sin $\phi = V_1 \times A_3$ sin ϕ , and $\frac{V_2 \times A_3 \sin \phi}{I_2} = A_3 \sin \phi = the$ wattless or idle line current.
- The above results will be readily understood by a reference to

Fig. 144 (corresponding to Fig. 143, a and c), in which OA, OB_1 OC, represents the voltages across the respective star stator phase windings in magnitude and phase difference (= 120°), AC, CB, BA = voltages V_1 , V_2 , V_3 between mains in relative magnitude and phase (= 120°).

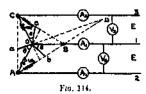
Then obviously $V_1 = AC = \sqrt{3} \partial A = \sqrt{3} \partial C$, also $V_2 = CB = \sqrt{3} \partial C = \sqrt{3} \partial B$, and $V_3 = BA = \sqrt{3} \partial B = \sqrt{3} \partial A$.

Now, since the three phase-windings are inductive we can draw three equal lines, Oa, Ob, Oc, to represent the currents in them lagging in phase by equal angles θ behind their respective voltages OA, OB, OC.

Then the current 0a in its phase winding differs in phase from the voltage $AB (= V_2)$ by an angle $aDA = \theta - 30^\circ$, and the

current θb in its phase winding differs in phase from the voltage $BG (= V_2)$ by an angle $\theta c B = \theta + 30^\circ$.

Now, if the current coil of wattmeter w_1 is in the circuit of ∂C_1 and hence of main 3, with its volt coil across CB (mains 3 and 1), it will carry the current C at a voltage V_{\bullet} . Similarly the current coil of wattmeter w_{\bullet} in the circuit of ∂A_1 and hence



of main 2, will carry the current Oa with its volt coil across AB (mains 2 and 1) at a voltage V_3 .

Then
$$w_1 = A_3 V_2 \cos(\theta - | -30^\circ),$$

 $= A_3 V_4 (\cos \theta \cos 30^\circ - \sin \theta \sin 30^\circ),$
and $w_2 = A_2 V_3 \cos(\theta - 30^\circ)$
 $= A_2 V_3 (\cos \theta \cos 30^\circ + \sin \theta \sin 30^\circ).$

... total power of the circuit $W = w_1 + w_2 = 2AV$ (cos θ cos 30°) = $\sqrt{3}AV$ cos θ , on the assumption that $A_1 = A_2 = A_3 = A$, and $V_1 = V_2 = V_3 = V$, which should be the case.

By adding and subtracting the values of w_1 and w_2 first given we have

$$\frac{w_1-w_2}{w_1+w_2} = \frac{1}{\sqrt{3}} \tan \theta, \text{ and putting } \frac{w_2}{w_1} = a$$

we have the power factor

$$\cos \theta = \frac{a+1}{2\sqrt{a^2 - a + 1}} = \frac{1}{\sqrt{1 + 3(\frac{w_1 - w_2}{w_1 + w_2})^2}} (\text{sec p. 399}),$$

when $\theta = 0$ the values of w_1 and w_2 are equal, and each $= \frac{1}{2} \sqrt{3AV} \cos \theta$.

As θ increases, w_1 decreases and w_2 increases, when $\theta = 30^{\circ}$ the value of $w_1 = \frac{1}{2}A_2V_3$ or $\frac{1}{2}AV$, and of $w_1 = A_1V_3$ or AV; when $\theta = 60^{\circ}$ the value of $w_1 = 0$, and of

$$w_2 = \frac{\sqrt{3}}{4} A_2 V_3 \text{ or } \frac{\sqrt{3}}{4} A V_4$$

Since in this case the current in the series coil of w_1 differs 90° in phase from that in its pressure coil, any further increase in θ will make w_1 negative and reverse its deflection, so that the connections of one of its coils must be interchanged in order to bring the deflection on to the scale again.

Hence in measuring the power of any inductive 3-phase circuit by either 1 or 2 wattmeters the total power = $w_1 + w_2$, i.e. if one of the readings reverses, substruct the smaller reading from the larger one to obtain the total power.

CIRCUITS UNEQUALLY LOADED AND INDUCTIVE—Two WATT-METERS ONLY needed to obtain the true power. Assuming the Wattmeters to have their thick coils in any two mains, as shown in Fig. 143c (a or b), then True Power absorbed $W = W_1 + W_2$.

Hence, when merely the true power in Watts only is required in a three-phase circuit, whether of the star or mesh type, one or two Wattmeters are required according to whether the circuits are squally or unequally loaded respectively. Also when such a three-phase circuit is both equally loaded and non-industive the

true power in Watts is given by the product $\sqrt{3} \times \text{amps}$, in one main \times volts, across any pair of mains. (See p. 395 et seq.), Apparatus.—Source of three-phase alternating current (K) and

circuit of variable nature to experiment upon (a and b, Fig. 143). Two Wattmeters W_1 and W_2 ; three Siemens dynamometers or Parr direct reading dynamometer ammeters $A_1 A_2 A_3$; three electrostatic or hot-wire voltmeters $V_1 V_2 V_3$.

Note.—It must be remembered that for any specific measurement, the foregoing rules, and the instruments they entail, can be at once used without reference to the following test, which is devised solely in order to prove these rules.

Observations.—(1) Connect up as in Fig. 143 (a and c), and adjust the instruments to zero, levelling them if necessary.

(2) With the load non-inductive and the circuits equally loaded, take the readings of all the instruments for five or six different loads, noting the Wattmeter reading when placing the fine coil of, say, W₁ successively on to A₁ and A₂ mains at each load,
(3) With an inductive load and circuits equally loaded, take the

readings of all the instruments for five or six loads, placing the fine coil of, say, W₁ successively on to A₁ and A₂ mains at each load and noting its reading at each. Tabulate your results as follows—

<u> </u>	8 4	Waite	netors.	Vo	ltmet	ers.	Ar	omete	TR,	15-		TP' _
E S	5 P. S.	В.	h. ³ .	F1.	i'b	P ₃ .	A ₁ .	A2	A ₃	W1+ W2	2 11/1.	Jäap.
		 	<u> </u>					_				

Inferences.—State very clearly all that can be inferred from your experimental results.

Measurement of Power in Two-Phase Alternating Current Circuits.

Introduction.—Two distinct forms of circuits are met with in the distribution of electrical energy by means of two-phase alternating currents of electricity.

The first entails the use of four wires, forming two circuits completely independent of one another, one to each phase. Since this requires four wires it is usually employed in short distance transmissions.

The second entails the use of only three main wires, and is therefore more economical in first outlay of copper than the above. It will therefore be at once obvious that the measurement of power in two-phase alternating current circuits will be made in more than one way, depending on the form and nature of the circuit in question. We will now deal with such measurements in the case of each possible condition.

TWO-PHARK CIECUITS OF THE 4-WIRE FORM.

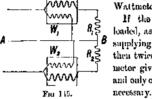
Here two cases are possible according to whether the circuits are carrying non-inductive loads, such as incandescent lamps, or inductive loads, such as two-phase motors or transformers, etc.

Non-inductive load.—The product of the amperes and volts in each circuit, obtained in the usual way, when added together gives the true power delivered from the generator; and if the two circuits are equally loaded, twice the PRODUCT for one circuit gives the Total True Power.

Inductive load.—Owing to the lag in phase between the current and voltage in each circuit, two non-inductive Wattmeters are necessary, one in each circuit, connected up in the ordinary way

as in single-phase circuits. Then the Total True Power delivered by the generator = sum of the two Wattmeter readings.

If the two circuits are equally loaded, as should be the case when



tourier, as should be the case when supplying such as two-phase motors, then twice the reading of one Wattmeter gives the Total True Power, and only one such instrument is then

Two-Phase Circuits of the 3-wire Form.

Here also there are two or three cases depending on whether the circuits are inductive or otherwise.

Equally lowed non-inductive sections.—Total True Power absorbed = twice the product of the current in one outer main and the voltage across the section.

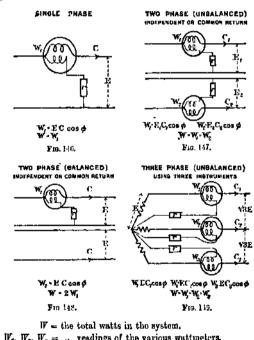
Equally loaded inductive sections.—Total True Power absorbed twice the reading of a Wattmeter connected with its thick coil in series with either outer main, and its thin coil connected to the centre or larger main which is common to both outers, Unequally loaded inductive sections.—Total True Power ab-

sorbed = sum of the two readings of the Wattucters connected with their thick coils in the outers respectively, and their thin coils connected to the common centre wire AB as shown in Fig. 145. This last case would be the one met with when the circuit was partly a lighting and partly a power one, running two-phase motors.

Where the reader may not be quite conversant with the preceding methods of measuring power in two-phase alternating current circuits, a most useful experiment will be to prove the above statements in much the same manner as was set forth in the preceding test on three-phase measurements of power, only three or four ammeters and voltmeters with the two Wattmeters W_1 and W_2 and the variable two-phase rheostat being required.

Measurement of Power in Polyphase Alternating Current Circuits.

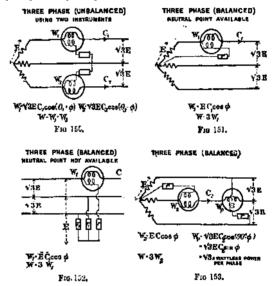
As a summary, with some additions, to the methods as given on pages 388-394, the principal arrangements of wattmeters employed for measuring the true power in different kinds of alternating current circuits commonly met with in practice, are given here in diagrammatic form.



r, r_1 , r_2 = the non-inductive resistances in series with the fine wire coils of the wattmeters.

φ, φ₁, φ₂, φ₃ = ,, angles of phase difference between currents and voltages,

The diagrams and deductions accompanying each explain the principle clearly enough.

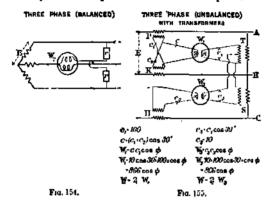


In Fig. 150, if the power factor of the system is less than 0.5, one of the wattmeters will read negatively and the connections of its fine wire circuit will have to be interchanged in order to obtain deflections on the scale. In this case the difference of the two scattmeter readings gives the total power.

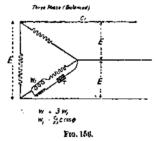
In Fig. 152, the resistances $r_1 = r_2 = (r + \text{fine wire coil})$, but an artificial neutral point can be formed by lamps without the expense of the resistances r_1 , r_2 .

In Fig. 156, unless the resistance of the fixed current coil is

amall compared with the resistance of the phase in series with which it is connected, its insertion will throw out the balance of a mesh system and $3W_1$ will not = the total true power. The

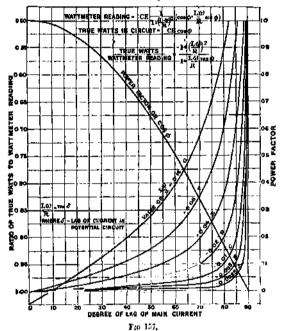


arrangement in Fig. 150, or if the system is balanced one wattmeter with a two-way key for connecting one end of the fine



wire coil in quick succession to the remaining two mains, is much to be preferred.

Fig. 155 shows a method of connecting two wattmeters in three-phase high tension mains ABC using current and pressure transformers, P and K are two 20 to 1 series transformers, giving a secondary current of 5 amps, at full load; while H is a 10 to 1 series transformer, giving a secondary current of 1 amp, at full load. T and S are each 100 to 1 pressure transformers, with 10,000 volts on the primaries. It can be shown



that each wattmeter indicates 865 kw. at full load, the total power of the circuit being 1732 kw.

Note.—The above methods are equally applicable to measuring the output of a generator or input into a motor or rheostats.

The measurement of power factor in alternating current circuits can be made by means of power factor indicating instruments, or by the method described on page 388, in the case of three-phase circuits. Another method is shown in Fig. 153 for three-phase circuits in which a wattmeter W_r connected as shown indicates the wattless power in a phase, or the power factor, if the scale be suitably graduated. The instrument in this case has a central zero and deflects to one side or the other according to whether the current lags or leads with respect to voltage.

As with such an arrangement, a considerable P.D. will exist between the fixed and moving coils, it can only be recommended for the lower voltages.

Another and safer method can be employed with balanced three-phase circuits using one wattmeter in one main and a two-way key for connecting one end of its fine wire circuit in quick succession to the remaining two mains.

If d_1 and d_2 are the two deflections so obtained, then the

Power factor of the circuit =
$$\sqrt{1+3} \left(\frac{d_1-d_1}{d_1+d_2}\right)^{3}$$

Correcting Factor for Wattmeters.—Considering the most common form, namely the electro-dynamometer type, used in practice, it is well known that the current through the moving coil should be exactly in phase with the P.D. at its terminals for the instrument to read true watts correctly. It is therefore both interesting and important to know the magnitude of the error introduced into the reading of the wattmeter and the correcting factor to be applied to obtain true watts when the current and pressure in the fine wire coil are not in phase due to the coil possessing inductance, which it must necessarily have to some small extent. The following considerations are quite general, and assume that the current and voltage are sine functions—

Let C = the maximum current in the fixed coil, I = the current (at time t) in the fixed coil,

E sin ωt = potential difference between the mains (at time t),

 ϕ = angle of lag of the current in the mains,

i = the current (at time t) in the moving coil of selfinduction L and total chanic resistance R,

including any resistance in series with it.

 $\omega = 2\pi \times \text{frequency of the supply.}$

Then the relations given in Fig. 1571 can be shown to hold good.

The relations apply to all types of wattmeters if ϕ , L and ω , the only quantities which vary with the nature of the load and type of wattmeter, are known.

. When $\phi=90^\circ$ the multiplying factor becomes zero, and the reading of the watemeter is zero, since there is no force between the coils carrying currents which differ in phase by 90° . The curves (Fig. 157) can be used as follows—Suppose we know that L=0.02 henry, R=628 ohms, frequency =50 ~ per sec., and the power factor =0.5. Then $\frac{L_{co}}{R}=0.01$.

Hence carve C is to be used. Now the horizontal line through

Hence curve C is to be used. Now the horizontal line through 0.5 on the power factor scale cuts the power factor curve cos. ϕ at a point, the vertical line through which passes through $\phi = 60^{\circ}$ and cuts curve C at 0.98, which is the correcting factor of the waltmeter.

Fundamental Considerations Relating to Alternating Current Static Transformers,

General Remarks.—Before considering actual methods of testing static transformers, the importance of which, in alternating current systems of distribution of electrical energy, arises from the ease with which a small current at high pressure can be converted to a large current at low pressure or vice versa by such an appliance and with very little loss, some introductory remarks are considered desirable.

There are a great many different forms and ways of building the kind of transformer in question, but they all come under one or other of two main heads, namely—

- (a) Those with closed magnetic circuits in which the magnetic induction or lines of force are contained solely, or nearly so, in iron.
- (b) Those with open magnetic circuits in which the lines of force run partly in the iron core of the transformer, and partly in the air through which they complete their path. This type,
- 1 Taken, together with Figs. 104 and 146-155 from a paper on "The Measurement of power in alternating current circults," by P. Hamilton, Proc. Inst. C.E., vol. citv, 1902-1903, by kind permission of the Author and Inst. C.E.

however, has now become practically obsolete. In either case (a and b) the iron core is surrounded by or wound with two distinct and separate coils of insulated copper wire termed the primary and secondary. In all cases the former is the coil connected to the source of supply, while the latter has induced in it an E.M.F. which supplies current to some separate circuit, usually

at quite a different E.M.F. to that acting on the primary.

The primary may be either the high tension (pressure) coil or the low, according as to whether the transformer is used as a step-down or step-up appliance respectively. Hence to avoid confusion, the primary will always be that coil which is connected to the source of supply, whother this be high or low tension.

It may now be well to consider certain phrases and quantities met with in static transformers, and which appear in testing work on them. Transformers with "closed" magnetic circuits only need be considered, the "open" magnetic circuit type not having been made for many years. The induced secondary voltage is evaluated as follows—

Let N = total magnetic flux threading the secondary winding of T_s turns,

f = periodicity of the primary supply-current, and hence of this flux,

 E_r and E_θ = maximum values of E.M.F.s at the terminals of primary and secondary.

Now since in one period of the current wave, the current and hence the flux varies from 0—max., max.—0, then reverses and again varies from 0—max. and then max.—0, the average rate of change in the flux = 4N lines per cycle or period, and the average change = 4Nf lines per sec. Therefore the average E.M.F. induced per turn = $\frac{4Nf}{100}$ and therefore the average E.M.F.

induced in the secondary winding of T_s turns = $k_s = \frac{4NfT_s}{10^8}$ volts. Since the virtual E.M.F. = average F.M.F. × form factor of the voltage wave, the virtual or R.M.S. E.M.F. $E_s = \frac{4 \times 1 \cdot 11NfT_s}{10^8} = \frac{4 \cdot 44NfT_s}{10^8}$ volts, where 1:11 is the value of the form factor of a sinusoidal wave. There will also be an

induced E.M.F. due to self-induction in the primary winding of Te turns, and since the same flux threads this also, this back E.M.F. of self-induction must $=\frac{4\cdot 44\,N_fT_p}{10^8}$ volts. On open

secondary circuit the primary supply pressure only exceeds this back E M.F. by a very small amount, namely, that sufficient to force the energy current through the resistance of the primary winding and provide the necessary magnetizing current for producing the flux in the core. We therefore have the following important relation, namely-

$$\frac{E_P}{E_S} = \frac{4.44 N f T_P}{4.14 N f T_S} \times \frac{10^8}{10^8} = T_P / T_S$$

very approximately, which is called the voltage ratio of conversion or ratio of transformation.

If A, and A, are the currents dowing in the primary and secondary having resistance R_r and R_θ , then the ohmic drop of voltage in each is A_PR_P and A_RR_S respectively, and the core flux is produced by an effective voltage $E_F - A_F R_P$, where the bar over the expression indicates that it is a vectorial-and not an algebraical—difference, the primary supply E.M.F., K_{P} and energy voltage, $A_{x}R_{p_{y}}$ not being in phase as indicated in Fig. 158.

The no-load secondary induced voltage will therefore

$$= (\overline{E_F - A_F} R_F) \frac{T_S}{T_F} \text{ volts,}$$

and the secondary voltage on load
$$= (K_F - \overline{A_F R_F}) \frac{T_S}{T_F} + A_S R_S \text{ volts.}$$

When the secondary circuit is open, the total loss occurring in the transformer is called the open-circuit lose, and the current flowing in the primary is called the no load primary current.

The open-circuit loss is made up of the copper Ftg. 158. loss due to the no-load current flowing in the primary winding, and which is usually very small compared with the remaining loss due to eddy currents and magnetic hysteresis which are termed the iron core losses.



The no-load primary current, such as would be indicated by an ammeter, consists of two components in quadrature, namely, (a) the true magnetizing component, which being an idle or wattless current logs 90° behind the supply voltage, and (b) the energy or load component in phase with the supply voltage, and overcoming the above open-circuit losses due to eddy currents, hysteresis, and copper loss.

These three currents can therefore be represented by a rightangled triangle such as Fig. 158, in which BD would be the no-load current, BU the energy component, and UD the magnetizing component. Thus, since $BD = \sqrt{BC^3 + CD^3}$, we see that the no load current = $\sqrt{(\text{energy current})^2 + (\text{magnetizing current})^2}$ -1/4, 2 + 1/2, and this no-load current would be in quadrature with the supply volts, except for the energy current, which makes the phase difference slightly less than 90°.

The magnetization or core flux, being directly proportional to the supply voltage at constant frequency, is constant at all secondary loads with a constant voltage supply, and hence the iron losses are constant at all loads. Further, since we have seen

that
$$\frac{E_r}{E_s} = \frac{T_r}{T_s}$$
, it follows that $\frac{A_s}{A_r} = \frac{T_r}{T_s} = \frac{E_r}{E_s}$, i.e. the primary and secondary currents are inversely c_r to the voltages.

and secondary currents are inversely at to the voltages.

The measurements of current, voltage, and power in tests connected, not only with transformers, but also with alternating currents generally, should be made with instruments possessing practically no self-induction and little or no iron. The best results will be obtained when employing electrostatic, hot-wire, and dynamometer instruments, for such measure the Josean sq. values of prossure and current and are independent of the variations of frequency. If a circuit supplied with alternating current is non-inductive, as for example a bank of electric incandescent lamps run off the secondary of a transformer, then the Jucan sq. values of the unperes x that of the volts = the true or mean power in Watts taken up by that circuit or bank of lamps.

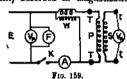
If, however, the circuit is inductive this product (amps. x volts) gives what is called the apparent power in Watts absorbed, which is in all cases greater than the true power. This would be the case if we tried to measure the power given to the primary of a transformer, which is always very inductive. Recourse must in such cases be had to the so-called non-inductive Wattneter, the fine wire coil of which must have as few a number of fine wire turns as will give the requisite sensibility. Such an instrument will measure the actual or true mean power given to any circuit, however inductive it is, and no difficulty presents itself in the use of the Wattneter on a low tension circuit. If, however, the power absorbed in a high tension circuit is required, then a special arrangement of Wattneter is needed (see p. 42). It is much better, however, to have all measuring instruments on the low tension circuit, and this can be accomplished by employing one of the double conversion methods given in the following pages, a course almost always possible in works and central stations in which two similar transformers as regards size and output can generally be obtained.

Another method of measuring the power given to or developed by a transformer is the 3-voltmeter one, and in the case of the primary circuit, a non-inductive resistance of such a known value is placed in series with this coil, that the P.D. across its terminals = that across the primary coil, or preferably as nearly so as possible, as this gives maximum accuracy. The method consequently has the somewhat serious disadvantage that the E.M.F. of the supply has to be double that required for the primary alone, which would in the majority of cases preclude its use. Then again a small error in observation may cause a large error in the results.

(136) The Effect on the No-Load Voltage Ratio, Current, and Watts of a Transformer, of Change of Primary Supply Voltage and Frequency. (Magnetization Curve or Open Circuit Characteristic.)

Introduction.—The present investigation is a very important one, in that, amongst other results, it gives the relation between primary terminal voltage (a to core flux at constant frequency) and magnetizing current, and which is termed the "open-circuit characteristic" or "magnetization curve" of the transformer.

The voltage used for the relation should, strictly speaking, be that of the back E.M.F. of self-induction, and therefore the vectorial difference $\overline{V_F} - \overline{AR_F}$; but as both A and R_F are small, their product is negligibly small compared with V_F , and can be neglected. Even with the special low-loss iron now used in transformer cores, these are seldom worked at magnetic induction densities outside the limits, 3500 to 7500 lines per sq. cm., in order to minimize the power (due to the iron-loss or energy-current component) absorbed in magnetization, which is con-



verted into heat in the core. For this reason the "knee" of the curve, which corresponds to about 15,000 to 17,000 lines per sq. cm., and is all-important in the design of D.C. apparatus, is never reached in the magnetization curve of a transformer.

Further, since the core loss is obtained in this test and is well known to be practically constant at all loads, it follows that, knowing the resistance of the windings, and hence copper losses $\{C^2R\}$ in P and S at any load current, the efficiency can be predetermined at all loads.

The test also shows that both the no-load current and watts decrease as the frequency increases, and hence that higher frequencies reduce the size of core and cost of manufacture for a given output.

Apparatus.—Transformer under test, of which P is the primary and S the secondary; low-reading wattmeter W; voltmeters V_PV_S ; switch K; frequency meter F; low-reading ammeter A; source of supply E, preferably a motor-driven alternator, the speed and excitation of which is variable over a wide range.

Observations. - With Variable Voltage Supply at Constant Frequency.

(1) Connect up as in Fig. 159, levelling and adjusting such instruments to zero as need it, the terminals tt of the high

tension winding used as the secondary being open-circuited as

(2) With the frequency adjusted to the normal value for the transformer, and the field regulator of the alternator full in. close K and take simultaneous reading of Vr. Vs. F, W and A at each of some ten different values of Vr, rising by about equal increments from the lowest readable values to not exceeding 20 % above normal, by adjustment of field regulation or otherwise, and

at constant normal frequency. (3) With Variable Frequency Supply at Constant Voltage.

With the voltage adjusted to the normal value for the transformer, take simultaneous readings of V_{P_1} , V_{P_2} , F_1 , W and A at each of some ten different values of F, rising by about equal increments between the lowest and highest values convenient, at constant voltage V.

(4) Measure the ohmic resistances of the primary and secondary windings P and S; that of P by either (a) the annueter. voltmeter method (p. 86), using Ohm's law and a direct current supply for E, taking care to connect a suitable main current variable rhoostat in circuit between E and P; or (b) the comparative deflection method (p. 84). The resistance of N may be obtained by either (c) method (a) above mentioned, or (d) a Wheatstone bridge. In the case of the numeter-voluncter method, the voltmeter must be connected to the actual terminals TT or tt of the windings.

Турс . . .

Maker . . .

Tabulate all your results as follows --

Transformer No . . .

Beech	dary ;	volls	E	٨		• •	Resid	tuico		. ohmu (e)	τ _N == εc.
* Trequency /	Printing V.	Secondary 7.5	Voltage Ratio	Amin A.	Altherent Water	True Watta IF.	Fower Partor	Angle of Lag 6".	Energy Current Component	Idle or Magnetaring Current Components $A_m = \sqrt{A^3 - A_s^3}$	Core Flux N = 10 EP.

(5) From obs. 2 plot the "open-circuit characteristic" (otherwise known as the "magnetization curvo") of the transformer having values of V_F as ordinates, with magnetizing current A_m as abscissa.

Also curves having the same scale values of V_p as ordinates, with (a) total no-load current A; (b) energy current component A_p ; (c) no-load watts W (practically all iron-core losses); (d) voltage ratio V_p/V_p , as abscisse, in each case. From olss 3 plot on another curve-sheet curves having values of frequency f as ordinates, with A, A_p , A_{pq} , W and V_p/V_p , respectively, as abscisse.

Inferences.—From a study of the table of results and shape of curves state clearly all that can be deduced.

√(137) Measurement of Copper Losses in a Transformer (by the Short Circuit Test).

Latroduction.—The total internal loss W in any static transformer is made up of the iron loss W_I due to eddy currents and magnetic hysteresis in the iron core, together with the copper loss W_{σ} due to the currents A_F and A_S in the primary and secondary windings of resistances K_F and K_S .

Then $W_{\sigma} = A_{\rho}^{2}R_{r} + A_{s}^{2}R_{s}$ and $W = W_{I} + W_{\sigma}$.

Knowing R_P and R_S , the copper loss W_C can be calculated for any or a series of measured load currents, but the value so found may differ considerably from the actual working or effective value, owing to the eddy current and "skin effect" present with the larger sizes of conductor, when carrying alternating current, causing an apparent increase in the resistances R_F and R_S . The present test, comprising the direct measurement of the total copper loss, would therefore appear to be a means of obtaining it under working conditions, and hence more accurately than by calculation.

Another source of error may, however, now creep in, for the wattmeter necessary for measuring the loss must obviously be a low-reading one, and have a current capacity equal to that of full load for the winding chosen as primary, while its pressure coil will be subject to a small fraction of what would probably be its normal pressure (a condition introducing an error in its

indication) unless, of course, the wattmeter is a specially designed one for low pressure. The small applied voltage necessary for keeping the short-circuit current within safe limits, will produce a very small induction, and therefore loss due to magnetization of the core. This last named may be negligibly small, when the wattmeter will indicate the corner loss only. If the iron loss

wattmeter will indicate the copper loss only. If the iron loss is not so small, the wattmeter will give a reading at the applied voltage of short circuit when the secondary is open-circuited, and this reading must be subtracted from all of its indications on short-circuited secondary. Further, care must be taken that the wattmeter reading does not include any losses in connecting

or short-circuiting cable. If it does, the loss in such must be separately calculated from their measured resistance and each current, and deducted from the reading.

If T and T = the number of primary and accordary turns

If T_r and T_s = the number of primary and secondary turns respectively, and V_r = a small supply voltage applied to the primary in order to send full-load current A_r through it with secondary short-circuited, then the total resistance "drop"

cuited, then the total resistance "drop
$$= A_r \left(R_F + R_s \left(\frac{T_F}{T_s} \right)^2 \right) \text{ volts},$$

From the values of this "drop" and V_r the characteristic triangle of the transformer can be drawn and the leakage drop determined.\(^1\)
Apparatus.—That for test No. 136, excepting that W and

 V_F must now both be low-reading instruments, while V_F is replaced by a low-resistance ammeter A_F for short-circuiting the terminals t of the secondary winding S, the range being large enough to indicate at least full-load current of that winding.

Observations.—(1) Connect up as in Fig. 159, with the

ammeter A_s across (tt) and the pressure circuit of W across TT, in order to eliminate errors due to including in the reading of W any copper loss in the primary connecting cables. Level and eligist to zero any instruments which need it.

(2) With an efficient chart circuit of S the primary P will

(2) With an efficient short circuit of S the primary P will practically constitute a metallic resistance and require, by Ohm's law, probably only two or three volts or so to be applied to it in order to obtain full-load current through it.

* Vide "The Testing of Transformers," Ly Moeris and Lister (Journal I.E.E., vol. 37, p. 284, 1906). This low voltage required at the normal frequency of the transformer, and from whatever source obtainable, must be adjusted by a suitable variable resistance, in series with P, so as to give eight or ten currents through P, varying by about equal amounts from its full-load value to the lowest readable, the readings of V_P , W, A and A_P being noted at each.

- (3) Disconnect the secondary short circuit and note the ironloss reading, w_I on W_I for the same value of V_P as used in obs. 2 (if any is readable).
- (4) Measure the resistance r_s of the short circuit (namely, A_s and its two short connecting leads) and tabulate your results as follows—

		1717 4	i year chi		i rentenna	(r)	· · complet
Frequency F. Tolas F. Franks Amps (4). Secondary short-ereut	Total Watts IF,	Power Factor con $\phi = \frac{R}{AT_F}$	Augle of Lag &.	Okade Drop F.	Core Wotts (if any)	4.5.	Actual Copper Iou IF $C = W - w_L - A_{S^T}^2$

(5) Plot a curve having values of copper loss W_{σ} as ordinates, with A as abscisse.

Note.—The impedance voltage V_P is entirely spent in overcoming the equivalent impedance of the windings with short-circuited secondary, being partly spent in overcoming resistance and partly in reactance.

The reactance voltage = $\sqrt{V_P^2 - (W/A)^2}$.

Deduction of the Regulation of a Transformer for any Load and Power Factor from the "Open" and "Short Circuit" Tests.

From the curves obtained in the preveding open and shortcircuit tests, the drop in volts in a transformer on non-inductive or inductive secondary load can be predefermined. To obtain this drop is needed the "open-circuit" volts and the triangle of voltages relating impedance voltage, obnic drop or resistance voltage, and the rearrance voltage as obtained from the "shortcircuit" test.

The voltage drop in the transformer for any load and power factor can thus be obtained from an exactly similar construction to that given on p. 182 for an alternator, and which will not, therefore, be repeated here.

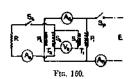
(138) Determination of the Regulation of a Static Transformer. (Differential Method.)

Introduction.—The meaning of the term "regulation," as applied to a transformer, was explained and defined in test No. 139, p. 412, and its measurement in a single transformer there given. When, however, two similar transformers T_1T_2 are available, the present method of measurement is both simple, convenient, and direct reading, whereas that of test No. 139 nocessitates taking the difference between two voltages, and is less accurate. It is applicable to any pair of high-tension or low-tension transformers, but the secondary circuit should preferably be the LT side, on account of the greater safety in handling instruments at low tension.

Apparatus.—Source of A.C. supply E, whether low or high tension; two transformers T_1T_2 , similar in all respects; voltmeter V_2 ; switches S_2S_3 ; load resistance E; ammeter A_3 ; and (if available—for interest, but not as a necessity) two ammeters A_{F_1} and A_{F_2}

Observations.--(1) Connect up as in Fig. 160, levelling and adjusting to zero such instruments as need it.

- (2) First connect for V_R a voltmeter capable of reading (or glow lamps capable of absorbing) the sum of the normal voltages S_1S_3 . Then with S_R and S_P open, and E giving the normal voltage and frequency of T_1 or T_2 , close S_P . If V_R shows a fairly large voltage, S_1 and S_2 are in helping series, and the connections of one of them must be interchanged to bring their voltages into opposing series, when V_R will show very little.
- (3) Now replace V_{δ} by a low-reading notmeter, and, with N_{P} closed (N_{P} still being open), note the readings of A_{P1} , A_{P2} and V_{δ} (if any). If $P_{1}P_{2}$ are either exactly similar, or unloaded, or both, V_{δ} should now read 0.



(4) With the supply voltage constant, and R non-inductive and full in, close N_k, taking the readings of all the instruments for each of a series of six or eight load currents A_s, rising by about equal increments from 0 to the full-load current of T₁ or T₂.

Note. – $\Gamma_{\mathbf{a}}$ gives the difference of the voltages between the terminals of the loaded (T_2) and unleaded $\{T_1\}$ transformer, which is the required "drop."

The secondary output of transformers is usually expressed in kilo-volt-amperes (K.V.A.), irrespective of the power factor of the secondary circuit, and not in true K.W. at unity or some lower P.F. The values of V_d may, however, he obtained if desired on inductive loads by repeating obs. 4 with a variable choker (ℓ ') (not shown), connected in series with the non-inductive resistance R (preferably a bank of lamps) and a voltmeter with key to measure the volts V_d across R and V_d across the cloker at the same current, when the power factor of the circuit will be

$$\cos \theta = \frac{R}{\text{impedance}} = \frac{V_s}{V_o}.$$

ELECTRICAL ENGINEERING TESTING

Tabulate your results as shown-

Currents fo	r reference.	Becondary Load Current	Voltage Drop
$A_{P_{\vec{1}}}$	Ap.	Ag	<i>P_E</i> .

(5) Plot curves having values of V_S, as ordinates, with values of A_s as abscisse.

(139) Determination of the Efficiency and Regulation of Transformers. (Single Conversion Method.)

Introduction.—This method is one of the simplest, though not the most accurate, and entails using only the one transformer to be tested. In all cases by the primary of the transformer is meant that winding connected to the supply mains whether these are at high or low tension.

The efficiency of any transformer, supplied at constant voltage and frequency, is the ratio of the secondary output to the primary input, or W_2/W_1 .

The regulation of a transformer is the amount by which the secondary terminal voltage at any secondary load differs from that on open secondary circuit, i.e. it is the "drop" in voltage under load, and is due to both the resistance and reactance of the winding.

The regulation curve therefore relates secondary terminal voltage as ordinates and secondary load current as abscisse. The ordinate intercept between this curve and a horizontal straight line through the "open circuit" voltage point at any secondary load gives the "drop" of voltage at that load.

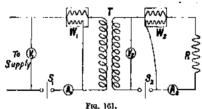
Caution.—In the case of transformers which have to be run off a high tension alternator and are tested by this method, the one operating the high tension instruments must not only wear a pair of carefully selected and good india-rubber gloves, but must also stand on an india-rubber mat, and to guard against the possibility of accidents even in the case of manipulating the low tension instruments, the one operating these must either wear the pair of india-rubber gloves provided or stand on an india-

rubber mat. Before switching on, the "danger boards" provided must be placed close to the high tension wires.

Note.—Great care must be taken that the india-rubber gloves are not scratched, cut, or pierced in any way, as this would tend to render them useless for the purposes of insulation.

Apparatus.—Alternating current ammeters $A_1 A_2$ (Fig. 251), and voltmeters $V_1 V_2$; non-inductive Wattmeters $W_1 W_2$ (with their separate anti-inductive resistances $r_1 r_2$ if any); load absorbing resistance R, preferably non-inductive (p. 598); switches $S_1 S_2$; source of alternating current supply and transformer T to be tested.

Mote.— V_1 and V_2 should be either hot-wire or electrostatic instruments, of which V_2 may preferably be of the latter type. If R is strictly non-inductive, then W_2 could be dispensed with; it may, however, as well be used if available.



Tests.—(1) Measure the ohmic resistances R_1 of primary and R_1 of secondary coils in a suitable manner.

- (2) Connect up the apparatus as indicated in Fig. 161, carefully levelling such instruments as need it, and seeing that their pointers are at c. Adjust the voltage and frequency (if possible) of the supply to the normal value required for the transformer.
- (3) With S₂ open, close S₁ and note the readings of A₁, V₁ and W₁ simultaneously. The "open circuit losses" occurring in the transformer will thus be obtained.
- (4) Make R large, and close S₂ as well as S₁. Then note simultaneously the readings of all the instruments for about ten different secondary currents from 0 to full load or to 15% over full load, rising by about ~ increments.

-414

In all cases the frequency and primary voltage must be kept constant.

- (5) Repeat 4 with a higher and lower frequency than the normal.
- (6) Repeat 4 and 5 on an inductive load of constant power factor, or otherwise obtain the readings, as detailed on p. 182, necessary for plotting the regulation curves between secondary volts and current, each at different but constant power factors,
- (7) Find, experimentally, the copper losses in primary and secondary by passing direct currents of various strengths, between 0 and full load, through the coils, and noting the losses by means of a Wattmeter.

NAME	DATE
Transformer: No	Frequency per Sec. Type
Primary, Secondary, Watts, W	Translation Transl

(8) Plot the following curves having values of-(a) Total copper losses; (b) total iron losses; (c) secondary voltage; (d) primary power factor; (e) efficiency; (f) voltage ratio, respectively as ordinates and secondary load currents as abscisse in each case.

Inferences. -- State concisely all the inferences which you can draw from the results of your experiments.

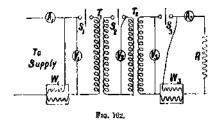
(140) Determination of the Efficiency of Transformers. (Double Conversion Method.)

Introduction.—This method can be used when two similar transformers are at hand, and particularly when only low tension measuring instruments are available.

Caution .- To guard against the possibility of accidents, even in the case of manipulating the low tension instruments, the pair of india-rubber gloves provided must be worn by the one manipulating the tertiary circuit instruments, and the india-rubber mat must be used by the one reading those on the primary circuit. On no account must any part of the secondary (high tension) circuit be touchal while "alive," and before switching on the primary current, the "danger boards" provided must be placed close to the high tension leads.

Note.—Great care must be taken that the india-rubber gloves are not scratched, out, or pierced in any way, as this would tend to render them useless for the purposes of insulation.

Apparatus.—Alternating current ammeters A_1A_2 (Fig. 254), and voltmeters V_1 V_2 V_3 , of which V_2 is not absolutely essential to the



test; non-inductive Wattmeters W_1 and W_3 (with their separate anti-inductive resistances r_1, r_3 , if any); switches S_1, S_2, S_3 ; load absorbing resistance R, preferably non-inductive (p. 598); source of alternating current supply and the two transformers T_1, T_2 to be tested.

Note.—Both V_3 and the high tension voltmeter V_2 should, if possible, be of the electrostatic type. If R is strictly non-inductive, then W_3 can be dispensed with; it may, however, as well be used if available.

Tests.—(1) Measure the chmic resistance of each of the coils of the transformers T_1 and T_2 in a suitable manner.

(2) Connect up the above apparatus as indicated, carefully levelling such instruments as need it, and seeing that their pointers are at zero. Adjust the voltage and frequency (if possible) of the supply to the normal value required for the transformers,

- (3) With S_0 and S_0 open, close S_1 , and note simultaneously the readings of A_1 , P_1 , W_1 . The "open circuit losses" occurring in transformer T_1 will thus be obtained.
- (4) Make R large and close all the switches. Then note simultaneously the readings of all the instruments for about ten different tertiary currents from 0 to full lead, rising by about = increments.
- (5) Interchange T_1 and T_2 so that the latter now becomes the "step-up," and repeat exp. 3 and 4, tabulating your results in two tables similar to that shown.

Note.—In all cases the frequency and secondary voltage must be kept constant,

- (51) Repeat 3-5 for a higher and lower frequency than the normal.
- (6) Find, experimentally, the copper losses in each of the coils by passing direct currents of various strengths between 0 and full lead through them, and noting the losses by means of a Wattmeter.

NAME		Darm				
	Туре	Mode by	Used as			
$rac{P_1}{P_2}$ { Normal Output	ıt	ite, Frequency =				
	Change ratio _	• •				
	1		1			

_		Chings 14	Lio	
Wetta.	Con. 0 = 4,1,7, Angle of Lag 9. Volta Fp.	Tertiary. Watta.	Cobber Tosses in Fig. 1 and 1	Iron Loss in Waith $N_1 = N_2 - I_4$ Combination N_1 Each Transition or k_1 N_2 N_3 N_4 N_4 N_4 N_3 N_4 N

Resistances : Frimary = ... ohms. Total Secondary - ... ohms. Tettiary = ... ohms. at °C. Frequency mad - ... - per sec. Total Secondary drop $\frac{T_1}{T_1} =$... volts.

(7) Plot the following curves having values of—(a) Total copper losses; (b) total iron losses; (c) tertiary voltage; (d) power factor; (e) efficiency respectively as ordinates and tertiary load currents as abscisse in each case.

Inferences.—State clearly all the inferences which you can draw from your experimental results.

(141) Efficiency of High Tension Transformers. (Sumpner's Differential Method.)

Introduction.—A neat and convenient method of measuring the efficiency of high tension transformers, and which is susceptible of greater accuracy than most methods, is that due to Dr. W. E. Sumpner, and detailed as follows:—A small auxiliary transformer (C), the output of which need not be greater than the waste of power occurring in the two larger transformers A and B, to be tested, at full lead, is required for the purpose of furnishing a small extra voltage (say 5 to 12 volts) necessary for driving the full lead or any other currents through A and B. Its efficiency, goodness, or badness is a matter of indifference, and all we need in connection with it, is the output (w_1) of its secondary in Watts as measured by the Wattmeter (W_1) .

The particulars as regards this output can be deduced as follows:—Suppose that two 2250 Watt transformers have to be tested each converting from 100 to 2000 volts or view versa. Then their probable efficiency would be about 94% (say), and hence each would absorb $22.5 \times 6 = 135$ Watts at full lead. Consequently the output of the auxiliary transformer C need not exceed 2×135 or 270 Watts.

Hence if used on low-pressure 100 volt mains the primary should take about 2.7 amps. at 100 volts, and the secondary give out 22.5 amps. at 12 volts. In the ordinary test of efficiency of high tension transformers, in which two similar ones are used—one as a step-up from the low-pressure primary mains, and the other as a step-down to the tertiary mains, the efficiency is deduced from measurements of primary imput and tertiary output which are of nearly equal magnitude. Consequently the percentage error in measuring these two quantities re-appears as the same percentage error in the efficiency so obtained.

The present method, which is much to be preferred of the two, consists in actually measuring the losses (w) occurring in the two transformers directly, and comparing these with the input to obtain the efficiency.

The method is economical in cost of energy used, especially when testing large transformers; with the methods used in tests 139 and 140 it would be a scrious consideration, while the supply of full-load current would make a scrious demand on a public supply, or necessitate a large testing alternator. The present method is accurate because the total loss (ω) in the two transformers is obtained by adding together two quantities, and

not by subtracting them, and is most convenient for finding the temperature rise after a run of a prescribed number of hours on full load.

The principle of the present method is surikingly analogous to Dr. Hopkinson's combined efficiency test of a pair of dynamos,

the distinguishing feature of which is to couple two similar

machines together both mechanically and electrically, one to run as a dynamo and the other as a motor. Energy is supplied to one by which it is transferred to the other, this latter returning it again to the source; the balance of energy supplied actually by the source is therefore equal to the waste which occurs in the double transformation and corresponds with the loss (w) above mentioned. This then is what takes place in the present case, for energy is taken from the mains by the "step-up" (A or B, whichever is used as such), then transferred to the "step-down" transformer, and finally back to the mains again.

controlling the current circulating between them, the power taken from the supply is only same 4 to 20 % of the full-load K.W. capacity of either, depending on their efficiency—being only that necessary to make up the total internal losses in the two transformers together. Whether the L.T. or H.T. windings are connected to the supply is merely a matter of convenience depending on which supply is available, but usually the L.T. sides are connected to an L.T. supply for safety in handling the more commonly available low-tension instruments, etc. Calling whichever are connected to the supply the primarica, the accordance must be so connected in series that their E.M.F.s oppose each

Thus, while both transformers can be leaded to any extent by

windings. By making the small auxiliary transformer in series with one of the primaries provide a + " or - " boosting E.M.F., the out-of balance primary F.M.F.s so produced will cause out-of-balance secondary E.M.F.s and a circulating secondary

other. If the primary E.M.F.s are equal, so also will be the secondary E.M.F.s, and no current will flow in the secondary current, the strength of this current depending on the difference between the E.M.F.s. Should the connections be such that the secondary E.M.F.s are in helping series instead of opposing series, as they should be, a short circuit will result. To avoid this, and to ensure the connections of the secondaries being correct, close S and S_1 , when B will induce a voltage in the L.T. winding of A equal to that of the supply, but opposite in phase if the connections are correct. Hence, if either a voltmeter or lamps, each having a voltage range equalling twice that of the supply, are connected across the open switch S_a and neither show any voltage, the connections are correct for the two L.T. windings, and therefore also the two H.T. windings are then in opposition. If otherwise, the voltmeter or lamps will show twice the voltage of the supply. In this event the connections of one of the H.T. secondaries must be reversed, It should be noted that (a) will indicate the load current, while an ammeter (a_1) in series with S_1 will give the magnetizing current,

If W= load in Watts supplied to the primary of the "step-up," and $w_1 w_2 =$ the Watts at this load as measured by w_1 and w_2 , and $\lambda =$ loss of power in the connecting leads, current meter a and the current coil of W_1 , then the total loss in the two transformers

$$w = w_1 + w_2 - \lambda.$$

Hence the efficiency of double conversion = $1 - \frac{10}{W}$ and the efficiency of either transformer = $\sqrt{1 - \frac{10}{|V|}}$

As the ratio of $\frac{40}{|V|}$ is small—not greater than $\frac{1}{10}$ with a transformer of 95% efficiency, the efficiency of each transformer is given quite accurately enough by the relation

$$\Sigma = 1 - \frac{1}{2} \frac{vr}{|\dot{y}|} - \frac{1}{8} \frac{v\sigma^2}{|\dot{y}|^2}$$

An error of 10% in estimating $\frac{\omega}{|W|}$ only affects the combined efficiency to 1% and that of either transformers to $\frac{1}{2}\%$ only. Hence can be seen the superiority of the present method over the preceding one. The quantity |W| can be obtained with quite

420

in volts supplied to the primary of the "step-up." If (A) is the "step-up," then W=100 x current in low tension

coil of A, whereas if B is the "step-up," the power returned to the mains by A =the above quantity, and hence the input of the primary of B is $W = 100 \times \text{ current of } A + (w_1 + w_2 - \lambda),$

That transformer will be acting as "step-up" which has the higher P.D. of the two (A and B) on its low tension coil. If, say, 12 volts are supplied by C to the primary of B, the P.D. at the terminals of B will be either 112 or 88 volts according as

the 12 volts from the auxiliary and the 100 of the mains are to phase or opposite phase. If R was very inductive, the above voltages would be out of phase, and Bs P.D. might be anything between 88 and 112 volts. Apparatus.—The two high-tension transformers A and B to be tested of say 2000/100 volts; an auxiliary Boosting one C,

the primary of which is in series with a variable non-inductive resistance R of sufficient range to produce only a few secondary volts; two non-inductive Wattmeters W, W, Siemens electrodynamometer or direct reading alternating current ammeter (a); switches S, S, S, and S; voltmeter V for maintaining the mains at 100 volts; alternator D, or some other source of alternating

from accidental shock, or break down of the insulation between

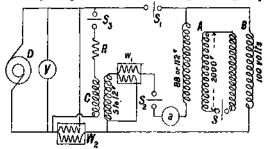
instruments employing alternating currents, which can be done

Caution .- On no account whatever is the high tension circuit of either A or B to be touched while "alive." The india-rubber gloves and must be used by the operators to ensure immunity

primary and secondary of A and B. Observations.—(I) Connect up as in Fig. 163, and adjust the instruments to zero where necessary. See that all inoricating arrangements are working properly, also that the gloves are in good order and the mat suitably placed. (2) Measure the losses due to the resistance of the leads and

without altering any of the connections thus-with S and S, open, short circuit the primaries of A and B and close $S_2 S_3$. (3) Vary K so as to obtain about six different currents through (a) from 0 to the full load current of A or B by causing the secondary voltage of C to vary suitably. Note the corresponding readings on W_1 (the power given out by the secondary of C), which therefore at once gives the required losses in Watts in leads and instruments for each particular current passing through them.

- (4) Measure the copper losses in the coils of the two transformers A and B by opening S₁ and closing S, S₂ and S₅ and observing the readings of W₁ for some six different currents from 0 to the maximum of A and B, as read off on a.
- (5) Measure the iron or core losses in the two transformers A and B by closing all the switches and observing the reading of W₂.



Fm, 163

(6) With S_2 and S_3 open, close S_1 and S and note the readings of a_1 , a_2 and W_2 . Then a_1 will indicate twice the no-load current of either transformers A or B, and W_2 twice the no-load lesses in either.

Tabulate your results as follows-

Transformer used as Step-up: No Type Wake; Resist. R " " Blop-down: No " " " " R " No Output Volta Aupt Consector wa					Resist. R _i R _i actor Wul	. =	_M				
Г	Ι,	Current			Total Losses in				, e,	Biliciency	
Spend in Reva.	Prequency in per nec.	Volta F.	Reading on	Апр. с.	Couls, Leads and Instruments (17, in 4) we.	Iron Cores (IVs to 5) was	Leads and Instruments W. to 3 = 3.	the two Transformers w = w ₁ + w ₂ - A.	Total Input into Privaty of Skep-1 W = 140 a + 40	of Combination $\ln \chi$ 100 $\left(1 - \frac{w}{W}\right)$.	transfirmer $\sqrt{1 - \frac{10}{W}}$

Watts as abscissa.

(7) Plot the following curves on the same curve sheet having currents (a) as abscisse, and for the ordinates the following—
(i) Losses in leads and instruments; (ii) iron core losses; (iii) a²R losses in the coils of A and B; (iv) total a³R losses in A and B. Also with efficiency as ordinates, and load IV in

(8) Reverse the positions of A and B, and repeat the above tests. Inferences.—State very clearly all that you can infer from your experimental results.

(142) Measurement of the Efficiency of ordinary Single-Phase Transformers by Blakesley's 3-dynamometer Method.

Introduction.—This method necessitates the use of two ordinary Siemens electro-dynamometers, in which of course the moving coil is in series with and carries the same current as the fixed coil, whence the angle of torsion is proportional to the \(\sqrt{mean square} \) value of the alternating current, and in addition the use of a third Siemens electro-dynamometer, arranged so that the moving coil has its own separate terminals, and is not in series with the fixed coil.

If then two alternating currents of equal period, from either the same or different sources, flow through the two independent coils, the periodic time of oscillation of the moving coil bring very large compared with that of the current, the angle of tersion is proportional to the mean product of the simultaneous instantaneous values of current throughout the period, and is called the "split dynamometer" reading.

If A_o and $A_o^1 =$ maximum values, and A, A^1 the mean values of two simple periodic alternating currents, one of which lags behind the other by an angle a, then the ordinary dynamometer will give $A = \frac{1}{2}A_o^2$ and $A^1 = \frac{1}{2}(A_o^{-1})^3$. On passing these currents through the split dynamometer its reading ϕ would be $= \frac{1}{2}A_oA_o^{-1}\cos a$, and hence $\cos a = -\frac{\Phi}{2}$.

hence
$$\cos a = \frac{\phi}{\sqrt{AA^4}}$$
.

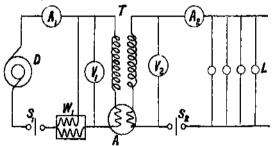
The following method is quite general, and does not assume that the current is a simple sine function of the time, but does assume that there is no magnetic leakage, i.e. that the number of lines cutting the primary and secondary are the same. This is not true in all types of transformers on full load, but is nearly so in closed magnetic circuit types.

Since the split dynamometer gives no reading on open secondary circuit, this method is useless for determining the "open circuit" losses.

Apparatus. — Two, ordinary Siemens electro-dynamometers A_1A_2 , and one split dynamometer (A); transformer T to be tested; non-inductive resistance L (such as a lank of lamps to take up the secondary lead) (p. 598); alternator H; switches S_1S_2 ; voltmeters V_1V_2 ; non-inductive Wattmeter W_1 inserted merely for the purposes of comparison.

Observations.—(1) Connect up as in Fig. 164, and adjust the instruments to zero where nece-sary. See that all lubricating cups in use feed slowly and properly, then start D.

(2) S_3 being open, close S_1 , and adjust the spend and excitation



Fto. 164,

so that V_1 reads the normal voltage required for the primary at the normal frequency of the transformer. Note the readings of A_1 , V_1 and W.

- (3) Close S_2 and adjust L so that A_2 reads about $\frac{1}{10}$ of the maximum secondary current, the voltage V_1 being kept normal by varying the excitation. Now note the readings of A, A_1 , A_2 , V_1 , V_2 and W.
 - (4) Repeat 3 for about 10 secondary load currents, rising by

about equal increments to the maximum allowable, and tabulate as follows—

NAME			Date
Transformer tested: Primary turns $N_1 =$ Bocondary $_{\rm Pl}$ $N_2 =$ Normal: Volts	• • • •		Make
Byname-meter for a part of the	A ₁ . P A ₂ A ₂ A ₃ A ₄	True Watta W1. Apparent Primary Watts A1Pt. Frimary Input W2 = (R1A1 + N2 R2A).	Secondary Oniper Counce Aprile Counce Aprile Lag Addis Angle a. Power Reator Afril Fower Reator Afril

(5) Plot curves having values of Ws as abscisse, with efficiencies and V2 as ordinates.

(143) Measurement of the Efficiency of Multiphase Alternating Current Transformers.

Introduction.—The determination of the efficiency of ordinary single-phase transformers has already been fully considered in the preceding pages.

The present test does not differ materially in principle from those in question, and practically the only difference is in the method of measuring the power absorbed and developed by the multiphase transformer, and which possesses some characteristic differences from that used in the case of the ordinary singlephase transformer.

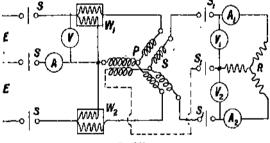
Most of the preceding methods are equally applicable in the present case whether the transformer is of the two or the three phase type. The reader should refer to p. 386 for the method of measuring electrical power in two and three phase alternating current circuits, where a more detailed description of them will be found. If in the present instance, as in fact with any others, the rheestats or circuits in which the load is to be absorbed are strictly non-inductive, i.e. are of the nature of incandescent lamps or water rheestats, then providing such load-absorbing devices operate equally on each of the sections of the circuit, thus main-

taining a balanced system, the output can quite accurately enough be obtained from the ammeter and voltmeter readings in the manner set forth on pp. 388 et sey.

For the present test we will assume that the efficiency of a 3-phase transformer is required by, say, the single conversion method.

Apparatus.—The 3-phase transformer to be tested, of which P is the primary winding and S the secondary shown in Fig. 165, with the star or open winding; two non-inductive Wattmeters W_1 and W_2 ; three Parr's direct-reading dynamometer ammeters A_1 , A_1 and A_2 (p. 572); three voltmeters V_1 , V_1 and V_3 ; 3-phase variable rheestat R (non-inductive) capable of operating equally on each line (p. 608); source of 3-phase current E_1 ; two 3-throw switches S S S and $S_1 S_1 S_1$.

Note.—If the 3-phase rheostat R is not non-inductive, then two additional Wattmeters will be necessary in the secondary



Fag. 165,

circuits connected up in precisely the same way as those shown in the primary circuit, the secondary output being then given by the sum of their readings at any particular lead.

Observations.—(1) Connect up as in Fig. 165, and adjust all the instruments to zero, levelling such as require it. See that all lubricating cups in use feed slowly and properly if the source of 3-phase current supply E is controllable.

(2) With S₁ S₂ S₁ open, close SSS, and adjust the speed of the generator so as to give the proper periodicity for the transformer and then the excitation, so as to have the desired voltage, shown by V across the primary.

Note the respective Wattmeter readings W_1 and W_2 , and if possible that of Λ in addition to V. Then $(W_1 + W_2) =$ the notional primary input = the magnetizing losses.

- (3) With R at its maximum, close $S_1S_1S_1$ and note the readings of all the instruments for some ten or twelve secondary load-currents from the smallest to the maximum permissible, rising by about equal increments at a time for constant secondary voltage.
 - (4) Calculate the secondary loads (W_{δ}) from the relation— $W_{\delta} = \sqrt{3} A_1 V_1 = \sqrt{3} A_2 V_2 \text{ etc.},$

and tabulate as follows-

Pennary Circuit.	J. I.,	Becomiary Circu	dt. Total Loss in	
Apparent Watts Apparent Watts 7.1.4 Watts	Power Factor H ₁ + W ₂ . \[\langle A.O. \] Angle of Lag &.	Flor Fg.	Transformer Transformer	Efficiency $r = 100 \frac{W_c}{W_c} Z_c$

(5) Measure the resistance of the transformer coils by means of either the Wheatstone Bridge or Potential Difference method.

(6) Plot the following curves between-

Efficiencies η as ordinates and secondary loads ($\sqrt{3} A_1 V_1$) as abscisse.

Power Factor as ordinates and secondary loads ($\sqrt{3}A_1V_1$) as abscisse.

Inferences.—State clearly all that can be inferred from your experimental results.

(144) Efficiency of a Nodon Valve Electrolytic Rectifier.

Introduction.—The necessity of obtaining continuous current for certain purposes, such as electrolytic work and the charging of secondary cells, where, frequently, the only available public supply is alternating current, has led to the introduction of rectifiers for rectifying alternating into continuous or unidirectional current.

Of such appliances, there are new several commercially successful forms; that known as the noden valve consists of as many pairs of cells grouped according to the Lee Gratz method (Fig. 166) as there are phases of current or distributing mains, in order to obtain a single rectified current. Each cell consists of plates formed of an alloy, mainly composed of aluminium, acting as cathode, immersed in a solution of borate or phosphate of amnonium or other salt formed from tartaric, acetic, exalic or gallic acids. The solution is capable of rapidly altering the condition of the polarizing film formed by an alternating current on the aluminium. The containing cell is made of lead and constitutes the anote. The electrolytic action taking place is as follows—

In one half period of the alternating current, current tends to flow from aluminium to lead, but cannot, owing to an insulating film of very high resistances being formed over the aluminium (cathode) plate. In the next half (reversed) period, the current actually is able to flow from lead to aluminium owing to the instantaneous de-polarization or reduction of the film on the aluminium plate. The principle on which both semi-waves of the period of an a.c. supply are utilized, is that proposed by Leo Gratz, and shown in Fig. 166, for a single phase alternating to direct—current transformation. A and L are the aluminium and lead plates respectively of the four cells I, I, and II, II. The continuous arrows represent the direction of current in the valve during one half of a period when the current of the alternating supply flows from P to R. The dotted arrows show the direction of current in the valve in the next half period when the supply current flows in the reverse direction from

supply between Q and R.

of all the instruments.

R to P. Thus for the first half period it is blocked in cells II, II, and in the second half period it is blocked in cells I, I. A unidirectional current therefore always flows from D to C through any load (r) whether motor, secondary cells or resistance, etc. To obtain greater constancy or uniformity of d.c. voltage a suitable condenser can be connected across D and C. A single

valve will stand a.c. pressures up to 140 volts between Q and R, that between D and C being about 90% of this. For higher a.c. pressures two or more valves may be combined, or an "economy coil" type of transformer connected between valve and a.c. supply. The pressure between D and C may be varied to any extent by a corresponding variation of that of the

The temperature of the electrolyte must not be allowed to rise

much above 50° C., and in large valves, forced air draught around the cells is resorted to in order to keep down the temperature. The valve may be used on any periodicity employed in practice up to $100 \sim$ per sec. or more. A starting resistance (S) must be employed with the valve when this has been out of use for a few hours, in order to reform the insulating pellicule on the aluminium plate. This only takes a few seconds and provents a sudden heavy rush of current through the valve. The resistance or inductance of S is cut out entirely afterwards.

Evaporation of the solution is made up by adding distilled water and the solution need only be renewed at long intervals.

Apparatus.—The nodon valve complete; starting resistance

(S); alternating current ammeter (A), voltmeter (V), wattmeter (P); direct current ammeter (a), voltmeter (v); load or variable resistance (r); thermometer; source of a.c. supply; economy coil or transformer if a.c. supply exceeds 140 volts; switches S₁, S₂.

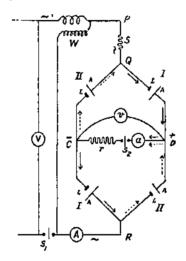
Observations.—(1) Connect up as in Fig. 166, and adjust all the instruments to zero, levelling such as require it. Q and R are the terminals marked ALT on the valve, and are to be connected to the a.c. supply: D and C are the terminals marked + and -.

oil cups feed very slowly and properly.

(2) With S_1 and S_2 open and B full in, adjust the a.c. supply so that V reads about 140 volts, the periodicity being kept constant at normal value. Now close S_1 , and note, the readings

If machinery is being run for supplying the valve, see that all

- (3) With S₄ still open, gradually cut out S to short circuit and again note all instrumental readings and the temperature of the electrolyte.
- (4) Re-insert S and with (r) full in, close S_2 and gradually cut out (S) to short circuit. Next adjust (r) so that (a) reads about $\frac{1}{10}$ th full output current and note the readings of all the instruments.



Three Phase (Balonced)

Fra, 106,

- (5) Re-adjust (r) so as to obtain some ten different load currents on (a) rising by about equal increments to the maximum for which the value is intended, and note the temperature and readings of all instruments at each.
- (6) Repeat (5) for a widely different but constant periodicity (if available) above and below normal at the same voltage if possible.

- (7) Repeat (5) for a constant supply voltage, say 50% less than before, at normal periodicity.
- (8) Open (S₁) and at constant normal periodicity, note the readings of all the instruments for ten different voltages between 0 and 140 volts.
- (9) With a convenient constant supply voltage and S₂ open, take readings of all the instruments for ten different periodicities, ranging from the maximum obtainable downwards.
- (10) Repeat both (8 and 9) for S₂ closed, constant full load being maintained on (a) by varying (r), and tabulate all results as follows—

 DATE . . . No, of cells . . .

of Anale . . . sq. ln, Are of Cathole . . . sq ln.

				lura zami	lance -								
Г	T	—. 		Primary.					Scontdary,			Voltage Batto	
Value of S.	Tempr. of Bolu- tion,	Periods prr Sec,		Ampe,	Walt- meter Read- ing DIV.	True Wett- if.	Ap- parent Walts AV.	Power Factor IV	Volta (v).	Amps.	Watts (140).	of	Red- ency 17
-	1		 —	<u></u>	· —		[—			¦	<u> </u>	<u> </u> —-	

Note.—If the valve is cooled by forced air draught, the power absorbed in producing the draught must be added to the true watts (IV), or watts (av), according to whether it is supplied by the primary or secondary circuit respectively.

- (11) Plot curves on the same sheet, having values of—power factor; volts (v); efficiency; and voltage ratio as ordinates, with secondary load (av) as abscisse; also between efficiency as ordinates and temperature as abscisse at constant secondary
- lead.

 (12) Plot curves (for Exp. 8 and 10) with voltage as abscisses and the other quantities as ordinates; also (for Exp. 9 and 10) with periodicity as abscisse and the other quantities as ordinates.

Inferences.—State clearly all the inferences deducible from experimental results.

(145) Efficiency of a Rotary Rectifier.

Introduction.—Rotary rectifiers are employed for the purpose of rectifying single-phase alternating current into unidirectional or continuous current, and comprise a special form of commutator driven at synchronous speed by a suitable single-phase synchronous a.c. motor.

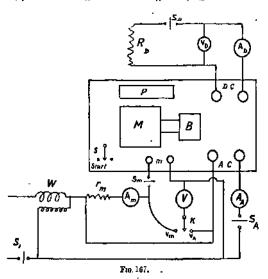
The new well-known Ferranti retary rectifier comprises, in addition, a constant-current static transformer, which, when supplied with varying a.e. at constant pressure, automatically delivers constant direct current at varying pressure for supplying are lamps in series. Since the motor is driven in this case from a separate secondary coil on the static transformer, the ratio of the d.e. power output to the a.e. power intake by the primaries of the transformer gives the overall net efficiency which may be over 91% at a full load of 40 H.P. with a power factor of 0.90.

In the Morton and Wright rotary rectifier there is merely the special commutator and synchronous motor, the roctification being from varying current at constant a.c. voltage to "arying current at constant voltage on the d.c. side.

Apparatus.—The rectifier complete comprising—motor M, commutator B, diphaser P and starting switch S; ammeters A_n , A_A and A_B ; voltmeters V and V_B ; switches S_B , S_m , S_A and S_B , and two-way voltmeter key K; wattenever W; load absorbing device R_B ; and non-inductive regulating resistance r_{-} (if necessary).

Observations.—(1) Connect up as in Fig. 167. The terminals marked (m) Fig. 167, are for the motor circuit, and those marked DG and AG are the terminals for the direct and alternating currents sides of the rectifying commutator B. Adjust all the instruments to zero, levelling such as require it, and see that the bearings of the rectifier, and those of any other machine in use, are properly lubricated before starting. See also that the two brushes, which rub on the central-sectioned part of the rectifying commutator, are adjusted to touch on the thin strips simultaneously.

- (2) With the woitch (S) on the stud marked Start, close S_1 and S_m only, and move the brush rocker on the motor itself, until the machine emits a constant hum and runs quite sparklessly, when it will then be in synchronism with the supply. Now switch S to the right-hand contact and if necessary re-adjust the position of the rocker to obtain sparkless commutation.
 - (3) With K on Vm note the readings of IV, Am and V.



- (4) With R_B full in and S_B open close S_A and again note W, A_m, V, A_A and V_B, K now being on stud V_A and V_m in quick succession.
- (5) Close S_D and note the readings of all the instruments for about ten different currents on A_D , from 0 to full load, by varying R_D ; adjusting the brush rocker of the rectifying commutator to get sparkless rectification at all loads.

Tabulate all your results as follows-

Name Rectifier: No Full-load Output =						٠	tauçe n	1						
Wattmeter Bending Dw. True Watta W.	Amps. de.	Apparent Apparent	Power Factor	Volts P.	3mls. 4.c.	4.7.2.	JP - IF.	445+4405	Volta F.p.	Amps, Ap.	Watts IF D.	Overall Efficiency Ap V p W - Am vr	Conversion Vb.	

(6) Plot the following curves:—between output W_D as abscissed and volts V_D; watts W; W = W_N/A_AV_A; efficiency; and voltage ratio of conversion, as ordinates in each case on the same curve sheet. Inferences.—State concisely all the inferences which may be deduced from the results of the above tests.

(146) Efficiency and Characteristic of Alternating Current Rotatory Converters. (Run from the Direct Current Side.)

Introduction.—The rapid development of multiphase alternating current machinery, but perhaps more especially of that particular class of the same, known new commonly by the name of the Rotatory Converter, marks one important epoch in the history of this all-important and ever-increasing branch of industry—Electrical Engineering. There are several different types of transformers, but all come under one or other of two main heads.

- (1) Static transformers or converters with no moving parts.
- (2) Rotatory transformers or converters having moving parts, and on which latter their very existence depends. The former of course include the ordinary every-day transformer which we are so accustomed to see.

The type 1 transforms electrical energy of one species at a particular pressure into the same species but at a different pressure, while type 2 transforms electrical energy of one species into that of another. To this class belong the various forms of multiphase rotatory converters. Those converting from multiphase alternating currents to continuous currents or vice verea, are usually multipolar machines, having any number of pairs of poles up to about 16 or more, with a periodicity ranging from 20 to something like 60 ____ per sec. Owing, however, to the conditions imposed by the relations between voltage, speed and size, they usually operate best at the lower periodicities.

The rotatory converter to be tested convicts of an ordinary

The rotatory converter to be tested consists of an ordinary direct-current machine, with the usual armature winding and its commutator at one end and three slip rings at the other, connected to three points on the armsture winding -0, & and & of the polar pitch apart, i.e. in a two-pole machine at 120° apart. machine when driven as a motor by direct currents taken in at the ordinary commutator end develops a 3-phase alternating current at the slip rings. It is this type of converter which is beginning to be used now on a large scale, only with more than one pair of poles, in long distance transmission of power, as follows-Polyphase alternating currents being transmitted at high pressure from the distant generating station, are reduced to, say, 100 to 300 volts by static transformers at the near end and then converted by the rotatory converter into direct currents, which may be employed for tramway, lighting, electrolytic purposes, or for charging storage cells. In any converting appliance, and therefore in any converter, the (total energy put in) - (total energy given out) = (total internal losses). These are made up of mechanical frictions at journals, brushes, and due to wind or air churning, magnetic hysteresis, eddy currents and copper lossos.

Owing to the armature reactions of the dynamo and motor currents practically balancing one another, no lead of the brushes in either direction is needed for sparkless running. A rotary converter is usually run from the A.C. side in

A rotary converter is usually run from the A.C. side in practice, but when "inverted," i.e. run from the D.C. side, as in the present instance, the nature of the external circuit will have the same effect on its field as it has on that of an A.C. generator, but with additional effects.

Thus on inductive load or power factor less than unity, a

leading current will cause an armature reaction which will atrengthen the field and hence reduce the speed, while a lagging

current will cause a reaction that will weaken the field and honce increase the speed, in either cause producing a change of frequency.

In fact, the increase of speed may become excessive from either small lagging power factors or short circuit causing excessive weakening of the field, which can only be counteracted by an *increase* in the natural excitation of the field proportional to the effect causing the increase of speed.

Apparatus.—Multiphase convertor U to be tested in the present case assumed to be for 3-phase currents; source of direct-current supply E; direct-current ammeters A and a and voltmeter V; alternating current ammeters $A_1 A_2 A_3$, and voltmeters $V_1 V_2 V_3$; non-inductive 3-phase rheostat $R_1 R_2 R_4$, and ordinary ones R

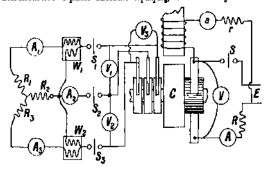


Fig. 168,

(p. 606) and r (p. 599); triple-pole switch S_1 S_2 S_3 and S; non-inductive Wattmeters W_1 and W_2 ; tachemeter.

Note.—Certain pieces of the above apparatus are not absolutely necessary to the text, but when available may preferably be inserted and used so as to clearly show what is actually taking place. Thus if the three resistances $R_1\,R_2\,R_3$ constitute a proper 3-phase rheostat (water or otherwise) (p. 607), which operates equally on each of the mains, then in addition to apparatus as before we need only have—one single 3-phase rhoostat $R_1\,R_2\,R_3$; one sumeter A_1 and voltmeter V_1 instead of the three; one 3-throw switch $S_1\,S_2\,S_3$, to close the three circuits simultaneously, and one Wattmeter.

The reason for such an alteration is fully described on p. 389, in connection with power measurements in multiphase circuits that are symmetrically leaded. The method or rule for deducing the power absorbed in such cases will be found there, and must then be used. In the present case we will assume that the circuits are not symmetrically leaded.

For a more detailed description of power measurements in multiphase circuits, see p. 388 et seq.

Observations.—(1) Connect up as in Fig 168, and adjust all the instruments to zero, levelling such as require it. See that all lubricating arrangements in use act properly. Increase $R_1 R_2 R_3$ to a maximum and r to a minimum. See that all the switches are open and that the brushes are fixed in the neutral position.

- (2) Start C like an ordinary D.C. motor, the speed and volts V being adjusted to, and kept constant at, the normal values. Take readings of all the instruments with S_1 S_2 S_3 open, and again with S_1 S_2 S_3 closed, for about ten different load currents on A_1 A_2 A_3 rising by about equal amounts to the maximum
- permissible by varying R_1 R_2 R_3 .

 (3) The excitation (a) and volts (V) being now kept constant at normal value, repeat the readings in 2.
- (4) The speed and excitation being next kept constant at normal value, repeat 2.

	NAME.		Date				
Rotatur	y Convertee	; No	Type	Maker			
91				Amps a Speed =			
*	Þ		•	, olong at *O,			
		Artusto	ne , ram,				
		Mormal ratio of	conversion a				
		Periods not make	ni≅. K⇔				

Sysool Raves, per min, Jr. Programmy (E) Programmy (E)		₩aLls				Am) + 4.	1	Month of the	Reve. per min.
--	--	-------	--	--	--	----------	---	--------------	----------------

(5) Report 2-4 for a highly inductive circuit R_1 R_2 R_3 .

(6) From observations 2-5 plot the efficiency curve having

 H_1 as albacissm and Σ as ordinates. The external or a-c characteristic with V_1 as ordinates and A_1

as abscisse. The current characteristic with A as ordinates and A_1 as abscisse.

The voltage ratio, input, and speed as ordinates and H_2 as abscisses.

From the current characteristic indicate how the officiency of the convertor could be calculated at any load and also work out the ratio of current transformation.

Inferences.—State very clearly all that can be deduced from your experimental results.

Note.—If n = number of armature windings per radian,

e maximum E.M.F. per turn of winding, and if we assume the flux in the interpolar space to be sinusoidally distributed, and that the E.M.F. is a sine function of the

time, then the voltage ratio of conversion with 3 phase connections

$$=\frac{\sqrt{\frac{3}{2}}}{2}\frac{nc}{nc}=\frac{1}{2}\sqrt{\frac{3}{2}}$$

and the virtual voltage across any pair of slip collector rings will ~ 61.23 when that impressed on the direct current side = 100 volts.

In other words, the voltage ratio of conversion with sins distribution of flux in the interpolar space = 61.23 %.

As, however, the flux is never so distributed, and, moreover, as the voltage ratio depends to a large extent on the polar arc, pole, shape and position of the brushes, the above ratio is only roughly about what may be expected.

The C^2R total loss and temperature rise will be less in the machine used as a convertor than when used as a dyname.

(147) No-Load (open circuit) Characteristic or Magnetization Curve of Continuous-Alternating Current Rotary Converters. (Run from the Continuous Current Side.)

The No-Load Characteristic or curve of magnetization of a converter from which its magnetic properties and most suitable excitation is seen can be obtained in one of the two following ways—

- (1) By driving the retary at constant speed from a direct coupled motor, or by belting, and noting the readings of the voltmeters across the d.e. and a c. sides respectively for each of some ten values of exciting current obtained from some outside d.e. supply, and differing by about equal amounts from 0 to say 25% above normal excitation and taking a similar descending set of
- readings.

 (2) By connecting up exactly as in Fig. 168 and driving the rotary as a motor from its d.c. side.

With the field current (a) adjusted to say 20 % above its normal value (if possible) start the retary up in the usual way to maximum speed obtainable with this excitation, and R cut out. Note the readings of speed (to insure constancy throughout) and both a.c. and d.c. voltages for this maximum excitation, and for each of about ten smaller values obtained by increasing r and differing by about equal amounts down to the minimum practicable, the speed being kept at the same constant value by increasing R, and tabulate as on page 436. Plot the magnetization curva, having exciting currents as abscissa, and the a.c. and d.c.

voltages as ordinates respectively.

Deduce a third curve by joining the points obtained on deducting the armature drop (= current × its resistance) from each of the d.c. voltage ordinates.

Plot also a curve having a.c. volts as ordinates with d.c. volts as abscisse and deduce the voltage ratio of conversion. Compare this ratio with the theoretical value and explain the reason for any difference.

(148) Effect of Variation of (1) Excitation (2) Speed on the Voltage Ratio of a Rotary Converter (Run from the Direct Current Side.)

Observations.—(1) With exactly the same connections as in Fig. 168, and with S_1 , S_2 , S_3 open, note the readings of all the instruments for constant speed throughout, for about eight different values of exciting current (a) differing by about equal amounts between the minimum and maximum values possible.

(2) Repeat (1) with S_1 , S_2 , S_3 closed, and at $\frac{1}{4}$, $\frac{1}{4}$ and full load respectively, the load being kept constant by varying

 R_1 , R_2 , R_3 .

(3) Repeat 1 and 2 for a similar variation of speed at constant normal excitation and tabulate as on p. 436.

Plot curves for Tests 1 and 2 at each load having exciting currents (a) as abscisses, and (1) a.c. volts, (2) d.c. amps, (3) voltage ratio of conversion, as ordinates in each case, and for tests (3) curves having speeds as abscisses with voltage ratio; a.c. volts' and d.c. amps. as ordinates.

Inferences.—State concisely all that can be deduced from the results of your investigations in the present test.

(149) Efficiency and Characteristics of Alternating-Continuous Current Rotary Converters. (Run from the Alternating Current Side.)

Introduction.—The investigations to be made in the present case are all the more important and instructive because the usual application of this kind of rotary, commercially, is to convert a.c. to d.c., the machine being supplied with a.c. and running as a synchronous a.c. motor. The speed at which it runs will therefore solely depend on the number of poles in the field, and on the periodicity of the a.c. supply, and if this latter is constant the speed will be also, irrespective of the load developed at the d.c. side, or of the excitation. As the load increases, for constant power factor, a.c. voltage, and frequency, "armature reaction" causes an increasing drop of d.c. voltage, and, further, a decrease of excitation is necessary to maintain constant power factor, but

an increased variation of d.c. voltage results. On the other hand, a constant excitation increases the intake current, but decreases the variation of d.c. voltage. By varying the excitation to maintain constant d.c. voltage, this latter, and also the efficiency, is increased. In order to minimize the variation of d.c. volt ge, and maintain a constant voltage ratio as the load changes, retaries are usually compound wound, the series coils. just as in the case of an ordinary compound dynamo, producing an increase of excitation proportional to the load, and simultaneously, the necessary change of power factor. A rotary can be over-compounded so as to give an increasing d.c. voltage with load to make up for loss of voltage in transmission, in which case unit power factor is obtained by field regulation at some fraction of full load, thereby giving leading currents at full load. On a light constant load, a given variation in the excitation causes a much greater change in the current intake and power factor than it would do on a heavy constant load. Since the lest armature volts in a rotary run from its a.c. sido = (current x armature impedance), while when run from its d.c. side this quantity =current xurmature resistance, and also owing to the power factor not being unity; to the wave-forms of a.e. supply, and of the rotary (cun from the d.c. side) being different; and to armature reaction, the voltage ratio of conversion will be different when run from the d.c. and a c. sides. Further, when the power factor of the circuit is low and the current comparatively large and lagging, the supply and lost armsture volts will be more nearly opposite in phase, and hence a larger armature drop results at the small excitations. A rotary has unit power factor at a particular excitation, also too low an excitation causes the current to lag, while too high an excitation causes it to lead as shown by the V curves between excitation and power factor obtained in

Apparatus.—Precisely that prescribed for Test 146, except that the s.c. supply is substituted for, and takes the place of, R_1 , R_2 , R_3 , and that some form of synchronizer is needed. If the phases are equally balanced, or if all the instruments on the s.c. side are unavailable, then any two ammeters such as A_1 and A_3 and any two voltmeters such as V_1 , V_2 may be omitted. Also one

the above investigation. Constant d.c. voltage at all leads can be maintained by adjusting the excitation to give unit power

factor at full loud.

of the two wattmeters shown might be omitted, means being provided by a two-way key for connecting one end of the fine wire coil of the wattmeter used to the remaining two supply mains in quick succession. It will be noticed that a three phase rotary is assumed for the test, but the same considerations and investigations would apply to single- and two-phase rotarios.

Connections.—To be as shown in Fig. 168, unless modified by a reduction in the number of a.c. instruments as mentioned above. The simplest and most convenient form of synchronizer to employ consists of two ordinary glow lamps supported in two ordinary beyonet holders connected in series and carried on a base board with two terminals. The sum of the voltages marked on the lamp bulbs must not be less than the sum of the supply and converter a.c. voltages. The two terminals of this "lamp synchronizer" may be connected so as to short circuit S_1 , say a piece of thin wire short circuiting, say, S_2 .

The Process of Synchronizing the rotary with the a.c. supply is usually most conveniently accomplished as follows—

- (a) Adjust all instruments which need it, and with S_1 , S_2 , S_3 open, start the rotary up as a d.c. motor from a d.c. supply E, by closing S_1 and operating the starter (not shown), with which the machine is provided, in the usual way,
- N.B.—If there is no startor, the adjustable load resistance R may be used for starting up.
- (b) Adjust R so as to obtain the same voltage on V_2 as that of the main a.e. supply, and then adjust r to give such a speed that the lamps go out. The a.e. supply and a.e. voltage of the rotary are now equal to, and opposing, one another, and of the same frequency, and hence in synchronism. The switch $S_1S_2S_2$ must now be closed, and S at once opened, when the rotary will continue to run, now as a self-exciting three-phase synchronous a.e. motor.

It may be mentioned that the a.c. voltages of the main supply and of the rotary are in assisting series when the lamps show steady luminosity, while between this and the "quite out" condition they pulsate in brightness due to the current pulses of the two-E.M.F.s trying to eatch up to one another.

Of course, a separate motor, or driving source, if available, might be used to run the rotary up to synchronous speed instead of the d.c. supply above named. If the d.c. supply used for starting-up purposes is unsuitable for giving the necessary a.c. voltage on the rotary at the required speed, the rotary may be run up to a much higher speed than that of synchronism, S then being opened, and afterwards $S_1S_2S_3$ closed, at the moment when the speed falls to such a value that the lamps go out.

Note.—If an outside d.c. supply is used in synchronizing, then directly the rotary is running synchronously on the a.c. supply and S is opened, at once disconnect the mains E from the auxiliary d.c. supply, and connect them together to avoid the presibility of a future mishap by forgetting to do this at the time. Several investigations on the operation of the converter under different conditions can now be undertaken.

Effect of variation of Direct Current Load on the operation of the Converter at Constant Direct Current Voltage and Excitation, and Alternate Current Frequency.

Observations.—(1) Adjust the exciting current (s) by means of (r) until the intake a.c is a minimum, then with S still open, note the readings of all the instruments and the speeds of the retary and generator (giving the main a.c. supply) respectively for normal frequency.

- (2) Close S and note the readings of all the instruments and the speed, for about eight different d.e. leads rising by about equal amounts between 0 and full lead, by varying R; keeping the current (a), the supply frequency, and the d.e. voltage (V) (by varying the excitation of the main generator), constant throughout.
- (3) Repeat (1 and 2) above for a lower and also for a higher constant excitation than that proviously found in Test 1 above, and tabulate your results as shown in the table.
- (4) Plot curves between d.c. output in amps. A as abscicate, and (a) efficiency S, (b) power factor, (c) mean intake a.c. amperes, (d) mean a.c. volts, as ordinates in each case.

(150) Effect of variation of Direct Current Load on the operation of the Converter at Constant Alternate Current Voltage and Frequency, and Direct Current Excitation.

Observations.—(1) With constant normal a.c. voltage and frequency maintained throughout, repeat (1-4) Test 149 above, plotting for (4d) above the d.c. volts instead of mean a.c. volts as ordinates. The curve between V and A is called the d.c. characteristic of the rotary.

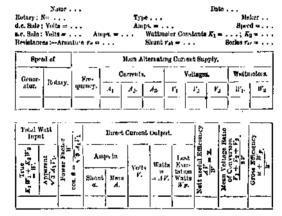
(151) Effect of variation of Excitation on the operation of a Converter at Constant Alternate Current Voltage and Frequency, and Direct Current Load ("V" curves).

Observations.—(1) With S open, and the converter running at constant normal a.e. voltage and frequency, note the readings of all the instruments, and the speeds of the main generator and relary for about eight different exciting currents (a) between the lowest and highest permissible by altering $\langle r \rangle$.

- (2) Close (S) and repeat (1) for constant leads of about \(\frac{1}{4}\), \(\frac{1}{2}\), and full d.c. lead and tabulate as indicated.
- (3) Plot curves between d.c. amperes of excitation as abscisse and (a) power factor, (b) intake alternating current, (c) voltage ratio of conversion, (d) intake a.c. Watts.
- (152) Variation of Excitation to Maintain Maximum Power Factor for Varying Direct Current Load at Constant Alternate Current Voltage and Frequency.

Observations.—(1) With S open, and the retary running at constant normal a.c. voltage and frequency, adjust the excitation (a) so as to obtain minimum intake current, and note the readings of all the instruments and the speeds of main generator and

- (2) Close S and note the value of the exciting current (a) necessary to give minimum intake current at about 8 different d.c. loads between 0 and the maximum (by altering R), the a.c. voltage and frequency being the same at each load. Note all the other instrumental readings and tabulate as indicated.
- (3) Plot curves between d.c. load in watts as abscisse and (a) d.c. volts, (b) exciting current, (c) a.c. amperes, (d) power factor, (e) voltage ratio of conversion, (f) efficiency.



Inferences .- Very carefully consider and state all the inferences which can be deduced from the results of your investigations. (153) Efficiency and Output of a "Booster"

or of a "Motor Generator Set."

Introduction.—It frequently happens in practice that either electrical power in one form at a certain pressure is required in the same form but at a different pressure, or that electrical power of one nature is required in quite a different nature at the same pressure or otherwise. The electrical appliance by means of which such transformations can be effected is variously termed a "Motor Generator," "Booster," "Rotatory Converter," "Continuous Current Transformer," etc.

In all these appliances the desired effect is produced by machinery in motion, and only so long as it is in motion. The motor-driven Booster at the present day is essentially a device for transforming direct-current energy from one pressure to another. Speaking in general terms a Booster is a machine for adding a small percentage of E.M.F. to a large generator and is much used in storage battery systems. The Motor Generator and Converter very frequently constitute a device for transforming electrical energy in the form of direct currents into that of the

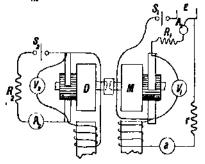


Fig. 109.

form of single and multiphase alternating currents or vice versal. The motor generator frequently takes the form of two separate machines, on the same bed plate, with their shafts in alignment and coupled mechanically. One machine M constitutes an electromotor, fed from an external source of electric supply, the other is a generator D which is driven direct by the motor and develops electrical power.

As machines of this nature are used to some considerable extent as "regulators" to "feeder mains," and also with some slight constructional difference as "equalizers" on the various systems of parallel distribution, the determination of their efficiency and output becomes of considerable importance.

Apparatus.—Motor generator MD; source of electrical energy E; ammeters A_1A_4 and a; voltmeters V_1 and V_2 ; theostats R_1R_2 (p. 606) and r (p. 599); switches S_1 and S_2 ; tachometer.

Note.-Prior to starting, all lubricators must be seen to feed Observations.—(1) Connect up as in Fig. 169, and adjust the

pointers of all the instruments to zero. Increase R_1 R_2 to their maximum and τ to a minimum. See that $S_1 S_2$ are open and both sets of brashes down,

- (2) Close S_i and adjust R₁ so that the normal speed N for the particular "set" tested is obtained. Note simultaneously the readings of A_1 , a, V_1 , V_2 and N.
- (3) Close S_2 and adjust $R_1 R_2$ so that A_2 reads about $\frac{1}{10}$ full load current in amperes, N being the same as before. Again read all the instruments.

N.B.—It may be found necessary to vary the excitation of M by means of the resistance r in order to keep the speed constant throughout any one set of readings.

 Repeat 3 for about ten different load currents Λ_s up to the maximum, rising by about equal increments at a time.

NAME . . .

(5) Repeat 3 and 4 for speeds 20% above and 50% below normal, and tabulate your results as follows-

DATE . . .

(6) Plot an officiency curve for each spred having W₂ as abscisse and X as ordinates. Also curves having ordinates.

Inferences.—State clearly all the inferences which you can draw from the results of your experiment. Could the combined efficiency be increased by any structural alterations in the "set" tested t

(154) Determination of the Periodic E.M.F. and Current Curves of an Alternator.

Introduction.—It may sometimes be desirable to determine the periodic curve or wave of E.M.F. and current in an alternating current circuit, for the shape of such curves has an important influence on the losses occurring in the iron cores of any appliances in the circuit. In fact, the more peaked the E.M.F. curve, or the more nearly it approximates to a sine or even a triangular curve, the less will be the losses occurring in such appliances and the greater will be what is called the "form factor."

Two cases may arise in which it is desired to obtain the

periodic curves, namuly (1) when the alternator supplying the circuit is at a long distance away, and consequently inaccessible in a sense, (2) when the test can be applied close to the alternator, if necessary. In either case some convenient form of rotating contact maker must be used to close the circuit of a suitable measuring arrangement for an instant once every revolution, at any definite point in the period of alternation, corresponding to the position of the brush or contact arm. Hence by moving this contact arm into various angular positions, the periodic curve of instantaneous values of varying E.M.F. and current at different instants can be obtained throughout the whole period or wave. Such a contact maker is illustrated and described in the Appendix, p. 619, and in case I above it is fitted to and driven

shall here consider, the contact maker is fixed to, and is driven by, the rotating portion of the alternator itself.

Knowing then the periodic curves of E.M.F. and current in a circuit together with their phase difference, at once seen from the relative positions of the two curves, the true instantaneous power developed in that alternating current circuit can at once be

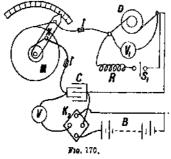
by a synchronous alternating current electromotor run off the supply of which the E.M.F. or current curve is desired. Such a motor always runs at a speed bearing a definite and fixed ratio to the periodicity of the supply current. In case 2, the one we

The following method of obtaining such curves consists in charging a condenser to a certain E.M.F. by periodically connecting it, by means of the contact breaker, to the alternating circuit to be tested, and measuring this E.M.F. by an electrostatic volumeter. This will therefore be the instantaneous value of the potential at the point of the period of alternation corresponding to the position of contact of the brush on the contact maker.

deduced.

The function of the condenser is to maintain the instantaneous voltage at a uniform value and so insure a steady reading on the voltmeter, notwithstanding the leakage usually occurring from it, in the interval between successive contacts.

If a Kelvin multicellular voltmeter (preferably dead beat type) is used for the test it will be necessary to obtain a falso zero of about 30 on its scale, as the one volt graduations only commence from this point upwards. For this purpose an auxiliary voltage of about 30, which can be supplied by a battery of about 15 small secondary cells, may be used. As the circuit is closed by the contact maker for a small fraction of a second only, the condenser should have a small capacity, otherwise it may not be fully charged. Even though V and C are well insulated a certain amount of leakage may occur, depending on the rate of contact—i.e. on the speed of D. A known steady P.D. should therefore be applied in place of the alternator P.D., and the speed adjusted to the value above, then if there is leakage I will read differently when the contact is stationary and when periodic; the ratio of these two x V, gives the instantaneous P.D. In the determination of the current curve a low non-inductive resistance should be used, so that its introduction may not affect the existing conditions of the circuit to any appreciable extent. The P.D.s in this case will be small, and can be measured by the ordinary "Null deflection," or balance method on a potentiometer. The amperes per scale division can be found by passing a "known steady direct



current" through (r)
from a supply in place
of D, the rate of contact being as above;
then known current
÷ scale reading = amperes per div.

Apparatus. — Alternator D with its exciting circuit; contact maker M (p. 619); well-insulated electrostatic voltmeter V (p. 503), and also $\frac{1}{4}$ to $\frac{1}{8}$ $m_1 f.d.$

condenser C; well-insulated battery B; A.C. voltmeter V_1 ; A.C.

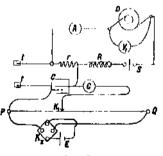
numeter A; switches S and S_1 ; load resistance R, in which the current wave is to be found; non-inductive resistance r, of such a size as will carry the current without sensible heating; sensitive H.R. galvanometer (p. 569); potentiometer PQ (Fig. 171), with its slider key K_1 ; E.M.F.—E (2 volts), and reversing key K_2 (p. 585). Note .- All lubricating arrangements must be seen to feed properly when the machines are started.

E.M.F. Conve.—Experiments—

- (1) Connect up as in Fig. 170. Set N to 0 on its scale and measure the auxiliary voltage (v) on V by short-circuiting C by a wire and afterward removing this,
- (2) Start D and adjust its speed to the normal value say, also its excitation so as to give about normal voltage on the voltmeter V₁.
- (3) With the speed and terminal P.D. constant, note the steady reading on V, which therefore is a measure of the instantaneous E,M,F, of D for this position of X.
- (4) Repeat 3 every 20° from 0 throughout the period of alternation (360°) by moving X_i noting the points when K_2 is used to reverse the E.M.F. of B.
- (6) Repeat 2-4 when D is giving a convenient constant current through a snitable inductive circuit R.

CURRENT CURVE. - Reperiments -

- (1) Connect up as in Fig. 171, Set X to 0 and repeat 2 above. (2) With R at its
- maximum, close S and adjust the current to the same value as mentioned in 5 above, by means of the exciting current.
- (3) With the speed normal and terminal P.D. constant, obtain balance with K, so that, on pressing it, no deflec-



Fra. 171,

tion occurs on G. Note the scale reading (d) of $K_{\mathcal{D}}$ which

therefore is a measure of the instantaneous P.D. at the resistance r

• • • • • • • • • • • • • • • • • • • •	odate your results as follows—
NAME,	DATE
Speed of $B = \dots$ Revul per tain Cap alty of $C = \dots$ and $f \in A$.	Frequency per sec.
Reading of voltmeter $Y_1 =$ volts Reminster $A =$ and a .	For any Resistance $r = \dots = 0$ blues, Volta per dist, of P Q (a) $\rightarrow \dots$ Altips $q = q = q$ (B) $\sigma = q$
Reading of Total Nelt last. Reading of	day Actual Inst. Angle of Physics

battery switch, according to whether (v) was previously in helping or opposing series. Half the difference between the readings = v. It will be obvious that the instantaneous terminal voltage of D can be obtained in addition to the current, if in Fig. 171 E has a value at least = the maximum value of that voltage; PQ has

Note.—2 v must either be added or subtracted, on reversing the

has a value at least = the maximum value of that voltage; PQ has a high resistance, and a two-way key be used in place of the permanent connecting wire between C and r, so that it will connect C successively to (r) as shown, and to the junction of R and S, which latter gives the terminal instantaneous voltage.

R and S, which latter gives the terminal instantaneous voltage, (5) Plot the E.M.F. and current curves on the same curve sheet, having θ^* as abscisse in each case and V_1 and A_1 as ordinates respectively, and calculate out from them the $\sqrt{\text{mean square}}$ of the instantaneous values of V and A_1 .

In determining the periodic curves of K.M.F. in a high tension circuit a potentiometer arrangement should be used; the wires going to D (Fig. 170) being connected to the ends of a suitable known fraction of a known high resistance placed across the mains, and which can carry an appreciable current, say $\frac{1}{4}$ to $\frac{1}{2}$ an ampere, thus illuminating any error arising from the capacity current of the voltmeter.

(155) Determination of the Periodic E.M.F. and Current Curves of an Alternating Current Circuit. (Ballistically.)

Introduction.—Should an electrostatic voltmeter not be available as in the preceding method, a reflecting ballistic galvanometer

G may be used, and it should preferably be of the moving coul . D'Arsonval type, so as not to be affected by the stray magnetic fields invariably met with in a dynamo-room. In all other respects the present method is precisely similar to the last. K_2 is a reversing key (Fig. 255) for obtaining deflections each side of zero. When the two-way key K (Fig. 256) is put to stud 1 the condenser C is charged to an E.M.F. corresponding to that for the position of the contact arm X in the period of alternation. On putting K to 2, C is discharged through G, and since the resulting throw is so the quantity flowing out of C, which in turn is or $C \times V$, where C =capacity of the condensor and V the E.M.F. to which it is charged, we see that the resulting momentary throw on $G \propto V_1$ since the capacity is a constant. This should be larger the smaller the charging H.M.F. to be measured The carrent carve is obtained in a precisely similar manner to that indi-

(156) Delineation of Wave-Forms by means of the Duddell Oscillograph.

cated in Fig. 171.

Introduction.—The shape of wave-forms in general, but perhaps more especially those of current and pressure in alternating current circuits, are of the utmost importance to electrical engineers. For instance the efficiency of transformers and a.c. motors, and even the working of the latter, is in some cases seriously affected by the wave-form of the supply. On the other hand, the optical efficiency of the a.c. are has been found to be 44% higher with a flat-topped E.M.F. curve than with a peaked curve, while transformers work most efficiently on peaked curves. Again the wave-form reveals the presence or otherwise of higher harmonics due to accidental though often avoidable resonance effects, so dangerous in causing the breakdown of the insulation of high-tension electric cables.

The oscillograph itself consists of a highly specialized reflecting d'Arsonval galvanometer having an extremely small periodic time, when undamped, of from $\gamma_{\theta | \sigma}$ th to $\gamma_{\theta | \theta | \sigma}$ th of a second, depending on the type of instrument,

For all ordinary frequencies the oscillograph is perfectly deadbest, absolutely free from hystoretic errors, and has practically no self-induction or capacity.

It is therefore an accurate instantaneous animeter or voltmeter capable of giving a deflection which is at any moment accurately proportional to the instantaneous value of the variable even with frequencies of 300 or more periods per second on any wave-form whether periodic irregular, or non-periodic and whether continuous or alternating.

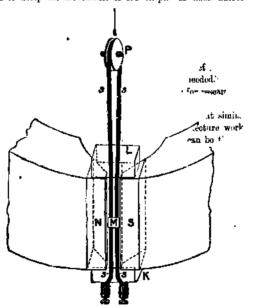
Thus in addition to recording E.M.F. and current waves, such an instrument will indicate the charge and discharge curves of condensers, the changes of P.D. and current on breaking an inductive circuit, the P.D. and current changes in the armature coils of a dynamo or motor, or in the primary of an induction coil or even the very rapid changes when the d.e. are hisses. Doubtless it will be employed for a vast number of other determinations as time and necessity arise, but the preceding merely serve to indicate some of the uses to which this highly important instrument has already been put.

Construction of the Duddell Oscillographs.

The apparatus consists of the galvanometer, combined either with a rotating or vibrating mirror, moving photographic film, or falling photographic plate.

Fig. 173 is a diagrammatic view of the galvanomoter part of the instrument showing the principle on which it works. In the narrow gap between the poles N, S of a powerful magnet are stretched two parallel conductors s, s formed by bending a strip of phosphor-bronze back on itself over the palley P which is attached to a light spring balance. At the bottom ends the strips are clamped on a block, K, while at the top they are held in position by the bridge piece L. By altering the tension on the spring stretching the phosphor-bronze loop, the periodicity of the instrument cun be varied at will. Each strip or leg of the loop passes through a separate gap (not shown) in the magnetic circuit. The clearance between the sides of the

gaps and the moving strip is but 0.38 mm, and these gaps are filled with a viscous oil, over which is placed a small lens, which is held in position entirely by the surface tension of the oil, and serves in its turn to keep the oil in place. The object of the oil is to damp the movements of the strips. A small mirror



Fro. 173.--Essentials of the Vibrating System.

marked M is attached to the loop, as shown. The effect of passing a current through one of these loops is to cause one leg of it to advance whilst the other recedes, and the mirror is thus turned about a vertical axis. In the high frequency instrument the hatural period of vibration of the loop is Trioth of a second, and the clearances being, as stated, extremely small, the damping effect of the oil is so great, that the instrument can be relied

upon to give accurate results even when the periodicity of the current to be tested is over 300 periods per second. Small fuses below the loops protect these from injury in case of accidental excessive current. The fuses consist of very fine wires enclosed

in glass tubes, which are held in position by spring clamps. The beam of light reflected from the mirror M is received on a screen or photographic plate, the instantaneous value of the current being proportional to the linear displacement of the spot of light so formed. With alternating currents the spot of light oscillates to and fro as the current varies and would thus trace a straight line. Foor e to obtain an image of the wave-form, it is necessary to tes in addie photographic plate or film in a direction at right angletrumant direction of movement of the spot of light. A secon mirror can be interposed in the path of the beam of light, ductive mirror caused to vibrate or rotate so as to impart to the roils of a u, t, a uniform motion propertional to time in a plane at right even is to the plane of vibration of the Januar due to the current. The spot of light will now trace out on a stationary screen or plate the time curve of the variation of the P.D. or current as the case may be. If the variations are periodic, as in alternating currents, then the second mirror can be synchronized and the spot of light caused to trace out the wave-form over and

over again.

The various methods of examining and recording the waveforms will be described later.

The Oscillograph is provided with an adjustment for slightly increasing the periodic time and sensibility. This may be done by altering the tension of the strips. This is not advisable, however, as it is hable to spoil the definition of the spots.

Four standard types of Duddell Oscillograph are made and are in common uso, namely—

Type I. The Double High Frequency Oscillograph, which is the

most sensitive type and has a powerful electro magnetic field. The magnetizing coils are wound in eight sections, and by suitably connecting them the field can be excited direct from any voltage between 25 and 100 volts or from 200 volts with an 8-c.p. lamp in series. The magnetic circuit being saturated, a change of 4% up or demand a continuous convent only changes the sensibility shout. 1%

series. The magnetic circuit being saturated, a change of 4% up or down in exciting current only changes the sensibility about 1%. To introduce damping oil, the vibrator cover should, be removed, the lens lifted up, the vibrator being held horizontal and a drop

or two of the special oil placed on the gaps over the mirrors. The lens is then Iowered into place, the lower edge first, cure being taken not to imprison any air bulls. The temperature of this oil is measured by inserting the bulb of a thermometer at the back of the vibrator.

II. The Single Permanent magnet, and III. the Double Per-

manent magnet, Oscillographs are similar to one another. In each the electro magnet of Type I is replaced by a permanent magnet, and the damping oil, which is introduced by means of a small cup at the back of the instrument, is adjusted to give correct damping at 15° C., and practically correct damping

between 10° C. and 20° C., so that no thermometer is needed. These two types are portable and can be easily insulated for research on 10,000 volt circuits by placing it on an aboutto table.

IV. The Double Projection Oscillograph is somewhat similar

to Type I, and is most suitable for teaching and lecture work. Wave-forms having a total amplitude of 1 metre can be thrown

on to a serven.

The above types are single or double according as they possess

one or two strips respectively. The double or two-strip pattern is practically two single instruments built compactly in one magnetic field and capable of recording simultaneously any two distinct wave forms. A fixed mirror is fitted in addition to give the datum or zero line. Types II. and III. can be arranged in portable form.

Three Methods are generally employed for Observing and Recording the Movements of the Spots.

- 1. Visual observation. A rotating mirror is placed with its axis horizontal in such a position that the reflection in it of the moving spot on the screen can be examined; when, owing to persistence of vision, the moving spot will appear drawn out into a bright time curve of the variations which it is required to observe, and this curve can be sketched if required for future reference.
 - 2. Recording by photography. A photographic plate or film

is caused to move rapidly at right angles to the plane of vibration of the beam of light, so that the moving spot traces out on it the required variations.

The photographic method is very expeditions, and gives permunent records which are free from all errors of a personal nature; it is the only satisfactory method of recording irregular non-periodic variations of P.D. and current.

3. Tracing In this method, which is only applicable to periodic variations, the beam of light from the Oscillograph is reflected by an additional mirror with its axis horizontal before

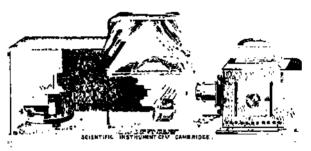


Fig. 174. Type I Double Oscillograph with Synchronous Matter and Tracing Desk.

reaching the screen, and this latter mirror is caused to move uniformly and synchronously with the period of the variations to be recorded. This combination of the two motions at right angles, the one proportional to the instantaneous value of the current through the Oscillograph, and the other to the time, causes the spot to travel continuously along the time curve of variation of the current, which curve, if the frequency is sufficiently high, will appear as a stationary bright line of light. This curve may be recorded by tracing or photography. In the Projection Oscillograph, this stationary line of light can be thrown either on the screen or on the tracing desk.

The arrangement employed for tracing a.c. wave forms which remain fairly constant in shape and frequency and thus obviating the necessity for using photography is shown in Fig. 174. In it the light from the Oscillograph mirrors is reflected vertically by a small mirror which is made to vibrate synchronously by means of a specially designed alternate current motor. The light is thrown on to a curved screen, on which tracing paper is held by means of a clip and on which the wave-forms appear as

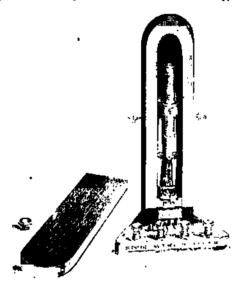


Fig. 175,-Type III. Double Permanent Magnet Oscillograph,

stationary curves of light, and may be traced by hand. The small mirror is vibrated by means of a can attached to the motor shaft. The cam is so arranged that the mirror moves uniformly for about 1½ complete periods during which the waveform is observed; it then returns rapidly to its starting point during the remaining ½ period. During the half period of return motion, the light is cut off from the Oscillograph by means of a sector fixed to the motor.

The Oscillograph shown in Fig. 175 can of course be substituted for that shown in Fig. 174, the tangent screw heads s, s, Fig. 175, being for the purpose of bringing the spots of the Oscillograph to zero on the screen.

The Synchronous Motor.—Seeing that this must run dead synchronously with the wave-forms to be recorded, it should be supplied from the same circuit.

To start the latest type of motor, connect the three terminals on it to the phase-splitting board by means of the three-way flexible lead attached to the latter. Care must be taken to connect the wires to the terminals correspondingly marked, the remaining two terminals on the phase-splitting board being connected to the a.c. supply having a P.D. of 100 to 120 volts with any frequency between 30 and 100 — per sec.

See that the armature of the motor is quite free by turning the milled head, and that the bearings are well oiled, then after pushing the movable core of the choking coil in as far as it will go, close the switch. Now give the armature a start by sharply twisting the milled head on its spindle at the vibrating mirror end in the clockwise direction, when it should continue to run and increase in speed up to synchronism.

If the motor does not attain synchronism (indicated by the "beats" in the sound emitted), draw out the core of the choker little by little until a constant rhythmic hum is given out.

The position of the core for synchronism depends on the wave-form and frequency, being further out the higher the latter. If the core is too far in, the motor will not attain synchronism, and if too far out the motor will take too much current and get hot.

It might be necessary to remove the load from the motor at starting by pressing back the mirror so as to lift the "follower" of the cam.

The wave-forms will have more than one complete period, and will move to and fro on the tracing disc or screen if the motor is running below synchronous speed.

Method of Connection of Oscillographs to 'the Circuits to be Investigated.

The P.D. required to work the Oscillographs when fuses are used in series with the strips is only 1 to 1.5 volts. For current curves a non-inductive shunt R_2 should be placed in the main circuit and connected as shown in Figs. 176 and 177. The low resistance R_2 serves to adjust the sensibility to a round number of amperes per millimetre. An Ayrton-Mather shunt giving six sensibilities for currents from 1.5 to 60 amperes is made for this purpose. When the sensibility is adjusted by altering R_2 to a round number of amperes per millimetre for any one of the

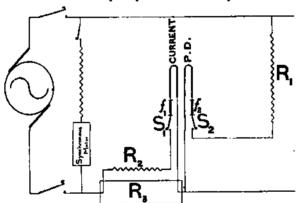


Fig. 178.—Diagram of Connection of Oscillagraph to Low Tension Circuit.

sensibilities, all the other positions of shunt are simple multiples of the same; thus with Oscillographs Types I., II. and III. the sensibilities may be 0.05, 0.1, 0.2, 0.5, 1.0, 2.0 amperes per millimetre. Standard Potentiometer shunts constructed for a drop of 1 to 1.5 volts can also be used in place of R_8 .

For P.D. measurements up to 250 volts a non-inductive resistance R_1 is placed in series with the strips, Fig. 176, which is adjusted to give a round number of volts per millimetre deflection. The switches S_1 , S_2 and fuses f_1 , f_2 should be arranged as

shown in the diagram so that no P.D. can exist between the P.D. and current strips due to their action.

For P.D.s up to 15,000 volts the arrangement shown in Fig. 177 is much safer. R_1 consists of several specially wound 10,000 ohm resistance frames joined in series and giving about 7 to 10 ohms for each volt, so that on a 10,000 volt circuit R_1 would be 70,000 to 100,000 ohms; R_2 is a 100 or 200 ohm coil forming with R_1 a potential divider; R_2 is a resistance to adjust the sensibility

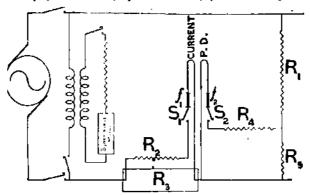


Fig. 177, - Diagram of Connection of Oscillograph to High Tension Circuit.

to a round number of volts per millimetre deflection. The same resistance box as is used for R_1 , in Fig. 176, is suitable. When P.D. curves only are being recorded then R_δ should be connected at that point in R_1 which has the least potential above earth. All the resistances R_1 , R_2 , R_3 , R_4 and R_5 must be insulated so as to stand four or five times the working voltage to earth. Unless the side of the circuit containing R_δ is permanently connected to earth it is better not to use any switches or fuses in the Oscillographs circuit as shown, and permanent magnet Oscillographs Types Nos. II. or III, should be used. It is also advisable to connect one terminal of the strips to the frame so as to screen it from electrostatic effects. On high voltage circuits the synchronous motor if used is best supplied through a suitable transformer.

When using the double Oscillographs the two pairs of strips should be so consected to the circuit that it is impossible under any circumstances that a higher potential difference than 50 volts should exist between one pair of strips and the other, or between either pair and the frame.

The Oscillographs should be calibrated with continuous currents and the resistances R_1 , R_2 , R_4 adjusted so that one mm, deflection corresponds to a convenient number of amperes or volts, as the case may be.

The following table gives some useful approximate data for the various forms of Duddell Oscillographs.

TABLE VII.

	Double High Frequency Oscillograph	Single Pananent Magnet and Portable Oscillograph,	Datable Permanent Magnet and Purtable Oscillograph,	Double Projection Oscillagizph.
lieustance of Field				
Cods in saries at 80°C	36 0 ohras	-	_	660 to 700 alms
Current with the Code in garies Working Tempera- ture for conject	0:28 мирет	_	-	0 27 анде г в
damping with the oil supplied. Normal Tension on	25" C. to 85" C.	10° C. to 20° ().	10° (%, to 20° C	30° C. t. 35 C.
strips . Periodic Time (un-	Birigat.	1] 0/%	9 <u>4</u> 1174.	@ than
damped) with the above tension .	enta to rates	and to relia	and to the	Islanto
Normal Scale dis- tance	50 cms.	50 cms (25 cms, when t	të curi. Peri sa Peristile	SKN cins.
Sensibility with the above tension, normal exerting gurrent and scale distance with		Cacining	i alamy	
damping oil in instrument Normal Working Current in starps	1990 man 1985 1990 pages 1	\$20 mm per Enclose	200 mm jer amjere	. 50 сыя, рег вырыв
for alternate cur- rent wave-forms .	0:05 to 0:10	0 05 to 0:10 naipero	0 05 to 0 10 ampère	0:5 впірего
Resistance of atripy without fees and connections Do. do. with me	about 6 ohus	about 5 obms	about 5 ohms	about I ohu
first and sunnec-	about 10 chiza	no fuses	no fuses	about 14 shut

(157) Determination of the Efficiency of an Electro-Motor-Fan, Set.

Introduction.—The very extensive use to which the electrically driven fan is put, coupled with the large number of combinations of different types of motors and fans in use at the present day, makes it desirable to obtain some measure or gauge of the efficiency of such an electric fan as an air circulating device,

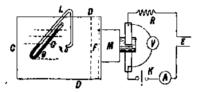
From a commercial point of view, the utility of a fan can best be judged by knowing (1) the quantity of air, reckened say in cubic feet, passed by the fan in unit time, say I minute; (2) the power required to drive the fan to give this. Also, from a mechanical point of view, the speed of the fan under these conditions, and, as a matter of scientific interest, the pressure of the air thus passed.

In order to carry out the test, it will be necessary to provide the fan with an air conduit for the purpose of restricting the current of air to a definite path. This may very simply and conveniently consist of a tubular casing of either circular or square cross section, open at both ends, and from three to four diameters long. The fan must just fit into one end, and any crevices due to loose fitting between the sides of the conduit and fan must be filled in air-tight, so that the only path for the air is through the fan itself.

The determination of the pressure of the draught through the conduit CD, but which, however, is not essential to the test, and merely of interest, can be determined by a special form of water or spirit gauge C.

Since the pressure of the draught is very small, an ordinary vertical U pressure tube would hardly indicate it, and not sufficiently accurately for any practical use. To measure such small pressures, the gauge, in the present instance, may conveniently take the form of a slanting U glass tube about \(\frac{1}{2} \)" to ξ'' bore, one limb L of which is extended and bent into the form shown at LO, the end O being bent so as to face the incoming draught of air from the end C of the conduit.

If now this U tube contains coloured alcohol, any slight pressure at O will cause a difference in level of the liquid in the two limbs, the vertical distance between the ends of the columns being a measure of the pressure at O. Thus even though this is very small, the end of the liquid column in either limb may have moved through a considerable distance, which increases as the angle of slope (θ) gets smaller. Hence if the tube is provided with a scale and calibrated, it can be made to read small fractions of an inch pressure of water, etc.



Fro. 178.

A little cotton wood placed in each end of the tube helps to damp the motions of the liquid column caused by rapid fluctuations of air pressure.

In order to obtain the volumetric discharge of air for any particular speed of the motor M, the velocity of the propelled air must be obtained by means of a rotatory anemometer placed in different positions in the cross section of the conduit some little distance from the end C, the instrument being supported at the end of a stout wire or rod so as not to alter the flow of air. From the various readings a mean may be obtained for the whole section.

Now let v = mean velocity of the air in feet per minute as given by the anemometer, and let s = area of cross section of the conduit in square feet, then the volume of air discharged per unit time, i.s. number of cubic feet of air per minute = w; this will vary with the speed of the motor.

Let w = weight in lbs. of I enhic foot of air at the harometric pressure and temperature of the room in which the test is made (see table, p. 650), then W = mw = the weight in lbs. of air discharged per minute; but the kinetic energy of a mass (m) lbs, moving with a velocity v feet per second = $\frac{1}{2}mv^2$ foot-poundals, and this is a measure of the work done.

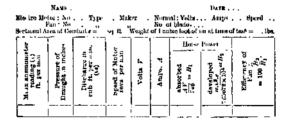
Hence the work done on the air = $\frac{1}{2}mv^2 \div q$ foot lbs.

$$\label{eq:h.P.} \text{developed} = \frac{\frac{1}{2} \frac{W \, \sigma^2}{3 \times 33000} = \frac{8 \sigma r g}{2 \times 322} \times \left(\frac{r}{60}\right)^2 \times \frac{1}{33000}.$$

Apparatus.—Motor M with its attached fan F to be tested; suitable conduit GD; anemometer; air pressure gauge G; voltameter Y; ammeter A; switch K; rheostat R (p. 606) and source of electrical supply E; speed indicator for obtaining the speed of the motor.

Observations. —(I) Connect up as shown in Fig. 178, and adjust the instruments to zero if they require it. See that all lubricating cops feed slowly and properly.

- (2) With R at its maximum, close K, and adjust the speed of the motor M to the lowest convenient amount, then note the readings of V, A, speed, anomometer, and gauge G.
- (3) Take the anemometer reading at different positions in the cross section of the conduit at this speed of M, and take the mean.
- (4) Repeat 2 and 3 for twelvo or fifteen different speeds of the motor, rising by about equal increments to the maximum permissible, by varying the rhoostat R, noting simultaneously the readings of all the instruments at each speed. Tabulate your results as follows —



(5) Plot the following curves on the same curve sheet having (a) the speed in revolutions per minute of the motor, (b) H.P. absorbed by the motor as abscissar, with the volume of air discharged per minute as ordinates in each case; also between (a) as abscissar with (c) the mean velocity of the air draught as given by the anemometer, (d) the H.P. absorbed in the transference of air as ordinates in each case; lastly, between efficiency as ordinates and speed as abscissar.

(158) Determination of the Commercial Efficiency of a Gas Engine-Dynamo Generating Set.

Introduction.—It is most desirable that any generating unit such as the above should be tested at various loads or electrical outputs in order that the best running conditions may be discovered and the performance generally of the unit observed.

This is done by "indicating" the engine at the various electrical load outputs desired, and so finding the relation between the total power exerted on the piston of the engine, commonly termed its indicated horse-power (I.II.P.), and the corresponding power utilized or developed by the generator in the external circuit, which may be reckeded in \frac{Watts}{746} or electrical horse-power (E.H.P.).

In order that the cost of running at any given electrical output per hour (say) may be determined, it will be necessary to measure the volume of yas used in the engine, which can usually be done easily enough, as nearly all gas engines are provided with separate gas-meters on the inlet pipe of the engine. Should, however, this not be the case, the test must be made when all gas-jets are out and the realings on the main meter recorded.

The jacket water, or volume of cooling water passed through the water jacket of the cylinder of the engine, should be measured, and this can best be done by a water-meter inserted in the inlet water-pipe. If such a meter is not available, a fairly large tank can be used (the volume of which can be calculated) to supply the water jacket, then the time taken to empty the calculated known volume of water will enable us to get what is required temperature of the inlet and outlet water of the jacket is taken, the heat removed from the cylinder in thermal units can at once be deduced, knowing the volume of water passed in a given time.

The engine must be provided with a stop-cock in communication with the interior of the cylinder, and into the outer end of which the nipple of the indicator is screwed. This indicator may be of the Richards' type, and, if the gas engine is running at a high speed, the indicator should be a high speed one. If the diagrams taken by this indicator in such cases are not shortened, a stronger drum-spring will be needed to get over the effects of inertia in the drum which carries the card. If the engine has an ordinary double (Otto) cycle and gets the

maximum number of explosions possible, which would occur when it is running at or near full load, then the speed in revolutions per min. + 2 will give the number of explosions per min. If, however, the gas engine is running on light loads it will "miss" an explosion frequently, in which case, since the number of such per min. is a factor of the L.H.P., they must be counted separately, either mentally or automatically by an attachment or counter actuated by the inlet gas-valve lever.

Furthermore, in order to obtain the total cost of electrical energy delivered at the switch-board, we must know the amount of oil, cotton waste, wages, and interest on depreciation and first cost of the plant for the period over which the run extends; these items, however, pertain merely to what we may term the economic efficiency of the plant.

The electrical power developed by the dynamo can be taken up

either in the apparatus on the circuit to be supplied, or in suitably designed water rheostats having ample plate area to avoid variations in the output. This may take the form of a rectangular water-tight wooden trough, having a fixed zinc, iron, or copper plate at one end, connected to one terminal of the dynamo, and a similar movable plate, capable of being moved to a considerable distance from the fixed plate, thus enabling the current output to be varied; this plate is perforce connected to the other terminal of the generator. The mean effective pressure P in lbs, per sq. in. during the

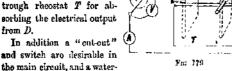
explosion, which is required in the calculations, is calculated, from the indicator diagrams taken, in the manner described on pp. 471 and 530,

Note. The effective area of each plate of the water rheestat should be something like 4-9 sq. ft. for currents of about 500 amperes,

Apparatus.—Gas engine-dynamo set D to be tested, of which the gas engine is not shown; indicator (p. 531) and reciprocating lever gear for rotating the card drum; tachometer;

trough rheostat T for absorbing the electrical output from D.

voltmeter V; ammeter A;



meter with necessary separate gas-meter for the engine.

Observations.—(1) Connect up the electrical circuit as in Fig. 179, and adjust all instruments to zero. Fill T with water in which a few handfuls of washing soda have been discolved and set the plates at the extremities of the rhoustat.

- N.B.—The plates may be provided with massive terminals for connection to the main leads, otherwise the ends of these latter should be spread out, fan-wise, and soldered to the plates.
- (2) Measure approximately how much oil is required to fill all lubricators in use, which must be set to feed properly just before starting the trial.

Insert the most suitable spring in the indicator and a card on the drum, then screw the indicator to the cylinder cock and connect to the reciprocating gear.

- (3) Start the "set" up to its normal speed and take an . indicator diagram from the engine with D on open circuit.
- (4) At a noted instant simultaneously read all the instruments and meters, then quickly switch on and adjust A to full load and take an "engine card" again.
- Mote.—At least four observers will be required for the
 - (5) Simultaneously read all the appliances every twenty minutes

throughout the trial, which should last at least three hours, taking a "card" at each.

(6) Repeat 2—5 for $\frac{1}{2}$ full load on D if possible, and tabulate your results as follows—

Name	DATE
Gas Engine : No Makers Typ Paton : Aven (a) = 60, m	e Normal speed = icvs per min.
Dynamo: No Makers Type No	rmal: Volta = , Ampa, = , , , Specd = , , ,
Indicator: No Type Scale of Spri	$\log used \dots Mean \left(\frac{E.U.P.}{U.U.P.} = \dots\right) \frac{during}{during}$

İ	T	me			from					Jan E	ıglı	n			_		
			١,)j i uu	IIII	(in,n				Water,			₩.	:_	중다12		
	of observations.	in House from Start.	Volts 7.	Amps. 4.	E.H.P 4F	Explosions per min. (n).	Meter rending.	Total Yol. used		E'E'.	Meter reading.	Total Vol. used in trail.	þ	er er en. A. H	1, H.P. calculate	Trom cards - 38ang	Effectory of "

Inferences.—What inferences can be deduced from the results of the trial?

Calculate the total cost per E.H.P. hour delivered at the switch-boards, taking the approximate average costs of the various factors.

(159) Determination of the Commercial Efficiency of a Steam Engine - Dynamo Generating Set.

Introduction.—We have already described in detail the usual methods of determining the efficiency of both direct and alternating current generators without reference to any prime mover such as a steam, gas, or oil engine. The common practice, however, at the present day, of employing "direct coupled sets" in central stations, consisting of the generator placed on, and fixed to, the same bed-plate as the engine and coupled direct to it, makes the test of the performance of such a combined generating set one of extreme importance.

This practice has resulted from the endeavours of central

station engineers to curtail the amount of floor area required for a given station and to avoid the loss of power and trouble inseparable from driving by belts and ropes. In order to determine the combined efficiency of a generating unit, whether direct coupled or otherwise, we require to measure the useful or nett electrical output, which can be done with the aid of an ammeter, voltmeter, and one or more suitable rheestats in the manner described in the earlier pages of this book.

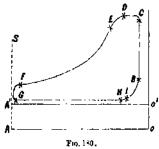
In addition we must know the gross or total II.P. exerted by the piston of the engine, usually termed the Indicated II.P. This can be determined by aid of the engine indicator, for the detailed theory of which the reader is referred to special "works" dealing with such indicators almost entirely. There are, however, some important details connected with the use in general of the various forms of these instruments, which may with advantage be mentioned here, but otherwise it will be assumed that the theory, construction and action of the engine indicator is understood.

Relation between length of indicator diagram and engine speed.—
It must be carefully remembered that as the paper drum of the indicator is rotated by a reciprocating motion from the piston or cross-head of the engine, its inertia at the higher speeds may introduce errors in the diagram; in other words, its motion may continue, from this cause, beyond what actually represents the true driving motion. To minimize such an error the angular motion of the drum must be reduced, and consequently a shorter diagram obtained as the speed increases, in order to insure a true and properly proportioned diagram.

In this connection it may be noted that for speeds up to 200 revs. per min. the driving of the dram should be so arranged that its angular motion gives a diagram about 4½" long, and this should be made to diminish almost inversely proportional to the increase of speed. Since in addition increase of speed will require a stronger piston spring, the height and length of diagram will decrease in about the same proportion for increase of speed, thus giving a proporty proportioned and accurate diagram.

Gedring of Engine Indicators.—In order that an accurate diagram may be obtained it is all-important that the reducinggear for driving the drum should reduce the piston motion in exactly the same proportion at any and every part of the stroke. For such gears the reader is referred to works dealing with the subject of engine indicators. In the use of the indicator great care should be taken to keep it froe from all dust and well oiled with watch oil, as the least friction in the cylinder or multiplying levers may cause a distortion of the diagram, the boiler prossure and engine speed will determine what strength of spring is to be used in the cylinder, and the lighter this is, the higher the diagram and the more accurate the measurement, providing inertia effects are absent.

The engine piston must of course never be allowed to close the outlet pipe between the engine and indicator cylinders, hence the latter should be screwed on to a cock at the end of the engine



the cylinder. Fig. 180 represents the approximate shape of a diagram which would be taken from an ordinary non-condensing engine. The indicator is first made to draw the straight line O'A', done by putting both sides

cylinder. For accurate work diagrams must be taken at both ends of

of its piston in communication with the atmosphere by opening the stop-cock so as to cut off all steam from the cylinder of the engine and allow the air to enter undermeath the indicator-piston. The pressure both sides of this latter will thus be the same and equal to that of the atmosphere, consequently if the puncil be lightly pressed against the moving card, the horizontal straight line O'A', termed the atmospheric line, will be described. OA is the absolute zero line, parallel to O'A', and drawn below it at a distance representing, to the scale of the diagram, the atmospheric pressure at the time of the test.

In Fig. 180 B is the point of admission of steam to the engine cylinder, D the point at which the alide-valve begins to close, E the point at which it is quite closed. From E to F the admitted

steam is expanding, and at F the release begins, being completed at G. The exhaust valve begins to shut at H and is quite shut at I, the steam still left in the cylinder being compressed between I and B. The rounded corners, such as DR and FG, show the slow acting of the steam valves in closing and opening the steam ports, which is called wire drawing. In the ideal engine these rounded corners would become sharp ones.

Determination of I.H.P. from the diagram.—Referring to the diagram, Fig. 180, the horizontal distance between the extreme points of the diagram, i. e. between the vertical lines A'S and BC, represents the stroke of the engine piston in fact. The ordinates of the diagram perpendicular to the atmospheric line C'A' represent to the scale of the indicator spring used the pressures of the steam in lbs. per \Box'' .

If the scale of the indicator spring used in taking the diagram $=\frac{1}{10}$, each inch of the ordinates represents 30 lbs. pressure per square inch, consequently each square inch of the diagram represents $\frac{10}{12} = 2\frac{1}{2}$ ft. lbs. The whole area of the diagram will therefore represent the indicated work in ft. lbs. per square inch of enginepiston, done on one side of it, during one stroke. Since the pressure exerted by the steam on the piston varies at different parts of the stroke, we must know the mean effective pressure for the complete stroke. This is found by dividing the area of the diagram by the base line, both being reckoned in inch units. The result is the value of the mean ordinate of the diagram or mean effective Pressure (P_{in}) in lbs. per square inch of piston area.

Hence if L = length of stroke in feet, A = piston area in square inches, and N = number of revs. per min. which the engine is making, then the I.H.P. $= \frac{2}{33000} \frac{P_{in}LAN}{3000}$

Apparatus.—Generating set to be tested; engine indicator (p. 531); speed indicator; planimeter (p. 528); ammeter; voltmeter; rhoostat for absorbing the load from the generator (p. 467), and a switch.

Observations.—(I) Connect the ammeter, rheestat and switch in series with one another and with the generator, also the voltmeter across the terminals of the machine, and open the switch.

(2) Disconnect the generator and engine and start the latter, running alone for some little time before making a test. Prepare the engine indicator by first seeing that all the parts are quite clean, well ciled, and work practically frictionlessly. Insert the right spring in the cylinder suitable for the boiler pressure and engine speed to be used, and note its "scale" for future reference.

(3) Blow off steam at the cock which is to carry the indicator for a second or two so as to clear away superfluous water and dirt. Now screw the indicator to it. Place a card on the drum, and make sure the cord which is to actuate the drum will be attached to the proper point on the reducing gear so as to give a suitable length of diagram for the speed of the engine.

- (4) Turn the cock so as to admit air under the indicator piston, cutting off all steam. Then hook on the cord so as to rotate the drum and draw the "atmospheric line." Then turn the cock so as to communicate with the engine cylinder and take a full diagram, noting simultaneously the speed of the engine, and in addition which end of the cylinder the diagram is taken from.
- (5) Cut off the steam by the cock, unbook the cord, and quickly repeat 3 and 4 at the other end of the cylinder of the engine. This interchange should be repeated two or three times so that an average may be obtained, for the constant speed, when working out the results.
- (6) Now run the generator by the engine, absorbing \$\frac{1}{2}\$, \$\frac{3}{4}\$, and full load successively in the rheastat, repeating \$3-5\$ at each load for the same speed, both load and speed being maintained constant during the time required for taking the readings. Note the volts and amperes at each load, and tabulate your observations as follows—

	NAME .	• •					Date		
Dynamo: Scale of I		ring usod	,, ,	Vo Type	of Indi	. An			
4		Desp	inur,					ج ا	ı
inder wid is made.	offndar hich taken.	Engane r min.	e ctire	CH.P	<u>.</u>	4	weloped AF	Efficiency H	

Note.—The value of P_m in the above table is the mean of the means of the worked-out results for the two ends of the cylinder of a single cylinder engine. In the case of a compound or triple expansion engine, the L.R.P. can be found from the diagram taken from either cylinder as follows—

Sum the products of A and P_m for each cylinder (P_m) being given by the diagram for that cylinder found in the usual way) and divide by the A for that cylinder from which the particular diagram under consideration was taken. Thus if $A_2 = p$ iston area in eq. ins. of, say, the "intermediate cylinder" of a triple expansion engine, the mean effective pressure to be used in the formula, say $P_m = \frac{\sum_{i=1}^{n} P_m(A)}{A_2}$ where $\sum_{i=1}^{n}$ indicates the sum of the products for the H.P. intermediate and L.P. cylinders.

The value of the mean effective pressure as obtained from any particular indicator diagram can be obtained by the aid of the planimeter, the use of which in measuring the area of the diagram is described on p. 550.

General Observations on Jointing Electric Lighting Cables.

Good and reliable joints both in core and insulation can only be made with practice, care, and attention to the following essential details:—All joints in conductors must be as mechanically and electrically perfect as possible, for they are in most cases a source of weakness in an installation.

The Joint.—That of the metallic core should have a conductivity not less than that of an equal length of the ordinary core, if possible, and to obtain this care must be taken not to nick the copper cores of the cables to be jointed either with the paring knife or pliers, which not only reduces the conductivity, but causes the wire of the strand so nicked to break off at once if bent at that point. Before making the joint, all the wires must be straight and theroughly cleaned with fine emery cloth, care being taken not to remove the tinning of already tinned wires. The cleaned wires may preferably be re-tinned with the soldering-fron, and must be handled as little as possible, even with clean hands.

No joint will ever solder properly unless it is quite clean throughout, and in a hot, clean, and well-tinned soldering-iron.

The Soldering-Irons.—These must be properly grooved to take the size of joint to be soldered, and should never be allowed to get too he's and "burn." This always gives rise to an excessive lurid green flame, and is not only injurious to the "copper bit," but burns all the tinning off them, thereby giving extra labour and wasting time in re-tinning. Irons may be cleaned with either salammoniac, emery cloth, or carefully with a suitable file. Salts or soldering fluid may be used as a flex in tinning them. Irons should be uself tinned, and hot enough when used to be unbearable when placed about 1½" from the cheek. They should be wiped when taken out of the stove before applying to the joint. Quick soldering is essential, as continued application of heat seriously weakens coppor wire and makes it brittle. Too great a heat causes solder to "rot" and become useless.

Solder.—This should be in thin sticks, and should contain enough tin to enable one to hear it crinkle when bent double close to the ear.

Flux.—Nothing but resin (applied in the lump) should be used in soldering copper joints. All liquid fluxes and other substances containing corrective ingredients should be avoided if the joint is required to remain unimpaired with time.

Insulation.—Great care should be taken to make the insulation of the joint as nearly as possible equal to that of the rest of the cable. In rubber-insulated cables the braiding or taping is removed from the rubber without nicking it, and the pure I.-R. strip wound with lap winding over the joint and taperell ends of the rubber thus bared. I.-R. solution is now rubbed over the joint, but must never touch the bare joint. The taping should be done tightly, and be quite solid when completed.

(160) Detailed Instructions for Jointing Electric Light Cables.

Introduction.—For successful and efficient jointing the following remarks must be rigidly adhered to—

(1) In baring any wire or cable preparatory to making a joint,

great care must be taken not to nick any one or more of the copperwires forming the core, which would not only cause the wire so nicked to break off on bending it once or twice, but would also diminish the sectional area of the cable and so also its current carrying capacity.

- (2) In deaning the copper wires of the core fine emery cloth must be used and all dirt removed, but as little as possible (if any) of the original tinning.
- (3) Just expicient and no more cable must be bared as will make a satisfactory joint, considerations of the cost of insulating materials, and particularly of the ultimate insulation resistance of the joint, making it imperative to keep the dimensions of the joint, in the matter of length, a minimum.
- (4) Cleanliness is of vital importance in the actual winding or making of the joint, and a few extra seconds spent in insuring this will almost invariably save many minutes, much solder and soldering flux in the end, and even possibly the necessity for a second attempt at the whole joint,
- (5) A badly made joint, or a badly insulated one, is a source of considerable danger in an electric light installation.
- (6) Too much attention cannot be paid to the soldering irons, as it is perfectly hopeless to attempt to solder a joint with—a dirty iron, badly tinned iron, or a soldering iron that is not hot enough.

COURSE IN JOINTING ELECTRIC LIGHT WIRES, CABLES, AND MAINS.

The following series of joints constitute a course in the actual practice of "jointing making" which the author instituted in his department at The University, Leeds. They comprise practically all the principal distinctive types of joints commonly met with in practice, and which might be required to be made by any ordinary wireman—

No.					
	Twist-J	oint	betwee	n two	No. 7/18 S.W.C. insulated E.L. cables.
	ፐ-	**	11	**	No. 7/18
9	Twist-	31	+,		No. 7/11 ,, ,, ,, ,,
10	T-	11	11	,,	No. 7/14
11	Twist-				No 19/16 ,, ., .,
	T·	,		,,	No. 19/16 ,, ,, ,,
18	Tuist-	.,	1)	*1	No. 37/18 ,, ,, ,,
14	T-	,,		17	No. 37/16 ,, ,, ,,
15	Twist-		"		No. 7/16 S.W.G. insulated lead-covered
					E. L. cables.
18	T·		12		No. 7/16 S.W.G. insulated lead-covered
	-				E. L. cables.
17	Twist-	,,	.,	19	No. 16 S.W.G. insulated gutta-percha-
					covered wires.
18	T-	,,			No. 16 S.W.G. insulated gutta-percha-
	-		•		covered wires.
19	Tuist-		,,	*1	No. 19/16 and a No. 7/18 S. W.G. insulated
		•	•		electric light oables.
20	Slanting	⊈ T -	Joint b	otween	two No. 19/16 S.W.G. insulated electric light
		- •			cables.

Nors.—No. 5 is a joint used for agrial tolegraph and telephone lines. Nos. 17 and 18 are joints used for telegraph work principally.

21 Twist-Joint on a large concentric load-covered electric light main.

Twist-Joints Nos. I and 2,

To prepare.—Carefully bare, with a sharp knifs, about $1\frac{1}{2}$ inches of the ends of the two wires to be jointed. This must not be done by a cut perpendicular to the wire, but by a short slicing motion round the wire, when the piece of insulation will in most cases come off whole with a suitable pull.

Clean each bared wire with fine emery cloth, straighten and place them across each other, then lightly gripping them at the crossing point with a pair of pliers, bend one free end round the other wire. Do this with the other end and finally straighten and trim the ends up close, so that they do not project outwards, as they are then liable to pierce the insulation.

To solder.—Place the joint in a well-tinned groove of the iron containing solder, then when hot just touch with a lump of resin and draw a thin stick of solder over the joint. This usually suffices, but if not, repeat the operation, using very little resin. The soldered joint must leave the iron quite bright and without any globules of solder hanging to the underside of it. The soldered joint should appear as in Fig. 181.

To insulate.-When cool, taper the ends of the insulation, and

starting from over the rubber of the wire, wind the joint over with a spiral half overlap of pure I.R. strip (para tape) to the other end, gently stretching the tape all the time so as to obtain a firm (not spongy) layer of I.R., which, since it is wound in half

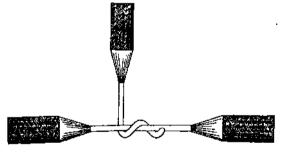


Ftd. 191,

overlap, constitutes a double layer. Apply I.R. solution to the outside of this I.R. lapping (on no account next to the copper joint) and rub evenly all over the lapping with the finger. Next, when the spirit last evaporated out of the rubber solution, wind on a similar layer of black prepared rubber tape, overlapping the outer insulation of the wire at each end, and scaling the ends down with solution. Lastly, paint the outside of the joint with black waterproof varnish and allow it to dry.

T-Joints Nos. 3 and 4.

To prepare.—Carefully here about 11 to 11 inches of the wire to be tapped (the larger of the two) and clean with fine emery



Fta. 192

cloth. Bare about 14 of the end of the other wire, riean and straighten, then placing this across the other wire twist it round two or three times to produce the joint shown in Fig. 182, and trim the end so that it does not project to any extent. Solder in the manner described for joints 1 and 2.

To insulate.—Proceed as in these last named joints, but on arriving at the T with each serving, carefully branch off down it and back, stretching the tapes more tightly to allow for increased thickness of insulation; finally, continue along the remaining straight portion of the cable, and varnishing over the last layer of tape. Considerable care is required in insulating a T-joint, as it is more difficult to get round the corners (i.e. angles) of the T with the tapes, and these parts therefore are most liable to imperfect insulation.

BRITANNIA-JOINT No. 5.

To prepare.—Gently straighten the ends of the wires to be jointed by lightly tapping them with a mallet on the anvil. Clean each with fine emery cloth, tin them both for a distance of about 2 inches from the end, and bend sharply round the tips of



Fro. 183.

their ends. Next place them together with the bent ends pointing in opposite directions, and with an overlap of about 2°; then bind them together with about No. 20 tinned copper binding wire as shown in Fig. 183. Trim off the ends of this wire, and solder the whole into one solid mass as described in joints Nos. 1 and 2.

SCARF-JOINT No. 6.

To prepare.—Gently straighten the ends of the wires to be jointed by lightly tapping thom with a mallet on the anvil. Clean each for a distance of about 1 inch from their ends with emery cloth.



Fro. 181.

Next scarf them with a flat file as shown in Fig. 184, so that

they taper to thin edges and fit. Then tin them both, wiping off nearly all the superfluous solder by a clean cloth. Now warm the ends up, and when the surface solder on the scarfed portions is melted, place them together to form a continuous wire and

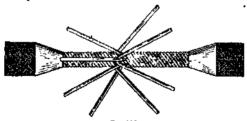


Fro. 185.

allow to cool. Bind the joint with No. 18 or 20 tinned copper wire for about 3" from the centre each way as in Fig. 185. Instly, trim the ends of the wire and solder into one solid mass, care being taken to just keep the scarfed ends in gentle contact while soldering and until set.

TWIST-JOINTS NOS. 7 AND 9.

To prepare.—Carefully bare about 4" of the two ends to be jointed with a sharp knife and a slicing motion (not a cutting one perpendicular to the cable).



Fro. 186.

Separate out each wire and clean them all with fine emery cloth carefully, so as not to remove any tinning if possible. Straighten each, cutting off half the centre wire of each cable, and then re-twist the enter six up to the end of the centre wire with about the same pitch as the rest of the cable itself in both cases, arranging them so that the six free straight ends form a cone with its apex at the end of the centre wire.

Now push the cones together, so that the six wires of each

interface alternately, and their apoxes touch as shown in Fig. 186, i. s. the two middle wires butt against each other. Now press down the left-hand set on to the cable, and hold tightly in the hand. Then wind with the other hand the remaining six wires of the office cable, one by one, by, say, half a turn at a time, and evenly to, say, 1 or 1½ inches from the centre, snipping off each what is not wanted, and trimming the ends so as not to project outwards. Repeat these operations with the other half, and



Fra. 187.

finally trim the centre also by pressing with the pliers, but not scraping the cable in so doing.

N.R.—The joint may then appear like Fig. 187 or 188, preferably the latter, which makes the neater joint and is, as seen, wound in the same sense as the main cable.

'To solder.—Place in the well-tinned groove of a fairly large soldering iron and run in some solder around it, then when quite hot just touch the joint for merely an instant with a lump of



Fig. 188.

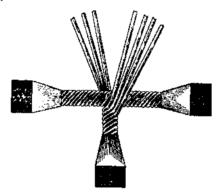
resin, and draw a stick of solder over the joint. This, as a rule, will suffice to cause the whole joint to become tinned; if it does not, repeat. When properly tinned the joint should leave the iron in a bright state, and with no globules of solder hanging to the underside of it, and should be one solid mass.

To insulate.—When cool taper the ends of the insulation, and starting over the rubber of the cable, wind on spirally with a half overlap two layers of pure I.R. tape in opposite directions and with enough tension to make the insulation firm and solid. The end of this tape is fixed down by I.R. solution, which is also

applied to the outside of the rubber-taping all over the joint by means of the finger. When the spirit has evaporated repeat the above winding process with two layers of black prepared rubber tape overlapping the outer braiding of the cable. Lastly, varnish the joint all over with black waterproof varnish and allow it to dry.

T-Joints Nos. 8 and 10.

To prepare.—Cerefully bare about $2\frac{1}{2}$ " to 3" of the cable to be tapped. Clean the outside of the stranded core with fine emery cloth and re-tin well.



F1g. 189.

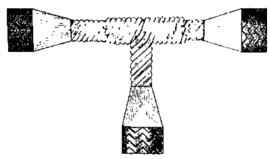
Next carefully bare about 3" of the end of the other cable, separate out all the wires, clean each with fine emery cloth, straighten and re-twist them up to about \frac{1}{2}" from the end of the insulation in a slightly sharper twist than the ordinary cable. Now spread the 7 wires out to form a V, the apex of which is at \frac{1}{2}" from the insulation, \frac{1}{2} wires being one side and \frac{3}{2} the other.

Next press the other cable into the V as shown in Fig. 189, then, holding the two tightly together, wind one by one the 4 wires round in one direction, and the 3 in the opposite direction to, say, ?" either side of the centre. Clip off what is not wanted

of each wire, and trim so as to not project outwards, when the joint should be as in Fig. 190.

To solder. - Repeat the operation described for joints 7 and 9.

To insulate. - Repeat the operation described for joints 7



Fm. 190.

and 9, except that when the T is reached, wrap carefully round the angles, down the T and back, stretching the tapes tighter here to allow for the extra lapping this part will receive, then finish off the joint as in 7 and 9 above.

Twist-Joint No. 11.

To prepare.—Carefully bare about $4\frac{1}{2}''$ of the two ends to be jointed, and separate out the outer layer of 12 wires, clean them with fine emery cloth and straighten. Without unwinding the inner 7 solder them into a solid mass and cut half off in both cables alike. Now re-twist the outer 12 up to the end of the inner 7 with about the same pitch as the ordinary cable, and armnge them to form a cone with the apex at the end of the inner 7. Then pushing the two cones together and interlucing alternately, proceed to finish exactly as in joints 7 and 9.

T-JOINT No. 12.

To prepare.—Carefully bare about 3" of the cable to be tapped, clean the outside of the stranded core with fine emery cloth, and re-tin it well.

Next carefully bare about 32" of the end of the other cable. Separate out each wire, clean with fine emery cloth, and straighten. Next re-twist both inner and outer sets up to about 3" from the insulation with a slightly sharper pitch than the ordinary cable, then carefully spread out all the wires in the best possible manner to form n V with 10 one side and 9 the other. Lastly, press the other cable into this V, and finish the joint precisely as in Nos. 8 and 14.

TWIST-JOINT No. 13,

To prepare.—Carefully bare about 5½" of the ends of the cables to be jointed, unwinding the outermost layer of 18 wires, and proceed precisely as in No. 11, except that half the inner 19 must now be cut off after soldering them together.

T-JOINT No. 14.

To prepare.—Carefully bare about $4\frac{1}{2}$ " to 5" of the cable to be tapped and about $5\frac{1}{4}$ " of the end of the other, and proceed exactly as set forth for joint 12, excepting that the V will now have 19 wires on one side and 18 the other. Finish it off as there indicated.

Twist-Joint No. 15.

To prepare.—Carefully out the lead sheathing away, without in any way nicking the capper core of the cable, for about 4" of the ends of the cables to be jointed. Next slip on to one cable, to some little distance from the joint to be undo so as to be out of the way, a lead sleeve consisting of a length of lead pining, a little larger than the size of the lead-covered cable and some 2" longer than the finished joint will be. Then proceed to make the joint and insulate it precisely as in Nos. 7 and 9, taking extra care to get the insulating tapes on tightly and efficiently. Now slip back the loose sleeve over the joint and either carefully "solder" or "solder-wipe" the ends, thus completely scaling in the cable.

Note.—If lead piping to the right size is not available, a sleeve may be cut out of lead sheet, bent round the joint and finally scaled along the edge; this, however, does not make so neat a joint as that with the pipe.

T-JOINT No. 16.

To prepare.—Carefully cut away about 4" of the lead sheathing of the cable to be tapped, great pains being taken to avoid nicking the copper core. Next remove about 3½" of the lead sheathing from the end of the other cable and alip over this latter a short sleeve of lead piping slightly larger than the ordinary lead-covered cable, and of sufficient length to cover the insulation of the joint and overlap the end of it. Now make and insulate the joint precisely as described in Nos. 8 and 10 and slip back the small sleeve over the insulation; also cut out a piece of sheet lead to form a sleeve over the rest of the joint, its ends overlapping those of the lead covering on the cable by about 1"; lastly, train and trim these lead coverings to fit closely, and solder or solder-wipe the seams to make a neat water-tight joint.

TWIST-JOINT No. 17.

Prepare and make the joint precisely as in Nos. 1 and 2, when it will have the appearance shown in Fig. 191, and it may preferably be kept as short as possible in order to facilitate insulating it.

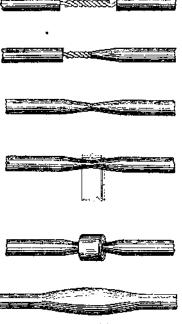
To insulate.—Warm up the G.P. covering on either side of the joint, then work and draw down with moistened fingers that on one side half-way over the joint as in Fig. 192, and next that on the other side, giving the form shown in Fig. 193; work the two draw-downs together and sear all the joint with a hot searing iron.

Wrap a strip of G.P. well warmed over a flame round the centre of the draw-down as in Figs. 194 and 195; now work this roll both ways with moistened fingers until it is uniformly distributed over the joint as seen in Fig. 196, finally smoothing all over with a searing iron, and lastly with wetted fingers so as to leave the whole joint quite smooth.

T-Joint No. 18.

Prepare and make the joint precisely as in Nos. 3 and 4, keeping its dimensions small.

Insulate in a somewhat similar manner as in No. 17, working the three branch G.P. coverings into each other at the T. Warm narrow G.P. strip must now be wrapped round the T, first one way and then the other, and drawn down in the three directions so as to leave a clean, smooth, insulated joint.



Figs. 191—196.

Twist-Joint No. 19,

This joint is made in precisely the same way as No. 11, and is insulated in the same manner, and is shown in Fig. 197.

SLANTING T-JOINT No. 20.

The cable to be tapped is prepared exactly as in No. 12, the other cable having its inner seven wires softered together, cut half off and scarfed to the desired angle or stant. The remaining twelve wires are then wound as before in opposite directions, six one way and six the other, round the other cable, giving the joint shown in Fig. 198. The scarf should but up against the tapped cable and be soldered to it in the final sweating.



Fig. 197.

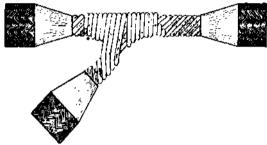
STRAIGHT CONCENTRIC-JOINT No. 21.

We will assume that the cable or main is a 37-stranded, lead-covered and armoured one, the gauge being any one of the usual sizes in practice. Treat each of the two ends to be jointed as follows:—Unwarp the enter serving of yarm or hemp for a distance of something like 13 inches from the end, but do not cut it off. Next unwrap the strip armouring for about the same, or a slightly loss distance, say 11 or 12 inches, without cutting it off. Then unwrap the inner serving of yarn, which separates the armour and lead sheathing, for some 10 inches, without cutting it off.

Now remove the lead sheathing for about 9 inches altogether. Joint in Inner Main.—Carefully bare the cuter conductors for about 7 inches from the end with a sharp knife. Spread out and clean them each with fine emery cloth and straighten, leaving them outspread. Next bare, carefully, the inner conductors for about 5 inches. Spread out and clean each conductor with fine emery cloth and straighten each. Re-twist up the innermost 19 as they were originally, and cut \(\frac{1}{2} \) of this inner 19 strand off. Remove any jagged edges and solder so as to form them into a solid mass.

Each main will now appear as in Fig. 199, except that the unwrapped ends of the yarn and armonring are not shown. Now cut off 3 of every alternate wire immediately, surrounding

the inner 19, and bringing the two ends of the cables thus prepared together, so that the inner 19's butt up to each other. Interlace these enter wires so that the respective pairs also butt though alternately on either side of the centre. Then bind this



Fra. 198.

first joint of the inner cable with four strips of tinned copper binding wire, each of some ten turns, and the strips equally spaced over the joint, so that the three sets of butts come in between the four strips of binding wire. Lastly, by means of two

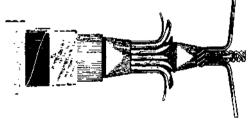


Fig. 199.

ladies, keep pouring melted solder over the joint, catching it in the ladie held underneath and using it over again and again until the joint takes the solder and becomes tinned and soldered into a solid mass. Fine powdered resin must be used as a flux in just sufficient quantity. When cool enough, taper the end of the first insulating covering, when the joint should then present the form shown in Fig. 200. Now wrap on tightly in the usual way, first pure rubber strip, with the application of rubber solution between layers, and then prepared tape up to a thickness slightly exceeding the other insulation.

Joint in Outer Main.—Wrap a sheet or sleeve of copper plate which has been proviously cleaned on the outside carefully with emery cloth, and which is of such a thickness as to be comfortably pliable. This sleeve must be the length of the outer conductors, and make one turn or wrap fitting the insulated cable closely. Now cut off half of every alternate wire of each outer main and interlace, after cleaning and straightening each as before. Then bend them closely over the sleeve of copper by tinned binding wire in, say, four strips about \(\frac{1}{2} \) wide, the butts of the conductors being between the pair of strips, either end.

Solder as before with the ladles. The joint now has the

appearance shown in Fig. 201.

When cool enough insulate up in the usual way, tapering the

ends of the old insulation of the cable beforehand.

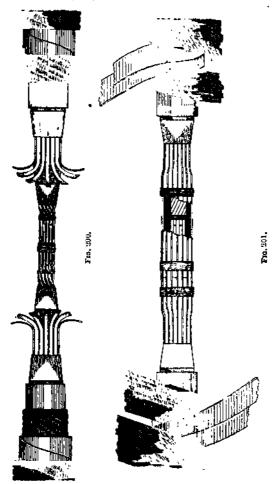
Protections to insulated joint.—Wrap a piece of sheet lead

over the last insulation, so as to form a sloove of just one complete turn and overlapping the ends of the ordinary lead sheathing of the cable. Then solder wine the ends and down the seam so as to make a good water- and air-tight joint.

Mote.—Any part of the lead may be previously painted if desired so as to prevent the lead solder wiping from taking to that part. Next re-serve the inner yarn as far as it will go over the lead joint, adding more to complete the serving.

Then repeat this operation with the strip armouring, and lastly with the outer yarn, when the joint may finally be well tarred over and is then complete for laying in.

Generally speaking, all joints larger than about Ys can be more expeditiously and effectively soldered by using flux and pouring molten solder out of one ladle over the joint and catching it in a second and larger ladle underneath. The reason is that by this means the joint can be raised to, and kept at, the proper temperature, which is difficult to obtain with soldering irons.



CONTENTS

	PAGE
Curve Plotting	1
Calibration and standardization of Ammeters	4
Calibration and standardization of Voltmeters	10
Complete Test of D.C. and A.C. Ammeters and Voltmeters for all Sources of Error	29
Calibration and standardization of Wattmeters	34
Calibration and other tests on Electricity Meters	43
Efficiency and other Photometric tests on Electric Glow	50
Efficiency and other Photometric tests on Electric Arc Lamps	61
Efficiency and other tests on Secondary Cells	73
Measurement and comparison of High, Ordinary, and Low Metallic Resistances	8
Measurement of the Insulation Resistance of Cables, Cells, Insulators, Machines, and Installations	91
Localization of Faults in Electric Light Mains	130
Measurement of Rotational Speed by Speed Counter and Watch, and also Strobescopically	13:
Determination of the "Characteristics" of Direct Current Dynamos	140
Determination of Field Winding and Speed Conditions for True Compounding of D.C. machines	168
Determination of the Characteristics, Regulation, and Efficiency of Alternators	168
Determination of Potential around the Commutators of Dynamos and Motors	19:
Separation of Losses, Leakage Coefficient, Effect of Airgap, Faults in Field Coils, Temperature Rise, in Dynamos and Motors	203
Efficiency and regulation of Direct Current Dynamos .	219
xi	

All COMIENTS	
Efficiency, B.H.P., and regulation of Direct Current Motors	PAGE, 232
Efficiency, B.H.P., and regulation of Alternating Current Induction Motors	260
Efficiency, B.H.P., Regulation, and other Characteristics of A.C. Commutator Motors	299
Efficiency, B.H.P., Regulation, "V" Curves, and other Characteristics of A.C. Synchronous Motors	305
Miscellaneous tests on the Effects of Self-Induction and Capacity in Alternating Current Series and Pamilel Circuits	310
Effects of Position of Core, Air Gap, and of one Cheker on another in open and closed Magnetic Circuits, etc.	339
Measurement of Magnetic Permeability, Hysteresis, Self- Induction, and Iron Core losses	345
Measurement of the Electrostatic Capacity of Concentric and other Cables	309
Measurement of Power in Single and Polyphase Alternating Current Circuits	379
Efficiency, Regulation, and other tests on Single and Polyphaso Alternating Current Static Transformers	400
Efficiency and Regulation of Electrolytic and Rotary Rectifiers	427
Efficiency and regulation of Continuous and Polyphase Current Rotary Converters	433
Determination of the Periodic E.M.F. and Current Curves of an Alternator or A.C. Circuit by Joubert's Contact Maker and the Duddell Oscillograph	446
Efficiency and Performance of Ventilating Steam- and Gas- Engine Generating "Sets"	462
Jointing in Electric Light Wires and Cables	473
Appendix-Proof of Formulæ used in the Tests	490
Description of Appliances and Apparatus .	504
Tables of Constants, Variables, Copper and Resistance Wires, and Useful Numbers .	640
Tables of Logarithms, Squares, Reciprocals and	657
Doubled Square Roots of Numbers	887 887

INDEX

Test l	Ma,	Page
•	Å	
	Absolute C.G.S. Units, Table relating Practical and	643
	Absorption Brake for measuring Horse-power of Motors . 234 &	
	Dynamometer	633
	Dynamometer, Cradle	621
28	- of Light by Shades and Globes, Measurement of the	68
	Air at different Temperatures and Pressures, Table of Densities	•••
	of Dry	650
	Condenser, Kelvin's	818
119		
	Self-Induction, Current and Power, Effect of Length of	341
79	- Gaps in a Dynamo, Effect on the Magnetic Characteristic of the	211
	Alternating and D.C. Electro-Motore, General Remarks on the	
	Testing of	232
127	Current, Absolute Measurement of Solf-Induction by Row-	
	land's Method and	862
	Current Circuits, Effects of Variation of Frequency in .	310
117	- Current Circuits, Load and Wattless Currents in Industive	336
109	- Current Circuits, Measurement of Power Factor in	816
ī85	— Current Circuits, Messurement of Power in 3-phase 388 &	
	—— Current Circuits, Measurement of Power in 2-phase 393 &	
138	- Current Circuits, Power absorbed in, by 3-Voltmeter method	379
184	- Current Circuits, Power (by 3-Ammeter Method) in	383
	Current Circuits, Relation of Supply Factors to Constants of	810
106	Current Commutator Motors, Efficiency and B. H. P. of Single-	
	Phase	200
128	- Current, comparison of two Self-Inductions by Rowland's	
	Method and	365
100		272
99	- Current Electro-Motors, Efficiency and B.H.P. of Single-	***
	phase	269
134	- Current Frequency, Method of Separating Iron Losses - Current, General Remarks on Measurement of Self Induction	862
	by Rowland's Method and	362
	- Current Induction Motors, Testing of Asynchronous	260
104	Current, Measurement of Self-Induction by using Single-phase	358
	& 149 — Current Rotatory Converters, Efficiency of Multi-	and
140	phase	440
184_	148 Current Static Transformers, Measurement of Efficiency	LEVI
144-		426
106	- Current Synchronous Motors, Excitation and Armsture Cur-	
240	rent and V Curves of .	805
66		400
-	Speed in an	188
	407	

668

Test	No. Page
67	Alternator (at Constant Speed), Variation of E.M.F. with Exci-
	tation in an
71	— Characteristic for different Power Factors
70	Determination of the Characteristic of an 177
154	Determination of the Periodic E.M.F. and Current Curves
	of an
155	- Determination of the Periodic E. M. F. and Current Curves
	of an
73	Efficiency without loading it up
	- Graphical Deduction of Total Characteristic of an
	- Internal Lesses in au
	Iron Losses by Retardation Method
68	- Magnetization Curve on Full Load of an
67	- Magnetization or Open Chronit Characteristic of an 169
85	— Measurement by Transmission Dynamometer of Efficiency
	of an
72	
	stant Voltage on Load
	Separation of the Internal Losses in an
69	Short Circuit Characteristic of an
	"Yoltage Drop" in an
133	Alternators, 3-voltmeter Method of finding the Electrical Power
	developed by
74	Efficiency and External Loss Test of a Pair of 192
126	- Impedance, Reactance, Self-Induction by Alternating
	Currents
	Aluminium and Copper, Comparative Table for
5	Ammeter Calibration by comparison with a Crompton Potentic-
	meter. , , ,
de i	8—— Calibration by comparison with a Kelvin Composite Balanco $7 & 8$
4	—— Calibration by comparison with a Kelvin Centi-Ampere
	Balance
1	- Calibration by comparison with Standard D'Arsonval Am-
	proter
13	Complete Test for Various Sources of Error in Direct and
	Alternating Current
6	- Standardization by means of a Copper Voltameter 14
	Ams'or's Planimeter, Direction for using to give area of Indicator
	Diagram
	- Planimeter, Instructions for working 528
77	Analysis of Total Internal Lors of Power in Dynamos and Motors 205
	Angle of Lead of the brushes of a Generator
	Auti-inductive Resistance for use with Kelvin Standard Electric
	Balance
	Anti-logarithms, Tables of
	Arc Lamp Photometer Cradle
26	Arc Lamps, Determination of the Distribution of Light from . 67
31	Examination of Alternating Current
	- General Remarks on the Photometry of Electric , 61
24	
25	Measurement of the Nett Optical Efficiency of
30	Relation between Voltage and Current in
28	Relation between Voltage and Current with consumption of
	Carbons in

Carbons in

Relation between Voltage and Distance botween the Carbons in

Armstore Resistance of Dynamos and Motors, Messurement of the

Tout No.

689

Page

Řά

```
Cables, Measurement by Kelvin Voltmeter Method of Electrostatio
 121
            874
  85
                                                                                   w 84
       Calibration of a High Tension Alternating Current Voltmeter
  12
                                                                                     28
           of a High Tension Wattmeter by application of Ohm's Law
of a Voltmeter by comparison with a Crompton Potentic-
  17
                                                                                     41
  11
         meter
                                                                                     23
            of a Voltmeter by comparison with a Kelvin Centi-Ampere
  10
            Balance
                                                                                     22
            of a Voltmeter by comparison with a Kelvin Composite
                                                                                     21
            of a Voltmeter by comparison with a Standard D'Arsonval
            Voltmeter
            of a Wattmeter by comparison with a Kelvin Composite
           of a Wattmeter by comparison with a Standard Ammeter
  15
            and Voltmeter
                                                                                     87
            of a Wattmeter with Alternating Currents (3-Voltmeter
  16
            Method
                                                                                     38
            of an Ammoter by comparison with a Kelvin Centi-Ampere
            Balanco
                                                                                     10
            of an Ammeter by comparison with a Kelvin Composite
            Balance
                                                                                      7
            of an Ammeter by comparison with a Kelvin Composite
            Balance
            of an Ammeter by comparison with a Standard D'Arsonyal
                                                                                      ő
            Ammeter
         of an Ammeter by means of a Crompton Potentiameter - of an Electricity Meter
                                                                                     11
  18
                                                                                     43
           of Birect Current Voltmeters (Poggundorff's Method)
- of Electrical Measuring Instruments, General Remarks on the
  7
                                                                                     16
           of Speed Indicators
                                                                                    134
 51
      Candla Power and Efficiency of Electric Glow Lamps, Measure-
  21
           ment of the
                                                                                     БQ
           - Power (mean spherical) of an Electric Arc Lamp
- Power (mean spherical) of an Electric Clow Lam
                                                                                     70
           - Power, Variation of, with direction around on Electric Glow
 22
           Limp
      Capacity and Ohmic Resistance in Circuits, Effect of Frequency
113
          and Efficiency of Secondary Calls, Measurement of the Storage
         -- and Efficiency of Secondary Cells, Ways of Denoting
Current of a Cable or Main
                                                                                   872
         of Cables (Kelvin Valtmeter Method), Proof of Formula in of Cables (Kelvin Valtmeter Method), Proof of Formula in of Cables (Magueto Inductor Method), Proof of Formula in of Concentric Cables, Folmula expressing the of Concentric Cables, Formula expressing the
                                                                                   500
                                                                                   601
                                                                                   877
132
                                                                                   371
THO
           Method), Electrostatic
           of Electrical Wires and Cables, Measurement of the Electro-
           etatio
           of Short Cables (Kelvin "Voltmeter Mothod"), the Electro-
181
      Carbon Rheostat, Adjustable
Carbart-Clark Standard Cell, Temperature coefficient of the
```

Colla, Proof of Formula giving Internal Resistance of Secondary Conti-Ampere Balance, Constants (when used as a Voltageter) of

"Characteristic" of a Compound Wound Dynamo (Long Shunt),

Determination of the . - of a Compound Wound Dynamo (Long Shunt), Graphical

or Curve of Magnetization of Separately Excited Dynamo,

or Curve of Magnetization of Series Wound Dynamo,

or Curve of Magnetization of Shunt Wound Dynamo,

"Characteristics" of Dynamos, Introductory Remarks on the

of Magnoto Dynamo, Debornination of the Chemical Equivalents, Table of Choker, Variation of Impedance, Reactance and Salf-Induction with Position of Mayable Core to Solsmoddal

- Effects of Variation of Frequency of Supply in Alternating

Current
- having Capacity and Resistance only, Variation of Impedance with Capacity, Frequency and Resistance,
- having Capacity in Serice with Resistance, Numerical and
Phase Rolation between Voltages and between Voltage and

having Ohmic Resistance and Belf-Induction only, Relation

between Frequency and Temperature .

- having Resistance in Parallel with Self-Induction or Capacity,

Numerical and Phase Relation between Main and Branch

- having Self-Induction and Resistance only, Variation of Impedance with Self-Induction, Frequency and Resistance

671

Pege

491

650

546

140

162

155

169

143

143 644 330

810

333

810

326

328

310

and A.C. Sides

Internal

Internal .

Internal

Current

Corrent

Cultrents

118

118

112

110

111

Ampere Belance, Kelvin's

Turk No.

82

Kalvin's

Test	No, Pa
114	Circuits having Self-Induction, Capacity and Resistance, Variation
	of Impedance with Self-Induction, Capacity, Resistance and
	Frequency , , , , , , , , , , , , , , , , , , ,
	- Measurement of Power in 2 Phase 393 & 39
135	
100	Clark Standard Cell, Preparation of the
	Clark's Standard Cell, relation between E M F, and tempera-
	ture of
78	Coefficient of Magnetic Leakage in Machines (Ballistic Method) . 20
10	
100	- of Magnetic Dispersion in Induction Motors . 28
128	Coefficients of Self-Induction (by Alternating Currents), Com-
	parison of two
24	Commercial Efficiency of an Arc Lamp, Measurement of the
78	Efficiency of an Alternator 18
85	- Efficiency of a Generator, Determination by Transmission
	Dynamometer
84	- or Nett Efficiency of D. C. Dynamos (Kapp's Electrical Method) 22
105	Commutator Motors, Efficiency and B.H.P. of Single Phase . 29
	Composite Relance, Constants for Kelvin's
	- Balance, Krlvin's 55
84	Compounding a Dynamo, Determination of Field Magnet Wind-
	ings for truly
65	- a Dynamo, Determination of Speed and E.M.F. for tinly . 16
62	Compound Wound Dyname (Long Shunt), Determination of the
	Characteristic of a
	Wound Dynamo (Long Shunt), Graphical deduction of Total
	Characteristic of a
53	Wound Dynamo, Relation between Speed and E. M. F. in 14
63	Wound Dynamo (Short Shunt), Determination of the
	Characteristic of s
	Wound Dynamo (Short Short), Graphical deduction of Total
	(Theracteristic of a
93	Wound Electro-Motors, Efficiency and B.H.P. of Direct
	Current
132	Concentric Cubles, Measurement ballistically of Electrostatic
	Capacity of
	Main, Straight Joint in a
130	- or Ordinary Cables and Condensers (A.C. Method), Electro-
	static Capacity of
	Condensers, Kelvin's Air
	Conductivity Test of Copper Wire by Siemens' Low Resistance
	Bridge
99 b	44 Conductor Resistance, Measurement by a Portable Testing Set
00 4	of Metallic
4	"Constant" of an Ammeter, Determination of, by a Copper
A	Voltameter
	Countants, useful
	Contact Maker, Revolving
	Continuous and A.C. Electro-Motors, General Bemarks on the
	Testing of 25
	Conversion in Multi-phase Rotaries, Voltage ratio of . 487 & 43
	ratio of A.C. Static Transformera
	k 149 Converters, Efficiency of Multi-phase Rotatory . 438 & 43
	"No Load" characteristic of Rotary
148-	152 — Other tests on Rotary

	INDEX	673
Test I	C a	Page
	Converters, Synchronising Rotary	. 441
_	Copper and Aluminium, Comparative Table for	. 645
•	Conductors, Standards for	640-2
	— Electro-Chemical Equivalent of	. 11
137	Losses in Transformer (Short Circuit Tost) .	. 407
	- Voltameters, Directions as to the use and arrangement of	. 14
	Cradle, Absorption Dynamometer	, 621
94	- Arc Lamp Photometer - Balance Method of finding the Efficiency and B.H.P. of D.C	. 587
D.7	or A.C. Motors	. 252
	Critical Resistance at a given Speed for a Series Wound Dynam	
	- Resistance at a given Speed for a Shirat Wound Dynamo	. 169
	Commutator of a Dynamo, General Remarks on, and Thompson'	
	Method of finding the Distribution of Potential round the	. 196
75	- of a Dynamo, Morday's Mathed of Finding the Distribution	
	of Potential round the .	. 199
76	of a Dynamo, Mordey Swinburne Method, ditto	. 201
80	Coils, Localization of Faults in Magnetizing	. 213
	Crompton D'Arsonval Galvanometer	. 589
154	Crompton's Potentiometer . Outrent and E. M. F. Curves of an Alternator, the Periodic	. 510 . 446
194	in Circuits having Ohmuc Resistance and Self-Induction only	
	Relation of Frequency and	. 310
	Curve Plotting	. 1
	Curve Plotting, Nebtlion for points in	. ŝ
	- Tracer, Ewing's Magnetic	609
	Curves of Electrical Horse-power Developed	147
	Polar	. 56
	ъ	
	D	
	D'Arsonval Galvanometer, Crompton	. 559
	Bensitics of Dry Air at different Temperatures and Pressures	
	Table of	. 650
78	Distribution of Waste Field in Dynamos, Determination of the	
D.F	Relative	. 207
25 22	of Light from an Electric Arc Lamp	. 67
22	- of Light from an Electris Glow Lump - of Potential round the Commutator of a Dynamo, Genera	. 55
	romarks on, and Thompson's Method ,	. 195
76	- of Potential round the Commutator of a Dynamo (Mordey)	
	Biethod)	. 199
76	- of Potential round the Communister of a Dynamo (Mordey	
•••	Swinburne)	. 201
	Double Square Roots for Kelvin Balances, Table of	. 665
156	Duddell Oscillograph, "Wave-forms" by the	. 451
61	Dynamo, Determination of Separate Field Magnet Winding for	t
	Truly Compounding	. 165
65	- Determination of Speed and E M.F. which produces a Tru	
	Compounding	. 167
62	Determination of the Characteristic of a Compound Wood	
	(song Shunt)	. 160
63	Determination of the Characteristic of a Compound Woon	
-	(Short Shunt)	. 163
80	Determination of the Characteristic of a Shunt Would	. 166

Test	No.	Page
	Dynamq, Determination of the Critical Resistance (at given speed)	Ţ.
59	for a Series Determination of the Curve of Magnetization of a Series	r ¹⁵⁴
61	Wound. Determination of the Curve of Magnetization of a Shunt	156
91	Would	159
58	- Determination of the External Characteristic of a Series	150
	Determination of the Total Characteristic of a Compound Wound (Long Shunt)	162
	- Determination of the Total Characteristic of a Compound	104
	Wound (Short Shunt) . Determination of Total Characteristic of Series Wound	164 152
	- Determination of the Total Characteristic of a Shint Wound	157
	Despersion Coefficient in Induction Motors	288
75	Mordey's Method of finding the distribution of Potential round the Commutator of a	199
76	Mordey-Swinburno Method, ditto	201
	- Thompson's Method of finding the Distribution of Potential	
79	round the Commutator of a	195 211
,,,	Denamometer, Absorption .	633
	— Cradle Absorption	621
85	Measurement of Efficiency of a Generator by Transmission . Measuring Instruments, Parr's Direct reading	230 57%
	- Kiemens Electro-	677
	Siemens Horse-power Transmission	623
	Spring Transmission	626 580
77	Dynamus and Motors, Analysis of Internal Loss of Power in	202
	k 40 — Measurement of the Insulation Resistance of . 113 &	
54 55	Determination of the "Characteristic" of Magneto Determination of the "Characteristic" of separately excited	143 147
88	- Efficiency by Hopkinson's Electrical Method of Direct	117
	Current	223 '
84 82	Efficiency by Kapp's Electrical Method of Direct Current Efficiency by Swindarne's Electrical Method of Direct	226
02	Current	219
58	Internal Characteristic or Curve of Magnetization of sepa-	148
	rately excited Introductory Remarks on the "Characteristics" of .	142
57	Relation between External and Exciting Currents of separ-	
53	ntely excited	149 140
89	Bountion between blood said is at. F. to Priest Carraits	134
	X.	
	Riddy Current Absorption Dynamometer Brake	835
123	Currents in Magnetic Material, Measurement of . 348 & Efficiency and B.H.P. of D.C. Compound Wound Electro-Motors	352 451
9 3 89	and B.H.P. of D.O. Series Wound Electro-Motors	241
92	- and R.H.P. of D.C. Shunt Wound Electro-Motors	248
96	and B.H.P. of Electro-Mater: (Swinburne's Electrical Method) and B.H.P. of 500 Volt Direct Current Tram and Railway	265
90	Motors	245
94	and B.H.P. of small Electro-Motors (Crails Balance Method)	252

Test ?	M'n	W
100	Efficiency and B.H.P. of Multi-phase A.C. Electro-Motors .	Page 272
200	and B.H.P. of Single-phase A.C. Electro-Motors	
	and C.P. of Floring Law Towns Mountains of the	269
24		
~-	Commercial	68
25	- and C.P. of Electric Arc Lamps, Measurement of the Nett	
	Optical	66
21	- and C i'. of Electric Glow Lamps, Measurement of the	50
74	- and Internal Loss Test of a Part of Alternators .	192
33	- and Storage Capacity of Secondary Cells, Measurement of the	74
	and Storage Capacity of Secondary Cells, Ways of represent-	
_	ing the	78
105	- Is. H. P. &c., of Single-phase Commutator Motors .	299
107	- B.H.P. &c., of Synchronous A.C. Motors .	809
153	of a Recetor or Motor Generator Set .	444
158		465
86	- of a Generator, Measurement by Transmission Dynamometer	100
CD	of the	220
144		
145	— of a Nodon Valve Rectifler	427
145	— of a Rotary Rectifier	431
159		468
73		185
167		462
90		256
83	- of Direct-Current Dynamos (Hopkinson's Electrical Method)	223
84	of Direct-Current Dynamos (Kapp's Ricctrical Method) of Direct-Current Dynamos (Swinburne's Electrical Method)	226
82	- of Direct-Current Dynamos (Swinburne's Electrical Method)	219
	of Dynamos (Hepkinson's Method), Proof of Formula for the	497
101	of Induction Motor (Heyland Method)	277
102	of Induction Motor (Sumpner-Weekes method)	238
146		& 439
149	- of Multi-phase A.C. Static Transformers	424
		2-424
142	- of Single-phase A.C. Static Transformers (Biskosley's	
142	Dynamometer Mathod)	422
146	of Single above A.C. Static Transferrence the Death Con-	444
140		
4 00	version)	414
189	- of Single phase A.C Static Transformers (by Single Con-	
	Yerkion)	412
141	of Single-phase A C. Static Transformers (by Sumpner's	
	Method)	417
	- of Transformers (Blakesley's Method), Proof of Formula for	
	the	502
108	Slip, Torque, Load, &c., in Induction Motor with Variable	
	Rotor Circuit Resistance, Relation between	294
18		48
* 19	Moter, Complete Test of an	1.5
	Electro-Chemical Equivalents of Copper for various current den-	
	aitles. Table of	41
	- Equivalents, Table of	844
		577
144	Electro-Dynamometer, Siemens	
144		427
94	Risciro-Motors, Efficiency and B. H. P. (by Cradis Ralance Method)	
	ofemeli .	252
95	- Efficiency and B.H.P. (by Swinburne's Electrical Method)	

Test No. Page		Page
93	Electro-Motors, Efficiency and B.H.P. of D.C. Compound Wound	251
88	- Efficiency and B.H P. of D.C. Series Wound	211
P2	- Efficiency and R H.P. of D.C. Shuut Wound . /	P 18
	Efficiency and B H. P. of Multi-phase A C.	272
	- Efficiency and B H P. of Single-phase A C	249
96		258
***	- General remarks on the Testing of continuous and A.C.	232
132	Electrostatic Capacity of Concentric Cables by Standard Magneto	
102	Inductor Method	377
180	- Capacity of Concentric or Ordinary Cables and Condensers	411
100	by the Alternating Current Method	572,
	Capacity of Electric Wires and Cables, General Notes on	V/ 4,
	the	869
131	Capacity of Short Cables by Kelvin Multicellular Voltmeter	400
101	Method	374
	Vultmaters	562
	Voltmeters, Kelvin's Multicollular .	563
155	E. M. F. and Current Curves of an Alternator (Ballistically), the	000
100	Periodic .	450
154	- and Curent Curves of an Alternator (Electrostatically), the	100
101	Periodic	446
65	- and Speed at which a Dynamo truly Compounds, Determina-	110
	tion of	167
5.3	and Speed in Direct Current Dynamos, Relation between .	140
-	and Temperature of Clark's Weston Cadmium and Carhart-	+
	Clark's Standard Colls, Table giving	613
	- of an Alternator, Algebraical Relation expressing the	***
	Total	179
	- of an Armature Coil at different positions (Thompson's	
	Method), Investigation of	198
	- of Armature Corls, Thompson's Method of Measuring the .	198
67	- with Excitation (at constant speed) in Alternators, Varia-	
	tion of	169
66	with Speed (at constant excitation) in Alternators, Variation	
	nf `	148
	Errors in Ammeters and Voltmeters, Enumeration of	49
	Eureka Resistance Material, Table for	648
	Evershed Bridge-Megger Constant Pressure Generator for	544
	- Hrbigo-Megget Index, Adjuster for	546
	- Bridge-Megger Insulation Testing Set, Description of the .	ñ41
	- Maggar Insulation Testing Set, Description of the	539
	Portable Testing Sets, Description of the	589
	Ewing's Hysteresis Testor, Measurement of Magnetic Hysteresis by	356
	Magnetic Curve Tracer	609
87	Excitation with Speed of D.C. Motors, Variation of (for Constant	
·	Voltage)	238
58	External Characteristic of Series Dynamo, Determination of the .	160
	• •	
r		
	Factor in Induction Motors, Leakage	288
		316
	in A.C. Circuits, Measurement of Power	462
	Fan Set, Efficiency of an Electro-Motor	180
	Faults in Electric Mains, Loudization of	213
••	Faults in Magnetizing Colls, Localization of	210

	INDEX	677
Test :		Page
64	Field Magnet Windings for Truly Compounding a Dynamo, Determination of	166
111	Frequency, Slip and Speed, Measurement by Stroboscopic Method and Current, Power, Impedance, and Angle of Lag in Curenita having Ohmic Resistance and Self-Induction only,	282
110	Relation between	321
113	Soif-Induction only, Relation between on Circuits having Copecity and Ohmic Resistance, Effect of	319 326
. 114	on Circults having Self-Induction, Capacity, and Ohmic Resistance, Effect of	828
	of the Supply in A.C. Circuits, Effects of Variation of the . Face Table for Different Diameters and Currents .	310 654
	G	
	Galvanometer, Crompton D'Arsonval Galvanometers, Deviation of deflection from direct proportionality	669
	in Kellecting	490
	Somitive Portable	571
158		465
	Gauges, Weights, Resistances and Sections, Table giving relation	
	of different metals of	653
	— Comparison of different Wire.	650
	Gearing of Engine Indicators Generator, the Evershed Budge-Megger Constant Pressure	469 514
21	Glow Lamp, Measurement of the Efficiency and C.P. of Electric.	50
22	- Variation of C.P. with direction around an Electric	55 55
	Guard-wire in Tests on the Insulation Resistance of Cablea, Price's	100
	н	
101	Heyland Diagram, Experimental and Graphical Deduction of .	277
74	Hopkinson Principle for Tesling a Pair of Alternators , ,	192
83	Hopkinson's Electrical Method of Measuring Reficiency of D.C.	
	Dynamos	223
	Method of Measuring Dynamo Efficiency, Proof of Formula	497
122	Permeamotor, Measurement of Magnotic Permeability by	347
102	Ropkinson-Sumpner Method of Testing Induction Motors .	288
	Horse-power Curves	147
	— Transmission Dynamometer, Siemons Houseman's Method of Separating the Internal Losses in a Dynamo	623
400	or Motor	204
126 123	Hysteresis by Kwing's Hysteresis Testor, Messarement of Magnetic — in Magnetic Material (Single-phase A.C.s), Measurement of	956
	Magnetic Tost, I'reparation of Iron samples for	848 350
	ilorizontal Carolle Power, Mean	56
	I.H P. of a Compound or Triple-Expansion Engine, Determination	
	of the	478
	Illumination Photometer, Trotter's	590

678

110	Timbourdes with young tremitous octation officents in Citemas	
	having Capacity and Self Ind. in Parallel, Variation of	H
118	- Resotance and Self-Ind. with Position of Movable Core in	•
	Selencidal Choker	83
126	- Reactance, and Self-Ind. of Alternators, Motors, Trans-	
		8:
119	- Reactance, Self-Ind., Current and Power, Effect of Longth	
	of Air Cap in a Closed Magnetic Circuit on	84
118	- with Capacity, Frequency, and Resistance in Circuits having	•
110	Capacity and Resistance only, Variation of	82
114	- A Political Country of Paristons in Country Land	02
114	- with Self-Ind., Capacity, and Resistance in Circuits having	
	Self-Ind., Capacity, and Resistance, Variation of	25
111	with Solf-Ind., Frequency and Resistance in Circuits having	
	Self-Ind, and Resistance only, Variation of .	32
	Indicator Diagram, Determination of the l.H.F. from the	47
	— Diagram, Form and Explanation of an	42
51	Indicators, Calibration of Speed	18
	Gearing of Engine	46
	- Table of Springs for Thoropson's Steam-Engine	52
	- Thompson's Steam-Engine ,	53
101	Induction Motor, Complete Test without loading it up .	27
102	- Motor, Complete Test by Summer Weekes method .	2
	Motor, Relation between Starting Torque, Current, Voltage,	20
104		
	and the Rotor Circuit resistance of an	29
100	Motors, Efficiency and B. H. P. of Polyphase	27
99	- Motors, Efficiency and H. H. P. of Single Phase	26
97	Motors, No-Load Open-circuit Test on	26
98	Motors, No-Load Short-erronit, Test of	26
	Motora, Ratio of Transformation in	26
	— Motors, Testing of Asynchronous A.C.	26
103	- Motors with variable Rotor Circuit Resistance, Relation	
	between Efficiency, Slip, Torque, Load, &c., in	29
117	Inductive A.C. Circuits, Determination of Load and Wattless	~
	Corrents in	38
120	- Effects due to the relative Positions of 2 Coded Circuits, In-	
	vestigation of Mutual	34
	- Drop of an Alternator with Load and Power Factor	17
	- Retardation	37
108	Inductiveness of a Circuit, Determination of the	81
140	Instruments, General Remarks on the Calibration of Electrical	٠.
	Messaring	
	Insulation Resistance, Actual Values for given Voltage and	
	Number of Lemps	11
	Resistance by Direct Delication Method, Proof of Formula for	49
_	Resistance, General Remarks on	10
42	- Resistance, Measurement by the Silvertown Portable Testing	
	Set	10
41	Resistance of Cables, Measurement by Direct Deflection	
	Mothod	8
49	Resistance of Dynamos and Motors, Measurement of the	12
	- Resistance of Dynamos and Motors, Proof of Formula for .	49
	- Resistance of Electrical Cables and Installations . 98 &	10
47	Resistance of Faulty Telegraph Insulators	12
43	- Rasistance of Installations, etc., by Evershed's Portable	-
	Mogger and Bridge-Magger Testing Sets , 113-116 &	58

	INDRI		671
Test	No.		Pag
	Insulation Resistance of Installations, etc., while working	-	III
44	Besistance of Installations, etc., while working	•	12
-	Besistance of installations while working, Proof of I	Formula	
. •	for		49
48	Resistance of Storage Batteries, Mosaurement of the	·	12
	- Resistance of Storage Batteries, Proof of Formula for		49
	Resistance with Testing Voltage, Variation of .		11
	Insulators for Postal and other Telegraph Lines		123
56	Internal Characteristic of Separately Excited Dynamos .		14
60			15.
. 61	Characteristic of Shunt Wound Dynamo		15
74			19
77	 Loss of Power in Dynamos and Motors, Analysis of 	the .	20
	— Losses in an Alternator		18
	Losses in an Alternator, Separation of the		181
32	Resistance of Secondary Cells, Measurement of the .		7.
	Resistance of Secondary Cells, Measurement of the Resistance of Secondary Cells, Proof of Formula givi	ing	49
	Iron Losses in Alternators by Retardation Method .		19
124	Losses, Separation of, by A.C. Frequency Method .		85
	j.		
	Jointing Electric Light Cables and Mains, Course in		47
160	- Electric Light Cables, Detailed Instructions for .		47
	- Electric Light Cables, General Observations on .		47
	Jolly's Photometer Screen		59
	•		
	• K		
84			2.7
	- Method of Separating the Internal Losses in Dynan	non utg	
	Motors		20
			61
•	Kelvin Air Condonser		
•	Magneto-static Current Moter	•	56
•			56:
•			56 56 56
•	Magneto-static Current Meter Multicellular Electrostatic Voltmetet Standard Indances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance		56 56 56
•	Magneto-static Current Moter Multicellular Electrostatic Voltmote: Standard Islances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Res		56 56 56 54
•	Magneto-static Current Moter Multicollular Electrostatic Voltmote: Standard Infances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Res for	istances	56
•	Magneto-static Current Moter Multicellular Electrostatic Voltmotes Standard Indances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Resfor Standard Centi-Ampere Balance, Constants when me	istancis	56: 56: 56: 54: 55:
•	Magneto-static Current Moter Multicellular Electrostatic Voltmote: Standard Infances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Resfor Standard Centi-Ampere Balance, Constants when an Voltmeter	istances	56: 56: 56: 54: 55:
•	Magneto-static Current Moter Multicellular Electrostatic Voltmotes Standard Indances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Constants when us Yelbrieter Standard Composite Balance,	istancis	56: 56: 54: 55: 55:
•	Magneto-static Current Meter Multicellular Electrostatic Voltmote: Standard Infances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Resfor Standard Centi-Ampere Balance, Constants when ne Voltmeter Standard Composite Balance, Standard Composite Balance, Constants for	istances	56: 56: 54: 55: 55: 56:
131	Magneto-static Current Moter Multicellular Electrostatic Voltmets: Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Constants when an Voltmeter Standard Composite Balance, Constants for Voltmeter Malance, Gonatanta for Voltmeter Method of funding Electrostatic Cap	istances	56: 56: 54: 55: 55: 56: 56-
131	Magneto-static Current Moter Multicellular Electrostatic Voltmote: Standard Indances, Adjustment of the Standard Centi-Ampere Balance Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Constants when us Voltmeter Standard Composite Balance, Standard Composite Balance, Constants for 'Voltmeter Method" of finding Electrostatic Cap Short Cables	istances	56: 56: 54: 55: 55: 56: 56: 57:
131	- Magneto-static Current Moter - Multiosllular Electrostatic Voltmetet - Standard Inlances, Adjustment of the - Standard Centi-Ampere Balance, Anti-Inductive Res- for - Standard Centi-Ampere Balance, Anti-Inductive Res- for - Standard Centi-Ampere Balance, Constants when us Voltmeter - Standard Composite Balance, Constants for - "Voltmeter Method" of fluding Electrostatic Cap- Short Cables - Key, Highly insulated 2-way spring tapping	istances	56: 56: 54: 55: 56: 56: 58:
131	Magneto-static Current Moter Multicellular Electrocatic Voltmets: Standard Infances, Adjustment of the Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Composite Balance, Constants when ne Yoltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluiding Electrostatic Cape Short Cables Key, Highly insulated 2-way spring tapping Pohl's change-over commutator	istances	56 56 56 54 55 55 56 56 58 58
131	Magneto-static Current Moter Multicollular Electrostatic Voltmote: Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Conti-Ampere Balance, Constants when ne Voltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluding Electrostatic Cap Short Cables Key, Highly insulated 2-way spring tapping Pohl's change-over commutator Simple reversing	istances	56 56 55 54 55 56 56 56 58 58
131	Magneto-static Current Moter Multicellular Electrocatic Voltmets: Standard Infances, Adjustment of the Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Composite Balance, Constants when ne Yoltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluiding Electrostatic Cape Short Cables Key, Highly insulated 2-way spring tapping Pohl's change-over commutator	istances	565 56 54 55 56 56 56 56 58
131	Magneto-static Current Moter Multicollular Electrostatic Voltmote: Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Conti-Ampere Balance, Constants when ne Voltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluding Electrostatic Cap Short Cables Key, Highly insulated 2-way spring tapping Pohl's change-over commutator Simple reversing	istances	56 56 55 54 55 56 56 56 58 58
•	Magneto-static Current Moter Multicellular Electroctatic Voltmets: Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Conti-Ampere Balance, Constants when ne Voltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluding Electrostatic Cap Short Cables Kry, Highly insulated 2-way spring tapping Pohl's change-over commutator Simple reversing Simple 2-way sliding	istances seel as a sacity of	56 56 55 54 55 56 56 56 58 58
131	Magneto-static Current Moter Multiosllular Electrostatic Voltmetet Standard Inlances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Conti-Ampere Balance, Constants when us Voltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluding Electrostatic Cape Short Cables Key, Highly insulated 2-way spring tapping Pohl's change-over commutator Simple 2-way skiding. L Lag is Circuits having Ohmic Resistance and Belf-Inductic	istances seel as a sacity of	56 56 56 54 55 56 56 58 58 58 58
•	Magneto-static Current Moter Multicellular Electroctatic Voltmets: Standard Infances, Adjustment of the Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Centi-Ampere Balance, Anti-Inductive Res for Standard Conti-Ampere Balance, Constants when ne Voltmeter Standard Composite Balance, Constants for "Voltmeter Method" of fluding Electrostatic Cap Short Cables Kry, Highly insulated 2-way spring tapping Pohl's change-over commutator Simple reversing Simple 2-way sliding	istances sed as a socity of	56: 56: 56: 54: 55:

	No. Lamp-box Resistanco, Incandescent	. 19 . 5
129		
146	Lead-covered Cables, Twist-Joint in	. 8
		1
	Cables, T-Joint in	. 4
	Lead of Brushes in a Dynamo, Anglo of	. 1
78		
	Magnetic	. 2
	— Factor in Industion Motors	. 2
	Liquid Rhoostat, Thros phase	. а
	Liquids, Table of Specific Resistance of	. 6
117	Load and Wattless Currents in an Inductive A.C. Circuit	
	Determination of the	3
100	Lead-Efficiency Test of an Induction Motor	. 2
50	Localization of Faults in Electric Mains	ī
80	of Faults in Magnetizing Coils	. 2
	Low Resistance, Approximate Test for a very	5
	- Resistance Bridge, Siemens form	5
	- Resistance Fixed Standard	6
	Resistance Measurer, Description of a	. G
40		de 5
	Paristens Management by Printer steamer M. M. 19	
37	Resistance, Measurement by Simple Potentiometer Method	
36	Resistance, Measurement by Voltmeter and Ammeter	
	Method	
35	- Resistance (Potential Difference Method), Measurement of	
	- Resistance (Potential Difference Method), Solution of Info:	
	eners for	. 4
	Logarithms, Tables of	. 6
124	Losses in Iron, Separation of, by A.C. Frequency Method	. 3
137	in Transformers (by Short Circuit Test). Copper	. 4
	—— in Transformers on Open Circuit (constant) .	. 4
	Lummer Brodhun Photometer Surson, Principle of	
	ж	•
81	Magnet Coils, Rise of Temperature and Increase of Resistance of	2
79	Magnetic Characteristic of a Dynamo with Varying Air Gapa	2
•-	— Curve Tracer, Ewing's	Ê
	- Dispersion in Industries Motors, Coefficient of	2
168		
125	Hysteresis, by Ewing's Hysteresis Toster, Measurement of	. 9
123	Il) steresis in Magnetic Material (Single-phase A.C.s)	
	Measurement of	. 8
78	- Leakage Coefficient """ in Dynamos, Determination (b)	
	Ballistic Method) of the	. 2
123-	 Material, Measurement of Hysteresis (Single-phase A.C.s) 	
	in samples of	8-3
400	- Permeability, by Honkinson's Permeameter, Measurement of	ſ ŝ
122	Permeability by the Permeameter, Measurement of .	. 8
123 121	- Blip in A.C. Motors	260
		. ĭi
221	Magnetization Characteristic of an Alternator	
121 67	Magnetization Characteristic of an Alternator	
121 67 68	— Curve of an Alternator on Full Local	. 1
221 67 68 66	Curve of an Alternator on Full Load Curve of Separately Excited Dynamo	1
121 67 68 66 59	Curve of an Alternator on Full Load Ourve of Separately Excited Dynamo Curve of Series Wound Dynamo	1 1
221 67 68 66 59 61	Curve of an Alternator on Full Load Curve of Separately Excited Dynamo Curve of Series Wound Dynamo Curve of Shunt Wound Dynamo	1 1
121 67 68 66 59	Curve of an Alternator on Full Load Ourve of Separately Excited Dynamo Curve of Series Wound Dynamo	1 1

INDEX 681

89 *Mi 54 Mi	sgnelization Curre or "Open Circuit" Characteristic of Robery Convecter genetizing Coils, Localization of Faults in agnete Dynamo, Determination of the Characteristic of a — Dynamo, Graphical Beneticion of Total Characteristic of a agnetic-state Current Meter, Kalvin's adjustable angenin Resistanco Material, Table giving his of Temperature for Different Currents in aw's Rule for finding the smallest size of a Ruske Pulley can spherical and Horizontal Cambe Power cosuring Instruments, Parr's Direct-Reading Dynamometer Megger 'Insulation Testing Set, Evershorf's 114 & ter, Catibration of an Electricity cityen Screen Photometric Standard of Eight orders' Method of finding the Distribution of Potential round a Dynamo Commutator — Method of Separating the Internal Losses in Mutors and	488 213 143 145 558 649 235 56 572 539 43 45 595
18 M.	agastizing Coils, Localization of Faults in agasto Dynamo, Determination of the Characteristic of a Dynamo, Orephical Beduction of Total Characteristic of a agnetic state Current Meter, Kalvin's adjustable angunit Resistance Material, Table giving Riso of Temperature for Different Currents in aw's Rule for finding the smallest size of a Rinko Pulley can spherizal and Horizontal Cambe Power casuring Instruments, Parr's Direct Reading Dynamometer Magger' Insulation Testing Set, Reveshed's etc., Calibration of an Electricity chiven Screen Photometric Biandard of Light orders Michod of finding the Distribution of Potential round a Dynamo Commutator.	213 143 145 558 649 235 56 572 539 43 45
18 M.	ngueto Dynamo, Determination of the Characteristic of a Dynamo, Graphical Daduction of Total Characteristic of a agneto-states Current Motor, Kalvin's adjustable of Different Currents in aw's Rulo for finding the smallest size of a linke Pulley can spherized and Horizontal Camble Power casuring Instruments, Paris Pintert Reading Dynamometer Mogger' Insulation Testing Set, Evershed's 114 & eter, Calibration of an Electricity	143 145 558 649 235 56 572 589 43 45
76 M 153 M 153 M 164 M 165 M 166 M 167 M 1	— Dynamo, Graphical Daduction of Total Characteristic of a asgreto-state Current Moter, Kalvin's adjustable anganin Resistance Material, Table giving him of Temperature for Different Currents in wa's Rule for finding the smallest size of a litake Pulley can spherical and Henizontal Cambe Power casuring Instruments, Parr's Direct Heading Dynamometer Magger 'Insulation Testing Set, Evending Dynamometer and Calibration of an Electricity of the Sector Photometric Standard of Light orders Airched of finding the Distribution of Potential round a Dynamo Commutator.	145 558 649 235 56 572 539 43 45
Mi M	agneto-stata Current Moter, Kalvin's adjustable anganin Resistance Material, Table giving Riso of Temperature for Different Currents in aw's Rule for finding the smallest size of a Ricake Pulley can spherical and Horizontal Cambe Power casuring Instruments, Parr's Direct-Reading Dynamometer Magger' Insulation Teating Set, Evershed's eter, Calibration of an Electricity — Complete Test of an Electricity cityen Screen Photometric Biandard of Light orders Michael of Inding the Distribution of Potential round a Dynamo Commutator.	558 649 235 56 572 539 43 45
Mi M	anganin Resistance Material, Table giving Rise of Temperature for Different Currents in aw's Rule for finding the smallest size of a Ricake Pulley can spherical and Rotizontal Camile Power casuring Instruments, Paris Pinert-Reading Dynamometer Magger' Insulation Testing Set, Eversholds 114 & etc., Calibration of an Electricity——Omplete Test of an Electricity citives Screen Photometric Standard of Light orders Michael of Inding the Distribution of Potential round a Dynamo Commutator.	649 235 56 572 539 43 45
18 M/M 19 M/M 18 M/M 19 M/M 15 M/M 153 M/M 153 M/M 86 M/M 88 — 87 4 102 — 101 —	for Different Currents in aw's Rule for finding the smallest size of a Rinke Pulley can spherizal and Horizontal Cambe Power casuring Instruments, Parr's Direct Reading Dynamometer Magger 'Insulation Testing Set, Reveshed's etc., Calibration of an Electrority — Complete Test of an Electrority chiven Screen Photometric Biandard of Light ordey & Method of finding the Distribution of Potential round a Dynamo Commutator.	235 56 572 539 43 45
18 Mon	aw's Rule for finding the smallest size of a Rinke Pulley can spherical and Horizontal Camble Power casuring Inatuments, Paris Direct Reading Dynamometer Megger' I naulation Testing Set, Evershed's 114 & eter, Calibration of an Electricity——Complete Test of an Electricity claves Screen Photometric Standard of Light ordey's Method of finding the Distribution of Potential round a Dynamo Commutator.	235 56 572 539 43 45
18 Mon	can apherical and Horizontal Caudle Power essuring Instruments, Parr's Direct-Reading Dynamometer Magger I Insulation Testing Set, Reverbed's 114 & eter, Calibration of an Electricity — Complete Test of an Electricity rtheon Screen Photometric Standard of Light orders Michael of finding the Distribution of Potential round a Dynamo Commutator	56 572 539 43 45
18 Mi 10 Mi 76 Mi 76 Mi 153 Mi 86 Mi 88 — 102 — 101 —	essuring Instruments, Parr's Direct-Reading Dynamometer Megger' Insulation Testing Set, Evershed's eter, Calibration of an Electricity — Complete Test of an Electricity chiven Screen Photometric Standard of Eight ondoy's Method of finding the Instrumation of Potential round a Dynamo Commutator.	572 539 43 45
18 M/19 M/15 M/15 M/16 M/16 M/16 M/16 M/16 M/16 M/16 M/16	Megget ²⁷ Insulation Testing Set, Evershed's 114 & eter, Chilbration of an Electronic —— Complete Test of an Electricity—— Complete Test of an Electricity others Screen Photometric Standard of Eight order's Method of finding the Distribution of Potential round a Tymano Commutator—	539 43 45
18 M-19 M-19 M-19 M-19 M-19 M-19 M-19 M-19	eter, Calibration of an Electricity — Complete Test of an Electricity chiven Screen Photometric Standard of Light orders Mithod of finding the Distribution of Potential round a Dynamo Commutator	43 45
19	Complete Test of an Electricity three Serven Photometric Standard of Light order's Method of finding the Instribution of Potential round a Dynamo Commutator.	45
76 M 153 M 86 M 88 — 87 — 102 — 101 —	chyon Screen Photometric Standard of Light order's Method of finding the Distribution of Potential round a Dynama Commutator	
75 Mi 76 M 153 M 86 M 88 — 87 — 102 — 101 —	ordey's Method of finding the Distribution of Potential round a Dynamo Commutator.	595
76 M 153 M 86 M 88 — 87 — 102 — 101 —	Dynamo Commutator	
153 M 86 M 88 — 87 — 102 — 101 —		
153 M 86 M 88 — 87 — 102 — 101 —	- Method of Separating the Internal Losses in Mutors and	199
153 M 86 M 88 — 87 — 102 — 101 —		
153 M 86 M 88 — 87 — 102 — 101 —	Dynamos	203
153 M 86 M 88 — 87 — 102 — 101 —	onley-Swinburne Method of finding the Distribution of Potential	
86 M 88 — 87 — 102 — 101 —	round a Dynamo Commutator	201
86 M 88 — 87 — 102 — 101 —	otor Generator Sot, Efficiency of a Bocater or	444
88 87 102 101	— Testing Brake, Sommes	637
88 87 102 101	otors (at Constant Excitation), Variation of Speed with Voltage	2414
87 - 102 - 101 -	on Armature	236
87 - 102 - 101 -	- (at Constant Excitation), Variation of Speed, Voltage Current	2110
102 — 101 —	with Brush position on Commutator of	239
102 — 101 —	— (at Constant Voltage), Variation of Speed with Excitation	200
101 —		238
101 —	in D.C.	
	— Complete Test by Sumpner-Workes method.	288
	— Complete Test without leading up, of Induction	277
94 —	- Efficiency and B.H.P. (by Cradle Balance Method) of small	
	Electro-	252
107	- Efficiency and B.H.P., etc., of Synchronous	309
93 —	- Efficiency and B.H.P. of D.C. Compound Wound Electro-	251
89 —	- Kinglency and B. H. P. of D.C. Series Wound Electro-	241
65 -	- Efficiency and B.H P. of D C. Shant Wound Electro-	248
Ū0	Efficiency and B H.P. of 500-Volt D.C. Series Wound	
	Tianway	245
100 -	- Efficiency and B.H.P. of Multi-phase A.C. Elcotro	272
- BB	- Efficiency and B.H.P. of Single-phase A.C. Electro-	269
105 —	- Efficiency and H. H. P. of Single-phase Commutator	299
95 —	- Efficiency and B.H.P. (Swinburne's Electrical Method) of	
**	Klectro	255
120	Impedance, Reartance, and Self-Ind. by Alternating	
,120 -	Ourrouts	358
97	No Load "Open Circuit" Test of Induction	264
98 -	No-Load Short-Circuit Test of Induction	267
89	— (Poole's Electrical Method), Efficiency of D.C. Electro-	259
9d —	— Ratio of Transformation in Industrion	205
		200
104 —	- Helation between Starting, Torque, Current, Voltage, and the	296
	Botor Circuit Basislance of an Induction	
91 —		246
106 —	- Relation between Starting Torque and Current in D.C.	
	Relation between Starting Torque and Current in D.C. Relation of Excitation to Armature Current and "V" Curves of Synchronous	305

Test No.		Page
Motors, Testing of Asynchronous A.C. Industion		260
- Testing of Continuous and A.C. Electro-		232
103 With Variable Rotor Circuit Resistance, Relation between	ď	e.
Efficiency, Slip, Torque, Load in an Induction		294
77 Motors and Dynamos, Analysis of Internal Loss of Power in		202
49 and Dynamos, Measurement of the Insulation Resistance of	ŧ	129
Multicollular Electrostatic Voltmeter, Kelvin'a		568
100 Multi-phase A C. Electro-Motors, Efficiency and B H.P. of		272
146 & 149 A C. Rotatory Converters, Measurement of Efficience	ý	
		439
143 - A.C. Static Transformers, Measurement of Efficiency of		424 .
60 Marray's Loop Test for faults in Cables		130
120 Mutual Inductive Effects due to Relative Positions of 2 Coile	d	
Circuits	-	343
	•	
.,		
N		
Nalder Low Resistance Measurer		621
Potentiometer	•	607
Nickel-Chrome Resistance Material, Table for	•	647
144 Nodon Valvo Rectifier, Efficiency of a	•	427
Non-Inductive Wattmeter, Conditions for, and Object of a	٠	404
	٠	
147 No. Load "Open Circuit" Characteristic of Rotary Convertor	•	438
136 "Open Circuit" Characteristic of Static Transformer	•	404
"Open Circuit" Less in an A.C. Static Transformer "Open-Circuit" Test on Induction Motor "Short Circuit Test on Induction Motor	-	402
97 - "Open-Circuit" Test on Induction Motor	•	261
98 - Short Circuit Test on Induction Motor		267
191 Test for Efficiency of Induction Motor (Heyland Method)		277
Notation for Points in Carve Plotting		3
Numbers and Constants, Useful	٠	654
Δ.		
0		
Ohmmeter, Description of the principle of the Evershed .		539
Open Carcuit Losses in Transformers	•	402
67 — Circuit Characteristic of an Alternator	•	189
147 - Clrenit (No Lond) Characteristic of Rotary Converter	•	438
97 Circuit (No Load) Test of Induction Motor .	•	264
156 Oscillograph, "Wave-forms by Duddoll.	•	451
the estimated in machine of Surgery	•	Ant
P		
Parr's Direct-Reading Dynamometer Measuring Instruments		672
155 Poriodic E M F. and Current Curves of an Alternator (Ballisti	c	
Method)	-	450
154 — E.M.F. and Current Curves of an Alternator (Electrostation)	0	
Method)		446
121 Permeability by the Permeameter, Measurement of Magnetic		345
122 by Hopkinson's Permeameter, Measurement of Magnetic		947
121 Permeameter, Measurement of Magnetic Permeability by the		945
122 Measurement of Magnetic Permeability by Hopkinson's		847
— The		616
112 Phase Holations between Vultages and between Voltage Curren	t	
in Circuits of Capacity in Series with Ohmic Resistance		828
TO ACCOUNT OF ANIMATING THE PARTY IN THE PROPERTY OF THE PARTY IN THE	-	

Took !		Page
115	Phasa Relations between Main and Branch Currents in Circuits	
	having Resistance in Parallel with Self-Ind. or Capitalty .	332
116		
	and Self-Ind. in Parallel, Variation of Impedance and	333
	Photometer Bench, Table giving Ratio of Squares of Distances for a	651
		92-5
	- Trotter's Direct-Reading Bar,	689
	- Trotter's Illumination	590
	Photometric Cradle, Arc Lamp	587
	Standard of Light, the Methven Screen	595
		1-72
		0-60
	- Use of Coloured Glam in	58
	Planimeter (Ameler's), Instructions for getting area of Indicator	-
		530
	Diagram	
	(Ameler's), Instructions for working the	528
	l'Iotting Curvea	1
	l'ohl's Commutator	583
	Polar Curves of Distribution of Potential around Commutators .	200
	Curves of Light Distribution from an Electric Arc Lamp .	68
	Curves of Light Distribution from an Electric Glow Lamp .	56
		-400
96	Poole's Electrical Method for Efflorency of D.C. Motors	258
	Portable Galvanometer, Sensitive	571
	Testing Set (Evershed's), Description of a	-546
	Testing Set (Silvertown), Description of	434
34		
	by the	81
	Potential around a Commutator, Polar Curves of Distribution of .	200
35	- Difference Method of Measuring Low Resistance	84
00	- Difference Method of Measuring Low Resistance, Proof of	
	Formula in	492
	round the Commutator of a Dyname, General Remarks (and	7.04
	Thompson's method) on Distribution of	195
75		14.
76	round the Commutator of a Dynamo (Monley's method),	
	Distribution of	199
76	round the Commutator of a Dynamo (Mordey-Swinburns),	
	Distribution of	201
	Potentiemeter, Orompton's	510
39	Method of Comparing Resistances by Method of "Setting" Crompton's	94
	Method of "Setting" Crompton's	614
	Precention in using, and Sources of Error in	515
	The N.C.S.	507
	Volt Box	621
L83	Power absorbed in A.C. Circuits, Three-voltmeter Mathed of find-	
	ing the Ricctrical	379
109		
	— Factor, Measurement of 292, 216 — in Alternating Current Circuits, the Apparent	403
	in Alternative Commet Circuits the Two	403
144	in Alternating Current Circuits, the True	100
134	in Alternating Current Circuits, Three-ammeter Method of	
	finding the Electrical	898
	- in 2 phase A.O. Circuits, Measurement of . 893 &	
135	- In 3-phase A.C. Circuits, Measurement of 388 &	
		623
	Practical and C.G.S. units, Table showing Relation between	643

	_	TI
Tal :		Page
	Preparation of Iron Samples for Magnetic Hysteresis Test	85C
	Price's Guard-wire in Tests on Insulation Resistance of Cables .	130
	Prony Brakes , 234	693
	7	
	R	
126	Reactance, Impedance and Self-Ind of Alternators, Motors, Trans-	
	formers, etc., by Alternating Currents	358
118	- Impedance and Self-Ird with Position of Movable Core in	000
110	Solenoidal Choker, Variation of	389
110	Terral and Call I. J. On the Street of Street of Street of	908
119	Impedance, Self-Ind., Current and Power, Effect of Longth of	'
	Air Gap in a Closed Magnetic Circuit on	341
	of a Cable with Alternating Currents	373
	Reciprocals of Numbers, Tables of	663
144	Rectifier, Efficiency of a Nodon Valvo	427
145	Efficiency of a Rotary	431
	Beflecting Galvanometers, Deviation of deflection from direct	
	proportionality	190
	Regulation of Static Transformers from "open" & "short circuit"	
	tests, Deduction of	410
158	- (by Differential method) Determination of	410
139	(in Single conversion method)	412
	Reastone Resistance Material, Table giving Rise of Temperature	
	for Different Currents in	618
	Resistance, Anti-Inductive, for Kelvin Standard Balances	653
	- Approximate Test for a very Low	621
	- by Interpolation, Calculation of Exact	83
34		81
01		492
89	by the Whest-tone Bridge, Proof of Formula giving	91/2
ov	Comparison of High, Medium, and Low (Potentiomster	
	Method)	91
44	- (Conductor), Measurement by Everahed's Bridge Megger	117
108	Determination of the Non-inductiveness of a	314
	Fixed Standard Low .	1104
	— Coneral return ks on Insulation 98 &	
20	- heated by a Current, Measurement of a	46
	(High) by the Direct Deflection Method, Solution of Infer-	
	encen for	493
	Incandescent Lamp Rox	598
42	(Insulation) by Silvertown Portable Testing Set	105
49	— (Insulation) of Dynamos and Motors, etc.	129
	(Insulation) of Electrical Muina and Installations , 98 &	109
47	(Insulation) of Faulty Telegraph Insulators	123
43	(Insulation) of Installations, Cables, Machines, etc., by	
	Evershed's Megger & Bridge-Megger Portable Testing Sets 113	-116
45	- (Insulation) of Installations, etc., Measurement while working	119
46	(Insulation) of Installations, etc., Measurement while	
	working	121
48	(Insulation) of Storage Betteries	127
	- Low) by the Potential Difference Method, Solution of	
	Inferences for	492
40	(Low), Measurement by Nalder Measurer	97
37	- (Low), Measurement by Simple Potentiometer Method	88
26	(Low), Measurement by Voltmoter and Ammoter Method .	80
	Material Table for Furcks	210

INDEX	686
Test No.	Page
Resistance Material Table for Manganin	649
Material Table for Nickel Chronic	647
- Material Table for Recotern	648
- Measurer, Description of a Low	521
of a Dynamo Circuit, Graphical way of linding the .	154
41 of Cables (Direct Deflection Method), Measurement of the	
Insulation	99
35 of Dynamo Armstures, Electric Light Cables, etc., Measure-	
ment of the	81
- of Dynamus and Motors, Proof of Formula giving Insulation	496
- of Eleutric Light Installations while working, Proof of	
Formula giving the Insulation of Liquids, Specific	194
81 — of Magnet Coils, Rise of Temperature and increase in	615
38 — of Metallic Conductors by Silvertown Portable Testing Set .	216
of Pure Metal and Alloys, Table of Specific .	00 614
32 of Secondary Cells, Measurement of the Internal	75
	491
— of Secondary Cells, Proof of Formula for the Internal — of Single & Polyphase Windings, Measurement of	263
- of Stonge Battery, Proof of Formula giving Insulation	496
Summers Bridge for Low	525
- Test by Siemens Low Resistance Bridge	625
Resonance (Pressure) in Series Circuits	330
(Current) in Parallel Circuits	334
Retardation Method of Measuring Iron Loss in Alternators	190
Reversing Key, Sumple	685
Baralving Contact Maker	619
Bevolving Contact Maker . Bhoo-tat, Adjustable Carbon	596
- Adjustable	600
	-604
- Stand coil (step by step)	606
Three-phase liquid	607
81 Rise of temperature and increase in Resistance of Magnet Coils .	216
146 & 140 Rolery Converters, Efficiency of Multi-place 423 &	
147 - Converters, No-Load Characteristic of	438
149-152 - Converters, Other Tests on	-443
Converters, Synchronizing of	411
145 Roctifier, Efficiency of a	431
52 Rotational Spead, Measurement of, by Strohoscopic Fork	185
Rotor of an A.C. Motor, Definition of the	270
129 Howland's Method of Comparing Self-Induction by Alternating	
Currents	365
127 - Method of Measuring Self-Induction absolutely by Alter-	
nating Currents	362
•	
S	
U U	
Searf-Joint in Bare Wires	478
Screens (Bunsen's, Jolly's and Lummer-Brodhun's), Photometer 5	
- (Methven's) Photometric Standard of Light	695
48 Secondary Batteries, Measurement of the Insulation Resistance of	127
83 - Cells, Measurement of the Efficiency and Storage Capacity of	76
32 - Cells, Measurement of the Internal Resistance of	75
- Cells, Proof of Formula for the Internal Resistance of	491

127	No. Self-Induction, Absolute Measurement (by Rowland's A.C.	Pu
124	Method) of	80
126	(by Impedance Method), Measurement, using Single-phases A.C.s of	35
114	Capacity, and Ohmic Resistance in Circuits, Effects of Frequency with	82
128	- Comparison (by Alternating Current) of two Coefficients of .	36
118	Impedance and Reactance with Position of Movable Core in Sciencidal Choker, Variation of	83
	(Impedance Method using Single-phase A.C.s), Proof of Formula	49
110	Impedance, Reaclance, Current and Power, Effect of Longth	
126	of Air Gap in a Closed Magnetic Circuit on	34
	formers, stc., by Alternating Currents	35
129	- in Series and Parallel, Determination of Laws of Com- bination of	36
	in Series and Parallel, Proof of Laws of Combination	49
127	- Measurement (by Rowland's A.C. Method) of	86
57	Separately Excited Dynamo (at Constant Speed), Relation between	
	External and Exciting Currents	14
55	- Excited Dynamo, Determination of the "Characteristic" of a	14
БĠ	Excited Dynamo, Internal Characteristic or Curve of Mag-	
	netization of	14
Б3	Excited Dynamo, Relation between Speed and E.M.F. in Separation of Internal Losses in an Alternator	16
	of Internal Lesses in Dynamos and Motors, by Housman's	•
	Method	20
	— of Internal Lossos in Dynamos and Motors, by Kapp's Method	
124	- of Iron Losses by A.C. Frequency Method	20 35
	Series Wound Dynamo, Critical Resistance at a given Speed in a .	15
58		
	of a	15
59	 Wound Dynamo, Determination of Total Characteristic of a Wound Dynamo, Internal Characteristic or Curve of Mag- 	15
22	netization of a.	15
89	- Wound Electro-Motors, Efficiency and B.H.P. of Direct	
	Current	24
90		
69	D.C. Short-circuit Characteristic of an Alternator	24 17
98	-— and No-Load Test of Induction Motor	26
137	Test for Copper Losses in Transformers	40
	Shunt Wound Dynamo, Critical Resistance of a	15
60		16
	- Wound Dynamo, Graphical Deduction of Total Characteristic in .	15
61	Wound Dynamo, Internal Characteristic or Curve of Mag-	
	notization of a	15
59	Wound Dynamo, Relation between Speed and E.M.F. in	14
99	- Wound Electro-Motors, Efficiency and B.H.P. of Direct	
	Current Siemens Dynamometer-Wattmeter	24: 58:

Test	No.	Page
١.	Sistanta Electro-Dynamometer ,	577
•	— H.P. Transmission Dynamometer	623
•	Low Resistance Bridge	525
	- Torsional Spring Control Voltmeter	575
	Silvertown Portable Testing Set ,	534
42	Portable Testing Set, Insulation Resistance by	105
33		
	by the	90
	- Portable Testing Set, Table showing best way to work the .	22
	Sine and other Curves of E.M.F. Waves of a Dynamo	197
99	Single-phase A.C. Electro-Motors, Measurement of Efficiency and	
	R.H.P.	269
142	- Phase A.C. Static Transformers, Efficiency by Blakesley's	
	Method of	422
140	- Phase A.O. Static Transformers, Efficiency by Double Con-	
	version of	414
139	Phase A.C. Static Transformers, Efficiency by Single Con-	
	version of	412
141	- Phase A.O. Static Transformers, Efficiency by Sumpar's	
	Method of	417
		2-424
105		299
	Slanting T Joint in Electric Light Cable	486
	Slip in an A.C. Motor, Definition and Measurement of Magnetic 28	
	Scames Motor Testing Brake	637
	Roldering Irons for Cable Jointing.	474
118		
	Induction with Position of Movable Core in	339
	Specific Gravities, Table of.	644
	- Resistances of Liquids, Table of	645
	Resistances of Metals and Alloys, Table of .	G44
65	Speed and E.M.F. at which a Dynamo truly Compounds, Deter-	1.00
70	mination of	167
53	- and E.M.F. in Direct-Current Dynamos, Relation between .	140
62	by Stroboscopic Fork, Measurement of	135
	- Frequency, and Slip by the Stroboscopic Method	262
51	— Indicators, Calibration of Voltage and Current with Brush Position on Communicator	134
88	- Cottage and Cartest with Druss Position of Continuator	239
66	of D.C. Motors, Variation of . — with E.M.F. in Alternators (at Constant Escitation),	200
00	Variation of	168
87	with Excitation on Armsture of D.C. Motors (at Constant	
•••	Voitage)	238
86	- with Voltage on Armature of D.C. Motors (at Constant	
-	Excitation)	236
	Spend Torque Cures of an Induction Motor, General Form of .	295
	Speeds of Target with Stroboscopic Fork, Table of	140
	Spherical Candle Power of an Electric Arc Lamp	70
	Candle Power of an Electric Glow Lamp	бå
27	- O.P. and Efficiency, Determination of the effect of various	
	Carbons on	70
	Spring tapping key, two-way high insulation	586
	Spring tapping key, two-way high insulation Transmission Dynamometer, Expression for amount of	
	Coiling of Spring	682
	- Transmission Dynamometer, Stroud	625
	•	

INDEX

687 ,

INDRX

Test	Na.	Page
	Springs for Thompson's Steam-Engine Indicator; Table of	58e
	Square Koots for Kelvin Balances, Tables of doubled	665
	Squares of Numbers, Table of	861
	Stand Coil Rhecatat	606
	Standard Cell, Preparation of the Clark	604
	Standard Kelvin Balance	646
	Standardization of Electrical Measuring Instruments, General	420
	remarks on the	4
91	Starting Torque and Current in D.C. Motors, Relation between	246
104	- Torque, Voltage, Current, and the Rotor Circuit Resistance	
	of an Induction Motor, Relation between	298 -
138	Static T.ansformers (from Differential Method) Determination of	
	Regulation of	410
	- Transformers (from "open" and Short Circuit Tests) De-	
	duction of Regulation of	410
	- Transformers, Fundamental Considerations relating to A.C.	400
	Stator of an A.C. Motor	270
159	Steam-Engine Generating Sets, the Commercial Efficiency of	468
	Stray Power in Dynamos and Motors	255
52	Strohoscopic Fork, Measurement of Rotational Speed by	135
	Target, the	188
141	Sumpner's Method of Measuring the Efficiency of Single-phase	
	Static Transformers	417
102	Sumpher-Weekes Method of Testing Induction Motors	288
76	Swinburne-Mordey Method of fluding Distribution of Potential	
	round Commutators	201
95	Swinbarne's Electrical Method of Measuring Efficiency and B.H.P.	
	of Electro-Motors	255
82	- Riestrical Method of Measuring Efficiency of D. C. Dynamos	219
	Switch, Change-over and Reversing	582
	— Two-way slidnig	587
	Synchronizing Rolary Converter	441
	Synchronous Alternating Current Motors	305
300	- A.C. Motor, Variation of Excitation and Armature Current	
	and the "V" with other Curves of a	305
107	- A. C. Motors, Efficiency and B.H.P., etc., of	309
	- A.C. Synchronous Motors, etc., by Lamps and "Synchroscope"	206
	Speed, Definition with Industion Motors of	260
	T	
	#1.7 #1311-15 #	440
61		-140
	Target, the Stinbuscopie	138
47	Telegraph Insulators, Measurement of the Insulation Resistance	1150
110	of faulty	123
110		319
	and Self-Induction only, Relation between	
	Coefficient of Metals and Alloys, Table of	644
	Coefficient of variation of E.M.F. in Clark's and Weston Colls	649
81	- Rise and Increase in Resistance of Magnet Coils	216
91		-646 ·
	Tasting Sets, the Evershed	686
	Thompson Steam Engine Indicator	581
	Thompson's Method of Sampling the E.M. F. of Armstere Coils .	198
	THAIR AND A WANTED AS AND MINES AND WHEN T. AS WITHING CAME A	

_		Pı,
184	Three-Ammeter Method of Measuring the Electrical Power in	
		38
		42
135		
	in	
		60
16	Three-Voltmeter Method of Calibrating a Wattmeter	
133	- Method of Measuring the Electrical Power absorbed in an	
		3
	Method of measuring power in A.C. Circuits, Proof of	
		5(
	T-Joint between two Electric Light Cables on the slant r	41
	between two Gutta-percha-ros ored Wires	4
	between two Lead-covered Electric Light Leads	41
	- between two shigle-wire Electric Light Lends , .	43
	between two 7-stranded Electric Light Leads	41
	between two 19-stranded Electric Light Leads	48
		4
91	Torque and Current of D.C. Motors, Relation between Starting .	2
163		
	Variable Rotor Circuit Registance	25
	- exerted by a Motor, Expression for .	2
	exerted by Series Motors, Expression for	2
	apard Curves of Induction Motor, General form of ,	2
	"Total Characteristic" of an Alternator (analytically)	ī
	- (haracteristic of an Alternator (graphically)	i
	- Characteristic" of Compound Dynamo (Long Shunt),	•
	Graphical deduction of the	1
	- Characteristic " of Compound Dyname (Short Shunt),	•
	Graphical deduction of the	1
	- Characteristic of Magneto Dynamo, Gtaphical deduction	•
	of the	1
	Characteristic" of Series Dynamo, Graphical deduction of	•
	the	1.
	- Characteristic " of Shunt Dynamo, Graphical deduction of the	i
	Tra er, Ewing's Magnetic Curvo	8
90	Tram and Railway Motors, B.H.P. and Efficiency of 500 Volt	۰
ΒŲ	Direct Cuttent	2
	Transformation Ratio in Induction Motors	2
139	Transformers (by Pufferential Method) Determination of Regu-	-
Tea	lation of	4
197	- (by Short Circuit Test) Copper Losses in	ì
137	Efficiency (by Blakesley a 3-dynamometer Method) of Alter-	1
142		
	nating Current	4
	Ediciency (by double conversion) of Alternating Current	4
139		4
141	- Efficiency (by Sumpner's Method) of Alternating Current - Efficiency of Multi-phase Alternating Current	4
143	Emercine of Mark-phase Alternating Current	4
139	-142 - Efficiency of Single-phase Alternating Current Static 413	-41
	(from Open and Short Circuit Tests) Deduction of Regu-	
	lation of	4
		4
	- Fundamental Considerations relating to A C Static	
126 85	— Appedance, Reactance and Self-ind, by Alternating Currents Transmission Dynamometer, Measurement of Efficiency of a	3

690

Test 1	No.				Page
	Transmission Dynamometer, Siemens !	HP.			628
	- Dynamometer, Spring .				t is
	of Power by bolts	4			633
	Trotter's Direct reading Ber Photomet	er .			689
		and Witne	•		590 481
	— Joint between Lead-covered Cabl				133
	Joint between Single Core Electri		7îre	: : :	476
	- Joint between 7-strandel Electric				479
	Joint between 19-stranged Electr				482
	- Joint botween 37-stranded Electr				483
	Two phose A.O. Circuite, heasurement		ml Powo	rin 3937	
	Two-way high insulating pring tappin	ng key			584
	ordinary simple sliding key	•			687
	47.±				
	σ				
	Units, Table showing relation between	practical	and C, G	l, S	643
	Useful numbers and constants .	•	4		645
	₹				
106	"V" Curves of Synchronous Motors,	Detomine	tion of		805
88	Voltage, Current, and Speed with Bru				000
ue	of D.C. Motors, Variation of .		. 011 055		239
	- "drop" of an Alternator with Le	and Po	wer Fac	tor .	174
	ratio of conversion in Multi-phase	o Rotaries			437
148	- ratio with secitation and speed it with Speed of Armature of D.C.	a Rotarica	, Variat	ion of 🐪	439
86	- with Speed of Armature of D.C.	Motors (4	t Const	ant Exci-	
	tation), Variation of		•		296
	Voltameter, Useful details for obtaining Volt Box for the Potentiometer	ig a good	eopper	•	14 521
11	Voltmeter calibration by comparison	with a Co	omatan	Potentio.	921
	meter	********	Dilison		23
10	- calibration by comparison with	ı a Kelv	in Cent	i-Amnere	
	Balance				22
9	calibration by comparison with a				21
8	- calibration by comparison wit	h a Blan	dard D	'Arsonyal	
-	Voltmeter		•		18
7 12	- calibration by Poggenslorff's Met - calibration of a High Tension Al	nou . Lockatine :	Coment		16 26
13	Voltageters, Complete test for various	Latinating	of Error	in Direct	
	and Alternating Current .				29
	Electrostatio	· ·		: :	562
	- Kelvin Kulticellular Electrostati	υ.			563
	- Siemens Torsional Spring Contro	l.			575
	W				
78	Waste Field of Dynamos, Determination	on of relat	iva distr	ibution of	207
117	Wattless or Idle Current and Load	Corrent.	Determi	ination of	
,	the			. 836	k 390
14	Wattmeter calibration by comparison	ı with a l	Kelvin (Composite	
	Balance	•	•		34

Test	No.						Pag
Ŋ.	Wattmeter salibration by comp and Voltmeter.	aricon	with f	Standar	մ ≰աս	aeter	
'n	calibration of a High Tensi	oz. bs	applies	tion of	Ohm's	Iaw	4
16	calibration with Alternatin	g Cari	cuts (3	Yoltme	ter Met	liui)	3
_	— Constant of a	•	•		-		3
-	Correcting Factor of a						39
	— - Slemena Dynamometer						58
	the conditions for and obje-						40
156	Wave Forms by the Duddell Osc	illo b t	ւրն ,				45
154-	 5 —— by Jodbert Contact Maker 	় ``	í.			446-	- 45
102	Weeken-Sumpner Method of test	ing 3-	late I	aductio	n Marai		28
	Weston (Cadmium) Standard Cel	LËM	/. with	Lemme	n lude u	13.4	
84	Wheatatone Bridge, Measuremen						•••
D-3	form of		T. Manne	o by and	"	HILL	8
	- Bridge, Method of Measuri			. D			٠
		ng rec	arriante		of apri	IIII	
	for the second	4	. :	•	•	•	49
	Windings, Resistance of Single s	mu ro	1 A Importe	-			25
-	"Wire-diawing" in Steam-Engi						47
	—— Games, Comparison of Daf	iorent -	_				A.

PREFACE

This work is intended to form a systematic course of instruction in the very extensive field of testing connected with pure Electrical Engineering. While much has been written, from time to time, about the more elementary branch of testing in Electrical Physics, relating in a measure to Electrical Engineering, I believe that, so far, no extensive attempt has been made to treat the more advanced and practical portions of the subject in that systematic manner which it requires.

I therefore venture to think that the present work, which not only embodies much of, if not all, the experimental work that it is usually possible to do at most colleges, but also many tests on heavier electrical machinery, together with a highly descriptive course on jointing Electric Light cables, should be eminently suitable for constituting the electrical laboratory practice in the second and third years of a complete course of instruction in Electrical Engineering, and in addition should be of considerable service to the electrical engineer in electrical works and central stations. As far as possible the tests have been arranged in the order in which they may be worked, when used as a course for students, but there are exceptions to this rule, owing to the advisability of keeping tests of a similar nature together. I have endeavoured to make the tests as complete and descriptive as possible, and applicable in the case of any college and testing room. Each test comprises—an Introduction giving the chief features, advantages, and disadvantages of the test, condensed as much as possible; the Apparatus necessary; the Observations to be carried out, in other words, a complete and carefully arranged digest of the method of carrying out the actual test, with h Diagram of Apparatus and connections represented symbolically; a Tabular Form indicating the most convenient and proper way of recording the observations; and finally, Inferences which can be drawn from the results of the test. These latter if conscientionaly worked out are calculated to cause the experimenter to "
think and reason for himself.

Following the series of tests is an Appendix, containing the Algebraical solutions of the various formulæ met with in the tests, and these the student is strongly urged not to refer to until he has tried, by all the means in his power, to solve the inference for himself.

The Appendix also contains complete descriptions and illustrations of a large amount of the apparatus which may be employed in carrying out the tests, a considerable proportion of it being such as will be found in almost every college and testing-room.

Useful constants and tables which are frequently needed in electrical engineering tests are added at the end of the book. A good deal of the apparatus illustrated has been constructed by the mechanical assistants, Mesers. John Watkinson and Herbert Addy, of the Electrical Engineering Department of the University, Leeds.

In conclusion, I wish to express my sincere thanks to my valued friend, Mr. Charles Mercer, M.A., for the very considerable amount of trouble he has taken in producing the photographs from which many of the illustrations are obtained: to Dr. John Henderson, for permission to use the tables of squares and reciprocals of numbers; to Messra. Kelvin & James White. for permission to use the tables of doubled square roots; to His Majesty's Stationery Office, for allowing me to use the tables of logarithms and anti-logarithms; to Mesers, Longmans, Green & Co., for their kindness in lending eight illustrations and a little printed matter from Practical Electrical Testing; to Mr. Herbert Addy, for the trouble he has taken in making the drawings from which the illustrations of joints, made in electric light cables, are taken, and also for reading through the proofs simultaneously with myself; and further to Messrs. Nalder Bros. & Co., Kelvin & James White, Siemens Bros. & Co., Crompton & Co., and Evershed & Vignoles, for their kindness in lending me the blocks of some of the illustrations of the very excellent apparatus and appliances made by them.

G. D. A. P.

PREFACE TO THE FOURTH EDITION

While opportunity has been taken, in previous editions, to both enlarge and improve the book, the scope of it has undergone very considerable oxtension and rearrangement in the present edition. Of some 132 extra pages of new matter, no less than 116 represent entirely new tests, including a little callificational theoretical explanatory matter to the previously existing tests, while the remainder comprise descriptive matter and tables of useful figures.

Some of the new tests are of a direct current nature and bring the direct current portion of the book more thoroughly up-to-date, but the remainder, forming by far the greater proportion of new tests, relate to alternating currents. This branch of practical work—always more difficult to understand than that of direct currents—has therefore been greatly strengthened by additional matter dealing with modern theory, laboratory and commercial tests supplemented by vector diagrams which enable the phase relations between current and pressure to be more easily understood.

Further, the greater portion of the work has been completely rearranged so as to have all tests of a like nature together, though not necessarily numbered in the order in which they should be taken. The author therefore hopes that this edition will be found to offer many advantages over previous ones, and he will welcome notification of any errors which may have escaped observation before going to press.

I would like to thank my friends who have so kindly helped me to read through the proofs of this edition simultaneously with myself; also Messrs. Evershed & Vignoles, Nalder Bros. & Co., and Elliott Bros. Ltd., for their kindness in lending mand additional blocks of illustrations of apparatus; and Messrs. The London Electric Wire Co., Smiths Ltd., for permission to reprint their Tables of Resistance Wires.

G. D. A. P.

EDITORIAL NOTE

THE DIRECTLY USEFUL TECHNICAL SERIES requires a few words by way of introduction. Technical books of the past have arranged themselves largely under two sections: the Theoretical and the Practical. 'Theoretical books have been written more for the training of college students than for the supply of information to men in practice, and have been greatly filled with descriptions of an academic character. Practical books have often sought the other extreme, emitting the scientific basis upon which all good practice is built, whether discernible or not. The present series is intended to occupy a midway position. The information, the problems, and the exercises are to be of a directly-useful character, but must at the same time be wedded to that proper amount of scientific explanation which alone will satisfy the inquiring mind. We shall thus appeal to all technical people throughout the land, either students or those in actual practice,

Electrical Engineering Testing

FROM THE DIRECTLY - USEFUL TECHNICAL SERIES

Please send for detailed List

ARITHMETIC FOR ENGINEERS INCLUDING SIMPLE ALGEBRA, MENSURATION, LOGANITHMS, GRAPHS, THE SLIDE RULE, VERNIERS AND MICROMITERS By CHARLES B. CLAPHAM

Hone, B Sc. Eng. (Lond.)

Lectures in Engineering and Alementary Mathematics at the
Unitersity of London-Holdsmith' Cell. ge Demy 8vo. 477 pages, 167 figures, and over 2,000 worked and set examples with answers

SECOND EDITION. Pince 7s. 6d. net

MATHEMATICS FOR ENGINEERS

By W. N. ROSE BSc. Eng (Lond)

Late Lecturer in Programming Mathematics at the University of London -Goldsmith Code o, Teacher of Mathematics, Horough Polytechnic Institute

The two volumes of Mathematics for Engineers form a most comprehensive and practical treathe on the subject, and will powe a valuable reference work reducating all the mathematics needed by engineers in their practice, and by students in all branches of engineering.

PART J

Demy 8vo. 510 pages, 257 figures with over 1,200 worked and set examples.

THIRD EDITION. Price 10s. 6d. net

PART II

Demy 8vo. 436 pages, 142 figures 4nd nearly 1,000 worked and set examples Price 13s. 6d. net

The Directly-Useful D.U. Technical Series

FOUNDED BY THE LATE WILFRID J. LINEHAM, B.Sc., M. Inst. C.E.

Electrical Engineering Testing

A PRACTICAL WORK

ON CONTINUOUS AND ALTERNATING CURRENTS FOR SECOND AND THIRD YEAR STUDENTS AND ENGINEERS

BY

G. D. ASPINALL PARR

M.Sc.; M.INST.E.E., A.C.G.I.

Diplomée in Physics and Electrical Engineering of the Gentral Technical College, City and Guilde of London.

Head of the Electrical Environmenty The University, Leeds,
Chairman of the North Middland Sation of the Inst. E. E.,
Enaminer in Electrical Engineering in the Universities of Leeds and New Zealand,
Th. Inical Advicer to the Mexican Government,
Associate Edvander of the Institute of Merbancal Engineers.

FOURTH EDITION
REPISED AND ENLARGED

LONDON

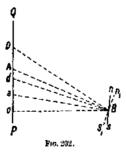
CHAPMAN AND HALL, LIMITED 11 HENRIETTA STREET, W.C. 2 1922 Primied in Gorat Britain by Richard Clay & Son, Lighted, Bungay, Burfolk,

APPENDIX

PROOFS OF FORMULAE

Deviation of the deflections of Reflecting Galvanometers from the direct proportional law.

It has been stated on p. 6 that the scale deflections of a D'Arsonval galvanometer are directly proportional to the currents producing them. Though this is not rigorously correct, it is sufficiently true for most practical purposes in the usual forms of instruments belonging to this class. For very accurate work, however, it is necessary to apply a correction, usually amounting to a small fraction of 1% for deviation from this law, and this we now proceed to indicate.



Let O be the zero of the scale PQ, presumably in the centre, though, for convenience, only one-half of the scale is shown, and let Od and OD be the scale deflections of the spot of light on PQ from zero for currents C_1 and C_2 through the galvanometer cell.

If B is the centre of the needle ns, then OB is the incident ray of light from some source at O and Bd, BD the reflected rays for

the two positions of the mirror and its attached acedle as.

By drawing the normals to the mirror in each position we get

Ba and BA respectively, and it can at once be shown that the angle dBD = 2aBA, or that the angular motion of the mirror is half that of the reflected ray,

Now since as is contained by the plane of its coil for no current and is parallel to PQ, we shall always have (for the small angular motion of as usually obtained in mirror galvanometers) --

$$C_1: C_3 = \tan \frac{1}{2} \frac{\partial Bd}{\partial B}: \tan \frac{1}{2} \frac{\partial BD}{\partial B},$$

$$\stackrel{!}{=} \tan \frac{1}{2} \frac{\partial d}{\partial B}: \tan \frac{1}{2} \frac{\partial DD}{\partial B}$$

$$= \frac{\sqrt{1 + \left(\frac{\partial d}{\partial B}\right)^2 - 1}}{\frac{\partial d}{\partial B}}: \frac{\sqrt{1 + \left(\frac{\partial D}{\partial B}\right)^2 - 1}}{\frac{\partial D}{\partial B}}$$
 (accurately),

or if Od and OD are not very different and are small, then- $C_1:C_2=Od:OD$ (approximately).

Measurement of the Internal Resistance of Secondary Cells. (Fall of Potential Method.)

Proof of Formula .-- Referring to p. 76, let E= the total E.M.F. of the cell or battery, and V the potential difference at its terminals, when sending a current A.

If then B is the internal resistance of the cell and B the resistance of the external circuit, we have by Ohm's Law-

Fall of Potential round external circuit = AR = V, in the cell itself ьна "

Hence we must have R = AR + AB = A(R + B).

But the Full of Potential in the cell itself is also = E - V, $\therefore E - V = AB$

and

$$\therefore B = \frac{E - Y}{A} \text{ ohms };$$

$$\frac{E}{V} = \frac{A(R + B)}{AR}$$

or thus

$$B = \frac{E - V}{V} R, \text{ but } AR = V, \text{ or } R = \frac{V}{A}$$

$$\therefore \ \ L = \frac{K - Y}{4} \text{ ohms.}$$

Measurement of Resistance. (Wheatstone Bridge Method.)

Proof A Formula.—Referring to Fig. 33 I., p. 82, let V_1 , V_4 and V_5 —the Potentials of the points P_t , N and T respectively; then the point Q will also be at the potential V_{2t} since when the bridge is "balanced" no deflection will occur on the galvanemeter, owing to there being no difference of potential between N and Q to cause a current to flow. Now let G_1 , G_{2t} , G_3 and G_4 be the currents passing through the resistances r_1 , r_2 , r_3 and r_4 respectively of the arms of the bridge.

Then $V_1 - V_2 = C_4 r_4 = C_4 r_4$; id $V_2 - V_3 = C_1 r_1 = C_5 r_3$;

but since on balance being obtained no current flows through the galvanometer, i. a. between the points N and Q, we get

whence by division $\begin{aligned} &C_1 = C_4 & \text{ and } & C_2 = C_{39} \\ &\frac{C_4 r_3}{C_1 r_2} = \frac{C_4 r_3}{C_1 r_1} \\ \text{or } &\frac{r_3}{r_2} = \frac{r_4}{r_1} \\ \text{and } & \therefore r_1 r_3 = r_4 r_6 \end{aligned}$

The resistance in the galvanometer and battery circuits is immaterial, so long as it is not great enough to diminish the sensitiveness of the tests; consequently it may vary without vitiating the results at all.

Measurement of Low Resistance. (Potential Difference Method.)

Solution of Inferences.—Referring to Fig. 34, p. 85, let A = current flowing through the resistances τ and R in series, and v, V = Potential Differences across their extremities respectively.

Then from Ohm's Law we have

$$A = \frac{V}{R} \Rightarrow \frac{\mathbf{v}}{\mathbf{r}}$$

but since the galvanometer resistance is high compared with

either r or R, we have its deflections d_r and d_R across these resistances respectively proportional to v and V, whence

$$d_{R_{\infty}}d_{r}$$

and \therefore the unknown resistance, assumed to be (r), is

$$\tau = \frac{d_r}{d_R} R$$
 ohms.

Assumptions.—(1) That no fluctuations of the current A have occurred in the interval of time between the observations d_R and d_r of any particular pair.

- (2) That the introduction of the galvanometer across the reeistance has not altered the P.D. at their respective terminals.
- (3) That the deflections are proportional to the currents, which is very nearly true for ordinary reflecting instruments.

Errors may arise from the warming up of the resistances to be compared, due to the passage of the current, and the consequent alteration of resistance. The current should not be strong enough to do this.

Also from the presence of thermo currents caused by the warming up of a junction of two dissimilar metals.

Lastly, from the inconstancy of the current, which can be minimized by taking readings with one of the resistances before and after that with the other, and noting the mean of the two.

Measurement of very high or Insulation Resistance. (Direct Deflection Method.)

Solution of Inferences.—Referring to p. 10!-

Let b = the internal resistance of the battery,

g = the galvanometer resistance,

 $C_R C_r$ = the currents through the galvanometer, causing deflections $d_R d_r$, when the resistances R and r are in circuit respectively and K be a constant converting these deflections to actual currents.

wrents.

Then if E is the E.M.F. of the battery we have by Ohm's Law

Then if E is the E.M.F. of the battery we have by Ohm's Lat
$$C_R = Kd_R = \frac{S_R}{S_R + g} \times \frac{E}{R + b + \frac{S_R g}{S_R + g}} = \frac{S_R E}{(R + b)(S_R + g) + gS_R}$$

Similarly
$$C_r = Kd_r \approx \frac{S_r}{S_r + g} \times \frac{E}{r + b + \frac{S_r g}{S_r + g}} = \frac{S_r E}{(r + b)(S_r + g) + gS_r}$$

whenco by division

$$\frac{d_R}{d_r} = \frac{(r+b)(S_r+g) + gS_r}{(R+b)(S_R+g) + gS_R} \times \frac{S_R}{S_r}$$

 $\frac{d_R}{d_r} = \frac{(r+b) \left(S_r + g\right) + gS_r}{(R+b) \left(S_R + g\right) + gS_R} \times \frac{S_R}{S_r}$ Now b will always be negligibly small compared with R or r.

Hence
$$\frac{d_R}{d_r} = \frac{r\left(S_r + g\right) + yS_r}{R\left(S_R + y\right) + gS_R} \times \frac{S_R}{S_r} = \frac{r\left(4 + \frac{g}{N_r}\right) + g}{R\left(1 + \frac{g}{N_r}\right) + g}$$

or
$$d_{B}\left[R\left(1+\frac{g}{N_{B}}\right)+g\right]=d_{r}\left[r\left(1+\frac{g}{N_{c}}\right)+g\right]. \quad (1)$$
 When no shunts are used S_{B} and S_{c} both = infinity and

 $d_R(R+g) = d_r(r+g)$

Lastly, if (y) is negligibly small compared with R and r, then

and

$$\therefore r = \frac{d_R}{d_r} R \dots \dots (2)$$

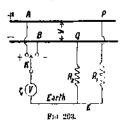
The assumption made in both formulas 1 and 2 above are that-

- (a) The E.M.F. of the testing battery remains constant throughout the tests, which is justifiable owing to its working through such high resistances,
- (b) The internal resistance of the battery is so small compared with R and r as to be quite negligible.
 - In the relation (2) above, it is assumed that—
 - (c) No shunts are used at all with the galvanouneter,
- (d) The galvanometer resistance (g) is so small compared with R and r as to be quite negligible.

Insulation Resistance of Electric Installations while working.

Solution of Inferences. -- Ict A and B be the two points of the circuit most convenient for attaching the wires to, that come from the two-way key K. Let r, = resistance of the voltmeter, and R_1R_2 = insulation resistances of the + ** and - ** sides, respectively, of the network or installation, in ohms. Then that of the whole

system, everything included, is $R = \frac{R_1 R_2}{R_1 + R_2}$. In Fig. 203, E represents the earth or nearest gas or water-pipe. If then V_1 and V_2 are the voltmeter readings when placed between the + m and - m sides of the circuit and earth, and Vthe voltage between the mains, we have



Fall of P,D, between A and E, viz.
$$V_1 = V \frac{R_1 r_s}{R_1 + r_s} \frac{R_1 r_s}{R_1 + r_s} + R_2$$

Similarly the fall of P.D. between B and E, viz. $V_2 = V \frac{R_2 v_*}{R_2 + v_*} + R_1$

Since EPA and EVA are in parallel, and the combination in series with EQB.

$$\begin{array}{c} \therefore \ V_1 + V_2 = V \frac{\left(R_1 + R_2\right) \, r_v}{\left(R_1 + R_2\right) \, r_v} + R_1 \frac{R_2}{R_2} \\ & \qquad \vdots \quad V_1 + V_2 = \frac{1}{V} \left(1 + \frac{R_1 \, R_2}{R_1 + R_2} \cdot \frac{1}{r_v}\right) \\ & \qquad R = r_v \left(\frac{V}{V_1 + V_2} - 1\right) \\ & \qquad R_2 = R \, \frac{V_1 + V_2}{V_1} = \frac{r_v \left[V - \left(V_1 + V_2\right)\right]}{V_1} \\ & \qquad R_1 = \frac{r_v \left[V - \left(V_1 + V_2\right)\right]}{V_2} \\ & \qquad \vdots \\ & \qquad \vdots \\ & \qquad \vdots \end{aligned}$$

 $\langle V_1 + V_2 \rangle$ representing the absolute sum of the two voltages, assuming they are to opposite sides of zero.

Insulation Resistance of a Storage Battery.

Solution of Inferences.—Referring to Fig. 50, p. 128 — Let P1 P2 P3 . . . be points on the battery which are partially

 $R_1 R_2 R_3$. . . be the resistances of these earths, $C_1 C_2 C_3 \ldots$ be the currents flowing from $P_1 P_2$ and $P_3 \ldots$ to earth when G is connected, K closed,

 $E_1 \, E_2 \, E_3$, , , the E.M.F.s between P and $P_1 \, P_2 \, P_3$, , , respectively.

Then if all the currents flow from battery to earth

$$\begin{array}{ll} C_1 \, R_1 - C_o \, g = E_1, & C_o \, g - C_8 \, R_8 = E_8, \\ C_2 \, R_2 - C_o \, g = E_2, & C_a \, g - C_9 \, R_0 = E_0, \\ & \text{etc.} & \text{etc.} \end{array}$$

Also

$$C_1 + C_2 + C_3 + \dots + C_n = 0.$$

$$\frac{E_1 + C_0 g}{R_1} + \frac{E_2 + C_0 g}{R_2} + \dots + \frac{C_0 g - E_0}{R_0} + \frac{C_0 g - E}{R_0} + \dots + C_0 = 0.$$

Now whon
$$C_0$$
 fulls to C_r by increasing g to $(g+r)$ we have
$$\frac{E_1+C_r(g+r)}{R_1}+\frac{E_2+C_r(g+r)}{R_2}+\ldots+\frac{C_r(g+r)-E_g}{R_g}\\+\frac{C_r(g+r)-E_g}{R_0}+\ldots+C_r=0.$$
 Hence from the difference of these two equations we have

(eight from the difference of these two equations we
$$\{C_{\theta}g - C_{r}(g+r)\}\left(\frac{1}{R_{1}} + \frac{1}{R_{2}} + \cdots\right) + C_{\theta} - C_{r} = 0,$$

$$R = \frac{C_{\theta}g - C_{r}(g+r)}{C_{r} - C_{\theta}}$$

whence

Insulation Resistance of Dynamos and Motors.

Solution of Inferences.—The proof of the formula employed in this test is precisely the same as that given on p. 494 for the insulation resistance of electric light installations. It will not therefore be repeated here.

Efficiency of Direct-Current Generators. (Hopkinson's Electrical Method.)

Solution of Inferences.-Referring to Fig. 85, p. 224, let $V_1 V_2 V_3$ be the terminal voltages of α , β and γ respectively, and A the main current through them all. Then we have-

Power developed by the generator a

, supplied by the auxiliary
$$\gamma = AV_3$$
, given to the motor $\beta = AV_2$, Hence $AV_3 = AV_2 - AV_1 = A (V_2 - V_1)$, which is the power lost in both machines together.

If V = normal working pressure of a and β when running as dynamos, ra and rs = normal resistances of their shunts.

Then $\frac{V^2}{r_a}$ and $\frac{V^2}{r_b}$. Watts wasted in their respective shunt circuits, neglecting any extra resistance such as R_1 and R_2 . Now let the total internal loss in a =that in β . Then—

Efficiency of dynamo a

$$\Sigma = \frac{\text{usoful power developed}}{\text{total power put in}} = \frac{A V_1}{\frac{1}{3}A V_8 + A V_1 + \frac{V^2}{I_8}}$$

Efficiency of motor β

$$\Sigma_{g} = \frac{\text{useful B.H.P. devoloped}}{\text{total E.H.P. put in}} = \frac{-\frac{1}{2}AV_{3} + AV_{2} + \frac{V^{2}}{r_{\theta}}}{AV_{2} + \frac{V^{2}}{r_{\theta}}}$$
$$= \frac{\frac{1}{2}A\left(V_{3} + V_{1}\right) + \frac{V^{2}}{r_{\theta}}}{AV_{2} + \frac{V^{2}}{r_{\theta}}}$$

If now we neglect the shunt losses $\frac{V^2}{v_s}$ and $\frac{V^2}{r_{\beta}}$ in comparison with the outputs of a and β , then

$$\Sigma_{a} \in \frac{2V_1}{V_1 + V_2}$$
 and $\Sigma_{b} = \frac{V_1 + V_2}{2V_3}$
 $\cdots \Sigma_{a} \Sigma_{b} \cdot \frac{V_1}{V_2}$

whonco

Lastly, if we assume that the machines are so alike that

$$\Sigma_a = \Xi_b = \Xi \text{ (say)}$$
 Then
$$\Sigma^c = \frac{V_1}{V_2} \quad \text{or } \Xi = \sqrt{\frac{V_1}{V_1}}$$

which is therefore the efficiency of either machine,

Self-Induction by the Impedence Method using Single-Phase Alternating Currents.

Bolution of Inferences .- Referring to Fig. 132, p. 360, let V. and V_{B} be the readings of the voltmeter when an alternating and direct current of the same strength A is successively passed through the self-induction whose value L is to be determined. Let n = frequency of the alternating current in \frown per sec.,

then its angular velocity $p = 2\pi n$. If R =the olume resistance of the self-inductive circuit we

have for the direct current, by Chin's Law,

$$R = \frac{V_D}{A}$$
 ohms,

and for the alternating current we have

$$\frac{V_n}{A} = \sqrt{L^2 p^2 + E^2}$$
 the impedence of the circuit,

If early by substitution
$$\frac{V_a}{A} = \sqrt{(Lp)^2 + \left(\frac{V_D}{A}\right)^2}$$

or
$$\left(\frac{V_a}{4}\right)^2 = (Lp)^2 + \left(\frac{V_h}{4}\right)^2$$

$$L^2 \mu^2 = \left(\frac{V_a}{A}\right)^2 + \left(\frac{V_B}{A}\right)^2 = \frac{1}{A^2} \left(V_a^2 + V_\mu^2\right)$$

 $L = \frac{1}{2\pi A} \sqrt{V_{\perp}^2 - V_{\parallel}^2}$ henries, and

Self-Inductions in Series and Parallel Laws of Combination.

Proof of Formula.—Suppose that we first take the arrangement represented in Fig. 135 y, p. 367, in which all the self-inductions $L_1 L_2 L_3$ and L_4 are in parallel.

Let them possess chinic resistance $R_1 R_2 R_3$ and R_4 respectively, but no matual induction,

Also let L_c and R_o be the combined or equivalent self-induction and ohmic resistance of the combined parallel circuit such that if substituted for the parallel branches the same potential difference V would exist at the terminals, causing the same current A to flow through,

If then the angular velocity of the alternating current be denoted as usual, by $p=2\pi n$ where n is the periodicity, we can apply the solution obtained by Lord Rayleigh for the impedence of parallel circuits and given in a paper by him "On Forced Harmonic Oscillations of Various Periods."—Phil. Mag., May 1886.

Thus
$$L_{\sigma} = \frac{B}{A^2 + B^2 p^2}$$
 and $R_{\sigma} = \frac{A}{A^2 + B^2 p^2}$ where $A = \mathbb{E}\left(\frac{R}{L^2 p^2 + R^2}\right)$ and $B = \mathbb{E}\left(\frac{L}{L^2 p^2 + R^2}\right)$
Hence $\frac{V}{A} = \sqrt{L_{\sigma}^2 p^2 + R_{\sigma}^2} = \sqrt{\frac{1}{A^2 + B^2 p^2}}$

Substituting the values of A and B given above we get

$$\begin{split} \frac{V}{A} &= \sqrt{L_{e}^{2}p^{2} + R_{e}^{2}} = \sqrt{\left(\mathbb{E} \frac{1}{\left(L^{2}p^{2} + R^{2}\tilde{p}^{2}\right)^{2}} \frac{1}{p^{2}} + \left(\mathbb{E} \left(f\tilde{p}p^{2} + R\tilde{p}^{2}\right)^{2}\right)^{2}} \\ &= \sqrt{\frac{1}{\left(\mathbb{E} \frac{L}{f^{2}}\right)^{2}p^{2} + \left(\mathbb{E} \frac{R}{f^{2}}\right)^{2}}} \end{split}$$

Next take the arrangement shown in Fig. 135 \$\textit{\theta}\$, in which the inductions are connected up, two in series and two in parallel.

Here, since self-inductions in series sum up like resistance in series, we have, applying the last equation for two parallel branches, that

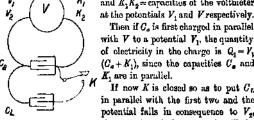
$$\begin{split} & \frac{V}{A} = \sqrt{\frac{L_a^2 p^2 + R_o^2}{L_1 + L_2}} \\ & = \sqrt{\frac{1}{\left(\frac{R_1 + R_2}{(I_1 + I_2)^2} + \frac{R_2 + R_4}{(I_2 + I_4)^2}\right)^3 + \left(\frac{L_1 + L_2}{(I_1 + I_2)^2} + \frac{L_2 + L_4}{(I_2 + I_4)^2}\right)^2} p^2} \\ & = \frac{(I_1 + I_2) \left(I_2 + I_4\right)}{\sqrt{(I_1 + L_2 + L_2 + L_4)^2 p^2 + (R_1 + R_2 + R_3 + R_4)^2}} \end{split}$$

$$\frac{\sqrt{(L_1 + L_2)^2 p^2 + (R_1 + R_3)^2} \sqrt{(L_3 + L_4)^2 p^2 + (R_3 + R_4)^2}}{\sqrt{(\Sigma L)^2 p^2 + (\Sigma R)^2}}$$

which is the combined or effective or equivalent impedence of this particular branched circuit.

Electrostatic Capacity of Electrical Cables. (Multicellular Voltmeter Method.)

Proof of Formula-Let Ca = capacity of the standard air condenser; $C_L =$ capacity of the cable, and $K_1K_2 =$ capacities of the voltmeter



with V to a potential V1, the quantity of electricity in the charge is $Q_1 = V_1$ $(C_a + K_1)$, since the capacities C_a and K_1 are in parallel. If now K is closed so as to put C_L

Then if C_{σ} is first charged in parallel

in parallel with the first two and the potential falls in consequence to V., the quantity of the charge is still the Fig. 204. samo assuming no leakage, and we have

 $Q_1 = V_2 (C_4 + C_L + K_2).$ Педсе

$$\begin{split} V_{1}\left(C_{a}+K_{1}\right) &= V_{2}\left(C_{a}+C_{L}+K_{2}\right), \\ \frac{V_{2}}{V_{1}} &= \frac{C_{a}+K_{1}}{C_{a}+C_{L}+K_{2}} \end{split}$$

and by a well-known rule in proportion we have

$$\frac{V_2}{V_1 - V_4} = \frac{C_a + K_1}{C_a + C_L + K_2 - C_a - K_1} = \frac{C_a + K_1}{C_L + K_2 - K_1}$$

$$\therefore V_2 C_L + V_2 K_2 - V_2 K_1 = V_1 C_a - V_3 C_a + V_1 K_1 - V_2 K_1.$$
Hence
$$V_1 C_1 + V_1 K_2 = C_1 (V_1 - V_2) + V_2 K_1.$$

 $V_{2}C_{L} + V_{2}K_{2} = C_{4}(V_{1} - V_{2}) + V_{1}K_{1}$ $\therefore C_{L} = \frac{C_{4}(V_{1} - V_{2}) + V_{1}K_{1} - V_{2}K_{2}}{V_{2}}$ Hence

and

or neglecting the capacity of the voltmeter in comparison with

 C_a and C_L we have $C_L = C_a \frac{V_1 - V_2}{V_a}$.

Capacity of Concentric Cables. (Standard Magneto Inductor Method.)

Proof of Formula .-- Referring to the test, p. 377, let N be the number of turns of wire on the standard inductor and F the total number of lines of magnetic force threading the gap, then the interlinking of turns and field = FN.

If now R = the total resistance in ohms of the inductor circuit, the whole quantity of electricity Q_1 producing the throw d_I is $Q_1 \propto d_I \propto \frac{NF}{R}.$

$$Q_1 \propto d_1 \propto \frac{NF}{\nu}$$
.

Again, let C = the capacity of the cable in microfarads, V = the potential difference in volts to which it is charged, then the quality of electricity Q_2 causing the throw d_a is

$$Q_2 \propto d \propto CV_1$$

and 1 interocoulomb = $\frac{10^{-1}}{10^6}$ = 10^{-7} C.G.S. units of quantity,

also I ohm

Hence

= 10° C G 8. units of resistance
$$\frac{d_1}{d_s} = \frac{FV}{10^{-7} \times 10^9 \ R \ VC} = \frac{FN}{100 \ R \ VC}$$

$$\frac{d_1}{d_s} = \frac{FV}{10^{-7} \times 10^9 \ R \ VC} = \frac{FN}{100 \ R \ VC}$$

and

$$\therefore C = \frac{FN}{100 \ RV} \frac{d\sigma}{d_I}$$
 microforads,

For the greatest accuracy we ought to have $d_I = d_{\sigma}$

Three Voltmeter Method of Measuring the "True Electrical Power" in Single-Phase Alternating Current Circuits.

Solution of Inferences.—Referring to Fig. 140, p. 382, let the Imean square value of the voltages, as given by either a hot wire or electrostatic voltmeter, be denoted by V_1 , V_1 and V_2 for the positions shown in the figure; also let (r) - the value of the non-inductive resistance QR in ohms.

Then we require the value of the mean or True Power in Watts W given to the whole circuit PR in which the whole power is absorbed; let v, v, and ve be the instantaneous values of the voltages corresponding to the $\sqrt{\max}$ square values V, V_1 and V_2 respectively at any instant (t), then $v=v_1+v_2$; also if (a) a instantaneous current in amps. flowing through PR at this same instant t, we have the instantaneous value of the power in Watts (w) given to PR at that instant as w=va;

but we also have
$$a = \frac{v_2}{r}, \quad \text{since } QR \text{ is non-inductive,}$$
 whence
$$w = va = v\frac{v_2}{r} = \frac{vv_2}{r}$$
 or
$$vv_2 = v\sigma r;$$
 now since
$$v = v_1 + v_2$$

$$v_1 = v - v_2$$
 and
$$2v_1v_2 = 2vv_2(v - v_2) = 2vv_2 - 2v_2^2.$$
 Hence by substitution
$$2v_1v_2 = 2vv_2 - 2v_2^2.$$
 but
$$v^2 = v_1^2 + 2v_1v_2 + v_2^2 \quad \text{by squaring,}$$

$$v^2 = v_1^2 + 2v\sigma - 2v_2^2 + v_2^3 \quad \text{by substitution.}$$
 Hence
$$vv = \frac{1}{2r} \left\{ v^2 - v_1^2 + v_2^2 \right\}.$$
 Integrating this equation for the period T we get
$$\int_0^T vv dt = \frac{1}{2r} \left\{ \int_0^T v^2 dt - \int_0^T v_1^2 dt + \int_0^T v_1^2 dt \right\}$$
 and finally
$$W = \frac{1}{2r} \left\{ V^2 - V_1^2 + V_2^2 \right\}.$$

Efficiency of Transformers. (Blakesley's Three Dynamometer Method.)

Solution of Inferences.—Referring to p. 423, on which will be found a formula derived by Mr. Blakesley for expressing the power given to the primary of a transformer in his method of measuring the efficiency of such an appliance, Professor Ayrton and Mr. Taylor have deduced the following general proof of this relation, which makes no assumption whatever as to the nature of the current, whether sinusoidal or otherwise, but only that there is no magnetic leakage between primary and secondary windings. This is approximately true for "closed circuit" though not for "open circuit" transformers, so that the method cannot be considered a very good one.

Let $a_1\,a_2\!=\!{\rm instantaneous}$ values of the currents and $v_1\,v_2$ these of the E.M.F.s in the primary and secondary windings having N, N_g turns respectively, and B = the mean density of lines in the core, then if $R_1 R_2 =$ ohmic resistances of the primary and secondary

we have

$$v_1 = R_1 a_1 + \frac{N_1}{10^8} \frac{dB}{d\hat{t}}.$$

But

$$\frac{N_1}{10^8} \frac{dB}{dt} = R_2 a_2$$
 since we assume no leakage,

 $\therefore \ v_1 = R_1 a_1 + \frac{N_1}{N_2} \ R_2 a_2 \ ;$ multiplying all through by a_1 we get

$$v_1 a_1 = R_1 a_1^2 + \frac{N_1}{N} R_2 a_3 a_1.$$

 $n_1a_1-R_1a_1^2+\frac{N_1}{N_2}R_2a_2a_1.$ Integrating this last equation between the limits of the period T we get

$$\frac{1}{\hat{T}} \int_{0}^{T} v_{1} a_{1} dt = \frac{R_{1}}{\hat{T}^{\prime}} \int_{0}^{T} a_{1}^{2} dt + \frac{N_{1}}{N_{2}} \frac{R_{2}}{\hat{T}^{\prime}} \int_{0}^{T} v_{1} a_{2} dt.$$

Hence if A is the split dynamometer reading we finally have

$$W_P = A_1 R_1 + \frac{N_1}{N_2} R_2 A$$

APPARATUS

Preparation of the Clark Standard Cell.

Definition of the Cell.—The cell consists of zine and mercury in a saturated solution of zine sulphate and mercurous sulphate in water, prepared with mercurous sulphate in excess, and is conveniently contained in a cylindrical glass vessel.

Preparation of Materials.—The Mercury,—To secure purity it should be first treated with acid in the usual way, and subsequently distilled in vacuum.

The Zinc.—Take a portion of a rod of pure zinc, and solder to one end a piece of copper wire. Clean the whole with glass paper, carefully removing any losse pieces of zinc. Just before making up the cell, dip the zinc into dilute sulphuric acid, wash with distilled water, and dry with a clean cloth or filter paper.

The Zine Sulphate Solution.—Propare a saturated solution of pure (re-crystallized) zine sulphate by mixing in a flask distilled water with nearly twice its weight of crystals of pure zine sulphate, and adding a little zine carbonate, in the proportion of about 2 per cent. by weight of zine sulphate crystals, to neutralize any free acid. The whole of the crystals should be dissolved with the aid of gentle heat, i. e. not greater than 30° C, and the solution filtered while still warm into a stock bottle. Crystals should form as it cools.

The Mercurous Sulphate.—Take mercurous sulphate sold as pure, which is white, and wash it thoroughly with cold distilled water by agitation in a flask; drain off the water, and repeat the process at least twice, but after the last washing, drain off as much water as possible. Mix the washed sulphate, in the proportion of about 12 per cent. by weight of ZnSO₄, crystals, with the zinc sulphate solution, adding sufficient crystals of zinc sulphate from the steek bottle to ensure saturation, and a small quantity of pure mercury. Shake them well up together to form a paste of the consistency of cream. Heat the paste sufficiently to dissolve the crystals, but not above 30°C. Keep the paste for one hour at

this temperature, agitating it from time to time, and then allow

it to cool.

Crystals of zinc sulphate should then be distinctly visible throughout the mass. If this is not the case, add more crystals from the stock bottle, and repeat the process. This method ensures the formation of a saturated solution of zinc and mercurous sulphates in water. The presence of the free mercury throughout the paste preserves the basicity of the salt, and is of the utnost importance. Contact is made with the mercury by means of a platimum wire about No. 22 B.W.G., which is prevented from making contact with the other materials of the cell by being scaled into a glass tube, the ends of the wire projecting boyond those of the tube. One cad forms the terminal; the other end, and part of the glass tube, dip into the mercury

To set up the Cell,—The cell may be conveniently set up in a small test tube of about 2 cms. in diameter and 6 or 7 cms. deep.

Place the mercury in the bottom of this tube, filling it to a depth of, say, 1.5 cms.

Cut a cork about 0.5 cm, thick to fit the tube. At one side

of the cork bore a hole through which the zine rod can pass tightly; at the other side bore another hole for the glass tube which covers the platinum. At the edge of the cork cut a nick through which the air can pass when the cork is pushed into the tube. Pass the zine rod about 1 cm. through the cork. Carefully

clean the glass tube and platinum wire, then heat the exposed end of the wire red hot, and insert it in the mercury in the test tube, taking care that the whole of the exposed platinum is covered.

Shake up the paste, and introduce it without contact with the upper part of the sides of the test tube, filling the tube above the mercury to a depth of rather more than 2 cms.

- :

Now insert the cork and zing rod, allowing the glass tube to pass through the hole in the cork made for it.

Push the cork gently down until its lower surface is nearly in contact with the liquid. The air will thus be nearly all expelled, rad the cell should be left in this condition for at least twenty-four hours before scaling, which should be done in the following way—

Molt some marine glue until it is fluid enough to pour by its own weight into the test tube above the cork, using enough to cover completely the zine and soldering. The glass tube should project above the top of the marine glue.

The cell thus set up may be mounted in any desirable way; do it so that the cell is immersed in a water-bath up to the level, say, of the upper surface of the cork. Its temperature can then be determined more accurately than is possible when the cell is in air.

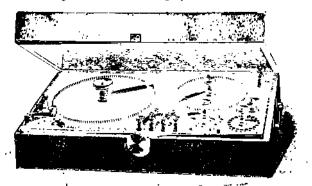
Instruments for Standard Measurements of the Highest Accuracy.

The patentionneter in general must rank as one of the first of this kind, not solely from the point of view of accuracy, but also because of the case and rapidity with which the measurements possible with it can be taken. The principle underlying its use is contained in the Clark-Poggendorff method of comparing E.M.F.s, and an elementary application of this principle in Poggendorff's method of calibrating a voltmeter, a dotailed description of which will be found in the author's work entitled Practical Electrical Testing for first and second year students. It may, however, here be remarked that when using the potentiometer for measuring current, resistance, and high voltages, the principle, as is well known, consists in reducing any of the three electrical quantities which are to be measured, to the form of electrical pressure, or E.M.F., so that it can be compared by means of a potentiometer with a standard pressure such as that of the Clark cell.

The N.C.S. Potentiometer.

This is a somewhat new type of potentiometer, in which there is no slide wire to get injured or deteriorate with time. It works entirely by means of adjusted resistances of perfectly definite values, the ends of which are permanently attached to circular rows of contact studs.

Fig. 205 shows a general view of the potentiometer in its containing case with the lid slightly raised. The internal



Fra 205.

arrangements and connections are seen in the symbolical diagram, Fig. 206, with reference to which the working of the instrument will be understood more clearly. The two diagrams exactly correspond with one another so far as the relative positions of the various parts are concerned.

A secondary battery is joined to the two terminals F, and sends a current through the two dials C and D in series and then through adjusting resistances K and H. The C dial has 150 exactly equal coils in it, numbered from 0 to 150. The D dial has 100 equal coils in it, the whole dial being exactly equal to the one coil in C. The two together are therefore

equivalent to a slide wire with 15,000 fixed contacts at equal distances. The dial K contains nineteen equal small wire resistances, and H is a carbon resistance for fine adjustment of the current, so that working with one secondary cell, the potentiometer can be set to read volts direct with a Clark cell.

A standard cell of known E.M.F. is joined up to A + and A -.

and the switch L is put over to A.

Any convenient galvanometer, the most convenient form being a D'Arsonyal, is joined up to the galvanometer terminals.

a D'Arsonval, is joined up to the galvanometer terminals.

Say the voltage of the standard cell, at the temperature used, is 1 4412; the arm of the C dial is then set to 144, and that of the D dial to 12.

The galvanometer key is then depressed on to its first step.

(taking care that the catch is underneath so that it cannot go

right down) and the outside resistance K is adjusted till—with the switch on one stop—the deflection is one way, and, with it on the next, in the opposite direction. The head H is then turned until an exact balance is obtained. A slight pressure should be put on the head H when turning it; it may not be found necessary to use H at all the next step.

Push aside the catch on the galvanemeter key and depressfully. This cuts out a $\frac{1}{2}$ megohin which was previously in circuit to protect the cell.

An exact balance can now be obtained by further adjustment H or possible K

of H or possibly K.

The instrument is now set so that each division on G is equal

to 01 of a volt, and each division on D is equal to 4001 volt.

Any low E.M.F. to be measured is joined to BB terminals and the switch L set to B; for example, a Leclanché coil or the

terminals of a low resistance for current measurement.

The galvanometer key is then again fully depressed and a

balance obtained by moving C and D.

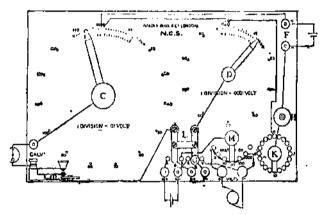
The E.M.F. between B and B is then read direct on the two dials; for example, if the reading on C is 83 and that on D is 67, the volts between B and B is 8367. Any volts higher than

1.6 have to be measured on the terminals marked voirs+ and —, and with the switch L turned to V. The switch M is taen turned to any convenient multiplying power, 3, 10, 30, etc., and the readings obtained from C and D (when the balance is

obtained as before) have to be multiplied by this multiplying power; for example, if C is 103 and D 26, and M is standing at 30, the volts on the terminals are 1.0326×30 or say 30.98.

The resistances in *H* and *K* are arranged so that any voltage up to 3 volts can be used at *F*, thus allowing either a secondary cell or two large Loclanchés to be used; it is well to leave the battery joined up to the instrument for some ten minutes or so, so as to steady down before beginning work.

A set of coils are required to potentiometer down high voltages smounting to 300 so as to bring them within range of the dials.



Fra. 206.

The three-way switch L according to its position inserts the known fraction of the high voltage, the standard cell, or any third unknown E.M.F. in circuit with the instrument.

The following points should be noted-

When using a standard cell, get a balance with the catch under the key before removing the catch.

Be careful to join up any cells, etc., to their right terminals and not + to -.

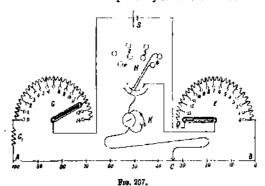
Do not serse the head H down too tight. It draws up a red which compresses a curbon resistance; there is plenty of runge to cover the difference between two stops K without squeezing it at all tight.

Press head H down when turning; it keeps the resistance stendier.

The total resistance in the M dial is 100,000 ohms; not more than 200 volts should be applied to votate terminals for any length of time. For higher values a known resistance can be added outside and allowed for.

Crompton's Potentiometer.

This potentiometer is shown diagrammatically in Fig. 207. It consists of a wire AB stretched over a scale and through which a constant current is maintained from one or more secondary cells of sufficient size to keep it fairly constant for three or four



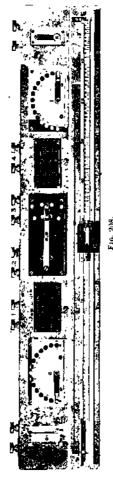
days' working. A variable resistance G and rheestat G_1 is introduced in series with the cell and wire, arranged so as to adjust this current to give a certain difference of potential at the two ends of the wire. The circuit which includes the E.M.F. to be measured is connected to one end D of the effective potentiometer wire, and through a galvanometer to a sliding saddle G, which carries a knife edge to make contact on the wire AB at any desired point of its length. This circuit is so coupled

up that the E.M.F. to be measured is opposed to the E.M.F. in

the portion of the slide wire BC, in order that the position of C on the slide wire can be adjusted until the two E.M.F.s balance one another so that no current passes through the galvanometer. In order to compare the E.M.F. to be measured with the standard E.M.F., a Clark cell is put in in circuit with the galvanometer, and the position of the slide C is noted when the above-mentioned balance has been obtained. The electrical pressure or E.M.F. required to be compared is then substituted for the Clark cell, and a similar balance found by adjusting the slider C a second time. Then the comparison between the two E.M.F.s can be made by comparing the respective lengths of the slide wire included between the points B and C in the first and second case. By dividing the slide wire AB into a suitable number of parts, and adjusting the variable resistance until the galvanometer comes to zero when the Clark cell is in circuit and

the contact C is at a point on the scale corresponding to the

temperature value of the Clark cell, say 1.434 at 15 C., the instrument becomes direct reading in volts or fractions of volts. Dr. Floming in the year 1883 first called attention to the advantages of this system of measuring, and since that time the system has been steadily developed, and refinements have been introduced. As the following description will apply to instruments such as are suitable for a municipal standardizing laboratory, it is here necessary to specify what are the requirements and limits of accuracy within which these instruments may be reasonably expected to measure. First comes the verification of voltmeters. This is of importance on account of the disputes that are likely to arise as to the pressure supplied from electric-lighting stations. Voltmeters for standard pressures of 150 to 200 and 220 volts are principally used for noting the pressures in the consumers' houses, and for such cases it is desirable that their readings at about the standard pressure should be verified to one-tenth of a volt or within one part in 1000. Next it should be possible to verify and certify the constant of the various kinds of meters by which the electrical supply is measured to the consumers. They also ought to be verified to one part in 1000. Next comes the verification of ordinary ammeters, or current instruments used for trade



purposes to about the same degree of accuracy. In both these last cases the range through which instruments would have to be compared is very considerable; for instance, the instruments sent for verification may be those used for tosting electric lamps or for telegraphic purposes, measuring currents of one milliampere, up to those used for motal-lurgical or electrolytic purposes up to 5000 ampores or more.

The correct comparison of resistance standards as well as the correctness of the ratios of resistance

ance standards as well as the correctness of the ratios of resistance boxes ought to be capable of verification to one part in 10,000. In the comparison of resistances must be included the testing of the conductivity of various metals, and the insulation resistance of various insulating materials.

In the first form of instrument proposed by Dr. Fleming, the potentiometer wire was made of an alloy of platino-iridium four metres long, and had a resistance of about 23 ohnos. The wire was divided into two parts and stretched over a scale; the whole of the wire, being required for measuring purposes, had to be carefully calibrated, that is

its entire length. This was a very tedious and expensive process. It was found very difficult, if not impossible, to obtain wire as it finally left the drawplate, which was suffi-

to say, its electrical resistance made equal per unit length throughout ciently homogeneous to be used without further adjustment. In most cases the whole of the wire had to be carefully scraped or rubbad until the required equality of resistance was obtained. Such a wire was very valuable, and if it was broken or accidentally melted, its loss was a serious matter.

In a later form of instrument (Fig. 208) Messra Crompton have abandoned the use of this expensive material, and at the same time have arranged so that only one-fifteenth part of the wire AB is stretched over the scale and subject to the wear of working. AB in the drawing shows this portion of the wire 25 in. long, strotched over a scale divided into 1000 parts: therefore each division on the scale being one-fortieth of an inch, represents one fifteen-thousandth of the pressure at the two ends of the wire; in other words, if the instrument being standardized to 1.5 volts at the terminals of its wire, each of the smallest divisions of the scale represents $\frac{1.5}{15.000}$ or one tenthousandth part of the volt. The resistance of this wire is usually about 2 ohms, and the remaining wire is divided into fourteen coils, each of about 2 ohms, so that the resistance of the whole is 30 ohms. These coils are paked spirals, the terminals of which are fixed to the underside of the fourteen contact blocks shown at E. The swinging area shown can make contact with any one of these blocks. It is an easy matter to adjust these fourteen coils when the instrument is first made so that their resistance will accurately equal one another, and the resistance of the working wire AB can thou be adjusted by slightly stretching it until it is also exactly equal to any of them. As the fourteen coils are protected they never need further adjustment, but if in the course of time the exposed portion of the wire AB becomes worn or is in any way damaged, a new piece of wire can be substituted in a few minutes and stretched by means of the stretching screw shown at F_i until its resistance over the parties from 0 to 100 exactly balances that of any one of the fourteen coils. C is the sliding saddle carrying the contact. This consists of an ebonite box arranged to slids smoothly on the scale. It is provided with a knife-edge spring contact so that the contact may be made with a regular pressure which is independent of the pressure of the hand of the user; it also has a micrometer adjustment for

accurate work. The semi-circular switch G and the cylindrical rheoslat G_1 shown to the left, which latter gives a graduation of resistance, form part of the variable resistances above described, and which are required to reduce the difference of potential between the terminals of the wire from that of the secondary cell 2 volts to any desired value. The value that has been chosen in this instrument is 15 volts. The instrument is provided with four pairs of terminals, 1, 2, 3, 4. A Clark cell can be put on to one of these, and any three other electrical pressures to be measured can be connected on to the others. The switching arrangement H shown in the centre brings the galvanometer into series circuit with any one of these pairs of terminals. The contact key K shown to the extreme right is used for short-circuiting the galvanometer.

Whenever it is required to measure an electrical pressure greater than that on the terminals of the potentiometer, that is to say, in this case, greater than 1.5 volts, the pressure to be measured is applied to certain terminals of a resistance box, and the terminals of the potentiometer are connected to other terminals on this box, which include between them a resistance which is an even part, say, one tenth, one lundredth, or one thousandth of the entire resistance of the box.

When, however, the potentiometer is employed for measuring currents, this is done by measuring the difference of pressure at two points on standard resistances which, in order to make the instrument direct-reading, must be either 1 ohm, one-tenth, one-hundredth, or one-thousandth and so on. As those low resistances have often to carry very high currents, they have to be designed so that they do not heat to a sufficient extent to introduce errors. A description of a few different forms of them will be found on p. 604.

METHOD OF "SETTING POTENTIONETER" BY STANDARD CRIZA

One secondary cell being connected direct to the extreme left-hand pair of terminals, the galvanomater to those on the extreme right and a standard Chark cell to terminals IV suppose. Note the temperature of the Clark cell on its own thermometer, and from the table showing its E.M.F. for different temperatures

affixed to the instrument or by calculation, using the formula on p. 17, or table p. 643, obtain its present E.M.F. corresponding to its present temperature. For example, suppose this to be 15°C., then the E.M.F. = 1.4340 volts.

Noxt place the double switch H on stude 4, the lever on stude 14 of E, and the slider key C at 340 on the scale, then pressing this latter, adjust the resistance G and rheostat G_1 so that the galvanometer comes back to the zero, at which it was originally set. Now every one of the scale divisions will be equal to one tenthousandth of a volt, and the potentiometer is thus "set." To use the instrument for voltage measurements H is turned to the unknown E.M.F., while G and G_1 remain untouched, only E and C now being varied to obtain balance with the unknown E.M.F. in circuit with the galvanometer.

Precautions.—A high resistance, such as 10,000 ohms, should always be connected up in series with the standard cell before placing this across the terminals of the potentiometer, but when balance in the "setting" is practically obtained, the resistance can be cut out of circuit to make the balance as sensitive as possible. By doing this the cell will not be able to send any but an extremely small current when the balance is far from perfect, and only under such conditions of use can the cell be relied on as an accurate and constant standard of E.M.F. of the value set forth in the table above mentioned.

In taking a series of readings with a potentiometer, care should be taken, at intervals, to see that the "setting" with the Clark cell remains constant, and if it doesn't, to adjust so that it is.

Sources of Error.—The current from the secondary or "Working ost" through the stretched wire and resistances Eulering, owing to the E.M.F. of this cell varying. To prevent this it is advisable not to use a newly-charged cell, the E.M.F. of such being liable to frequent alteration, but to use one amply large enough, that has already been 1 discharged. An axtremely constant E.M.F. and current will then be obtained.

Again, a further error will be introduced by the stretched wire not being uniform, and great pains should be taken to ensure that it is uniform. This may be proved by calibrating it carefully in the manner employed in thus testing a metre bridge wire, a full description of which is given in the author's work on Practical Electrical Testing; or by sending a perfectly steady and constant current through the wire and measuring the fall of potential down equal lengths throughout the scale.

Still another error may be caused by leakage causing the galvanometer to deflect when an accurate balance has been obtained. To avoid this, the insulating of the various pieces of apparatus should be attended to.

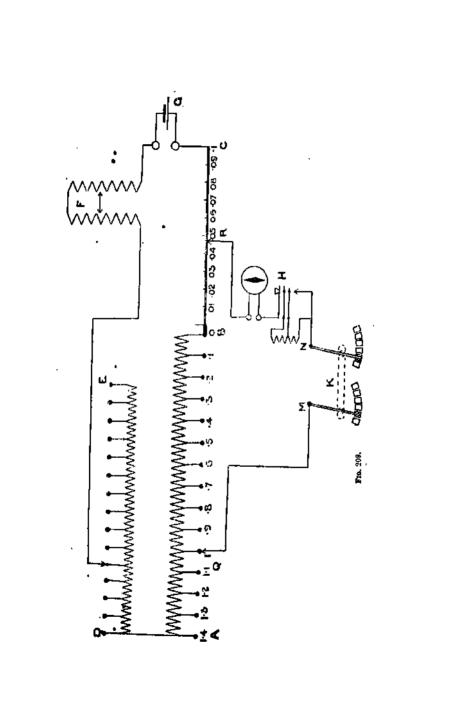
The above form of potentiometer has been much improved by

The above form of potentiometer has been much improved by the makers, and that made at the present time differs from the above in several constructional details. These, together with the appearance and connections of the latest type of instrument, will be easily understood from the following description by the makers.

The construction of the potentiometer itself is shown diagrammatically in Fig. 209. The calibrated wire is arranged in fourteen coils, called potentiometer coils, lottered AB, and a straight section BC, called the scale wire, the resistances of the several coils and of the straight section being equal. One sliding contact Q moves over the terminals of the fourteen woils, and another R along the straight wire. The reading of the instrument in the position shown is 1.046. The pairs of points whose potential differences are to be compared are connected to the

potential differences are to be compared are connected to the blocks of the double-pole switch K, whose levers, MN, connect them, one pair at a time, to the sliding contacts QR through the galvanometer. The galvanometer key H is arranged to complete the circuit through two resistances, which are short-circuited in succession as the key is depressed. The current required is derived from a small secondary battery G. An adjustable resistance, consisting of a set of coils DE, and a continuous rheostat E is placed in the circuit. By adjusting these the resistance of the circuit and the current passing through it from the storage cell, and consequently the fall of potential along the scale wire can be continuously altered, and the operator is able to obtain a

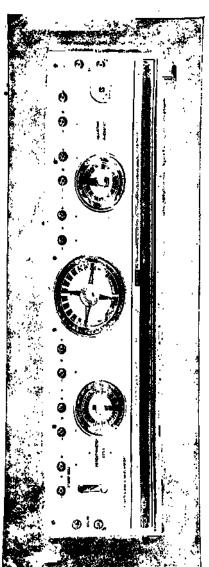
cell, and consequently the fall of potential along the scale wire can be continuously altered, and the operator is able to obtain a galvanometer balance against a standard cell when the reading of the sliders is that of the known E.M.F. of the cell at its actual temperature. If, for example, the temperature of the cell be 15°, so that its E.M.F. is 1434 volts, the sliders may be set to that reading, and the galvanometer brought to zero by



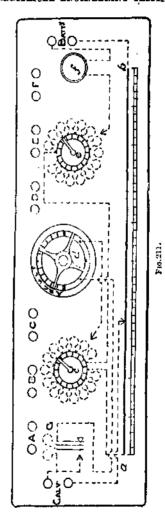
adjusting the resistance DE and the rheestat F. When this has been done the scale readings at all points are direct readings in volts.

A view of the potentiometer is given in Fig. 210, and a diagram of its internal connections in Fig. 211. Here ab is the scale wire; c the set of equal potentiometer coils in series with it; d is the double-pole switch connecting the six pairs of terminals ABCDEF in succession to the slide contacts; c f are the resistance coils and rheostat respectively, and G is the galvanometer key. All the moving contacts are under glass, and the coils and the scale wire are inside the box. The box itself is completely closed, but the inside can be inspected by removing a sliding bottom. Nearly all the measurements made, involve the use of a standard cell, and one pair of terminals, the pair A, is assigned to its connections to save confusion in working. Fuses of fine wire are inserted at all terminals except those for the galvanometer to save the instrument coils in the case of an accidental connection to a source of high pressure.

Two scales are ongraved for slide wire readings. One is a series of even divisions from 0 to 105, the resistance of the scale wire between 0 and 100 being the same as that of each potentiometer coil. It has been found convenient to be able to take readings a little boyond the 100 mark without having to move the potentiometer coil switch, and the scale is extended to 105 to admit of this. The other scale gives the values of the Clark cell at different temperatures, and is used in the following way:-The potentiometer coil switch is set to 14, and the slide to the temperature of the Clark cell taken from the thermometer attached to it. The potentiometer reading is then the correct value in volts of the Clark cell at that temperature. By adjustment of the rhoostat the galvanometer is balanced, and when this has been done the current in the potentiometer wire is such that readings at all points give correct values in volts, and the instrument is a direct-reading. voltmeter. Its maximum range is then 1.5 volts, resuling in thousandths of a volt, and by inspection to ten thousandths.



Pag. 210,



Potentiometer Volt Box.

This is a simple and most convenient piece of apparatus by means of which a known definite fraction of any voltage can be easily and quickly obtained. Hence such an instrument can be employed with a potentiometer for the measurement of high voltages, enabling the small requisite voltage to be taken off and used for measurement in the potentiometer. Fig. 212 shows a general view and Fig. 213 (p. 523) a plan of the internal connections of a variable volt box designed by the author for use with a Crompton potentioneter. It consists of two sets of resistance coils, each set having its own separate semi-circular row of contact study over which the spring contact levers work and make contact. Two pairs of terminals are provided, the high E.M.F. being directly connected to those marked M, which are Larger terminals than those marked B to distinguish them and avoid mistakes, B is the side at which the known fraction of the total P.D. is obtained; and of course go to the potentiometer direct. With the levers as shown, Fig. 213, $\frac{100}{9299+100}$ or $\frac{100}{100}$ th of the total P.D. across M will be taken from B.

Low Resistance Measurer.

The following instrument affords a simple and convenient means of measuring very low resistances, such as are met with in the armatures of large dynamos, motors, and electric light mains. These cannot be obtained by an ordinary Wheatstone Bridge, owing to the difficulty of making, and the resistance introduced by, the contacts, and other reasons which go to vitiate and make the results worthless (see Fig. 311).

The working of the instrument is as follows—The resistance to be measured is joined in series with a battery and the slide wire. One coil of a differential galvanometer is joined by two leads to the two ands of the resistance to be measured, and the other coil across more or less of the slide wire. The wire is divided into 1000 parts, and the whole is so arranged that the fall of potential over the whole wire, through the one galvanometer circuit, exactly balances that over γ_0 th ohm in the other.

The readings are then proportional throughout the scale. By



Fig 212.

shifting two plags the values may be multiplied by 5 or divided by 2, thus making the top read $\frac{1}{2}$ or $\frac{1}{3}$ of an ohm.

Directions for use.—Place the instrument on a fairly level table or bonch.

Free the galvanouncter needle by turning the screw at the back.

Turn the galvanometer on its shank till the needle points to zero.

Join the large terminals of the instrument in series with the resistance to be measured, and a cell capable of giving, say, 5 amperes; introducing somewhere in the circuit a resistance, to bring the current down to about 5 amperes.

Any odd bit of iron or German silver or other wire will do. A piece of G.S. suitable for use with a two-volt cell is sent with the instrument.

Join the long leads on to the small pair of terminals,

Depress the key on the contact arm to touch the wire; close the circuit switch, and the direction of the deflection.

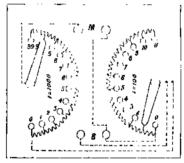


Fig. 213.

Press the two contact spears at the ends of the long leads on to the two points between which the resistance is to be measured the contact arm being up. Again close the circuit switch and note direction of deflection. If in same direction as before, reverse the two contact spears.

Then, keeping the spears pressed on the resistance to be measured, depress the key on the contact arm.

If the deflection reverses it shows that the full of potential over R (the unknown) is less than that over the wire, and the arm must be moved back towards the zero and until the galvanometer needle points to zero.

The arrow on the contact arm then points to the resistance on

the scale direct in ten-thousandths of an ohm, thus a reading of 517 is $\frac{151750}{15120}$ or 0517.

When the plugs are in 2 and 3 the instrument reads as above described. When in 1 and 2 the reads must be multiplied by 5, thus a read of $274 = 0274 \times 5 = 1370$ chm. When in 1 and 3 the reads must be divided by 2, thus $98 = 0098 \div 2 = 0049$ chm.

The spears should make fair metallic contact, but nothing more is necessary.

The galvanometer turns on its pillar, and can thus be set to zero. It should be set to zero with the current switch closed,

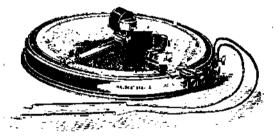


Fig. 211

but without the contact arm being pressed or the spears in contact. This avoids all disturbances from the heavy current leads

The contacts in the current leads do not need any care, their resistance, even if variable, does not affect the result.

Approximate Tests for very Low Resistances.

In armatures it is sometimes desirable to test each bar separately, to see that they are all the same, but if tested as above the reading would be so very small that there would be no certainty. A comparison of the bars can be taken by putting a shunt of any

convenient size, say 6" of No. 8 platinoid, across the heavy terminals T at the end of the slide iron; using a larger current and working as before. The results will be of course only comparative, but if the shant is firmly fixed, the readings will be quite sufficiently accurate for practical purposes. In the same way any two very low resistances can be compared by putting the two in series with the instrument and then transferring the point contacts from one to the other.

Siemens Low Resistance Bridge.

Instructions for use.—Connect up as shown in Fig. 215, which is a symbolical representation of the bridge and its connections, the general view being shown in Fig. 216.

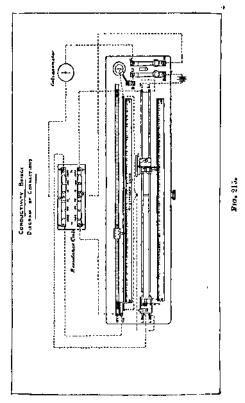
In each of the arms of the branch box marked x, unplug equal resistances and also on the \(\times\) side, the resistances being chosen according to the magnitude of the resistance to be measured.

The slide wire resistance is carefully calibrated and is compensated-for all changes of the air temperature so that 0 to 100 = 0.01 standard ohm. (At any time should the wire require cleaning, only changes leather should be used for the purpose.)

The contact slide vices, etc., are arranged for testing conductivity, but any other resistance may be tested on jointing it by four connection leads to L1, Ly and L2, Lz; L1 and L2 being the "current connections" and Ly and Lz the "potential connections," it must be remembered that any excessive resistance in the leads from the potential contacts to the branch box would increase the value of the branches and should be allowed for; they should therefore be as low as conveniently possible. The battery used should be one of low internal resistance; the galvanometer serves to indicate that there is a current flowing in the circuit.

Resistance Test.—The left-hand vice, otc., being clamped at zero, insert the specimen and clamp it at both ends; the length corresponding to the resistance measured will be given by the pointer on the meter scale, and is the distance between the two knife edges or "potential contacts." Alter the position of the sliding roller contact on the resistance wire until after closing

the battery circuit by means of the key B, and then pressing key M, no motion of the galvanometer needle is observed; the



position of the roller contact being then read off, will give the resistance on the slide wire (S).

Then the resistance of the specimen is X = S. $\frac{\times}{+}$ chma,



Example.—If the two tens be unplugged on the × side and the two thousands on the ÷ side and S = 45.5, then

 $X = \frac{45.6}{10.0} \times \frac{10}{10.06} \times 0.01 = 0.0000455$ standard ohm.

Conductivity Test of Copper Wire — For determining the conductivity of copper *wire, the wire where it will come in contact with the vices and knife edges must be cleaned from all evide. Then insert the end in the left-hand vice and clamp it. The right hand vice must now be

set by the pointer opposite the temperature of the specimen, as shown by the small scale, which is graduated from 45° to 75° F. The distance between the kuife edges when the pointer is opposite 60° F. is 816.06 m.m., and the scale is calculated

pensates for the difference of resistance due to temperature of the copper. Proceed as before to measure the resistance (A), taking note of the exact length

so that the difference in length com-

in millimetres as shown by the metre scale. Then cut off by means of the knives and ascertain its weight in grammes, and by simple proportion determine the weight of 816-06 m.m. (W). The resistance of a pure copper wire 816-06 m.m. long weighing 1 gramme is 0.1 standard dum @ 60° F.

Then the conductivity per cent, of pure copper is

 $\frac{0.1}{\vec{X} \times \vec{W}} \times 100.$

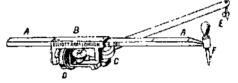
Example -

l	Length ent off 100 auto	Weight in grammer 14-63	Weight of k16 ob m in 14-76	Resistance X 0 00000.	Value of X × W 0:1027.	conductivity 97 88.
		•				

Amsler's Planimeter.

If any figure on paper is measured in the ordinary way with compass and rule, the figure is first divided into triangles the area of which can be calculated, and the sum of their areas will give the area of the figure.

This method was shortened very much in 1827 by Mr. Oppen-koffer, a Swiss engineer, who invented an instrument called the "Planimeter," which measured the area of plain surfaces by following the outlines of the figure with a pointed tracer, which, being connected with a dial-plate, showed the area of the figure. This instrument soon came into general use, although somewhat awkward and expensive.



Fra. 217.

In 1849 an improvement was made by Mr. Welty, another Swiss engineer, which was still rather clumsy. No further improvement was made till 1854, when Mr. J. Amsler, Professor of Mathematics at Schaffhausen, introduced the Planimeter which is now in use; the construction is simple, the instrument can be carried about without fear of damage. One experiment showed that an area which after dividing it into triangles took nearly three hours, was done by Amsler's Planimeter in about two or three minutes.

INSTRUCTIONS FOR WORKING THE PLANIMETER.

(1) Before working with the instrument, adjust the screw centres upon which the index roller D revolves, so that the roller works freely, and does not touch the vernier. The same care must also be taken with the centre pin C. It is good to grease

the screw centres now and then, so that they work easily. Care should be taken to prevent the tube B, the tracer F, and the point E from being bent, and also to see that the barrel D is kept uninjured.

- (2) To find the area of any figure, set the roller D and the counting which G to zero; the square rod A must be pushed into the tube B, and the line on A marked 1 sq. dem., or 0.1 sq. ft. etc., must come even with the small line on the bovelled part of the tube B; when this is done, place the instrument on the paper, and see that the roller D, the tracing point E, and the needle point E touch the paper. Press the point E slightly into the paper, and put the small German silver weight on the hole over the point E; the instrument is then ready for work.
- (3) Take any point P on the outline of the figure about to be measured, set the tracing point F to that point, and when it is marked, read off the index roller D and counting wheel G. For example, suppose the counting wheel G shows 2, the roller D 91, and the vernier 5, the number will be 2915. Follow the outline of the figure with the point F as accurately as possible to the right, until you come to the starting-point. Straight lines can be followed along a ruler; then read off the numbers on wheel and roller; say it is the second time 476-7.
- (4) When these two numbers are obtained, there are two cases to be observed....
- (1st) If the point E is outside the figure, subtract the first reading 291'5 from the second 476.7, the remainder is 185'2, which shows that the area contains 185'2 units. Of course the units depend entirely on the regulation of the bar A; if they are 0.1 sq. ft. we have $185.2 \times 0.1 = 18.52$ sq. feet, as the area of the figure measured on the paper.

The rule therefore is, when the point K is outside, multiply the difference of the two readings by the number on the bar to the right of the corresponding division.

' (2nd) When the point E is inside the figure, before making the subtraction, the number engraved on the top of har A, above the corresponding line of division, must be added to the second reading. In this instance, suppose the number on top of bar A is 20.985, the second reading is 4.767, the calculation would be as under—

2nd reading = 4.767

Number over 0.1 sq. ft. = 20.985

25.752

Deduct 1st reading = 2.915

Remainder 22.837

The area is therefore 22.837 units or $22.837 \times 0.1 = 2.2837$ square feet. It is of no consequence whether the roller is inside or outside the figure, provided it is on the same level.

(5) In measuring large figures, it may sometimes happen that the wheel G goes through one or two or more entire revolutions. If such is the case, 10,000 or 20,000, etc., must be added to the difference of the two realings before multiplication.

There is another form of planimeter which measures surfaces in square inches only; it is more simple than the other in construction, and can be worked with the above directions, always bearing in mind that the result is shown on the counting wheels in square inches and not as in the other instrument in 0.1 square decimetres, or 0.1 square feet, etc.

Amsler's Planimeter for Determining the Mean Pressure in an Indicator Diagram.

By the use of this instrument a great saving of time is effected in calculating large numbers of indicator diagrams, and the results obtained are more accurate than by any other method.

DIRECTIONS FOR USING THE PLANIMETER.

The diagram is carefully pinned to a perfectly flat board. The points 00 of the planimeter are adjusted so that the distance between them is equal to the length of the diagram projected on to the atmospheric line. The instrument is then placed upon the heard, the point b being brought into agreement with any fixed point of the diagram, while the weighted point c is placed in any convenient position outside the diagram. The point b is then passed once round along the lines of the diagram. The indication

on the wheel P and disc S, when the point b has again reached the starting-point, divided by 40 gives the mean height of the diagram a inches. Supposing, for instance, that the wheel P was adjusted to stand at zero before using the instrument, and that, after tracing the diagram, the disc S—which advances by one figure for every ten revolutions of the wheel P—stands between 1 and 2, while the wheel P indicates 21.2, a vernier being provided for reading the last figure, then the resulting number is 121.2, and this divided by 40 gives 3.03, which represents the mean height of the diagram in inches. Now, supposing that the diagram was taken by means of a No. 7 Richards Indicator Spring with a scale of 32 lbs. to the inch, then the mean pressure amounts to 3.03 \times 32 \approx 96.96 lbs. per square inch.

In practice the calculation is somewhat simplified, as the springs used are mostly of such scaler that instead of dividing by 40 and multiplying by the vertical scale, the mean pressure may be obtained by simply multiplying by a factor corresponding to the scales used.

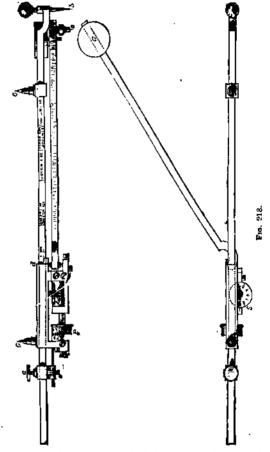
In order to secure accurate results, the instrument must be carefully eleaned before being used, and the board must be perfectly flat.

Thomps n's Indicator.

The chief distinguishing feature of this Indicator consists in a novel parallel motion which is preferable to the motion employed in the Richards Indicator on account of its greater lightness and rigidity. The irregularities in the diagram due to the inertia of the moving parts are consequently greatly reduced, and a figure is obtained which forms the nearest possible approximation to the correct diagram. The parallel motion is carefully designed to ensure that the pencil point describes a straight line, and that the motion of the pencil point is precisely proportional to the displacement of the indicator piston throughout the stroke.

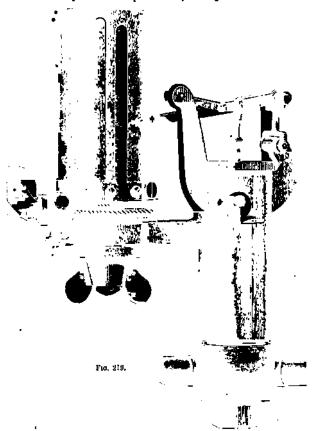
Owing to its general efficiency, this indicator is also particularly applicable for high spends, and it has been successfully employed at a speed of 400 revolutions per minute.

The piston is rigidly connected with the piston rod, which is guided in the cylinder cover, and in this way a perfect guide is obtained for the piston. The tension of the spring in the drum



can be varied to suit the speed of the engine by loosening the

nut on the top of the drum spindle and by turning the disc hold-



ing the spring until the required tension is obtained, the nut being then again screwed home.

TABLE VIII.

* LIST OF SPRINGS FOR THOMPSON'S INDICATOR."

Sizes, No	0 1	2	ĸ	4	5	ď	7	B	ø	10	ш	19
For resource from [Libs. per] so to to per squach so to the per squach	-16 -15 8 13	- J's 18	-15 30	-15 40	-15 50	-15 (8	-15 70	-15 95	-15 120	-15 150	-15 180	15 200
equals inch	3 3	115	114	20	4	10	3,1	1,0	18	νħ	74	4

Small Thompson Indicator.

This indicator is specially adapted for indicating high-speed steam engines, gas engines, etc., and will give correct diagrams at all ongine speeds occurring in practice without the necessity of taking special precautions, and has the further advantage of being very portable. It is, therefore, emmontly suited to the requirements of the engineer or engineering student. The apparent disadvantage of a somewhat smaller diagram obtained from this indicator at slow speeds is more than componsated for by increased accuracy.

Type IX.

List of Springs for Thompson's Small Indicator.

				—			-	_		-		_
Sizes, No	1	2 3	F 3	ij.	7	8 9	10	11	,12	11	14	15
I	-	1 - ()	- -	-1—	1·-					-1	_	
Fin Pressures from { Lbs per } up to { sq lach }	-25	-15-15	-15-1	5-15	1-15	-15-15	-15	-15	0	0	0	0
I արերիայիության	ð	351.90	.10 4	100	.0	SO LON	1.15	150	200	:50	300	375
Scale; 1 lb. per ag men repaire . meh	١.	. .	l . I .		Ĺ.	l. I.			. 1	١.١	_	_
] equals	i i'a	18.25	1. 1	عاد اه	140	20.00	3	n o	r že	t en	±6π	et al
1 '	١	1		-1	4 ⁻	1 - 1 -	- 1		1	1"		

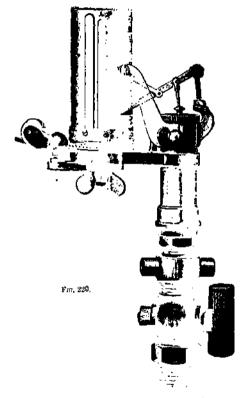
The Silvertown Portable Testing Set.

This is a small collection of the necessary instruments for testing electrically such insulated conductors as are used in telegraph, telephone, or electric-light work.

The whole set is contained in two small wonden boxes, of which one holds the batteries and the other the galvanometer, resistance coils, key, and commutators required for making the two most important measurements on such circuits. These are measure-

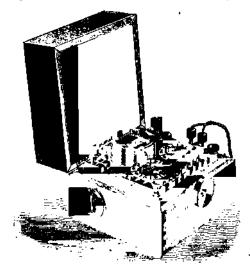
ments of the resistance of the conductor, and the efficiency of the insulation.

The battery consists of two parts: one-commonly called the



bridge battery—is a set of three Leclanché cells of low resistance intended to be used in testing conductor resistances only, a purpose for which currents of electricity of sensible magnitude are

required. The other part is a set of 36 small Leclanché cells having a total electro-motive force of 55 volts, intended exclusively for measuring insulation resistances, or other resistances, of considerable magnitude. These cells are designed to give only very small currents of electricity, and care should be taken not to connect them inadvertently to the Wheatstone Bridge or otherwise put them on a circuit of low resistance. This battery, called



F10, 221,

the insulation battery, is subdivided into three sections of 3, 15, and 39 cells, so that electro-motive forces of about 5, 25, or 60 volts can be employed as may be found convenient.

For connecting the battery to the testing instruments convenient leads are provided terminating in brass plugs with insulated handles for inserting in the proper plug-holes. The instruments shown in perspective in Fig. 221 are connected up together in their own box in such a way as to occure the greatest

portability and economy of space, and to enable the two tests to be taken with the greatest readiness.

A plan of this box showing the general arrangement of all the connections, resistance coils, and galvanometer is seen in Fig. 222.

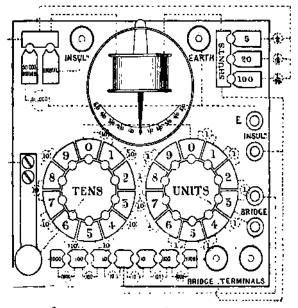
The galvanometer consists of a coil of fine wire on a brass bobbin, in the centre of which a small magnetic needle with an aluminium pointer is hung in the same way as is usual in compasses. The pointer projects through the opening in the end of the coil, and the excursions of the needle are limited by the size of the opening to about 45° on each side of the centre. On removing the glass cover the needle on its point may be taken out by withdrawing the slide on which it is pivoted from inside the coil. The scale, which is a scale of equal currents, is approximately a scale of tangents, and is obtained empirically by calibrating the instrument. The north and of the magnetic needle points to the left-hand side of the box when it is swinging freely in its zero position.

On the left-hand side of the box is placed the controlling magnet, and the position of this affects the sensitiveness of the gulvanometer. When the north pole of the controlling magnet is uppermost, the galvanometer will be most sensitive; on turning the magnet round, so that the south pole is uppermost, the described of the needle due to any given current will be reduced by about 40 per cent. Generally in testing the insulation of well-insulated wires, the galvanometer is required to be as sensitive as possible, and the north pole of the controlling magnet should be at the top; but for measuring conductor resistences, for which the galvanometer is generally amply sensitive, it will be found more convenient to bring the south pole uppermost, thereby causing the galvanometer needle to oscillate more rapidly.

Besides thus affecting the sensitiveness of the galvanometer, the magnet is also used to adjust the needle to the zero in its position of rost by turning it slightly in one direction or the other.

The shunts shown to the right of the galvanometer are also for the purpose of diminishing its sensibility by shunting definite known fractions of the main current past the galvanometer when the plug is inserted in the desired hole. If at any time the galvanometer needle should become insensitive and sluggish, it may be due to one of several causes, namely—

(a) That the needle has become demagnetized. This can be remedied by withdrawing and re-magnetizing it with an ordinary



General arrangement showing all connections

Fig. 222

horse-shoe magnet, care being taken that this is done in the same direction as before.

- (b) That some dirt has found its way into the jewel. This may be removed with a piece of soft wood cut to a fine point.
- (c) That the jewel or the needle point is injured. In this case the slide should be removed and sent with the needle and pointer

to the makers for repair. This will probably have occurred either through the whole instrument having received a blow when the lid is open and the jewel resting on the needle point, or through the brass spring in the lid of the box being bent so that it no longer presses on the lifter when the lid is closed, and the needle has consequently been resting on the point while the box has been carried about.

The remainder of the box consists of the two-way plug switch on the left of the galvanometer, by means of which either a known standard or unknown high resistance can be separately inserted in series with the galvanometer.

The spring tapping key seen on the left hand lower corner of the box is for closing the galvanemeter circuit when ordinary resistance other than that of insulation is being measured.

The two circular dials, marked Texts and UNIS, form the adjustable resistance arm of the Wheatstone Bridge arrangement, and consist of two sets of 9 cods each, totalling 99 ohms when both plugs are in the "9" holes, 0 when both plugs are in the "0" holes, and infinity when both plugs are out altogether.

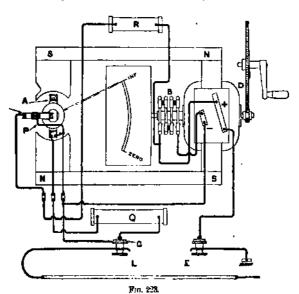
A double-set of proportional code or a sistences, each consisting of 10, 100, and 1000 ohms code, completes the bridge. These are connected to the row of blocks seen at the bottom of Fig. 222.

The terminals shown are for connecting the battery and unknown resistance to.

Evershed "Megger" and "Bridge-Megger" Testing Sets.

The "Megger" Insulation Set.—The general principle underlying the construction, as well as the internal connections, of this set will be seen by a reference to Fig. 223. As seen, the instrument is a combination of a magneto-generator on the right-hand side, with the olumeter portion on the left, in a somewhat unjuge form of magnetic circuit, common to both and consisting of two pairs of field poles braced by strong har magnets NS, NS, and forming two bi polar field magnets in series. In the right-

hand one, and rotated by a folding handle and spur gearing D_i is the armature of the generator with its brush gear B_i and terminal bars marked + and -. In the left-hand field is the current coil A_i pressure coil P_i and compensating coil C of the chammeter, connected to resistances Q and B_i a "guard plate" G_i and the only two external terminals L and E (marked Line and



Earth in Fig. 224), which shows the general view of this set ready for use, with one end of the carrying strap detached from its spring cleat, the scale lid lifted and driving handle unfolded ready for use.

The arrangement and connections of the moving coil system of the chumeter of this set are shown in Fig. 229, and that of the generator armature in Fig. 231, the coils of which are numbered consecutively in order of their winding, No. 1 being

next to the core. The generator of this set may be either of the variable or constant-pressure typo.

The Bridge-Megger" Testing Set is available for use both as an insulation testing set and as a specialized Whattstone



bridge. It differs from the above set in outward appearance only by the addition of two pairs of terminals at the left hand end, and of two switches near the top right-hand corner, as will



Fig. 225.

be seen by Fig. 225, showing a plan photograph of the box containing the chammeter and generator.

One of the two switches is a Ratio Switch for varying the proportion of the two ratio arms, when the instrument is used as a Wheatstone bridge, so as to make the nuknown resistance (X)

under test either equal to, or $\frac{1}{10}$ th, or $\frac{1}{10}$ th of that of the standard resistance box R, thus providing a wide range of measurement which can be again increased by merely interchinging positions of the standard R and unknown resistances X relatively to the two pairs of terminals at the end (as seen in Figs. 44 and 45), which gives the unknown (X) now in terms of $R \times 10$ (or \times 100) necording to the ratio employed.

The other, or two-way change over switch, when set to "Megger," prepares the instrument for measuring large metallic resistance

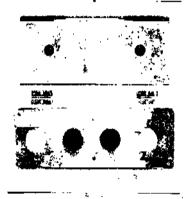
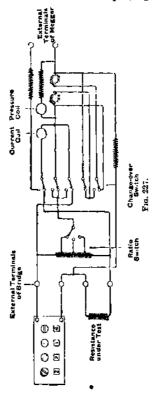


Fig. 226.

(vide p. 118), though principally insulation resistance, by coupling the two windings of the constant-pressure generator in series and making the two front terminals, marked *Line* and *Earth*, the only two available for connection.

When set to "Reidys," the instrument is converted for Wheat-stone bridge work—the two windings of the generator being now coupled in parallel in order to increase the current obtainable from it; the obnumeter part being changed into a galvanometer for the bridge; and the arms of the bridge being switched into their appropriate places in circuit and connected to the only available terminals (namely, the two pairs marked R and X at the end) for use now on the instrument.

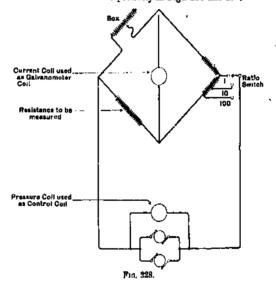
The variable standard direct-reading resistance box (R) for use in bridge measurements is shown in plan, Fig. 226, and is of



the sliding-contact type, operated by turning chonite handles. The figure appearing for each position of any handle is the resistance of that dial, and the total shown in Fig. 226 is 8,306 ohms. The complete internal connections of a "Bridge-Megger" set

with change-over switch set to "Bridge" are given in Fig. 227, while the connections forming the usual bridge circuits are depicted in Fig. 228.

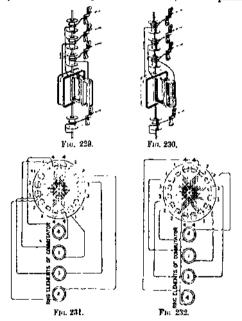
The connections of the moving-coil systems are shown separately for the "Megger" set, Fig. 229—and "Bridge-Megger" set, Fig. 230—while the armsture connections of the generator are shown for these sets respectively in Figs. 231 and 232.



The Constant Pressure Generator for the "Bridge-Megger" set is shown in Fig. 233, the permanent bar magnets NS of Fig. 223 being removed for clearness.

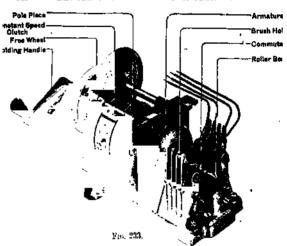
The free-wheel attachment prevents the armature and gearing being damaged by any sudden stopping of the folding handle, and permits the armature to be driven in one direction only. Between the armature and gearing is interposed a centrifugal friction clutch comprising a drum driven by gearing, on which two arms, attached to the armature and fitted with pads at their ends, are urged by springs. When the driving handle is turned above slipping speed, the speed of the armature, and hence its E.M. F., is extremely constant—varying as little as I part in 1000.

The Index Adjuster, fitted to the latest constant pressure sets, consists of a small piece of soft iron rod, mounted parallel



to the line joining the centres of the field poles and close to the moving coil C_1 Fig. 223. It is capable of being moved sideways in one direction or the other (relatively to C_1) by means of a knob.

The rod becoming magnetized inductively by the polar field causes some of its field to pass through the coil U, and hence, if the rod is moved, its field also moves slightly, which at the "infinity" position of the moving systems causes a slight deflec-

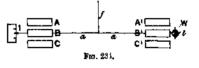


tion of the pointer one way or the other, facilitating accurate adjustment to infinity.

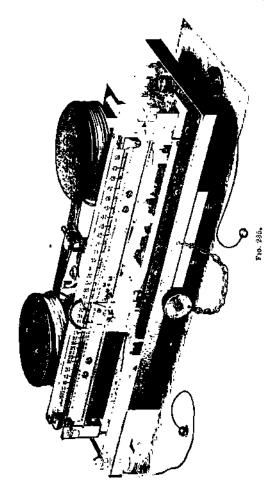
The adjustment does not affect the law of the instrument, which is altered only by the centre coil P.

Standard Direct-Reading Electric Balance.

Fig. 235 shows the general appearance (with glass cover removed), and Fig. 234 a part symbolical elevation of Lord Kelviu's centi-ampere balance.



(1) The instrument is founded on the principle of action of the mutual forces, discovered by Ampere, between movable and



fixed portions of an electric circuit. The shape chosen for the mutually influencing portions is circular, and each such part will be called for brevity an ampere ring, whether it consists of only one turn or of any number of turns of the conductor.

(2) In this balance, each movable ring, B and B, is actuated by two fixed rings, AC and A'C'—all three approximately horizontal. There are two such groups of three rings—two movable rings attached to the two ends of a horizontal balance arm pulled, one of them up and the other down, by a pair of fixed rings in its neighbourhood. The current is in opposite directions through the two movable rings to practically annul disturbance due to horziental components of terrestrial or local magnetic forces.

- (3) The balance arm is supported by two trunnions, each lung by an elastic ligament of fine wire f, through which the current passes into and out of the circuit of the movable rings.
- (4) The mid-range position of each movable ring is in the horizontal phase nearly midway between the two fixed rings which act on it.
- (5) The current goes in opposite directions through the two fixed rings, so that the movable ring is attracted by one of the fixed rings and repelled by the other. The position of the movable ring, equi-distant from the two fixed rings, is a position of minimum force, and the sighted position, for the sake of stability, is above it at one end of the beam and below it at the other, in each case being nearer to the repelling than to the attracting ring by such an amount as to give about 12 per cent. more than the minimum force.
- (6) The belancing is performed by means of a weight which slides on an approximately horizontal graduated arm attached to the balance; and there is a trough f, fixed on the right-hand end of the balance, into which a proper counterpoise weight W is placed, according to the particular one of the sliding weights in use at any time (sect. 9 below). For the fine adjustment of the zero a small metal fing is provided, as in an ordinary chemical balance. This flag is actuated by a fork having a handle below the case emisside, as shown at the bottom of Fig. 235. To set the zero the left-hand weight is placed with its pointer at the zero of the scale, and the flag is turned to one side or the other until it

is found that, with no current going through the rings, the balance rests in its sighted position.

(7) To monours a current the weight is slipped along the scale until the balance rests in its sighted position. The strength of the current is then read off approximately on the fixed scale (called the inspectional scale), with aid of the finely divided scale for

more minute accuracy, according to the explanations given in

sect. 11 below. Each number on the inspectional scale is twice the square root of the corresponding number on the fine scale of equal divisions.

(8) The slipping of the weight into its proper position is performed by means of a self-releasing pendant, langing from a hook carried by a sliding platform, which is pulled in the two directions by two silk threads passing through holes to the out-

side of the glass case.

(9) Four pairs of weights (sliding and counterpoise), of which
the skelge or carriage and its counterpoise constitute the first pair,
are supplied with the instrument. These weights are adjusted

in the ratios of 1:4:16:64, so that each pair gives a round number of amperes, or half-amperes, or quarter-amperes, or of decimal sub-divisions or multiples of these magnitudes of current, on the inspectional scale.

(10) The useful range of each instrument is from 1 to 100 of the smallest current for which its sensibility suffices. The range of this instrument is from 1 to 100 centi-amperes. The following table shows the value per division of the inspectional scale corresponding to each of the four pairs of weights—

				(°r P	nti-amperer r division
First pai	r of	Weights.			0.52
Second	я				0.50
Third	7)				1.0
Fourth	,,				2:0

(11) The fixed inspectional scale shows, approximately enough for most purposes, the strength of the current; the notches in the top of the pluminium scale show the precise position of the weight corresponding to each of the numbered divisions on the fixed scale, which practically annuls error of parallax due to the position of the eya. When the pointer is not exactly below one of "the notches corresponding to integral divisions, of the inspectional scale, the proportion of the space on each side to the space between two divisions may be estimated inspectionally with accuracy enough for almost all practical purposes. Thus we may readily read off 34.2 or 34.7 by estimation with little chance of being wrong by I in the decimal place. But when the utmost accuracy is required, the reading on the fine scale, of equal divisions must be taken, and the strength of current calculated by oid of the table of double square roots given at the end of this book. Thus, for example, if the reading is 292, we find 34.18, or say 34.2, as the true scale reading for strength of current; or, again, if the balancing position of the pointer be 301 on the fine scale, we find 34.70 as the true reading of the inspectional scale.

(12) The conti-ampere balance, with a thermometer to test the temperature of its ampere rings, and with platinoid resistances up to 1600 ohms, serves to measure potentials of from 10 volts to 400 volts, and up to 2000 volts with specially constructed high resistances.

Table X.

Constant of the Centi-ampere Balance when used as a Ventumeter.

W	eight used.		 	licalstance in curcuit.1	Volfs per division of fixed scale.
First Pair e	of Weights			400 800	1.0
	"	.,.			20
31	18	***	1	1700	\$0
	17	144	(1600	40
:		—-			· · · · · · · · · · · · · · · · · · ·

I Including resistance of the instrument, which is about 60 ohms.

If the second pair of weights is used, the constants will be double of those noted above.

- (13) Instructions for the Adjustment of the Standard Balances. —The instrument should be levelled in accordance with the indications of the attached spirit level, by means of the levelling screws on which the sole-plate of the instrument stands.
- (14) In this centi-ampure balance, the beam can be lifted off its supporting ligaments by turning a handle attached to a shaft

passing under the sole-plate of the instrument. This shaft carries an eccentric, on the edge of which rests the lower end of a vertical rod, which is fixed at its upper end to a tripod lifter, when the instrument is to be packed for carriage, or when it is to be removed by hand from place to place, the lifter should be raised; but when it is fixed up for regular use, it is advisable to keep the beam always hanging on the ligaments.

- (15) The carriage is fitted with an index to point to the movable scale, and is intended to remain always on the rail. One or other of the weights is to be placed on the carriage in such a way that the small hole and slot in the weight pass over the conical pins. The weights are moved by means of a slider, which slides on a rail fixed to the scle-plate of the instrument, and carries a pendant with a vertical arm intended to pass up through the rectangular recess in the front of the weight and carriage. The slider and weight are shown in position in the figures. The slider is moved by silk cords, which pass out at the ends of the glass case. When the cords are not being pulled for shifting the weight, their ends should be left free so that the pendant may hang clear of the weight. When a weight is to be placed on or removed from the carriage, the slider should be drawn forward at the top until it is clear of the weight, and then pushed to one side until the weight is adjusted, when it may be replaced in position in a similar manner.
- (16) Cylindrical counterpoise weights with a cross-bar passed through them are supplied for the purpose of balancing the sliding weights when they are placed at the zero of the scale. The sliding weight should be placed so that the index of the carriage points to the zero of the scale, and the proper counterpoise weight should be placed in the trough, fixed to the right-hand end of the beam, with its cross-bar passing through the hole in the bottom of the trough. The flag which is attached to the cross-trunnion of the beam should then be turned by means of the handle projecting from under the sole-plate, until the index on the end of the movable scale points to the middle one of the five black lines on the fixed scale opposite to it. Care must be taken when making this adjustment that the fork which moves the flag is not left in contact with it, as this would impede the free seeing of the beam. The fork should be turned back a little after

each adjustment of the flag, and, when the flag is being adjusted, it is better to watch the flag itself, and make successive small adjustments until the beam stands at zero, than to make, successive trials by pushing round the handle while watching the position of the index.

position or the index.

If the ligament has stretched since the instrument was standardized, the index at one end of the movable scale will be found to be below the middle line on its vertical scale, when the index at the other end is correctly pointing to the zero position. The error so introduced would be a small one, but it may be easily put right by slightly loosening the screws fixing the pillared frame, which supports the movable beam, to the base plate, and raising it by slipping one or two thicknesses of paper below it until the indices simultaneously point to their zero position.

(17) A lens is supplied with each instrument for facilitating accurate observation, either when reading the position of the weight or when adjusting the zero.

(18) The vibrations of the beam may be checked so as to facilitate reading by bringing the pendant, which moves the weight, lightly into contact with it, in such a way as to give a little friction without moving the weights.

(19) In using the centi-ampère balance as a voltmeter when great accuracy is required, care must be taken that the offect of change of temperature in changing the resistance of the coils of the instrument, and of the external resistance coils, is allowed for; and in this use of the instrument it is advisable to employ currents such as can be measured by the lightest weight on the beam. When the instrument is to be used as a voltmeter, four resistances are provided, three of which are each 400 ohms, and the fourth is less than 400 ohms by the resistance of the coils of the instrument at a certain specified temperature. The smallest resistance is intended to be included by itself in the circuit when the lowest potentials are being measured, and in series with one or more of the others when the potential is so high as to give a stronger current than can be measured with the lightest weight on the beam. The correction for temperature is, for the copper coils of the balance, about 0.38 per cent, per degree Centigrade, and for the platinoid resistances, about 0.024 per cent. per degree Centigrado,

Anti-Inductive Resistance for the Kelvin Standard Electric Balances.

When a balance of the above type, such as, for instance, the centi-ampers or composite instrument, is to be used as a voltmeter, four resistances are provided, three of which are each 400 chms, and the fourth is less than 400 chms by the resistance of the cells of the balance at a certain specified temperature. These resistances are doubly wound so as to be non-inductive, and are made of platinoid wire, wound on suitable frames, so as to pre-

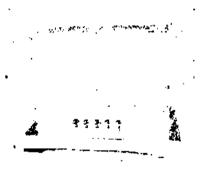


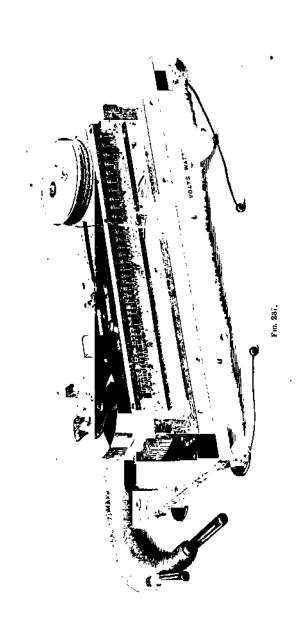
Fig. 236.

sent a maximum amount of cooling surface. The frames are enclosed in a box with apertures at the top to allow of the warm air getting out. Fig. 236 represents such a box for use with a Kelvin standard balance. The smallest resistance is intended to be included by itself in the circuit when the lowest potentials are being measured, and in series with one or more of the others, when the potential is so high as to give a stronger current than can be measured with the highest weight on the beam. The correction for temperature is, for these anti-inductive platinoid resistances, about 0.021% per degree Centigrade.

each adjustment of the flag, and, when the flag is being adjusted, it is better to watch the flag itself, and make successive small adjustments until the beam stands at zero, than to make, successive trials by pushing round the handle while watching the position of the index.

If the ligament has stretched since the instrument was standardized, the index at one end of the movable scale will be found to be below the middle line on its vertical scale, when the index at the other end is correctly pointing to the zero position. The error so introduced would be a small one, but it may be easily put right by slightly loosening the screws fixing the pillared frame, which supports the movable beam, to the base plate, and raising it by slipping one or two thicknesses of paper below it until the indices simultaneously point to their zero position.

- (17) A loss is supplied with each instrument for facilitating accurate observation, either when reading the position of the weight or when adjusting the zero.
- (18) The vibrations of the beam may be checked so as to facilitate reading by bringing the pendant, which moves the weight, lightly into contact with it, in such a way as to give a little friction without moving the weights.
- (19) In using the centi-ampero balance as a voltmeter when great accuracy is required, care must be taken that the effect of change of temperature in changing the resistance of the coils of the instrument, and of the external resistance coils, is allowed for; and in this use of the instrument it is advisable to employ currents such as can be measured by the lightest weight on the beam. When the instrument is to be used as a voltmeter, four resistances are provided, three of which are each 400 chins, and the fourth is less than 400 ohms by the resistance of the coils of the instrument at a certain specified temperature. The smallest resistance is intended to be included by itself in the circuit when the lowest potentials are being measured, and in series with one or more of the others when the potential is so high as to give a stronger current than can be measured with the lightest weight on the beam. The correction for temperature is, for the copper coils of the balance, about 0:38 per cent. per degree Centigrade, and for the platinoid resistances, about 0.024 per cent, per degree Centigrade,



Constant of Composite Balance when used as a Centiampric Balance.

Weight used.	Centi-emperes per Division of Fixed Scale,					
Sledge + VV_{ij}				0.5		
" + VIV"				1.0		
$_{11}$ + VW_{21}				2.0		

The volts on the terminals are calculated from the current in amperes and the resistance in ohms (including the anti-inductive resistance, if any) in circuit. If V be volts, C current, and R resistance,

V = CR.

The anti-inductive resistance is arranged so that the instrument reads a round number of volts per division.

Table XI.

CONSTANT OF COMPOSITE BALANCE WHEN USED AS A VOLTHETER.

Worgh	Weight used.		Resistance n Circuit.	Volta per Division of Fixed Scale.		
Sledge	+ 1111,		200		1.0	
,,	,,		400		2.0	
,,	,,		800		4.0	

I Inchesing the resistance of the instrument, which is about 30 chings.

If the second pair of weights (Sirdge+ VIV_2) be used the constants will be double of those noted above.

(5) To use the instrument as a lackte ampere meter the switch is turned to "Watt" and the thick wire coils inserted in the current circuit in such a way that the right-hand end of the beam is repelled up. Either the sledge alone or the weight marked WW is to be used in this case. A measured current is then passed through the suspended coils, and the constants given in the certificate for the balance used in this way are calculated on the assumption that this current is, as there stated, 0-25 ampere, but any other current which is convenient in the circumstances may be used. The current through the suspended coils may be measured by means of the instrument itself arranged for the measurement of volts. This may be done by first measurement of volts.

suring the current which the difference of potential between the supply conductors of an electrical installation, or between the poles of a battery, causes to flow through the coils of the instrument and its external resistance, and then turning the switch to "Watt," and at the same time introducing a resistance into the circuit equal to the resistance of the fixed coils.

CONSTANT OF COMPOSITE BALANCE WHEN USED AS A HEKTO-ANDERS BALANCE.

Weight usel	Amperes per Divisio of Movable Scale.				
Sledge + WW.,			0.250		
, + #W ₂ ,			0.500		
$_{0}$ + WW_{3}			1.000		

4 With 0 25 ampere through moveble code.

N.B.—The constants vary inversely as the current through the fine wire coils.

(6) To use the instrument as a Wattmeter, one terminal of the fine wire coils is joined to one end of the anti-inductive resistance and the other terminal to one of the leads; the other end of the resistance being joined to the other lead. The thick wire coils are inserted in the main circuit as described in sect. 5 above. With the instrument thus joined up, the current through the suspended coils and the E.M.F. between the leads may be obtained by the operations described in sect. 4 above, since the presence of the thick wire coil in the circuit causes no appreciable error: or the E.M.F. may be taken from the electrostatic voltmeter used on the circuit, and from its indications the current in the suspended coil circuit calculated. The watts are then to be calculated from the E.M.F. on the leads and the current through the thick wire coils by the formula

$$W = VC = cCR$$
,

where σ is the current in the suspended coil circuit, C the current in the thick wire coils, and R the resistance in the circuit.

The weights sent out with the instrument are arranged to give a round number of Watts per division of the scale with a known anti-inductive resistance in series with the fine wire movable coils,

TABLE XII.

CONSTANT OF COMPOSITE BALANCE WHEN USED AS A WATTMETER.

Weight med.			Resist with	morable (Watte per Division of Movable Scala.		
Sledge +	WW,	٠		200			12.5
**	91			400			25.0
"	,,			800			50.0
" +	W 11/2,			200	٠. ٠		25:0
"	,,			400			50-0
,,	97			800			100.0
" +	WW.			200			50.0
,,	,,			400			100-0
	,,			800			200.0

¹ It cluding resistance of movable cods, which is about 12 olims.

Adjustable Magneto-static Current Meter.

- (1) The magneto-static current meter (Fig. 238) consists essentially of a small steel magnet or system of magnets suspended in the centre of a uniform field of force due to two coils, each having one or more turns of copper ribbon or wire, and also under the directive influence of two systems of powerful steel magnets.
- (2) The suspended system of magnets is attached to one end of a vertical shaft passing down centrally through an opening in the sole-plate of the instrument from an indicating needle, which is supported by a jewelled cap resting upon an iridium point.
- (3) The two systems of directive magnets are circular in form, and each ring is composed of two semicircular magnets placed in a brass cylindrical frame with their similar poles together. Each system is securely fixed to a circular brass frame, which fits on to the cylindrical case of the instrument in such a manner that the systems are capable of being turned round, together or separately, as explained below.
- (4) The instrument has a "tangent scale," which is adjusted in its position before the instrument is sent out, so that the needle indicates equal differences of readings for equal differences of current. The scale consists of a hundred divisions, and for most purposes it is convenient to set the field magnets in such a position

that the needle points to 0, and to use the scale from that point upwards towards 100. Sometimes, however, it may be found convenient to measure currents, whose direction is being occasionally reversed, without being at the trouble of reversing the electrodes in the contact clip; in that case the zero should be set to the division 50 at the middle of the scale, and readings taken on each side of it. It must be remembered that when the point taken as zero is changed, the constant, by which the indications of the instrument have to be multiplied to give the current in amperes, is changed in proportion to the cosine of the angle between the zero point and the middle of the scale; and as this



Fm 248.

angle is 60°, the constant with the zero at 50 on the scale is exactly double the constant with the zero at 0 on the scale.

- (5) The instrument is provided with a "lifter," which serves to raise the needle off the iridium point when it is being moved about from place to place. This lifter is in the form of a ring placed below the needle, and may be raised or lowered by turning the handle attached to an eccentric passing through the side of the instrument on a level with the scale. It also serves as a checker, by bringing it lightly into contact with the pointer, so as to stop its vibrations.
- (6) The instrument has an advantage, important for some practical purposes, of being available as an accurate direct-reading

current meter, through a continuous range of from 1 to 100 times its smallest current, which may be anything from half a milliampere to 4 angles, according to the number of turns in the ceils supplied with the instrument. It is not, however, available as an alternate current instrument, and it must be remembered that the magnetism of the steel directing magnet does not remain absolutely constant. With good quality of steel, a proper pro-liminary ageing of the magnet (by heating it several times in boiling water and cooling it again, and subjecting it to somewhat varied rough usage) brings it to a condition in which its magnetism is found to remain exceedingly nearly constant month after month and year after year. Still, it should never be relied upon as absolutely constant, and for accurate laboratory work it is therefore necessary to occasionally standardize it.

- (7) Another advantage which the instrument has is that, when a standard instrument is available, its constant is capable of being varied to any desired value down to one-tenth of that which it has with its directive magnets in their strongest position. Thus if the constant should be 3 amps, per division of the scale, with the similar poles of the magnets coinciding, it may be adjusted to any value down to 0.3 amp, per division.
- (8) Instructions for Use of the Magneto-static Current Meters.—The instrument should be levelled, in accordance with the attached spirit-level, by means of the levelling screws.
- (9) To Adjust the Pointer to Zero.—(a) Loosen the two lower milled-headed screws clamping the magnet frame, and turn the frame round till the pointer stands at zero. (b) Reclamp the frame by tightening the two screws.
- (10) Adjustment of the Scale.—The scale, as stated above (sect. 4), is firmly clamped in its place before sending the instrument out, and this position is marked by two lines on the outside of the case, one horizontal and the other vertical, just below the 0 of the scale. The horizontal line is engraved below the movable top of the instrument, and the vertical one on the side of the case. Should the top of the instrument have been inadvertently moved, and the scale thus put out of adjustment, it may be set right by slightly loosening the two slotted screws and turning the top round till the extremities of the two lines coincide.

- (11) If the needle should by accident be elightly bent, I and so render a new adjustment of the scale necessary, this may readily be made in the following manner:—Set the zero, by the field magnets, to the division 50 at the middle of the scale, then join the instrument in series with another current instrument of convenient form, and pass a current through both sufficient to give a deflection of about 40 divisions on the magneto-static instrument; reverse the current on the magneto-static instrument only, and set the scale so that equal deflections, read in divisions, are given on each side of the zero for equal currents, as indicated on the auxiliary instrument. The zero must, of course, he reset by the magnets every time the scale is moved. When the scale has been adjusted to this position, firmly clamp the top of the instrument by the two slotted screws, and again mark the position of the horizontal line on the outside of the case.
- (12) Adjustment of Constant.—The constant may be quickly varied as follows:—Join the instrument in series with any reliable current instrument of known necurary, such as the deci-ampete balance, and pass a convenient current through both instruments, observing the readings. Hreak the current, loosen the two upper pairs of milled-headed screws, and turn the top system of magnets relatively to the lower, so that the similar poles of the two systems are brought closer together or moved further apart, according as it is desired to make the instrument respectively less or more sensitive. Reclamp the screws and adjust the zero as described in sect. 10. Again make the current, and note the reading on the two instruments. The desired reading on the magneto-static may be obtained quickly after one or two approximations, care being always taken to readjust the zero after each movement of the top magnets.
- (13) When convenient it is always best to standardize the instrument in the place where it is to be used; but when it is intended to move it from place to place, it should be standardized to such a position that when the needle is pointing to zero it is in a direction approximately east and west.
- ³ If it is bent so largely as to be perceptible to the eye, it ought to be straightened by hadd as nearly as may be.

Electrostatic Voltmeters.

These voltmeters have the great advantage of being available as accurate measurers of potential on direct and alternating systems, and, being electrostatic, they use no current, and consequently require no temperature correction. They are therefore free from the causes of error so prevalent in instruments of the electro-magnetic type, whose accuracy is impaired by variations of temperature, and which when used on alternating systems are affected by errors due to self-induction ranging with the period of alternation.

The instruments are made on the principle of an Ar condenser, having one of its parts movable about an axis, so as to increase or diminish the capacity. The condenser is enclosed in a metal case, for the double purpose of protecting the movable part from air currents, and from the disturbing influence of any electrified body, other than the fixed portion, differing from it in potential. In these instruments, the fixed portions consist of two sets of quadrant-shaped cells in metallic connection with each other, and formed by a number of parallel brass plates. These cells are fixed by an insulating support to the case of the instrument, and a terminal passes from them to an insulated binding scrow on the outside of the case.

The movable portion in all the instruments is in metallic connection with the surrounding case. In the multicellular voltmeters this connection is made through the suspending wire. The movable portion carries the pointer, which indicates by direct readings the difference of potential between the two parts of the condenser.

The action of the instrument, shortly stated, is as follows:—When the fixed and movable plates are connected respectively to two points of an electric circuit, between which there exists a difference of potential, the movable plate tends to move so as to augment the electrostatic capacity of the instrument, and the magnitude of the force concerned in any case is proportional to the square of the difference of potential by which it is produted. In the multicellular voltmeters this force of attraction is balanced by the torsion of the suspending wire.

The Kelvin Multicellular Electrostatic Voltmeter.

The arrangement of the parts of this instrument is shown in Figs. 239, 240, and 241. These figures apply to an early form of the



Fm 239,

voltmeter, and differ in two matters of detail from the voltmeter as now made. For simplicity in manufacture the cells are now made with straight backs, and the plates locked at in plan are, therefore, triangular instead of square, as shown in Fig. 241. A ceach-apring has now been interposed between the suspending wire and the spindle carrying the vance, as explained below.

564 · ELECTRICAL ENGINEERING TESTING

The insulated cells are formed of triangular brass plates fixed into saw cuts in a brass back piece so as to be equal distances apart and accurately parallel to each other. Two sets of those cells C are fixed relatively to each other, as shown in Fig. 240, by a vulcanite support to the sole-plate, so that their plates are

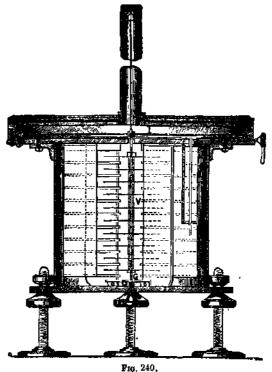
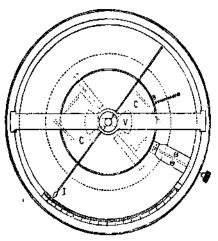


Fig. 210,

horizontal, and are completely enclosed within the brass cylindrical case of the instrument.

On the top of this cylinder is a shallow horizontal circular scale-box containing the scale of the instrument, and having a glass cover, which serves to protect from currents of air the movable indicator I, and the scale and interior parts from dust.

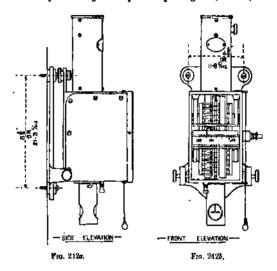
For the movable part a number of vanes, V, similar in form to those of the quadrant electrometer are used. These vanes are placed parallel to each other on a spindle with distant pieces between them. The top end of this spindle passes through a small hole in the sole-plate of the instrument, which forms the bottom of the scale-box, and is attached to a small conch-spring, which in turn is secured to one end of a fine irritic-platinum wire suspended from a toysion head at the top of a vertical bruss tube.



Fro. 211.

The torsion head may be turned by means of a forked key provided for the purpose, and is clamped, to protect it from accidental displacement, by a cap which scrows on to the end of the tube. The coach-spring has sufficient resilience to allow the spindle to touch a guard stop, and so saves the suspension from injury in event of the instrument being roughly set down.

Two vertical biass repelling plates, which also act as guard plates to prevent the movable part from turning beyond its prescribed limits, are fixed to the bottom of the sole-plate. These two plates carry a guide plate, G, with a circular opening in it, through which the lower end of the spindle passes. A little brass disc, or head, D, is attached to the end of the spindle, sufficiently large to prevent its passing back through the hole in the guide plat. Thus the movable part is effectually secured from swinging about so as to be injured, and by no possibility can it come into contact with the insulated quadrants. When the instrument is level the spindle hangs free by the suspending wire, so that the



vanes are horizontal, and each is in a plane exactly midway between those of two contiguous condenser plates.

An aluminium needle attached to the top of the spindle indicates, on the horizontal circular scale fixed to the upper side of the soleplate, the difference of potential between the movable and fixed portions of the condenser by direct readings in volts.

Engine-room Pattern Multicellular.—The description of the instrument given above refers to the horizontal scale or laboratory pattern. In the new engine-room pattern (Fig. 242 a and b), the

parts are in every way similar, but the instrument has a vertical scale. A vane attached to the spindle turns in un oil dash-pot and gives the instrument a dead-beat action.

Portability.—A small thumb-screw is placed in the centre of the base plate below the instrument, which can be screwed in so as to lift the weight of the spindle and vanes from the suspending wire and clamp the disc on the end of the spindle against the guide plate. A lifter or checker is also provided similar to that used in the magneto-static justraments.

A switch is attached to the insulated terminal of the instrument by which the voltmeter can be taken out of circuit when desired. The switch, after breaking circuit, puts the case and the insulated cells in metallic connection.

INSTRUCTIONS FOR THE USE OF THE MULTICELLULAR ELECTROSTATIO VOLTBEIGH.

When received from the maker the indicator needle with attached vanes will be found supported by means of the thumbsorew below the instrument, and also by the circular lifter, or checker, turned up so that the weight of the needle and vanes is taken off the suspending wire.

The scale is graduated to read directly in volts.

To set the instrument up for use, -(a) Unscrew the thumbserew, and turn down the checker, so that the needle swings clear; (b) level the instrument so that the spindle of the vanes passes down centrally through the intersection of the two black cross-lines on the sole-plate.

To adjust the zero, if necessary.—Unscrew the cap on the top of the tube, remove the washer, turn the torsion head by means of the forked key until the pointer stands at 0 on the scale. Replace the washer and screw on the cap again. Before adjusting the zero turn the switch so that the insulated cells are in metallic connection with the case.

Arrangement for portability.—When the instrument is to be removed from place to place, see that the needle is lifted by turning up the checker, and when it is packed for use as a portable instrument, always scraw up the thumb-screw as mentioned above.

As aluminium is electro-positive to brass, the instrument reads

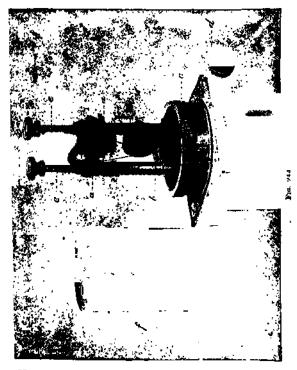
about $\frac{1}{4}$ of a volt too low when the positive pole of a battery or dynamo is attached to the upper or insulated terminal of the instrument; and about $\frac{1}{4}$ volt too high if connected, in the opposite direction. With alternating carrents it is correct.



Pig. 243,

Crompton D'Arsonval Galvanometer.

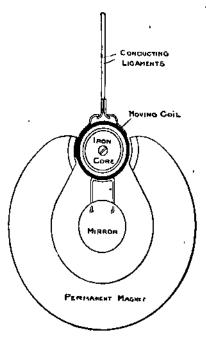
A convenient form of consitive galvanometer, designed for laboratory use, with a large range of adjustment, and made by



Mossrs. Crompton and Co., Cholmstord, is shown in Fig. 213, and the details of construction in Figs. 244 and 245.

The moving part of the instrument is shown in Fig. 245. A

circular coil of wire bangs by a bifilar suspension between the poles of a permanent magnet, an iron core being fixed in the centre. The suspension ligaments are of very thin copper strips, and are connected to the coil by means of a silver clip, which allows the coil to be easily disconnected.



Fta, 245.

The mirror is hung from the coil by fine aluminium books passing through holes pierced in the mirror, so that this is easily detached, and is not distorted by the setting of cement or the pressure of a clip. Fig. 245 shows the construction of the bifilar suspension head. The ligaments are attached to two pins as fixed in a disc, by turning which the tensions of the two may be made equal. They pass over two pins bb placed on another disc, by turning which the distance between the ligaments may be adjusted, and the sensitiveness of the instrument increased or diminished.

The whole head is raised or lowered by turning the milled edge C, and is rotated slowly by turning the worm spindle d.

The two pillars by which the cover f is secured serve as the terminals of the instrument.

Coils are made having different numbers of turns from 100 upwards, and the sensitiveness of the instrument when adjusted to give a complete period of oscillation of from eight to ten seconds is nearly as follows—

TABLE XIII.

No of Turas	Resistance, includ-	Deflection of beam in monites of Art	
on Call.	ing Ligaments.	For I Micro-volt. For I Micro-ampiar	
100	2 ohtus	6	35
399	30	3 5	105
1000	11600	0 8	350

The coils can be fitted with small closed rings of copper, which damp their movements to any desired degree.

Without these the coils are for practical purposes perfectly ballistic.

An electric lamp used without a lens is the most convenient light for the above galvanometer, the filamont being focused on the screen by the mirror. This latter is large (25 m.m. diameter) and ground to a radius of one metra.

Sensitive Portable Galvanometer.

When a Wheatstone Bridge has to be used for outside work, other than in a test-room or laboratory, or when fairly delicate tests have to be made on the "line," a portable type of galvanometer or detector which is as sensitive as possible must be

available. One of the best forms of such an instrument is illustrated in Fig. 246. It consists of a fairly flat-shaped coil of



fine insulated wire, having a resistance usually of between 1000 and 2000 ohms, placed on its side in a brass contain-case provided with a glass top and glass window in the side just opposite the scale, magnetic needle, to which a long light pointer is attached, is pivoted between jewelled bearings in the middle of a flat rectangular brass tube which is capable of being slipped inside the similarly shaped

aperture in the coil of wire. The pointer-protrudes outside one end of the coil and moves over a suitable scale, part of which is seen to the left of Fig. 216. A strip of mirror is let in under the scale and shows through an aperture in it, thus enabling errors due to parallax to be avoided. A needle clamper, actuated by a butten on the edge of the case, enables the needle to be clamped during transport and damage to the pivoting thus avoided.

When no current flows the magnetic axes of coil and needle are perpendicular, when the pointer is at 0 at the middle of the scale. Then the effect of a current is to cause the needle to set 'itself parallel to the axis of the coil, so giving a deflection to one side or the other of zero. This form of instrument is a very sensitive one and very suitable for portable work with a Wheatstone Bridge.

Parr's Direct-Reading Dynamometer Measuring Instruments.

These instruments depend for their action on the mutual force of repulsion between two circuits or coils carrying either the same or different currents, one circuit being fixed and the other movable. The instruments, which have been devised and perfeeted by the author, possess some very important properties that it may be well to note here. They contain no iron whatever and very few metal parts, consequently they measure either the true waits, volts, or amperes, as the case may be, in any alternating current circuit, and are quite independent of the periodicity of the circuit. They are of the switchboard type, direct-reading, and have extremely open scales, extending over \(\frac{1}{2} \) that of the circular dial.



Fig. 247.

Fig. 247 shows an ammeter for 84 amperes, the scale graduations commencing at 3 amps, and continuing nearly uniformly to the end. Fig. 248 shows an internal view of this same 7-inch ammeter. As seen it consists of two fixed coils and two moving coils, carried at the end of a horizontal arm capable of rotating on a vertical spindle pivoted in jewelled centres. This spindle has rigidly attached to it a horizontal arm, to the end of which is fixed a flexible metallic strip that passes almost once round a special pulley carried by a horizontal spindle moving in jewelled centres and carrying the pointer at the front end, a hair-spring, and balance-arm for the pointer. The moving coils and pointer are controlled by the hair-spring, the tension of which can be adjusted by a moving arm. Carrent is let into and out of the moving coils through non-spillable mercury cups. A damping vane and trough is added, also unspillable, by means of which the instruments are made dead beat to any desired



Fig. 248,

extent. The moving coils are changed by a suitable arrangement during transport and seen to the right of Fig. 248. The moving coils are in contact with their respective fixed coils when the pointer is at 0 and no current flows. Repulsion ensues when a current is sent through the instrument, and according to whether it is an animeter, voltmeter, or Wattmeter, so the pointer deflects and indicates directly the quantity to be measured. The instruments of course read equally accurately

on direct-current circuits, and having such very wide, open and uniform scales, a 6-inch instrument can be read with certainty many gards away.

Siemens Torsional Voltmeter.

This instrument may be used either as an ammeter for very small currents or as a voltmeter with a very extended range,

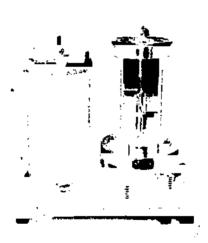


Fig. 242,

and provides a good example of the method of converting one into the other.

It consists of two coils, wound with fine insulated wire, and of elongated oval section, with their axes collinear and horizontal. They are connected in series and wound so that the north pole of one faces the south pole of the other, i. a the two coils may be regarded as one coil with a gap in the centre.

Between the coils is placed a horse-shoe or bell magnet suspended by a silk fibra. A spiral spring is attached to the magnet and to a torsion head at the top of the case, so that by turning the head, a twist is applied to the magnet, proportional,

of course, to the angle of turning of the torsion head. To the

magnet is attached a pointer, for the zero position of which the magnetic axes of coils and magnet are at right angles. The magnet also carries an aluminium vane, moving between two brass checks which act as stops, the vane assisting in stopping the vibrations.

On passing a current through the coils so as to induce the polarity indicated by the small letters no, no (Fig. 250), which represents a symbolical sectional plan of the coils C and usedle NS in a horizontal plane passing through their centres, the magnet NS touds to turn counter-clockwise in the direction of the

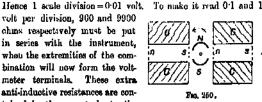
arrow, so that its augustic axis would coincide with that of us, us. Then the angle through which the torsion head has to be turned (in a clockwise direction) in order to bring the magnet pointer back to zero measures the moment of the couple

exerted by the coils on the magnet, i.e. the current flowing through those coils.

The colls C together have a resistance of 100 ohms in the instrument illustrated, and it is wound with such a number of turns that when 1.7 volts are placed across the terminals of the instrument itself, the torsion head makes one complete turn or 170 divisions to bring the magnet pointer back to zero.

Hence 1 scale division = 0.01 volt. To make it read 0.1 and 1 volt per division, 900 and 9900

meter terminals.



tained in the receptacle to the left in Fig. 249, which is provided with a plug top for inserting these resistances at pleasure. They should be wound with a material having a high specific resistance and low temperature coefficient of variation of resistance for reasons already given.

This instrument can be used as a low-reading ammeter, for since 1 division = 0.01 volt and the whole resistance of its coils = 100 ohms, $\cdot \cdot \cdot 1$ division = $\frac{600}{105} = 0.0001$ ampere.

Adjustment of voltmeter.—If the magnet has been changed for transport, release it by turning the milled-headed rod which passes through the edge of the base at the back.

Very carefully level the instrument by turning the levelling screws so that the pointed pin, attached to the moving magnet, is just over the cross marked on the fixed stud under it. The moving system should now be quite free, at all events laterally. See therefore that this is the case.

The height of the moving magnot can be adjusted to give freedom of motion by carefully turning the milled-headed pin which passes into the tersion head at the top of the instrument. Set the tersion head with its pointer to zero, and then bring the magnot pointer to its zero by turning the wooden base which carries the coils. Fix the instrument in this position by turning the milled-headed pin which projects from under the base. In using the instrument thus adjusted to measure current, place it directly across the low resistance provided, and to measure higher voltages connect it in series with the separate anti-inductive resistance provided with it, when the extremities of the combination will then be the terminals of the voltmeter.

Caution.—Make quite sure that the correct resistance is plugged in, otherwise the instrument may be fused up. The plug may be used as a make and break key. Being a + and — instrument, it must be connected up in circuit that the magnet pointer tends to move in the opposite direction to that of the torsion head

Siemens Electro-Dynamometer.

This instrument depends on the electro-dynamical action of one circuit which carries a current on another circuit carrying either the same or a different current, and is illustrated in Fig. 251. It consists of a base supported on three levelling screws and carrying

RLECTRICAL ENGINEERING TESTING an opright standard, to which latter is fixed two distinct stationary an uprigate spandard, to which latter is fixed two distinct standards code beneally would with two different gauges of wire and number of hirth 80 As to obtain a wider range of sonaiciveness and menurement than would be kearble with only one fixed coil ansurement than women no pressure with our one made con-A movable coil, the plane of which is perpendicular to that of A movable coil, the prime or winch is perpendicular to that or the excel coils in the normal position of the former when actually



necessiting a current, is cosponied by means of a silk filter from a increasing a current, is cooperated by mentagor a day above from a forsion head, at the top of the instrument, carried at the center of the contract of the co possion neon, as one sop or one measurement, carried as one course of a graduated saile, which is itself acrowed to the top of the A rather long helical spring, composed of a sufficient number of A rather long mencut syring, composed or a sumctons number of turns, has one end fixed to the under side of the torsion head and

the other to the top of the moving coil, which is thus controlled by the turning of the head. Electrical connection is made with the maving coil through two mercury cups into which its ends dip and which are directly in a line, under the point of suspension. A milled-headed pin or rod, carried by a light support, seen at the back of the scale, passes through the hollow torsion head, and has attached to it the silk thread that suspends the movable coil and which passes down through the torsion head. Hence, by turning the rod round the swing coil can be raised or lowered so as to clear the other fixed fittings. The moving coil, which may consist of more than one turn, can be raised and clamped during transport by a spring claim (not seen in Fig. 251) at the back, controlled by a milled nut. The instrument requires to be carofully levelled before using to ensure perfect freedom with the moving coil. The levelling screws and spirit-level are added for this purpose, though sometimes a plumb line is used in place of the latter. The fixed and moving cotts are in simple series; one end of each of the fixed coils goes to the outside terminals, the other ends both to the top mercury cup and the lower cup to the centre or common terminal, Thus there are two sensibilities, viz. the moving coil in series with either fixed one, according to whether the centre and left or centre and right pair of terminals are in use. Since at the actual moment of measuring a current by the dynamometer, the fixed and movable coils are always in the same position (i.e. their axes perpendicular) relatively to one another, due to the index pointer on the moving coil always being brought back to zero by turning the tersion head, the couple or force, whether of attraction or repulsion, exerted by one coil on the other is $F \propto C_1 \times C_2 \propto C_2 \times C_3$ $\propto C_1^{-2}$ where C_1 and C_2 are the currents in the two coils which are equal or the same. But this force is just balanced by the force of torsion exerted by the spring a angle of torsion or the deflection D of the torsion head. Hence, $D \propto C^2$,

$$\therefore C \propto \sqrt{D}$$
,

or
$$C = K\sqrt{D}$$
 amperes,

where K is the constant for the particular fixed coil used which gives an equation of equality.

This is the law of the Siemens electro-dynamometer.

Some of these instruments have scales divided into numbers to the square roots of the usual divisions, and in such cases the

current $C = K \times$ scale reading simply. In using these instruments care must be taken to either twist the "leading in and out" leads together, or run them very close so that the swing coil may not be affected by the current in these leads.

Ir calibrating or using the instrument with direct currents, it must be so placed that the plane of the suspended coil when in its zero position is perpendicular to the plane of the magnetic meridian of the earth. The reason for this is, that when the swing coil carries a direct current it is acted on by the earth's magnetism independently of the action due to the current in the fixed coil, and the position of rest for the first cause is when the planes of the magnetic meridian and swing coil are at right angles. For alternating currents there is no such action.

Siemens Dynamometer-Wattmeter.

Except for the swing or movable coil, this instrument is precisely similar to the preceding dynamometer. It is illustrated in Fig. 252, which indicates two or three alterations to the general form of the Wattmeter, which the author has thought it beneficial to make. The one illustrated is provided with two thick fixed coils, as in the dynamometer, Fig. 251, connected directly to the three large terminals in the middle, so that two distinct sensibilities can be obtained instead of usually only one.

The swing coil now consists of many turns of fine insulated wire wound on a light rectangular frame of ebonite or boxwood. Only a few of the turns are wound inductively, the rost being doubly wound and therefore non-inductive. The total resistance of the swing coil is, however, that due to the sum of all the turns, which may amount to 5000 chms or more. Current is led into and out of the swing coil through thicker wires soldered to the fine wire and which dip into the two mercury cups. These lastnamed are directly connected to a separate pair of small terminals seen on the extreme right and left, having no electrical connection whatever with the thick coils.

The scale is provided with a mirror for the purpose of avoiding errors due to parallax in reading the position of the torsion head pointer. The mirror glass covers the scale, but a circular strip of

ELECTRICAL ENGINEERING TESTING silvering is removed fast over the scale, enabling it to be seen but proventing is removed just over one scale, ensuing it to be seen our proventing it getting dusty and dirty. In all other respects this Wattonoter is the same as the dynamometer shown in Fig. 251, When the swing coil is referred to its zero, by turning the forsion head, we have as before its deflection $D \propto C_1 \times C_2$ but if $C_1 = \text{the}$



main current and C_3 the current in the fine coil, which is placed across the mains, and therefore is or to the voltage (V), we have

where R is the constant of the instrument for the thick coil used. Thus by combining the volumeter and ammeter in one and the same instrument, the deflection of the new instrument so formed measures the power in Watts absorbed by any circuit. Though the Wattmeter is of no great use in direct current work, since we usually require both the amperes and volts separately and can alwars multiply them and so obtain the power when desired, the instrument is of incabulable value in alternate current work, since, if nearly non-inductive, it is the best known means of obtaining the true power in such a circuit, the product—sumps. x volts not giving this quantity.

The same precautions are necessary in using the Wattmeter as in the dynamometer, and in addition errors may arise through the warming up of the swing coil and consequent alteration of its resistance, as in the case of electro-magnetic voltmeters. The error that may be introduced by the earth's field is explained on p. 580.

Change-over Switch.

Fig. 253 represents a form of switch suitable for large-currents and which can be used in one or other of four ways as follows—

- As a single-way, single-pole switch by connecting to the centre and either of the end terminals on the same side.
- (2) As a single-way, double-pole switch by connecting the centre and an end terminal on the same side in one main, while the other centre and corresponding terminal at the same end is put in the other main.
- (3) As a two-way double-pole switch by connecting the common circuit to the two centres and each branch circuit to the pair of terminals at one end.
- (4) As a reversing switch by connecting the circuit or portion to be reversed to the centre pair and the main current to the pair at either end, cross connecting the corner terminals at the ends by temporary wires.

The figure shows the construction fairly clearly, and it consists of two metal blades carried by smaller extensions at their lower extremities and capable of turning about a horizontal axis in the upright standards which form part of the base carrying the middle terminals and inner wedge blocks. Four similar wedge blocks

(two at each end) are carried by metal bases on which the four end terminals are fixed. When the blade levers are up (us seen), the metal parts, electrically connected to the six terminals, are insulated from each other, as the lever blades are also insulated from each other, their upper extremities being fixed by an insulator cross-piece to which the handle is fixed. When the blades are

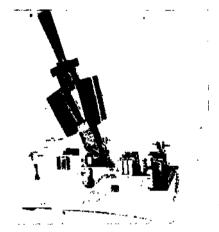


Fig. 253.

pushed down one side or the other into their respective pairs of wedge contact blocks they short circuit these, thus joining the centre and end terminals on one side together, and likewise those on the other side.

Keys.

A form of key, which, though not very portable, is extremely useful in a test room, is shown in Fig. 25t, and is otherwise known as a Pohl's commutator. It consists of a wooden, though preferably polished ebonite, base M, containing 6 small pure-copper

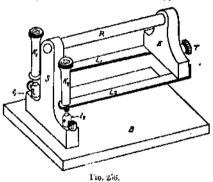
the circuit to be reversed to the other pair T_2 and T_4 or rice versa.

(4) As a 2-way key by joining one main to any one terminal, e. g. T₁ and the branches to T₂ and T₄.

A Highly-Insulated 2-Way Spring Tapping Key

is shown in Fig. 256, and consists of a well-polished obonito base B, supporting at one oud a well-polished obonite standard S, to which is fixed two bress contact terminal blocks t_1 t_2 .

Let into and carried by the top of the standard S is an chonite rod R, which at its other end supports an obmite



block E. To K is fixed two springy brass strip levers L_1 L_2 electrically connected together and to the common terminal T at that and

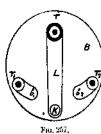
The free ends of the spring strips are provided with rather long about knobs K_1 K_2 for the finger of the operator to tap.

In the use of this key, if the high-potential wire is connected to the common terminal T_1 the path of any lockage lies from T across E, then along R and down S to the base E, and thence to earth. This being long gives the key a high-insulation resistance,

and to still further increase this, all the elemite parts should be well polished and quite clean and free from dust.

It will be noticed, that since there is a lever to each way, it would be possible to press both at once. Unless otherwise directed this must be absolutely avoided, as serious damage may be done in consequence.

Fig. 257 shows, in plan, a convenient form of 2-way diding switch. It consists of a wooden or about base B_1 to which is fixed three terminals T_1 T_1 and T_2 . The two latter, T_1 and T_2 , make permanent contact with the contact blocks b_1 b_2 respectively, while T acts also



as a centre for the contact lever L to turn on. The knob K is morely for the purpose of conveniently turning the lever L.

In the position shown in the Figure, there is no connection between T and either T_1 or T_2 , but by turning L so as to rest on b_1 or b_2 , then connection is made between T and T_1 or between T and T_2 respectively.

It will be noticed that only one contact can be made at one and the same time. This is an advantage in some cases, where the simultaneous making of both ways might cause an accident.

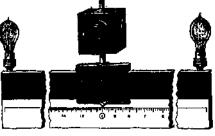
Arc Lamp Photometer Cradle.

In the photometrical testing of electric are lamps it is necessary to be able to have the means of measuring the candle-power of the are in several directions, making various angles with the horizontal line passing through it. In some cases this is done by raising or lowering the lamp vertically, the heam from it being reflected along the beach by a fixed plane mirror suitably placed, but capable of rotating on an axis.

The author has devised the cradle shown in Fig. 258, in which the lamp to be tested is placed. The lower part is a rigid frame-



Fig 258.

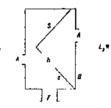


S10, 250,

work which is placed on the photometer bench and carries an upper frame capable of moving round a hollow tubular horizontal axis, which latter is itself capable of moving in the fixed frame and has attached to it a pointer, seen

in Fig. 258, just above the two large terminals. In this upper frame is placed the arc lamp, which can therefore be inclined at any angle to the vertical, as read off by the pointer on its scale.

The carbons of the lamp are first adjusted so as to touch at a point in the axis of rotation, as seen through the tubular axis.



Fm. 200.

Thus the are in turning as the cradle is turned, always maintains the same position relatively to the photometer bench, and the author has found that next to no difficulty in the regulation of the arc by its auto-mechanism occurs up to 50° or 60° from the vertical. After this the carbons have to be partly regulated by hand.

Direct-Reading Bar Photometer.

This form, due to Mr. Trotter, has a direct-reading scale on its bank which shows without calculation the ratio between the standard and lamp under test when the eight-box seen in the middle of the bank (Fig. 259) is moved so as to obtain an equal llumination of the screens. The general arrangement is very suitable for making rapid tests on electric glow lamps, as slight variations of E.M.F. affect both lamps equally and do not cause appreciable errors. Fig. 260 shows a sectional plan of the sight-box BB, in which AA are the apertures at the sides to admit the beams of light from the two lamps L_1L_2 to be compared. SN are two screens, the illuminations of which are compared. One of these contains a star-chaped hole for the purpose of enabling the further screen to be seen through the funnel or window F, through which the observer looks.

Illumination Photometer.

This is a portable direct-reading instrument devised by Mr. A. r. Trotter, by which the illumination at any spot in a street



Fia 281.

nich the illumination at any spot in a street or building can be at once measured in terms of the illumination given by an amyl-acetate standard of light, this being found more reliable and less troublesome than ordinary standards of light. A general view of the instrument is shown in Fig. 261, and a sectional elevation in Fig. 262.

Instructions for Use.

Remove the end cap with the mirror M on it by the bayonet joint; romove the cover from the lamp and light it, then replace the end cap. The flame can now be seen in the mirror. The top of the flame should just touch the point of the bent arm.

The flame is raised or lowered by acrewing the lampholder in or out by its lower end. By unscrewing the holder completely it can be drawn out for refilling.

Having adjusted the flame to the right height the cap on the top is removed and the photometer is set so that the paper screen S is horizontal.

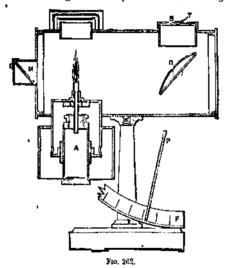
The general illumination to be measured falls on this screen S. Across the centre of it is a small slit T through which an inside screen R illuminated by the standard lamp can be seen. The observer's eye must be vertically over the hole in the screen. The inside screen R is then adjusted by the outside arm P. When the illumination of the outside screen S is greater than that of the inside, the slit T will appear dark; when less the slit will appear bright. With a little practice the slit can be made to nearly, if not quite, vanish; the illumination is then shown on the scale F by the pointer P. The unit used is the illumination due to one standard candle at one foot; that is, if a balance is obtained when the pointer is at "1," the illumination is equal

to that of 1 standard candle at 1 ft. distance, if at "2" the illumination is twice this, and if at "1," one-tenth of that which would be given by a standard candle a foot away.

The inside screen R has a slight blue tint which to a great extent removes the colour difficulty.

A slightly yellow upper screen is provided for measuring with very blue lights.

Be careful the eye is vertically over the slit. Holding one



finger near the eye and between it and the hole will make it easier to get the vertical line.

Be careful to stand so that the body is not between the screen and any source of light.

The slit must be square across the instrument.

See that the height of the flame is right before and after each reading; the flame sometimes increases a little, especially just after being lighted.

The flame is not affected by a gentle breeze, and on windy nights the instrument can easily be shielded by a piece of cardboard or brown paper.

Only pure amyl-acetate must be used, and the wick must be our square across without ragged points.

Keep the cap on over the screen when not in use, and do not let the screen get dirty.

There is a small pin at the centre of the pivot of the arm; when the instrument stands so that its shadow thrown by any lamp falls on the scale, it gives the cosine of the angle of incidence, having which the actual C.P. can be calculated. The height of the lamp is equal to the distance from the post when the shadow falls at 45°.

Photometer Screens.

Of these there are many different types, all of course effecting the same purpose, namely, that of enabling equality of illumination due to two different sources of light to be visibly determined and hence their relative intensities. Fig. 263 shows a form of Bunsen serven arranged inside a "sight-box" seen with its top on lid open to enable the inside to be seen. It consists of two disc of plain paper having its centre portion greased in the form of a star. These discs are seen one near each end of the "sight box," which is dull black inside and prevents stray light due to external or internal reflection from getting to the Bunsen star discs or screens. Two vertical plane mirrors are placed as shown symmetrically with regard to the discs, and each at 45° to the back of the box.

The images of the two discs can be seen in the two mirror through two rectangular open windows in the box shown in from of Fig. 263, and thus the intensities of their illuminations can be compared by the eye. It should be noticed that the sight-hor illustrated in Fig. 263 cannot give true results, since the ratio of the squares of the distances from the light sources to the standiscs and again to the centre of the box are not the same. The box is given, however, to indicate this fact and to act as a warning to users of it. Another form of this screen is shown

resting on the top of the "sight-box," illustrated in Fig. 264. Here there is but one disc with a plane mirror on either side of it, making equal angles with it, and enabling an image of each side of the screen to be seen without looking directly at the disc itself.

The lower part of Fig. 26! illustrates a form of balancing screen due to Jolly, and consisting of two rectangular blocks of clear paraffin wax, semented together but separated by a film of silver paper so as to prevent direct transmission of light right



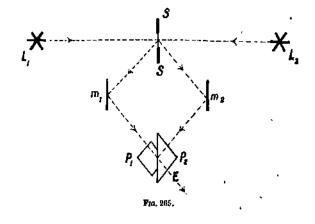
Fig. 263.

through the two blocks. They are placed inside a sight-box to prevent stray light getting to them, hence the two blocks will appear equally bright when the two sources of light to be compared, placed on either side of the sight-box, illuminate them equally.

One of the best photometer screens is that due to Messrs. Lemmer and Brodium, and is shown symbolically in Fig. 265. In this type the light from the two sources to be compared falls on a screen SS, having equally light surfaces. The rays are then



Fig. 264.



reflected by two similar plane mirrors m_1 and m_2 to two prisms P_1 and P_2 , of which P_2 is the ordinary form, while P_1 has a curved surface one side which touches P_n .

The reflected rays from m_1 are able to pass through the combination to the eye placed at E, while those from m_2 are deviated to E also. Thus the screen SS when equally illuminated both sides cannot be seen at E.

"Methven Screen" Photometric Standard of Light.

When used with just an ordinary amount of care this standard of light is one of the most convenient and accurate, requiring no elaborate preparation, as in the case of some other standards, before being used. A standard two-slot "Methven screen," together with a carburetter, is shown in Fig. 266. The former consists of a vertical brass plate or screen, bent round at right angles at the bottom, and to the under side of which is fixed a tubular metal foot which fits into the hellow standard supporting the whole screen.

To the upper side of this angle-piece is fixed a London Argund burner provided with a stettite cone and a cylindrical glass funnel. Two pairs of brass bars are screwed into the screen at respectively 21" and 3" above the top of the burner. The screen has a hole at its centre across which slides a silver plate containing two rectangular windows, the size of which are determined by the height of the flame and the C.P. of the light emitted from them. This in the Methven screen, shown in Fig. 266, is 2 C.P. either when the mean height of the peaks of the flame are on a level with the two top bars and the long narrow slot in use with ordinary coal-gas, or with the flame on a level with the two lower bars, the short broad slot and the coalgas carburetted. The carburettor is shown on the left of Fig. 266, and is merely a motal reservoir containing pentane liquid, which is highly volatile, the vapour mixing freely with the coal-gas and enriching it as this latter is made to pass through the receptacle by manipulating the three step taps seen on the branch tubes. For a more detailed description of the Methvan screen, see Slingo and Brooker's Electrical Engineering.



Fm 296.

It should be noticed that the position of the screen is rather misleading, arising from the fact that it is shown turned round out of its normal position to show more clearly the burner, etc.

Adjustable Carbon Rheostat.

An extremely useful form of continuously adjustable rheestat, suitable for large currents as well as small ones, is illustrated in Fig. 267, this particular one being capable of carrying about 25 amperes continuously or 30 to 40 amperes for short periods of some minutes' duration.

It consists of a row of square flat plates of hard gas-retort carbon, resting on a fairly broad ledge of slate or some other suitable insulating material acrewed to an iron bar underneath it which is fixed to the ends of the framework of the rheestat. These ends are also fixed to tie rods at the sides, to the top of each of which is screwed an over-lapping strip of vulcanized fibre to guide the plates, and at the sume time not to short-circuit them. The row of carbon plates are terminated by thick castiron plates, extended at the top and carrying the terminals shown. The left-hand terminal plate is insulated from that end by a plate of vulcanized fibre, while the row of plates is com-



Fig. 267.

pressed against this by a screw working against the right-hand end. In case at any time the right-hand terminal plate is removed and inserted in some intermediato position in the row, an extra cast-iron plate the same size as the carbons is provided this end to guard against the friction of the carbons should the screw press on them by mistake. One valuable advantage of this rheestat is that, being non-inductive, it can be used with alternating currents in cases where many other forms of rheestats could not be. The resistance varies from a minimum when the plates are tightly compressed, to a maximum when they are loose.

Incandescent Lamp-Box Resistance.

In many tests on alternating current appliances, such as transformers, alternators, etc., difficulties arise in obtaining a non-inductive resistance in which to take up the output of the appliance, for, as is well known, the product of the volts and amperes only represents the actual or true power in Watts absorbed, providing the load-absorbing recostats are truly non-inductive.

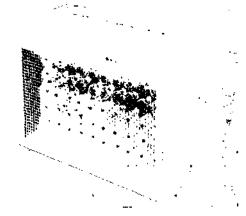


Fig 268,

This can be obtained with specially wound rheostats made of ordinary iron wire or other special alloy. A water rheostat is, however, simpler, though not perhaps so convenient to manipulate, while Fig. 268 illustrates a still more convenient form of non-inductive (to all practical purposes) rheostat, which the author has designed for his own purposes, and one that is fairly portable with care. The particular one shown consists of a containing case and box, with an internal partition which supports some 60

or 70 glow lamps, composed of 8, 16 and 32 C.P. lamps, capable of absorbing some 7 or 8 E.H.P. All the woodwork the lamp side of the partition is covered with a double layer of asbestos cloth, and the front of the box is protected only by a grating to allow of free circulation of cold and hot air. Each lamp is connected to its own pair of mercury cups in a special switch-board, seen on the top of the box towards the back, by means of which the lamps can at once be connected all in parallel, all in series, or



Fig. 269.

in any other intermediate combination, to suit requirements. The side opposite the grating hinges down, giving free access to the lamp-holders and connections to the mercury switch-board. This lamp-hox resistance requires care in carrying about, as the mercury tends to come out of the two long slots if the box is much tilted. It is, however, extremely convenient, and when the lamps are used in parallel in alternating current work, their effective self-induction is extremely small, so that when absorbing the load from the secondary side of a transformer (say), the amps. x volte will be the true power absorbed, i. s. developed by the transformer.

Adjustable Rheostat,

Fig. 269 shows a convenient wire-wound rheastat, capable of stor by-step variations between 0 and the maximum resistance. which is about 40 ohms, and of carrying continuously 6 or 7 amperes. It is a form of rheostat eminently suitable for regulating the shunt circuit of either a dynamo or motor of that type. As will be seen with reference to the figure, it consists of a box or case containing the coils (not seen), and which is fitted with a top carrying the multiple way lever switch of the form shown. The circular row of study seen in the upper part of Fig. 269 are connected to the coils inside in such a way that the right-hand end block gives the full resistance of all the coils in series between the terminals at the top, when the lever is on this block. The rheostat, being intended to be used in a vertical position, has a wire grating at the top and bottom in order to obtain a cooling circulation of cold air through the interior. The coils inside are strong between insulators, so that even if they do get very hot, the inside of the box will not be much harmed.

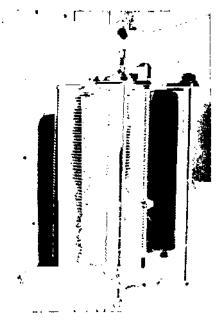
Continuously Variable Rheostat.

This rheestat is of the same type and make as that illustrated and described relative to Fig. 271, consequently a further description is unnecessary. By winding the rheestat with, say, the same gauge in a higher specific resistance material than platinoid, such as sureka, manganin, or roostene, it is easy to obtain a resistance which can be varied perfectly continuously from something like 30 or 40 ohms down to 0, and that will curry a maximum current of about 4 or 5 amperes. This in a test-room or laboratory is extremely useful, enabling very fine adjustments of resistance, and consequently of current or pressure, to be obtained when desired.

The reader is referred to the description of the same make of rheastat shown in Fig. 271.

Improved Rheostat.

The object of the rheostat, invented over forty years ago by Wheatstone, is to provide an electric resistance which can be varied continuously.

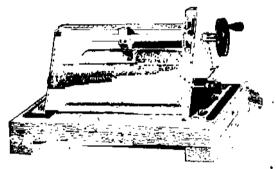


Fra. 270.

The instrument shown in Fig. 271 is an improved form (due to_lord Kelvin) of Wheatstone's rheostat, in which the wire is guided from one cylinder to the other by a fork carried along through the requisite range by a nut travelling on a long screw-

shaft. This screw-shaft carries a toothed wheel which turns the two cylinders by means of toothed wheels attached to their shafts. A watch-spring, as in Jolin's improvement of Wheatstone's rheostat, keeps the wire always tightened to the proper degree. A leather buffer at each end of the range of the nut acts as a guard-against overwinding in either direction.

In a high resistance rheostat the conducting cylinder and the wire are both of platinoid, a metallic alloy having properties which make it specially suitable for the purpose. It has very high electric resistance, very small temperature variation of resistance,



Fm. 271.

and its surface remains almost or altogether untarnished in the air. On account of the last-named property the contact between the wire and the conducting cylinder, and continuity in action, which was a great difficulty in the old form of apparatus, is very complete.

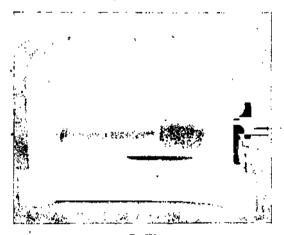
In a low resistance rheostat the conducting cylinder in this instrument is made of brass, nickel-plated so as to avoid tarnishing, and the wire used is copper, also nickel-plated. The rheostat can be supplied to carry currents as high as 30 amperes. The relation between material resistance and current for these rheostats is as follows, viz.—

TABLE XIV.

¶in.	Approximate Resistance.	Maximum Current
Platinoid.	600 ohms.	0.25 amperos.
p)	100 ,,	2.0 ,,
**	20 ,,	10.0 "
Copper.	0.4 "	30.0 "

Continuously Variable Rheostat.

Fig. 272 illustrates another slightly different form of Kelvin's improvement on the original Wheatstone rheestat. The actual



F10. 272.

construction is the same as that described in the two preceding, Figs. 270 and 271, except that the one here shown is intended for finer and lighter work, as seen from the smallness of the parts and gauge of wire employed. The second cylinder is just behind the one shown in the figure. Fairly fine wire is used, and

the rheostat so wound may have a resistance of about 100 ohms as a maximum, capable of carrying one or two amperes. Like the "Wirt" form of resistance, described in Practical Electrical Testing by the author, it forms a most useful type of resistance for small work, such as calibrating low resistance voltmeters, enabling a sories of different readings to be taken without actually altering the number of cells in the E.M.F. used.

The render should refer to the description of the principle of this form of rheestat which is given relative to Fig. 271.

Fixed Standard Low Resistances.

There are many different forms of these depending to a great extent on the value of the resistance, and also on the particular make. Fig. 273 shows a set of five different forms of standard low resistances made by Messrs. Crompton and Co., and primarily intended for use with the potentiometers made by them also. The resistances can, of course, be used for any other purpose than this which requires a standard resistance of accurately known value, capable of carrying large currents without sensible heating or alteration.

The one shown standing on end at the top is of a slightly different form to the rest, being of the tubular water-cooled type.

These resistances consist of a sheet or strip of metal, or a coil of wire, each provided with four terminals, two for connection to the circuit and two for connection to the potential leads.

The smaller resistances take the form of a coil or spiral fixed in a mahogany frame, and also of flat strips either bent or straight, the largest size—300 amperes and over are of sheet or water-cooled type.

They are constructed of manganin, an alloy which has been thoroughly tested, and which has the great advantage that within ordinary limits of accuracy (say one part in 1000) no temperature correction whatever is necessary: but for measurements with the potentiometer requiring an accuracy exceeding this, a curve, giving the temperature value for the whole range of current that the instrument is capable of carrying, is supplied with each resistance.

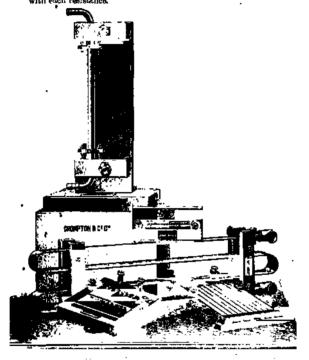


Fig. 273.

. Such a curve, together with other forms of adjustable and fixed standards of low resistance, are given in the author's work entitled Practical Electrical Testing.

Stand Coil Rheostat.

A most convenient form of current rheostat of a portable nature, at all events one that can be moved comfortably about any testing-room, is illustrated in Fig. 274. It consists of an



Fic 274.

iron frame or stand, of as light a construction as possible, in order to be light, between the top and bottom of which are stretched bare wire spirals of either iron or some high-resistance alloy. These coils are spaced sufficiently far apart to prevent them easily touching should the rheestat receive a slight knock, and are all connected in series, their junctions being connected

to a multiple way switch seen on the top. This latter consists of several stude or blocks arranged in a circular form and having their apper surfaces turned up in the lathe so as to be quite level. A suitable spring lover pivoted in the centre of the ring of blocks is capable of turning almost once round between two stops and of making contact with each block as it passes over it.

One of the two-terminals of this stand coil rhoostat (seen on the top) is connected to the lever centre, and the other to one end of the series of coils. Thus the resistance between the terminals can be varied from nothing (i.e. short circuit) to the maximum by as many steps as there are contact blocks on the switch. A great mistake, which is usually made by rhoostat makers, is to use the same gauge of wire throughout the rhoostat, for clearly the gauge should increase as we begin to cut out, since the current is thereby increased also. The above rhoostat, made to the author's designs, contains about four or five gauges of wire.

Three-Phase Liquid Rheostat.

For three-phase alternating current work there are two distinctive forms of rhoostate needed, differing merely in the terminal arrangements. One form may be termed a "through" rhoostat, which would be required for regulating the current supplied by a generator to, say, a motor; the other form may be termed a "closed" rhoostat, which would be required for absorbing the lead from a generator.

In all forms the rheostat must operate equally on each of the leads of a three-phase system, otherwise the balance and symmetry of the currents will be thrown out and will cause considerable trouble. Three-phase rheostats may be either metallic or fiquid in nature, but in any case the moving contacts must move simultaneously by equal amounts when manipulating the rheostat as a whole. Fig. 275 shows a three-phase liquid rheostat designed by the author, and which will negotiate currents up to about 30—40 amps. It can be employed either as a "through" or "closed" rheostat, and consists of three exactly similar flat semicircular-shaped iron troughs or boxes placed side by side in

alignment on a wooden base board, but not in contact with one another. Each is secured to the base board through its flat metal foot, carrying a terminal which therefore makes electrical connection with the box as a whole.

These terminals are clearly seen in Fig 275. Each box has a semicircular-shaped iron plate, carried by a brass spindle, which passes through bearings of insulating material let into the opposite sides of each box. The ends of each spindle terminate just outside the box in enlarged metal bosses, the successive adjoining pairs being direct coupled mechanically through couplings of insulating material, but are discontinuous electrically.



Fro. 275,

This compound shaft or spindle is rotated with the plates by means of a worm and worm-wheel gearing. Seen to the righthand end of Fig. 275.

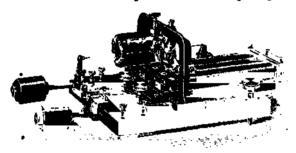
Three other terminals (not seen in the figure) at the back of the rheostat make electrical connection to each section of the spindle, and therefore to each plate through spring strips rubbing on the proper bosses as the spindle is turned.

A solution of washing soda and water of the same density is used in each trough, and must not, of course, reach up so high as to make contact with the spindles. Thus when none of the terminals are cross-connected, the rheostat becomes a "through type," but when the three at one side are all joined together, we have a closed rheestat, suitable for absorbing the load from a generator connected to the remaining three terminals.

It should be remembered that as each of the three sections of this water rheostat must operate equally on turning the shaft, the level of liquid must be the same in each trough in addition to it being of the same density.

Magnetic Curve Tracer.

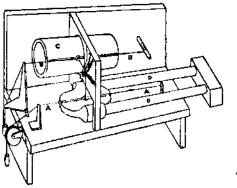
This instrument, devised by Prof. Ewing, shows the magnetic quality of iron, steel, or other magnetic metal, by exhibiting the curve which connects the magnetization B with the sunguesting



Fen. 278.

force H in any magnetizing process. The curve is exhibited upon a screen by the spot of light reflected from a mirror, which receives two components of motion. The vertical component is proportional to the magnetization, and the horizontal component to the magnetizing force. The instrument is shown in Fig. 276, and Fig. 277 is a diagram showing the functions of the various parts. The mirror is pivoted upon a single needle-point, which leaves it free to turn both ways, and it is connected by threads to the middle of two stretched wires, AA and BB, in such a manner that when either of the wires sage the mirror suffers a corresponding deflection. The throads

are kept taut by light springs, the tension of which is adjustable. The wires are stretched in narrow slots, forming gaps in two magnetic circuits, DD and C. One of these circuits, DD, is made up of the iron or steel to be examined, along with suitable p-k-pieces and yoke, and the current which passes through the magnetizing coils of this circuit passes also through the stretched wire, BB, in the gap of the other magnet. The other magnet is constantly magnetized by a steady current, and a steady current also flows through the stretched wire AA. Hence,



F10. 277.

when the magnetizing current of DD is altered, the wire BB sags out or in, and gives horizontal motion to the mirror proportional to the magnetizing force acting on DD. And when the magnetism of DD is altered, the wire AA sags up or down, giving vertical motions to the mirror proportional to the changes of magnetism.

The samples to be tested form the arms of DD. They may be solid rods, or rods built up of thin strips, or of wire. The rods supplied with the instrument are of soft sheet-iron, built up of insulated strips, with a net cross-section about 1 in. by \(\frac{1}{2} \) in., and about 18 in. long. In preparing other rods for comparison of magnetic quality, the same dimensions are to

be chosen as those of the standard rods. Clamps are provided at the pole-pieces to allow the rods to be readily inserted and removed.

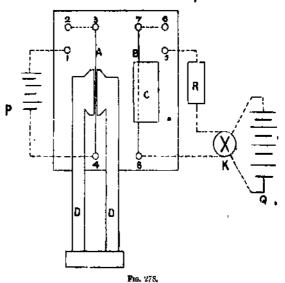
The same constant current will serve for the wire AA, and

the magnetizing coil of the tubular magnet C. A current of about four ampiers will serve well, but more or less may be used, according to the amount of movement which it is desired to give to the mirror. The amplitude of the movements can also be regulated by shifting in or out the weights on the bell-crank levers which keep the stretched wires tight. For high-speed work the wires should be kept very tight, and a small mirror should be used. The magnetizing current must be made to vary in a continuous manner; not by sudden makes and breaks. When these precautions are taken magnetic cycles may be performed so rapidly that the reflected light appears on the screen as a continuous curve. A special commutator is supplied, to allow if rapid but gradual variations and reversal of the magnetizing current. It consists, essentially, of two fixed and two revolving

plates of zine, immersed in a solution of zinc-sulphate. In ordinary testing it is more convenient to make the magnetic changes occur slowly, and to mark with a pencil the successive positions of the spot on the screen. A sheet of paper on a small drawing board, set up against a wall or other vertical support, is a suitable screen. The source of light may be an ordinary galvanometer lamp, furnished with a pair of cross wires instead of the usual single wire. For high-speed work a small spot of light is necessary, which is obtained by placing a screen with a small hole in it just in front of the lamp. Horizontal and vertical datum lines are marked by moving (by hand) the wires BR and AA respectively, and marking the path of the spot. A variable resistance is to be inserted in the magnetizing circuit of DD, to allow successive points of the magnetizing curve to be obtained: two zine plates suspended near together in a weak solution of zinc-sulphate, in such a way that they can be more or less deeply immersed, will serve well for this purpose. A rapid commutator is also to be put in this circuit, to allow the specimens under test to be demagnetized by rapid reversals of continuously diminishing magnetizing force, if it is wished to determine the curve of initial magnetization. In comparing other samples

with the standard bars, care must be taken to preserve the same scale of B and of H, by not changing the constant current in the wire AA and magnet C, nor the tension of the stretched wires.

The absolute scale of H may be calculated, if required, from a knowledge of the number of turns in the winding of the number turns in the winding of the number turns in the winding of an anglet limbs, and that of B may be found by means of an



,

auxiliary ballistic galvanemeter, by winding an induction coil of a few turns round one or both of the limbs.

Fig. 278 shows the electrical connections with the terminals as they are placed on the slate base of the instrument.

Terminals 1 and 2 are those of the coil which magnetize the tubular magnet C; terminals 5 and 6 are those of the main magnet coils on DD. The constant current is supplied by P,

and taking the course 1, 2, 3, 4, passes in series through the magnetizing coil of C and the stretched wire A. The variable current is supplied by Q, through the commutator K and adjustable resistance R. Taking the course b, b, b, it passes through the main magnetizing coil and the stretched wire B. The copper strip which is used to connect b with b may be put between b and b instead, b and b being then the battery

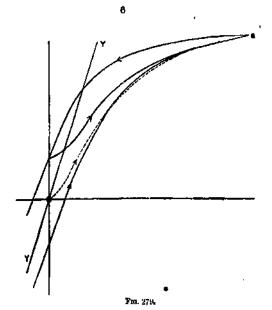
terminals in that circuit. The effect of this is to change the general slope of the figure on the screen from right to left or vice vered. One of the two arrangements is right when an ordinary screen is used; the other is right when the screen is a piece of trucing paper or ground glass, viewed from behind.

Care should be taken to adjust the instrument so that when

a complete cycle of magnetic reversal is performed, the figure on the screen will be symmetrical, with the extremities equidistant from the zero point or origin, which corresponds to the condition of no current in B and no magnetism in DD. To secure this, see that the strotched wires are as many as may be judged in the middle of their respective slots, both vertically and horizontally. Set the mean position of the mirror perpendicular to the pivot needle, by adjusting the needle's position by the screws provided for that purpose. The light springs which keep the connecting threads tant are to be set so that they remain considerably stretched even when the mirror moves to its furthest limit in the direction tending to shacken them.

Fig. 279 is an example of the curves obtained by the instrument shown in Fig. 27c. It is the copy of one half of a cyclic curve of reversal, along with the initial curve taken after demagnetizing the specimen by reversals, and also the curve obtained by reapplying the magnetizing current after it had been reduced from its maximum to zero. Owing to the existence of an air gap in the magnetic circuit under test, the diagram is sheared over to the right, and true values of the magnetic force would be found by measuring horizontal distances from some such line as YY, instead of from the vertical line. This shearing does not affect the crea enclosed by the cyclic curves of reversal, and need not therefore be taken account of in measuring the comparative amounts of energy dissipated by magnetic reversels in different specimens or in the same specimens with different values of the magnetism.

In addition to its use for determining these areas, for comparing the magnetic qualities of different samples of iron, and for investigating the properties of magnetic curves generally, the instrument may be used as a galvanometer by making the



current to be measured pass through either of the stretched wires, while the magnet, in the slot of which the wire is stretched, in kept in a constant state of magnetization. This will be found useful in cases where an extremely dead-heat indication is wanted, and by making the spot of light register its position photographically on a moving plate or paper satisfactory records of rapidly fluctuating currents may be obtained.

The Permeameter.

A useful piece of apparatus, known as the "Permeameter," is illustrated in Fig 280, by means of



Fig. 280.

s, known as the Permaneter, is illustrated in Fig 280, by means of which the magnetic quality of different materials can easily and rapidly be found. The method is essentially a workshop one, and the principle of it is due to Professor S. P. Thompson.

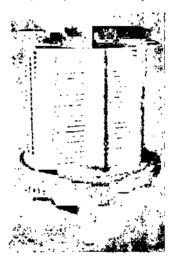
The arrangement consists of a somewhat massive hollow rectangular-shaped block of good soft wrought-iron forged to the shape shown. Inside this is a magnetizing selenoid would on a thin brass tube with thin flanges or ends, its length being just that between the insides of the block ends. The sufficiently long rod of magnetic material to be tested, having its lower end faced quite true, passes freely but closely through the top end of the block, down through the selencid, and beds on the carefully "faced" inside of the bottom end of the black. The pretruding end of the rod has a metal pin

through it, which is caught by a double hock on the lower end of an ordinary spring balance, the top end of which is suspended by a gut cord passing over a fixed pulley and attached to the lever shown. This permaneter is also fitted with an arrangoment for testing the specimen ballistically. It consists of a small flat coil fixed to a brass plate, which slides backwards and forwards between guides. The rod passes through this coil and beds as before on the block, at the same time keeping the coil back against the force of two spring strips on the outside of the

block. Immediately the rod is suddenly pulled up the call files out, and a circuit joined to its terminals will receive an electromagnetic impulse proportional to the field just broken. In this way the ballistic and traction methods can be made to check one another in the final results obtained.

Condensers.

Fig. 281 shows a general view of the Kelvin standard air Leyden condenser, and Figs. 282 and 283 a plan and rectional



Fro. 281.

elevation of the same. The instrument is formed by two mutually insulated metallic pieces, which we shall call A and B, constituting the two systems of the air condenser or Leyden. The systems are composed of parallel plates, each set bound together by four long metal bolts. The two extreme plates of set A are circles of much thicker metal than the rest, which are all squares of thin

sheet brass. The set B are all squares, the bottom one of which is of much thicker metal than the others, and the plates of this system are out less in number than the plates of system A. The four bolts binding together the plates of each system pass through well-fitted holes in the corners of the squares; and the distance from plate to plate of the same set is regulated by annular distance pieces, which are carefully made to fit the bolt, and are made exactly the same in all respects. Each system is bound

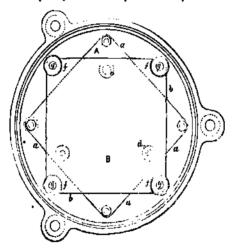
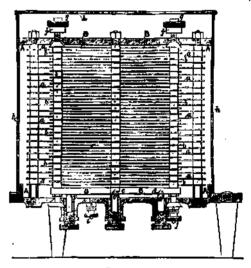


Fig. 282,

firmly together by screwing home nuts on the ends of the bolts, and thus the parallelism and rigidity of the entire set is secured.

The two systems are made up together, so that every plate of B is between two plates of A, and every plate of A, except the two end once, which only present one face to those of the opposite set, is between two plates of B. When the instrument is set up for use, the system B rests by means of the well-known "hole,

slot, and plane arrangement," I engraved on the under side of its bottom plate, on three glass columns, which are attached to three metal screws working through the sole-plate of system A. These screws can be raised or lowered at pleasure, and by means of a gauge the plates of system B can be adjusted to exactly midway between, and parallel to, the plates of system A. The complete Leyden stands upon three vulcanite feet attached to the lower side of the sole-plate of system A.



Fra. 283.

In order that the instrument may not be injured in carriage, an arrangement, described as follows, is provided, by which system B can be lifted from off the three glass columns and firmly clamped to the top and bottom plates of system A.

The bolts fixing the corners of the plates of system B are made long enough to pass through wide conical holes cut in the top and

Thomson and Tait's Natural Philosophy, § 198, example 8.

bottom plates of system A, and the nuts at the top end of the holts are also conical in form, while conical nuts are also fixed to their lower ends below the base-plate of system A. Thumbscrew nuts, f, are placed upon the upper ends of the bolts after they pass through the holes in the top plate of system A.

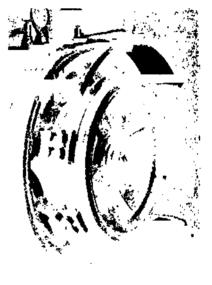
When the instrument is set up ready for use, these thumbscrews are turned up against fixed stops, g, so as to be well clear of the top plate of system A; but when the instrument is packed for carriage, they are screwed down against the plate until the conical nuts mentioned above are drawn up into the conical holes in the top and bottom plates of system A; system B is thus raised off the glass pillars, and the two systems are securely locked together so as to prevent damage to the instrument.

A dust-tight cylindrical metal case, h, which can be easily taken off for inspection, covers the two systems, and fits on to a flange on system A. The whole instrument rests on three valcanite legs attached to the base-plate on system A; and two terminals are provided, one, i, on the base of system A, and the other, j, on the end of one of the corner holts of system B.

Revolving Contact Maker.

This is an arrangement of two contact levers or spring strips, . and a revolving ring, whereby electrical contact is made between the two strips once every revolution of the ring at a certain particular and definite instant, and place on the circle of revolution depending on the position in which the levers touch the ring. Such an arrangement is necessary when it is desired to take the periodic E.M.F. and current curves of an alternator, and it may be fitted either to the alternator, or to a small single-phase synchronous alternating current motor, to be driven off the particular supply to be sampled. Fig. 284 represents a simple and convenient form of revolving contact maker, designed by the author and fitted to the rotating inductors of an inductor alter-It consists of a brass frame ring screwed to the alternator portion, and carrying an abonite ring acrewed to it securely by set screws through the inner edge of the frame ring. Half the total width of this ebonite ring is turned nearly away and a brass ring slipped on and fixed to the aboute ring by

sorews passing through it sideways. A thin slip of brass (seen just in front of the spring brushes in Fig. 284) is neatly let into the ebonite ring and makes electrical contact with the insalated brass ring only. Two spring strips, insulated from one another, and pressing against the two springs in a line, are carried by a holder capable of being slid along the curve baracen in the figure



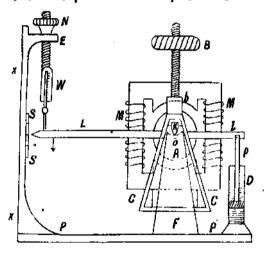
Pio. 284,

and provided with a pointer moving over a scale. Hence any circuit connected to these strips or brushes will be closed once every revolution at an instant in the period which depends on the position of them on the curved rod.

If the toes of the spring brushes are set, one in front of the other, the contact will be more instantaneous, otherwise it will last during the whole time required for the slip contact to pass under the brushes when sot level.

, 'Cradie Absorption Dynamometer.

In Fig. 285 is shown the principle of a typical form of oradle absorption dynamometer, suitable for testing the horse-power developed by small motors, but which can also be employed for larger powers up to a certain limit determined by the weight and



Fra. 285.

size of the motor, and the consequent difficulty in constructing the dynamometer.

It consists of a light framework (CC) carrying a small floor or platform at its lower extremities to which the motor M, to be tested, is bolted after being packed up so that the centre of its shaft is a line with the points of bearing O of the kuife edges K. The steel planes on which K work are at the top of standards F carried on a light bed-plate PP. A block (δ) is attached to the

top of the frame cc, which carries a screwed bolt on which can travel a heavy belance weight B. By raising this weight, therefore, the centre of gravity of M, its bed-plate and the cradle CC can be raised to the level of O. A light lever M is fixed to and moves with CC, one end being attached to the piston (p) of a dash-pot D containing some viscous fluid for damping the motions of the cradle cc.

The other end is attached to the lower portion of a suitable spring balance W, itself supported from a bracket E, carried by a standard (xx).

The end of the lever L moves in front of an index scale as, also carried by xx.

The tail rod l, together with the piston p, are made to, once for all, balance the other part of the beam L, so that after B is properly adjusted the cradle with its motor would rest in equilibrium in any position if W was disconnected from L.

The method of procedure is therefore as follows—When the cradle is exactly balanced in the manner indicated above, the spring balance W is attached to L and the nut N scrowed up or down so as to bring the lever L to the zero of the index scale SS. The motor M is now connected up so that the field magnets and consequently the cradle tend to turn counter-clockwise. This condition must be arranged for beforehand, and the motor placed in the cradle accordingly, to suit the orthodox direction of lotation of the armature A.

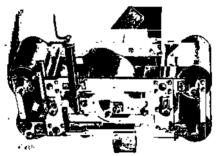
A cord is now wrapped once round the motor pullby, and its two ends stretched out horizontally. The motor will thus be made to do work against the friction between the cord and pulley, and the result will be a depression of the end L of the beam. Then bring L back to zero on the index scale by turning N and so raising the balance W.

If now W=reading of the spring balance in lbs. (say), and L = the distance in feet of its point of attachment to the lever, from the centre O, then the moment of the force resisting rotation, i.e. the torque T=WL (pound feet), and if the speed of the armature = a revs. per sec., the angular velocity $\omega = 2\pi n$.

Hence the work done per sec. = ωT , and the horse-power developed = $\frac{\omega T}{550}$, since 1 H.P. = 550 ft. lbs. per sec.

Horse-Power Transmission Dynamometer.

When the mechanical power required to drive some particular machine, as for instance a dynamo, is desired to be known, it can be obtained by means of a transmission dynamometer. This is an applicate for measuring mechanical power without absorbing any of it, as distinguished from the absorption dynamometer which measures the power by wasting it all. There are two main the transmission instrument, namely, those for measuring the power transmitted directly through a shaft, and secondly, those for measuring the power transmitted by a belt.

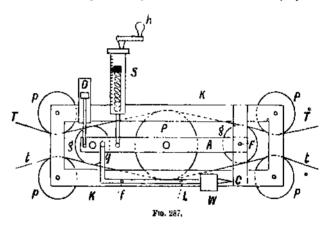


Fag. 286.

Fig. 286 represents the general view, and Fig. 287 the symbolical side elevation, of one belonging to the latter class and made by Messrs. Siemens Bros. and Co. of London. By means of it the difference in tension (T—4) between the driving (i.e. the tight) and slack sides of the best can be read off directly in pounds, and which is the only one troublesome factor required of the horse-power to be measured.

Referring to Fig. 247, this Siemens transmission dynamometer consists of four similar roller pulleys, running in bearings carried at the four corners of a light but strong iron framework (KK). Three other roller pulleys run in bearings carried by the arm or

frame (A), which is capable of oscillating about a fulcrum F on part of the main frame. The centre pulley P is really the actuating part of the dynamometer, the remaining $\sin x$, nawely p and g, merely acting in a sense as guide pulleys for the balt, the "tight" or driving side of which is TT and the slack side tt. The left-hand end of the arm or frame A has attached to it a link (l), which actuates a lever pointer L capable of moving on a fulcrum (f) over an index scale C, and carrying a balance weight W for the purpose of balancing the arm A with its fittings, etc. D is a dash-pot to steady, what would otherwise be, the jerky



movements of A. A strong, spiral spring S, capable of being extended by turning a handle (A), is attached to the left-hand part of A. The action of the dynamometer will now be fairly obvious, and is as follows—

The tight side of the belt TT tends to force down the left-hand end of A against the smaller upward force of the clack side tt, this causes L to turn about f in a counter-clockwise direction; but L is now brought back to zero by turning (h), and when this is the case, the force exerted by S just balances and is equal to the difference in tension (T-t), and is read off on the scale over

which the pointer, attached to the top end of S, moves. Thus according as to whether S is additionated in this, or kilograms so the quantity (T-t) is read off in these units. If now V= velocity of the belt in ft, per min, as obtained from the noted speed of the driven pulley (N) revs. per min, and its diameter d (ft.), then $V=\pi dN$, and the H.P. transmitted $=\frac{\pi dN}{33}\frac{(T-t)}{33}\frac{(T-t)}{33}$

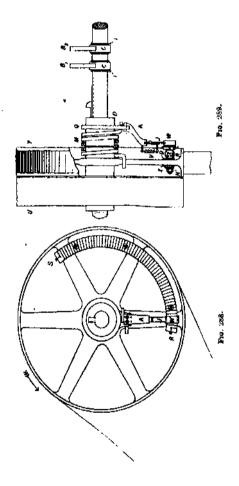
The Measurement of Power transmitted by Belts.

In the case where it is desired to measure the mechanical power absorbed by some particular machine, such as, for instance, a dynamo feeding a lamp circuit, or any other kind of machine driven by means of belting, the use of a form of Prony brake or other kind of absorption dynamometer is inadmissible, owing to the well-known fact that such an appliance wastes all the power which it measures. In this case a transmission dynamometer has to be resorted to, of which there are several different forms, some remaining permanently in position, so as to be capable of indicating at any moment the power transmitted, others being temporarily erected in position for the tests us, for instance, the ^oSiemens-Hefner-Alteneck belt transmission dynamometer. It is, however, manifestly more convenient to have a permanent arrangement, and the general principle of this type is to connect the driving pulley, which is loose on its sluft, by three or more helical springs, to a fixed collar or boss keyed to the shaft, and then to measure in some convenient way the "angular advance" of the shaft relatively to the pulley, due to the axial extension of the springs. This, as is well known, gives a measure of the power transmitted. Hitherto, however, the arrangements for observing this angular advance have not proved very satisfactory.

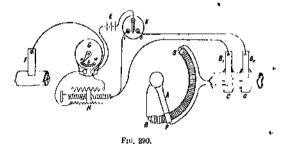
By the kind permission of the proprietors of *The Mechanical Engineer*, the author is enabled to give a reprint here of an article written by him in that journal of March 19, 1898, on a neat form of spring transmission dynamometer the recording arrangement of

which was devised by Professor W. Stroud some little time back, and is in use in the electrical engineering laboratories at the University, Leeds. It is accurate and extremely simple both in principle and working, and can be easily fitted to any shaft and kept permanently in position. It has the distinct advantage that the measurement of angular advance is solely an electrical one, and can consequently be obtained with considerable accuracy.

Fig. 288 shows an end elevation, and Fig. 289 a side elevation, of the arrangement, with the lower part of the driving pulley (y) out away. It is on a counter-shaft, and rotates in the direction of the arrow (Fig. 288), driving a machine. It consists of a boss O, which is keyed to the shaft, and is provided with a flange Q, having an extension at one part of its circumference in the form of a short projection or arm. One end of the steeldriving spring M, which is of square cross-section, is bent so as to partly embrace this arm and be driven by it; the other end is similarly bent, only in the opposite sense, to partly embrace one arm of y, which is loose on the shaft, and drive it. Only these two bent ends of M are shown in Fig. 289, two turns being cut away, as shown, in which is a part sectional elevation about a vertical diameter through shaft centre. The bolt can be thrown on to a loose pulley (u) by a fork not shown. To the short projection on the flange Q (Fig. 289) is holted a light but strong bent arm A into a saw-cut, in the end of which are sweated ' the ends of two rigid strips of brass side by side. The right-hand one ends in a hinge, which carries a similar strip J_i into the side of which is fixed a rigid pin, which passes freely through a slot cut in the end of the left-hand fixed strip. This latter is merely for the purpose of preventing J being pulled too far towards the pulley (y) by the spiral spring V. The hinged strip J carries at its end a light brass block W, to which is attached, but electrically insulated from it by means of abonits or vulcanized fibre (D), a rounded brase contact block . This makes electrical contact with a curved resistance frame HS, consisting of a curved piece of wood of somewhat smaller radius than the pulley rim, and of section something similar to that shown at R (Fig. 289). It embraces an angle of about 120 deg., and is provided with shallow saw-cuts on the inner and outer peripheries. Into these are

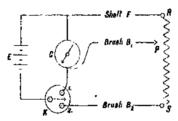


pressed the turns of wire with which it is wound, consisting in the present instance of between 280 and 300 turns of No. 18 or No. 20 Ji. W. G. platinoid wire, double silk covered, the ends being led out to brass terminal blocks at the extremities R and S. The arrangement is securely clasped to the arms of the pulley by the counter-anak bolts R, which pass through a similarly curved piece of wood of section shown at X (Fig. 289), placed on the other side of the arms. A thin piece of soft insulating material (B) is interposed between these latter and R to prevent some of the turns of wire being short-circuited, and thereby rendered useless, or damaged by pressure against the arms. The turns of wire are bared of their silk insulation, along the line on which T makes contact with them between R and S. Two thin strips of



vulcanite I I are bent completely round the shaft, and over them are stretched two thin strips of brass CC, the ends of each being soldered together so as to form continuous rings, against which, as they rotate, press two small copper ganze brushes B_1B_2 . It now remains to describe the method of indicating the angular advance, and so the measure of power transmitted. This is accomplished wholly electrically, a symbolical diagram of connections being shown in Figs. 290 and 291, corresponding parts being lettered alike. The brass rings CC are permanently and electrically connected by insulated copper wires to S and T, as shown, the shaft and arm A being depicted as taking up a position P on RS in advance of the pulley (Y). E is in electric connection with Y, and therefore with the shaft. F is a fixed brush, which

simply rubs on and makes contact with the shaft. K is a two-way key; E a buttery of about three cells, preferably secondaries; G is a sensitive galvanometer or potential difference indicator, as dead beat as possible, and preferably of the moving cell or D'Arsonval type, in order that, firstly, its deflections may be directly proportional to the potential difference at its terminals; and, secondly, that by winding the moving cell on a light but broad aluminium frame, it can be made very dead beat. G is provided with a "constant total current shunt," shown symbolically at H (Fig. 290), which is for the purpose of adjusting the sensibility of H, to which it is shunted without altering the gross resistance of the combination, and therefore the P.D. between the two points to which it is applied.



Fio. 291,

The principle of action of H is merely that the scrow, fixed as regards end play, when turned, actuates the contact block, rubbing between the top and bottom resistances, which are suitably proportioned to one another and to the galvanometer as well. The resistance between the terminals of the combination should be at least 20 times that of HS.

In starting the calibration, switch the lover of key (K) on to stop 1 (Figs. 290 and 291). G is then directly across E, and the number of cells together with the sensitiveness of G (by using H) should be adjusted to give a full scale deflection. This must always be re-obtained before starting subsequent tests. Now, switch to 2 on K, so completing the main circuit by way of F, shaft, R, S, B_{m} , K, E, and back to F. A certain current will flow,

depending, of course, on the total resistance and pressure at E, and for this current a definite P.D. will exist between E and E, and also between E and E, causing a deflection on E, as shown. The calibration is now finally effected by hanging known dead weights from the face of pulley (Y), thereby twisting up E (Fig. 26.1), and noting the corresponding deflections on E. The mean not pull with any particular dead weight will best be obtained by taking the mean of two readings on E, corresponding to the two extreme positions of equilibrium of the pulley, this latter being helped to take up these positions.

Fig. 292 shows two calibration curves A and B, for two totally distinct transmission dynamometers of this type, every detail in each being precisely the same with the exception of the springs M, being different as regards number of spirals and area of crosssection of these only. A few details about these may be worthy of note. The spring of the dynamometer giving curve A (Fig. 292) consists of three complete turns of tempered steel of normal internal diameter = $6\frac{1}{16}$ in., and square cross-section = $\frac{1}{3}\frac{1}{9}$ in. $\times \frac{11}{39}$ in. A pull = weight of 50 lbs. at the pulley face wound it up tight on the surface of the bosses $5\frac{1}{2}$ in, diameter, giving a deflection on G of 9.1 (10 being full). This result is clearly shown by the bending of the curve at the top park. The spring of the dynamometer giving curve B consists of five complete turns of same diameter. but equare cross sections = 1 in. x 1 in. Its internal diameter was approximately 1 in. in excess of that of its bosses (51 in.), for the largest weight used (180 lbs). Hence, not being tight up, there is no bending of the curve B. The turns of both springs nearly touch.

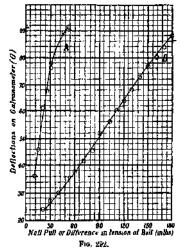
It may now be useful to note, with regard to the design of such a helical spring, the relation that subsists between the pull of the weight at the pulley face, the decrease of the diameter of the spiral, and the angular deflection of one end of the spring in a plane perpendicular to its axis, represented by the position or the point of contact P (Figs. 290 and 291) on RS. Let W= dead weight applied, i.e. the tangential force at the circumference of the pulley of radius R.

Then the moment (M) of the twisting couple in a plane perpendicular to the axis of the spring is M=WR. If the coils are quite flat, and their planes at right angles to this axis, there will

be no torsion in the spring itself, and it will be wholly subjected to a bending action due to M.

If $r_0 = \text{mean radius of the helix before } W$ is applied,

r= mean radius of the helix after W is applied, and $\theta=$ angle of twist, i. s. the angle through which it is wound up. Then, since the moment of the twisting couple must just balance that due to the elastic force of the spring when the arm A (Fig 290) has come to some steady position P on RS, we have



 $M=EI\left(\frac{1}{r}-\frac{1}{r_0}\right)=EI\frac{\theta}{l}=WR$, where l= length of the spring and EI represents the flaxural rigidity of the material of which the spring is made.

E being the modulus of clasticity for the material, i.s. tempered steel.

I being the moment of inertia of the section of the material, i. s. for a square.

In the present case, therefore, for square section $I = \frac{b^4}{10}$ where

(b) = length of a side of that square section. Substituting in the above equation we have

$$WR = \frac{Eh^4}{12} \left(\frac{1}{r} - \frac{1}{r_0} \right) = \frac{Eh^4}{12} \frac{\theta}{t}$$

the spring, and angle of twist, $W \propto \frac{(\operatorname{sectional area of apring)^2}}{|\operatorname{length.}|}$ We have also that the deflection or distance through which W

from which it can be seen that for a given pulley, material of

Writing the first equation in another form, we get an expression for the amount of coiling of the spring for a marticular weight W.

for the amount of coiling of the spring for a particular weight
$$W$$
. Thus
$$r = \frac{E F_{r_0}}{r_0} \frac{E F_{r_0} h^A}{\|FR + E\|^2} \frac{E F_{r_0} h^A}{\|FR + E\|^2}$$

W is evidently the nett pull on the circumference of pulley, and if T = tension (in lbs.) of the tight or driving side of the helt, and t = tension (in lbs.) of the slack side; then W = (T - t) = nett pull of belt in pounds, which is one factor of the horse-power transmitted. Also, if the pulley of the machine driven by (Y) is of railius (f) it, and makes (n) revolutions per minute, then, for no stipping of the helt, velocity of belt $(n) = (2\pi f n)$ it, per minute, and horse-power

$${\rm transmitted} = \frac{V(T-t)}{33,000} = \frac{2\pi fn~(T-t)}{33,000} = H_T$$

If the driven machine be a dynamo developing A appears of current at a pressure of V volts on the external circuit at that speed, then the useful horse-power developed $H_1 = \frac{AV}{7AG}$

Its commercial or nett efficiency is therefore =
$$\frac{H_1}{H_2}$$
 100 per cent.

In conclusion, it may be mentioned that the dynamometer forms a simple and accurate means of measuring the horse-power transmitted to any machine, and works very satisfactorily provided there is no skidding of the belts, and also that the spring (V) (Fig. 289) exerts sufficient tension on J to give a good reliable contact between the contact piece (P), to which the trans ring under B_1 is electrically attached, and the curved resistance RS.

Absorption Dynamometer. .

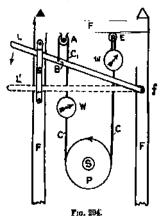
Fig. 293 illustrates an absorption dynamometer which is a modification of a Prony brake for making brake tests of the horse-power developed by electromotors. One great trouble in-



Fig. 29&

harent in all such tests is the high speed (relatively to other prime movers) at which these machines run, especially small once. This tends to cause a jerkiness of the brake and trouble consequently in reading the indications of the various parts. In Fig. 293, three plies of cord make a half-lap over the top side of the brake pulley, at one side supporting a scale pan, and at the other (the nearest to the observer looking at the figure) being attached to a single cord passing round a nearly frictionless pulley and hanging from the lower end of the spring-balance seen at the top of the illustration. This double bend of the cord is merely for convenience in having the balance in a position where it can be read easily. The three plies of cord over the pulley are kept in position by light brake blocks as shown. Thus the weights in the pan will represent the tension on the tight side, and the reading of the balance that on the slack side, so that their difference gives the nett load on the brake. The brake pulley shown is a special form of box pulley devised by the author, and water-cooled by an inlet or outlet pipe passing through a central opening.

Another form of Prony brake, giving excellent results with small motors from about \(\frac{1}{4}\) B.H P. upwards at speeds up to



2,000 revs. per min., is shown diagrammatically in Fig. 294, and consists of a light cast-iron flanged pulley P keyed to the shaft S of the motor to be tested and rotating truly on it. A light

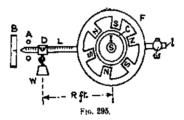
framework FFF carries an eyelet E, from which hangs a spring balance w. From the lower end of w a pliable cord passes 14 times found P and is attached to another spring balance W. From the upper end of W a cord C_1 passes round a small grooved pulley A (supported from F) to a fixed point B on an iron lever Lf. This lever is pivoted at f and is capable of moving in a guide & between the limits L and L. If P rotates counter-clockwise as shown, (W) will send the tension on the tight side, and (w) that on the slack side, of the brake rope C, so that (W - w) = nettpull in lbs., and if (r) = radius of (pulley face $+\frac{1}{2}$ diam. of C) in feet, then the torque exerted = (W - w) r lb.-ft., and the $\frac{2\pi nr(N-\omega)}{33,000}$, where n= speed of P in revs. per min. The ranges of W and w may be as 3:1, and if the face of P rotates quite trady, the deflections of w and W are quite steady and easy to read. The hand pressure on L can be both easily and very gradually applied, and when released, the weight of If raises L and releases P from the pressure of CC automatically a feature of some value in preserving the rops, and a convenience in motors which do not race on removal of load.

Eddy Current Brake.

One of the most convenient methods of measuring the brake horse-power of electro-motors, potrol, and other motors, especially when the speed is high, is by means of an electro-magnetic or eddy-current brake. While the principle has been used in commercial work to an enormous extent in light apparatus, s. y. in electricity meters and instruments, so far as the author is aware, Messrs. Morris & Lister of Charlton Works, Coventry, were the first to patent and put on the market a form suitable for absorbing and measuring the B.H.P. of electro-motors, etc. One of these, used by the author for many years, gave excellent results. Unfortunately the firm have ceased to make them, and it is therefore of little use to describe this particular form. The general principle underlying the construction and action of all auch brakes will readily be understood from Fig. 295.

A cylindrical ring U of copper is fixed securely to the outer surface of an iron drum I keyed to the shaft (S) of the motor, and rotates in a multipolar electro-magnetic field system F_{CC}

Fixed to F, and in a line passing through the centre of S, is a light graduated lever L, from two to five feet from tip to shaft centre, and made of thin aluminium or steel tube. This moves opposite a fixed index scale B between stops A, and carries a light slider D from which known weights W can be hung. A small sliding weight w, which can be clamped by a set screw on a light tail red (I), serves to counterbalance the weight of L and D. A direct current, flowing through the field coils of F, produces a powerful multipolar magnetic field through the gap between I and the poles in which C rotates. E.M.F.'s are therefore induced in C, causing eddy or Foucault current-



to flow in C, which oppose the driving source, and the output of the motor is thus expended in heating C. The strength of these carrents, and hence the B.H.P. of the motor absorbed, depends on the strength of field, which is readily controlled by means of a rhoostat in the exciting circuit.

The force or torque resulting from the interaction between field and currents in G tends to drag the floating field system F round, and this is opposed and balanced by a gravitational force due to the weighted lever L.

When a position of D (at a radius R feet from the shaft centre) in conjunction with the adjustment of excitation, is found, such that the above opposing forces balance, the lever L will float between the stops A. The torque or turning moment (in lb.ft.) exerted by the motor then = WR and its B.H.P. =

 $\frac{2\pi Rn W}{33,000}$ at a speed of (a) revs. per min.

The field frame F can either be carried by a separate support, giving freedom of oscillation, or on a sleeve by the motor spindle itself; but even in this method the weight due to the whole brake is considerably less than the pull due to a bell drive. For example, a 3-II.P. (continuous rating) size, made by Messrs, Morris & Lister, and running at 1,500 revs. per min., weighed 45 lbs., while a 35-11.P. (continuous rating) brake at 250 revs. per min, weighed 250 lbs complete. With a suitable provision in the design for ventilation, such brakes could be used for temperature load tests, but these are more economically effected by one or other of the well-known regenerative methods. brake suitable for a certain H.P. and speed (intermittent rating) will, of course, absorb smaller powers for longer periods, or one for continuous rating larger powers, up to 100%, for short periods. Higher speeds require smaller brakes. Anyone who has used this class of brake will have realized the many practical advantages it possesses over other kinds of absorption brakes, particularly in the matter of sensitiveness, control, smoothness of operation, and accuracy in repeating readings, to say nothing about the absence of wear, burnt blocks, bands, and rope and water-cooling arrangements.

Soames Motor Testing Brake.

This appliance belongs to the class of mechanical power measurers known as absorption dynamometers, and is a modified form of Prony bruko made by Messes. Nalder Bros. and Co. It is of extremely simple construction, and gives perfectly definite weighing of the torque on the pulley under test against ordinary dead weights. It consists of a steel lever working on knife edges, which can be raised or lowered by the hand-wheel at the top of the bruke. Holes are drilled in the lever at equal distances from the centre, corresponding to the ordinary sizes of pulley in use.

The centre of the brake is placed over the centre of the pulley, and from the two holes corresponding to the diameter of the pulley under test is suspended a piece of webbing, which passes round the pulley as in the diagram, Fig. 296.

When the pulley is running, a weight, say from 1 to 30 lbs., is suspended on the end of the arm as shown.

The whoie is then raised by turning the hand-wheel, tightening the belt on the pulley until sufficient friction is put on the belt to raise the arm to a horizontal position and keep it floating the e; the speed of the pulley being taken at the same time.

The weight is hung at either of the two holes at the end of the har marked respectively H.P. $K = \frac{1}{4} \log n$ and Watts $K = \frac{1}{4}$, the one



F10. 200.

hole giving H.P. direct by multiplying weight in lbs. by revolutions per minute, and dividing by 4000, the other hole similarly giving Watts direct by dividing by 6. The constant for H.P. is $2\pi L \div 33,000$, L being the distance of the weight from the centre.

The size of the pulley does not enter into the equation, so long as the distance between the holes in the arm is equal to its diameter.

The band wees, in all cases, be hung from two holes equidistant from the centre.

The pulley should be perfectly smooth and flat, and it is convenient but not necessary to have it flanged.

No intricant is generally required, but a little black-lead may be applied if necessary; no oil.

This brake is extremely accurate, and every reading can be repeated with certainty, each one not taking more than ten seconds at the outside.

TABLES OF

CONSTANTS, LOGARITHMS, ETC.

Standards for Copper Conductors.

(Adopted by the Electrical Standards Committee representing the General Post Office, Institution of Electrical Engineers, and all the leading rable manufacturers of Great Britain.) Revised March 1910.

A wire 1 metre long, weighing 1 gramme, at 60° F. (15.6° C.) has Matthiessen's value of resistance—

0.1539 standard olders for hard-drawn, high conductivity commercial copper.

0.150822 standard ohms for annealed, high conductivity commercial copper.

These figures at 60° F. being calculated from 0.1469 per metregramme for hard-drawn, and 0.1440 for annealed copper at 32° F.
by Matthiessen's formula-

$$R_{t'} = \frac{R_{xt'}}{1 - 0.00215006(t - 32) + 0.00000278(t - 32)^2}$$

Hard-drawn copper is defined as that which will not clongate more than 1% without fracture.

Copper is taken as weighing 555 lbs. per cubic foot at 60° F., and its corresponding specific gravity = 8.912.

The average temperature coefficient is = 0.00238 per degree F. A key of 20 times the pitch diameter is taken as the standard for calculating all tables.

The resistance and weight of conductors is calculated from the actual length of wire, or 1 01226 times the length of the cable for all except the centre wire.

Maximum variation of resistance or weight of any wire allowing for losses in manufacture is 2%.

Az allowance of 1% increased resistance as calculated from the diameter is permissible on all tinned copper between Nos. 22 and 12 gauges inclusive.

The following tables of figures are deduced from the above constants-

TABLE XV. COPPER WEIGHING 555 LES, PER CUBIC FOOT AT 60° F.

Helid Wiren	Resistance in Standard Chins of high conductivity Commercial Copper.					
	Annealed.	Hard-Brawn,				
Resistance per cubic tuch	0-00000066788 0-00000169689	0 000000681327 0 00000178054				
weighing 100 grains. Resistance per mile , per yard , per mil. foot	0·150158 0·042317 ÷area in C'' 0·000024044 ÷ ,, 10·2044	0.153181 0.0431689 + area in Ef 0.0000245277 + ,, 10.4099				

2 0350 x area in □" Weight per mile . 2 0350 × 4 ,, ,, yeld .

The following table refers to copper cables with a lay = 20 times. the pitch diameter.

TABLE XVI.

Cable.	Resistance in Standard Obnu.	Weight.
3-Strend	0:88749 ×=	3 03678×w
4- ,,	0.253065 x+	4 'Q4904 x 10'
7- "	0·1448557×r	7 '07356 × W
12-	0.084355 ×2	12·1471 × w
19- 0	0.0532424×r	19·2207 × ₩
87- ,,	0 0278498×7	37:4414 × 10
61- ,,	0 0165911×r	61·7356 × w
91- ",	0.0111222×7	92·1034 × w

where r=the relatance of each wire, and w = ,, weight ,, ,,, The resistance of a cable being equal to the resistance in parallel of the wires.

International Standards of Resistance for Copper.

Extract from the British Engineering Standards Association Report, No. 7, July 1919.

- The following standards fixed by the International Electro-Technical Commission, have been taken as normal values for standard annealed copper:—
 - (i) At a temperature of 20° C, the resistance of a wire of standard annealed copper, one metre in length and of a uniform section of one square millimetre, is 1/58 ohm (0·017241 . . . ohm).
 - (ii) At a temperature of 20° C, the density of standard annealed copper is 8.89 grammes per cubic continetre.
 - (iii) At a temperature of 20° C. the "constant-mass" temperature coefficient of resistance of standard unnealed copper, measured between two potential points rigidly fixed to the wire, is—

0.00393 = 1/254.45... per degree Cent.

(iv) As a consequence it follows from (i) and (ii) that at a temperature of 20° C, the resistance of a wire of standard annealed copper of uniform section, one metre in length and weighing one gramme, is— (1/58) × 8.89 = 0 15328 ohm.

COEFFICIENT OF LINEAR EXPANSION OF STANDARD ANNEALED COPPER.

2. The coefficient of linear expansion of standard annealed copper between 60° F. (15-6° C.) and 68° F. (20° C.) has been taken as—

0.00000944 per 1° F. (0.0000170 per 1° C.).

DENSITY OF STANDARD ANNEALED COPPER AT 60° F.

3. The density of standard annealed copper at a temperature of 60° F. has been taken as 8.892015, and the weight per one cubic foot of copper as 555.1108 lbs.

RESISTANCE OF A SOLID CONDUCTOR AT 60° F.

4. For the purpose of calculating the tables, the resistance of a solid conductor of standard annualed copper at 60° F., 1000 yards in length and of uniform cross-sectional area of one square inch, has been taken as 0.0240079 ohm.

TABLE XVII.

Relation between E.M.F. and Temperature of the Clark Standard Cell—made according to Regulations, of the Carhart-Clark, and of the Weston Cadelum Standard Cells (see pp. 13 and 17).

Temper-	E.M.	F. in Legal	Volts.	Temper.	B. R. F. 10 Legal Volta.				
*C.	Clark,	Carisart- Clark,	Weston Cadusting.	Weston store Carbert		Carhart- Clark,	Western Cadmium		
4	1-4461	1:4595	1-01893	16	1.4320	1.4885	1-01548		
۰	11450	1:4590	91	17	1 4313	1 4230	49		
	1:4430	1.4855	87	18	1:4807	1 4825] 8⊀		
7	14428	1.4580	B3	19	1.4290	1.4320	ĮH		
	3:4417	1 4376] 79	20	1 4985	1 4855	50		
	1 4404	1:4370	75	21	1 4274	1:4310	26		
10	1.4389	1 6305] 71	21 22	1 4263	1 4 506	99		
11	14381	1.4360	1 66	25	1 4252	1 4800	18		
13	1-4273	1.4855] 82	24	1 4241	1/4295	l 14		
18	1-4963	1.4350	1 50	25	1:4240	14200	10		
14	14951	1 4345	3 64	28	1:4219	1:4255] 05		
15	1:4340	1 14340	1-01850	97	1.4208	1 4250	2-01802		

TABLE XVIII.

RELATION DETWEEN PRACTICAL AND C.G.S. (AUSOLUTE) UNITS.

		Abe	olute C.G.S. units.	Dimensions.			
	Practical units.	Blectro- mag- netic.	Electrostatic.	Electro- static.	Electro- nagnetic.		
Current Potential	I cotilomb 1 ampere 1 voit 2 chra 1 fared 1 second 1 second 1 voit 1 voit 1 joule 1 woker	107 107 108 109 109 100 100 100 100 100 100 100 100	# 10 - 1 - 2 × 10	P-rL P-rL Pgr, 4-1	M ^{\$} 1, \$T - 1 M ^{\$} 1, \$T - 2 M ^{\$} 1, \$T - 2 LT - 1 L - 1, 2 L ML ^{\$} 2, - 2 ML ^{\$} 3, - 3 ML ^{\$} 3, - 3 ML ^{\$} 3, - 3		

==velocity of light=5×10¹⁰ cms. per second.

TABLE XIX.

ELECTRO-CHEMICAL EQUIVALENTS, SPECIFIC GRAVITIES, STC.

Ketal.	Atomic wought.	Ohemical oquivalent at. wt. valency	Electro-chamical equivalent, grains per coulomb.	Weight in grams per hour deposited by 1 amp.	Specific gravity in grama per cub cm.
Aluminium . Copper (monad) . (dyad) . Gold . Iron (dyad) . Lead . Rickel . Biliver . Tin (dyad) . Line . Hydrogen .	27 0 63:1 68:1 198 7 68: 205:4 53:6 108: 117:8 65	9-0 68-1 81-6 68-6 28 103-2 28-3 106 68-0 68-0 82-5	0-00009017 0-00065735 0-00067850 0-00067850 0-0010714 0-0005538 0-001190 0-0001197 0-0003544 0-00010552	0:3354 2:8465 1:1882 2:4410 1:0435 4:8371 1:0994 4:0249 2:1988 1:2112 0:08788	2-67 8-912 8-912 19-8 7-85 11-4 8-5 10-57 7-8 7-15 0 0000096

TABLE XX.

Temperature Coefficients and Specific Resistances of Pure Matals and Alloys, determined by Professors J. A. Fleming and J. Dewar.

Metals, pure, soft, and annealed,	Specific resistance, p, in microhus, per c.c. at 0° C.	Mean temperature coefficient, a, botween 0° and 100°C.	Alloys, ususi proportions.	Brecific realmance, p, in microlome, per c.c. at 0° C	Temperature coefficient, a, at 15°C,	
Patinum Gold Mondiam Silver - Pathadium Silver - Copper Alumniasa Inca 1 - Mickel Mickel - Mickel Sinc - Codmium Lead - Thailium Merchty - Bianuth - Cobatt Tantalum - Tangalum - Comium - Comium - Comium - Comium - Comium	10-917 2-197 10-219 1-681 2-685 12-928 12-928 12-928 12-928 12-928 10-928 10-928 119-160 119-160 19-5	D 003/00 O 007/10 S 006/00 C 007/10 C 004/20 C 004/	Piatinum-ailver , indum Gold-allver Gold-allver Gold-allver Gold-allver Gold-allver Gold-allver Mangaures sissed Meken steel German silver Pintanoid Menganin Mitestone Aluminum-silver he-copter he	21:582 60 386 60	0-00045 0-00043 0-00143 0-00124 0-00124 0-00124 0-00125 0-00010 0-00004 0-00004 0-00004 0-00004 0-00004 0-00004 0-00004 0-00004	

^{*} Approximately pure. Not determined by Floreing and Dewar,

TABLE XXI.

Approximate Specific Resistance of the Commoner Liquids, and which Diminishes with Increase of Temperature about 1.5% per 1°C.

Bolution.	Spessão Resistance (Legal obus per c.c.).	At a temperature (Degrees Cent.),
Sulphulo sold, 5% acid, sp. gr. 1933 " 105 " 1750 " 205 " 1750 " 205 " 1740 " 205 " 1740 " 1050 " 1050 " 1050 " 1050 Counteer sal (colors r) - structed solution Zine sulphate 2 (colors r) Sel-amponiae solution, sp. gr. 197 Water	4 82 2 84 1 74 0 99 1 34 5 10 90 3 82 0 6 50 0 5 × 106 120 × 106	15 ** ** ** ** ** ** ** ** ** ** ** **

TABLE XXII.

COMPARATIVE DATA FOR H.C. COPPER AND ALUMINIUM.

	Į	Copper,	Aluminism.
Conductivity (Electrical) Tensile Sirongth (unamosicd) Heising-Point Specific Grant Specific Grant Specific Grant Specific Grant Feight Weight Tensperstore Co efficient per 1° C.		100 25-50 tonu 1200° Cl b-W 1 1 1 1 0-0428	61-5 12-15 tons 700-11, 2-7 1-56 1-35 0-495 0-495

TABLE XXIII.

. Eureka Resistance Material

A CUPEO-NICKEL ALLOY (SUPPLIED BY THE LONDON ELECTRIC WIRE CO. AND SMITH'S LITD.), PERFARED WITH GREAT CARE TO SECURE A NON-COREODIBLE AND STABLE ALLOY.

SECURE A NUN-CORRODIBLE AND STABLE ALLO
Temperature Co-efficient ... 0.00022 per deg. G.
Blecule Resistance ... 48 Microham per cun cuba.
Gravity ... 8. 8.
Melling-Fourt ... 1250 C.
Comperative Resistance ... 23 times copper.
Tennic Strongth ... 40 coss per sy, inch.
Weight per cubic inch ... 0.32 ib.

Resistance and carrying capacity for "open spirals" of Eureka wire in air, well ventilated with free radiation.

Gauge	Dist	noter.	Approx. Am	Approx. Amps giving temperatures o					
3.W.G.	Inches.	re/m.	100° C.	2(0° C.	800° ().	Standard Ohm; per 1000 yds. a: 64° F. (16-5° t).			
•	192	4:877			ļ——-	29:2			
4	-178	41470			•	\$7.7			
a l	160	4 00	89-0	E2	B8'5	\$87.5			
اقا	744	E-65	26-0	43	ľю́	11.4			
ıń I	129	3 96	23 8	815	41.5	19-8			
11 11	718	2-94	19.0	30	85-5	69-7			
11	104	2-64	1618	24	29-5	79-9			
14 14 16	.092	5-11	12.7	20	24'2	101-1			
14	-060	2.08	9.5	15	19 6	183-9			
76	270	1-89	7%	1218	10.8	165-8			
13	-064	1.63	60	10 4	14.8	300.4			
13	-058	1.43	58	8/8	11:9	378*8			
38	1048	1:11	4.3	פיל	9.1	17T 6			
19	1040 1086	101	80	6.6	6·8 6·9	5X5-6 561-8			
20 21	1053	-811	28	4.7	5 TO	837.2			
21	-028	์ ซีที่	2'8	i i	4.1	1093			
23	*094	'609'	15	2-6	B:3	1467			
94 I	-012	-558	18	9.3	2-8	1770			
95	1020	15/08	1-25	211	2.5	2143			
26 27	·019	457	16	1.68	2·1	2645			
27	Q164	416	.9	147	19	8188			
# [-0148	575	'76	1.87	1.98	1988			
20	-0136	845	-88	1 15	1 47	4634			
90 81	10124	314	152	1.0	1.26	5576 2076			
33	-0709 -0119	1294 1274	1 17	-9 -81	1'05 6 5	6870 7540			
#3	4020	-263	45	74	·65	8571			
84	-0092	-259	-37	164	75	10128			
85	-D684	213	128	*04 *56	-66	12169			
54 87	-0078	199	28	-48 143	167 161	14940			
87	-0069	172	125	-03	11	18584			
99	706	*152	19	1811 26	*49	93506			
89	10069	*192	16	26	'81	81596			
40	10048	191 111	16	%	20	37184			
41	10044	-101	134 18	4 4 1	-16 123	44588 53864			
48	0006	1091	11 10	17	10 17 15	66I38			
#	10032	-081	ß <u>111</u> l	14		\$5044			
#	-0028 -0094	071 061	L 32	19	.10	109045			
47	100t	-050	160 107	7.0	111	148764			

TABLE XXIV.

Nickel Chrome Resistance Material

A High Resistance Allot (supplied by the London Electric Wire Co. and Smith's Ltd.).

Temperature Co-rfficient ,		00042 per dog. C.
Roscido Resintanco		100 Microbins not am amba
Gravity	٠	8 15. 16509 C
Comparative Brautance	:	58 Mines conner.
Tensile Strength		47 12 tons per sq. Inch.
Weight per culvo tuch		79 lb.

Resistance and carrying capacity of Nickel Chrome Wire.

8126		Realstance in S Jule, at temper	Approximate Amperes giving temporatures of				
4 W.G.	200° ().	400° C.	600° ().	200° C,	400° O.	600° C.	
16	452	401	b.78	71	12	18	
17	ÉOI	646	703	80	9-6	14	
16 19 20	Bi₁2	878	957	4.8	7.7 5.7	l ii	
19	1154	1206	1878	87	5.7	6.4	
20	1625	1800	1700	0.3	47	8.8	
21	• 1800	1079	2181	9:7	4.2	8.3	
22	23050	25/3	24.0	3.2	8.6	š·i	
23	8217	3535	3800	1.8	2 8	i i	
14	3826	4167	4555	16	34	ìi	
25	4732	500L	5505	14	ΝÍ	řĩ	
20	6790	#251	6870	14	1.0	5-0	
27	8890	7535	8400	1 10	16	94	
97 98 99 90	8460	9250	10010	-93	14	2.0	
20	10000	10050	11090	78	1.3	1.8	
90	12040	19170	14300	és.	11 .	14	
21	13760	15040	16370	41	*89	1.9	
89	15660	17300 -	18910	-65	180	14	
85	16550	20250	22050	50	71 1	11	
85 84 85	21580	239.20	26100	43	163	-95 -89	
85	20250	29700	9160)	-37	60	-89	
86	82200	86070	84880	-33	49	72	
87	40100	48900	49000	79	48	48 49	
36	å1400 -	56(00)	61270	-21	-34	49	
10	68500	74900	81600	-17	26	-80	
40	80210	87000	85700	-LN	-24	-35	

TABLE XXV.

THE POLLOWING TABLE BEOWS THE CURRENT THAT WILL GIVE CERTAIN ARES IN TRAPERATURE IN VARIOUS GAUGES OF REOSTENE RESISTANCE AND MATRIAL, AND ALSO THE RESISTANCES AND WATTS ABSORBED PER YARD IN EACH CASE (W. T. GLOVER AND CO.).

		56°C. rlı	e in te ature.	mper), rise per ati	IF4.	150°C temp	rise eratu		200° C. Pe	rise iz Paterze	ı tem
8. W. G.	Ohms per yard at 16-5' C.	Obtan per yard at 63.5 C.	Amperes giving a rise of 50° C.	Watta consumed per yard.	Ohme per yard at 115-4° G.	Amheres giving a	Watta consumed per yard.	Ohms per yard at 165 F C.	Amberne graps a. rise of 150° C.	Watta consumed per yard.	Ohms per yard at 215-5" C.	Auguste greing a	Watta consumed per yard.
6	-0641 -0660	10571 10708	99·1 17·6	23·1 22·4		85-0 28-1	05·6 58·0	-048] 10780	99 84	96 90	-0661 0817		183 151
10 11	0845 1024		18-3 18-3	50·3 18·8	1187		48·78 43·70	10084 110	27 8 23 7	76 00 66 7		35-6 30-5	191 116
18 18	·1200 1646	936 974	11:8 94	17.4 15.4	149 188		89 B5 84 85	·160 ·192		81 2 59 8	·157 ·201	2610 11.7	106 85
14 16	-2180 -2470	*230 -285	7·6 0·7	13·8 12 7	·342 ·206	11·6 10·0	82 55 20 60	-254 -311	13-0 12-1	49 0 45 5	-20d -33d	18°0 16°0	80 83
16 17	-2899 -1400	-857 -465	5-7 4-7	II-6 10-3	·377 ·480	8 60 7 90	27 190 25 4	-913 -304		43°4 80°7	:413 :847	19·4 11·3	74 70
18 19	6009 5677	-634 -915	6·0 8·3	10:15 9:38	·8/17 ·963		23 č 22 2	700 1'01		37 8 36 8	188 106	9-27 7-45	68 69
31 30	1.069 1.8628	1·18 1·49	2 64 2 6	9 19 8 94	1 19 1 50	6 25 8 75	2 5 2 1	1-24 1-50		34 2 88 8	1:90 1:65	6190 6190	
21 23	1-7666 1-1030	1-86 2 54	2·15 1·83	8 60 8 50	1-96 2 67		21:4 20:9	2.20 2.20		38 5 35-2	2·18 2·93	6-07 4-83	65-5 65-0
24 25	2:6558 8 4665	8 02 8 64	1.02 1.49	7-93 6 13	3·18 3·35		20 4 20 2	4 84 4 04	8 12 2 82	35.2 35.2	8-60 4-23	8:96 8:67	54-8 64-0
96 97	4 2764 6-1531	4-51 5-44	1·83 1·1	7:65 7:63	4.75 5-72	2105 1184	2010 1914	4198 6 00		31-6 31-4	5-22 6-29	#10 9100	69-9 62-8
98 99	G-8979 7-49 3 8	5 68 7:91	1:07 :98	7·65 7·69	7 09 8 39		10-j 10-0	7·27 8 75		80.7 31-0	7:78 9:14	2·50	90.8 98.9
80	9-01195	9-51	-806	7:61	10.00	1.96	16.2	10 50	1 60	20-0	11:00	\$115	50·8

TABLE XXVI.

Relation between gauges of covered Manganin wire and cubrents giving a rise of Temperature of 100° C, above the Odisida Air (W. T. Glover and Co.).

No. B. W.G	. Атпреттв,	No. D.W G.	Amperos.	No. B.W.G.	Анпретел.	No. B.W.G	Amperes
-	50°6	19	120	22	1.67	92	0.869
3	400	18	9-8	₽ В '	1 1 32	83	0.835
- 6	. BAR €	14	7 97	24	1-008	84	0.51
5	840	15	6 47	25	0.952	35	0 279
	7 50 6	16	8-65	26	O ROT	i 89	0 286
7	25.6		4 68	97	0.077	37	0 209
	22-5	17 18	1 63	28	0.5%	38	0.188
9	190	10	2-00	28 29	Ö 197	[[80	0:167
10	164	20	2-2	80	0.410	1 40	0.148
ii	liào	21	قةا	Bĩ .	0410	II	1

Note — For hore were in air Mr. L. D. Atturous allows 1 eq. in, of total external surface per Watt to be disappated for a temperature of 150° $\bf Q$.

TABLE XXVII.

Showing the Currents that will Produce 212° F. (100° C.) red in Temperature above the Surrounding Air for dare Manganim wire stretched horizontally and freely exposed to the Air (W. T. Glover and Co.).

S. W. C No. Amperes	8	50	10 40	11 85	19 80	19 25	14 20
H.W. G No.	15	14	17	18	8	20	21
Amperes	16	13	10	9	19		6

Nove.—If placed vertically or could, an allowance must be peaks.

TABLE XXVIII.

Densities of Dry Air in las, per cubic foot at different Temperatures and Pressures calculated by the Relation (lbs. per cubic foot) = $\left\{\frac{0.001293}{1+0.00367 \times T}, \frac{H}{760}\right\} \times 62.43$, where T=Temp. in °C. and H=Pressure in mm. of Mercury at 0°C., Lat. 46°, g=980.62, 0001293 = Density in grams per c.c. at 0°C. and 760 mm. Pressure of Mercury. I gram per c.c. = 62.43 lbs. per cubic foot.

Тапр		Baron	etric Pres	oure in X 1	dinekras o	i Mercusy	- п.	
TĊ.	710 miu, 27-95 ia.	720 28-34	730 28-74	740 20-13	750 29-52	700 29-9 5	770 80-31	780 20-70
0 8 10	0-07541 7400 7274 7148	0-07647 7609 7881 7249	0-07754 7017 7460 7346	0-07859 7716 7576 7447	0-07908 7821 7685 7554	0 08072 7930 7764 7647	0-58179 8030 7893 7754	0-08981 818- 2901 784
18 20 25 30	71138 6904 6791	7194 7008 68k5	7225 7008 8086	7823 7197 7079	7425 7500 7173	7821 7993 7974	7617 7419 7307	771 758 746

Table XXIX,
Comparison of Wire Gauges in Comnon Use.

No.	8 W.G. íach.	B,W.O. Inch.	B. & S. Inch.	No.	B.W.G. facia	B W.O.	B. & B.	No	8.W.G. inch.	B.W.G Inch.	R. & S. Inch,
4/0 8/4 0 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-972	- 454 - 425 - 380 - 340 - 300 - 280 - 280	-1000 -1006 -3648 -2648 -2698 -2698 -2694 -2694 -1620 -1448 -1620 -1444 -1019 -0801 -0801 -0801 -0801 -0801	16 10 17 19 19 20 21 25 25 27 29 29 21 25 25 25 25 25 25 25 25 25 25 25 25 25	944 945 945 945 945 952 953 953 953 953 953 953 953 953 953 953	-079 -015 -049 -049 -042 -028 -028 -025 -025 -026 -018 -014 -019 -019	-0571 -0506 -0458 -0458 -0459 -0255 -0255 -0265 -0265 -0160 -0142 -0100 -0100 -0035 -0078	######################################	-0100 -01092 -0184 -0078 -0068 -0069 -0062 -0046 -0086	408 4.67 406 404	-0071 -0003 -0056 -0050 -0040 -0040 -0085 -0040

Photometer Bench.

TABLE XXX.

RATIOS OF SQUARES OF DISTANCES FROM SCREEN TO SOURCES OF LIGHT FOR DIFFERENT DISTANCES (D) BETWEEN THE LATTER (FOR FACILITATING-CALCULATIONS OF CANDLE POWERS).

O.P. to be determined = 0.12, of standard $\times \frac{(D-d)^2}{2^2}$ where (d) = distance between some and shadard.

Norm.—Intermediate values may very approximately to found by proportion, but should be obtained from a surve between d and $\frac{(D-d)^2}{d^2}$ when required more accumately.

{ }			D =						D ==		_
(0 - 0)2	200	800	400	500	600	(P - 29)	200	800	400	500	600
69	4		đ	ď	4	- 42	ď	ا ا	đ	4	8
61-00	20 0 0 5	90°0 0.78	40	60 0 1 25	60.0	17:04	20.0	58.5	78	97-5	117-0
78-67	10	1.5	1 1	2.50	1-5	18.52 15.00	9.5 40.0	9-25	80	875	8.5
68-98	1.6	2.30	1	8.75	4.5	15-61	0.2	00 D 0 76	~~	1100 C 1123	120 0
65-44	2-0	80	1	60	80	18-04	10	1.5	4	175	1·5
62.91	2.5	8.75	1 6	0.25	7.6	14 50	13	1.25		8-75	4.5
10 24	8-0	4.6		7.5	90	14-16	10	100	1 4	80	0
50 ii i	₽6	6-25	ř	8.78	70.5	1874	9-6	876		6-25	7.4
88*77 P	60	6.0	á	60'0	2.0	11.52	80	4.6	i i	7-5	9.0
\$1.81	4-5	6-75	9	1.52	B-6	12 94	8-8	6.25	7	875	180 6
49-60	6-0	715	60	2.2	B-0	12.57	40	60		110 0	2.6
46'51	6 .5	8-25	1	875	8.9	12.21	4-5	6.75	9	1 25	8-5
44-78	8-0	B-0	3	5.0	840	11.87	6-0	7.5	90	2.9	6-0
49-85	0.9	9.15	8	6.52	₽.5	11.22	616	B-25	1	8.75	6.5
41 04	70	40.5	4	7.8	61-0	11-21	6.0	90	9	6-0	6.0
競性	7.6	1-25	ě	8.76	9.5	10.89	64	9.75		6-25	9.2
87.78	8-0 8-6	210	6	10 D 1 25	4·0 5·5	10.56	76	70:5 1:25	4	7-5	141.0
86°21 84°77	9.0	8-6	É	2.5	7-0	10-50	840	120	6	8*78	2.5
85-40	9.5	4 25	•	8.75	8-6	0.754	8.5	275	7	150 0	4-0
#9:11	80-0	3.0	60	6-0	90-0	9407	10	8.5	á	1.25	5-5 7-0
30 es 1	0.5	6.78	ű	6.25	1.5	D-247	9.5	4-25	ő	8-76	8-8
3973	iál	6.5		7.5	8.0	0.00	6010	60	100	5-0	160 0
98-61	1.5	7-25	i	8.78	415	8-686	ĭ	65	9	7.5	1000
97:54	20	8-0	4	80 0	6.0	B-102	· • ·	i i i	- 4	130 0	1
\$6.26	2-6	875	5	1.26	7.5	7 491	i i	9.5	ā	2.5	ē
25-61	8-0	9%	6	2.8	90	7:700	•	810	8	60	109
14-00	3.5	50.25	7	8.75	100.5	6:450	5	2.5	110	70	
125'93	410	1.0	8	6-0	2.0	6-618	4]	40	1	1400	8
25-01	4.5	178	. 9	6-38	846	61295	1	515	4	3.9	171
131-39	570	1.2	70	7.5	610	51985		70	•	5-0	
21.47	6.9	8.32	- 1	8:75 00:0	6-6	6710		8-5		1-9	<u></u>
2076	60	40	3	1.25	8.0	5°44 5°293	60	60.0	120	380-0	160
90-06 19-41	7-5	675 55	- 11	1.20	11110	4-906	1	14		2.5	
18-76	7-6	9.54	- 1	3-76	9.5	1780		4.5		F-5	•
18-17	7.	70	a i	5-0	4-0	4:53		60	3	100-0	192
17.60		175	ř	8-26	45	(41)		75	180	2.5	197
*****	**	1.19	٠,		T"	1 2 at a	•		100	7.3	•

					-						<u>'</u>
- }			D e						₽=		•
n - aba	200	900	400	500	600	(D - 4) ²	200	906	400	600	600
1/2	d	ď	d	4	4	4	ď	ď	ď	4	ď
6 125	6610	9910	134	165-0	108 1	0.0618	159.5	230-25	807	88176	460 1
8941	7	100 5	4	7.5	201	0.0603	4.0	1-0,	В.	6-0	20
8 769	8	3.0		170-0		-0967	4.5	1.76	. 9 .	6 25	9.0
3100d 3145	70-0	315 510	140	3.9	910	10842	6 D 5 S	9·5 5·95	810 .	7·8	5-0 6-2
8-091	25	875	145	181 25	7.5	0929 0-0795	60	4:0	8.	30u-0	840
2 777	60	112-5	150	76	225 0	0778	6.9	4.15	8	1.25	9.
2.500	7.6	6-25	156	193 75	232.5	-0751	70	8.6	ā	2.5	(71)
2-25	80.0	12010	160	200 0	240 0	-0728	7.5	6.25	š	8 75	3.0
2 029	2-5	8 75	165	206-25	7.5	-0707	80	7.0	ē	50	4-0
) (21	6-0	7.5	170	212.5	255 0	0.0065	8.2	7 75	7	6 25	5-6
7 654	715	131 26	175	218 76	262.6	0065	0.0	8-5	8	7.6	71
1'49	00.0	60	187	725 0	270 0	045	9.5	9.26	0	8.75	81
1.250 1.222	6-0	ቤ ተል 142 ቆ	185 190	231-26	7.5	10025 1006	100 0	240 Q	320	400-0	480 (
1.100	7.6	6-26	195	237.5 243.75	285 0 202 6	0.0597	1.0	075 18	1 2	1·25	17
1	100-0	120 0	200	250 0	200 0	0668	1.6	1.26	1	8.75	4-1
0 9045	25	3.75	206	251 25	7.5	10051	20	30	- 1	50	à
0 8185	50	7.5	210	2625	935 0	-0033	25	9.73		6 25	7.8
7407	7.5	161 25	216	206 75	822 5	10515	80	4.5	ě	7.5	94
0-0711	110-0	5-0	220	275-0	880-0	0.0199	3.5	5 25	7	8 75	190 8
-8046	26	8.78	225	281 26	7.5	0489	4.0	6.0		4100	210
0.6461	5-0	172.2	380	287%	\$16.0	-0408	4.5	5.76	9	1 25	8.5
1929	7.5	0.59	230	293.75	362 6	0480	80	7.5	380	20	64
0 44	120-0	180 0	140	800-6	360 0	10125	66	8-26	1	8.72	4.
400	8.0	8-10	245	806-25	7:5	0490	6.0	9.0	2	50	11
0 3601 -8286	7.6	7.5 191.:5	250 255	812·5 8·75	576 0 889 5	'0105	85 70	9.75 250-5	8	0·25	97 501 1
0-29	130 0	5-0	200	826 0	B90 0	0-039L -0377	7-1	1:26	4 5	875	8-2
2778	133	6.5	200	7.6	8	0503	80	10	6	120 0	- 60
2658	وَ ا	80	1 4	C30-0	6	-0849	8-6	1.74	Ť	1 25	64
2557	l ä	9.6	Ιā	25	اةا	0386	9.0	1.5	á	25	10
2425	l i	201-0		60	402	0394	9.5	4.26	Ē	8 75	8-6
2318	5	2-5	270	7-5	1 4 1	03114	170-0	255 0	MO	50	6100
-9217	4	40	3	340.0	8 9	0.0220	0.6	6.10	1	6 25	14
2114	1 1	5.5	4	2.5	411	10288	1-0	6.6	2	7.5	31
2037		7.0		5.0	4	0276	15	7:25	8	8 75	4:1
1026 0:1886	140%	5100 9100	280	7·5	425	-0246 -0254	#10 2.5	6 0 8 75	6	430 0 1 1·25	11
1751	1400	1.2	200	35	370	10244	8-0	9.5	6	3.6	93
1670	1 :	1 10	i	60		-0233	1.5	200 25	ř	175	620
169	1 i	4.5	l ē	7.6	lā 1	-0293	60	70	8	640	94
-1612	4	6-0		860 C	432	10216	4.5	176	ĕ	6.25	31
1489	5	7.5	200	8.0	1	0204	6-0	¥-5	850	7.5	31
1470		9.0	2	80	В	0.0195	6-6	9-26	i	8 75	81
1300	7	220 5	٠.	7.5	66L	0186	60	40		4400	81
1785	8	2.0		870-0	1 4 1	-0177	65	4-75		1-25	93
11172	1.30	3.5	8	1.7	ا ت. [0160	10	5.0	٠.	\$15	691 1
0.1111	160.0	575	820	510	450	40161	7.9	6:25		5.76	\$1 41
-1061 -1062	108	6.5	1	73	1 6 8 0	01:8	80	7.0	1	6.57	š:
1025	13	7-26		B 75	4.5	10138	60	176	1	7.5	73
1000	1 10	80	;	380-0	8-0	0130	P-5	9-25		875	K
-0071	2.5	876	5	1 25	7.5	0 0194	180-0	270-0	800	450.0	840

TABLE XXXI.

Talk bottel lb. Copper. Sections Sec	German Ellver. Remarkance have (approx.) per lh. per 100 ohns. ohns.	Platinoud. Registrance bars	Bureka	Manganin		Reoutene.	
Corporary Bear (Egypers) Corporary Copyright	Remetance bare (approx.) per lb. per 1000 obrus. otims.	Registrance barn	:	-	1		
10 10 10 10 10 10 10 10	per lb. per 1000 yds.	(approx.)	Benistanes.	Besla	Besistanne.	Regist	Registrance hards
15.00 15.0	ohme, ohms.		per 1b. per 1000	00 per th.	per 1000 yde.	yer 1000	Per Ja
10 10 10 10 10 10 10 10	15-059	1941 28-862	otma. otma.	4 obmer	opme	ALT:	de t
### 1951 19 19 19 19 19 19 19	999.81 191.	1808.	793 EL	- ::	11	2 2	í j
### 1949 1940	484 80:305 484 87:703	2965		ij	! i	198-1	i i
1422 5174 547 545 1547 1537 1537 1541 1570 1541 1570 1541 1570 1541 1570 1541 1570 1541 1570 1541 1570 1541 1570 1541 1570 1570 1541 1570 1570 1570 1570 1570 1570 1570 157	<u> </u>	1 9869 178-416	**************************************	201	33.411	161.6	10
18 18 18 18 18 18 18 18		4.85.90 180.538	5-124 15-963		.,-	1884 64.00 64.00	1-213
10.00 19.00	- 020 TEL 100	ㅗ		1000	100	Ţ	394-8
11.77 2 2.00 2.00 2.00 2.00 2.00 2.00 2.00	17-350 254-87						14.456
910 - 12.2 10.2 10.2 10.0 10.0 10.0 10.0 10.0		77-6430 721-368 77-6430 721-368	95-430 836-3	-		1262-8 1766-6	20-684 15-289
256.9 4-70.9 5-70.0 1-1		1-	1	1	1860-48	1	58.98
447 \$94 640-(000-000-000-000-000-000-000-000-000-	1019'60	508-7280 1526-154	625-200 2269			9974	185-568
\$55 199 00794 00710 1877 1877 1877 1877 1877 1878 1978 1979	157.40	1126-2750 2716-40				1-8919	830-930
781. 104. 71-646-41(670-71-71-71-71) 1950 777-4 105-94-8914-90-807-90-34-70-90-90-7-8090 7887 77 1801 1899 1106-96-910 1404-6-672 7104 1801 1899 1106-96-910 1404-96-910 7104-4-8-8-010-8-90-910-910-910-910-910-910-910-910-910-	1851-7	496-414-0 0-64-8da	Ι.,		Į .	6527-9	1045-992
1940 -58 1906 1791 1619 596 196 6573 1940 -58 1906 1791 1619 596 196 5274 15469	2600	THE POST OF THE PARTY OF THE PA				1	14.00
1164 -49 2050 made 2564 638-2 34678	7060-8	021-25-67-27-120 04:08-127-80-640	18984 10725	21307-13 17 24901-20	180600	; :	2001.00
	÷	62502 90518-560	73177		20033-0	 -	10202-07
1219 -21 4800 4865 - 6201 1215 44655	84858 37690	168888 23000-150	01100	0.05070	47130 0	Fi	6979
07:55 8297 31095 2947 428571		784.280 72186	903880 88634	2 1028150	78575-6	:	1 1
- 180 - 1819 - 1	1854415 70798	2468250 126254 A087250 184505	00555800	: :	i i		i

TABLE XXXII.

THE TABLE GIVEN RELOW SHOWS THE SIZES OF VARIOUS WINES OF DIFFERENT MATERIALS WHICH WILL FERS AT THE CURRENTS QUIEN IN THE FIRST COLUMN (SIE W. H. PRECE).

Current	Tin 7	Fire.	Losd	Wire.	Copper	Wire.	Irou l	Tize.
in Amperes.	Diameter Inches	Approx. B.W.G.	Diameter Inches.	Approx. B.W.(1,	Dismeter Inches,	Approx. 8. W.O.	Diameter Inches.	Approx 8. W.G
1 9 4 5	0-0072 0-0118 0-0140 0-0181 0-0910	26 81 98 25	0.0091 0.0128 0.0158 0.0208 0.0358	85 87 27 25	0 0091 0-0084 0 0044 0-0053 0-0049	44 48 48	0 0047 0 0074 0 0097 0 0117 0 0186	40 86 88 81 29
10 15 90 25	0-0984 0-0487 0-0520 0-0614 0-0084	-6384 21 -6487 18 -0520 17 -0614 16 -0684 15 -0760 14-5 -0840 12-5 -0000 12 -0675 12-5		\$0 18 17 13 14	0 0098 0-0129 0-0156 0 0161 0 0205	20 20 20 20 20 20 20 20 20 20 20 20 20 2	0.0216 0.0282 0.0348 0.0398 0.0480	94 93 20-5 19 18-5
36 40 45 60	0-0769 0-0840 0-0009 0-0076 0-1161			18:5 13 12 11:5 10	0-0227 0-0245 0-0268 0-0288 0-0225	94 25 39 59 21	0-0498 0-0645 0-0589 0-0682 0-0714	16 17 16 5 16
70 80 90 100 190	0·1230 0·1884 0·1448 0·1548 0·1748	0·11c1 11 0·1220 10 0·1884 8·5 0·1449 9 0·1548 8·5		0·1237 10 0·1371 9·5 0·1499 8.5 0·1491 8 0·1789 7 0·1064 6		20 19 18-5 18 17-5	0-0791 0-0864 0-0965 0-1008 0-1188	14 18:5 19 19 11
140 360 190 900 800	0-1037 0-2118 0-2291 0-2457 0-2861	6 5 4 8:5 1.5	0 2176 0 2379 0 2573 0 2700 0 8903	6 4 3 1	0.0678 0.0625 0.0674 0.0725 0.0841	17 16 16 15 18 6	0°1955 0°1871 0°1434 0°1598 0°1848	10 9.6 9 8 8.0

Nove.—The above numbers can only be taken as approximate, as the actual current required to free any gauge will depend on the length of fuse and cooling effects of the fuse took in which it is placed.

In Allo-tin diameters 3 % % greater than those of lead fuse at the same currents.

Useful Numbers.

Metres	×	3.2809	=	feet,
Feet	×	0.3048	=	metres.
Centimetres	×	0.3937	=	inches.
Inches	X	2.54	=	ems.
Mila.	Х	0.0254	=	millimetres,
Sq. ems.	×	0.155	-	aq, inches.
Sq. inches	X	0.00155	=	sq. mm,
Sq. inches	×	6:451	=	aq. ems.
Cubic ,	×	16:387	=	cub. n
sı eras.	×	0.061027	=	, inches.

```
Kilogrammes ×
                          2.2046
                                    = pounds.
       Miles
                           1-609
                                    = kilometres.
                     х
       Kilometres
                          1094

⇒ yarda.

                     х
       Pounds (avoir.) ×
                         0.4536 = kilogrammes.
       Gallons
                           0.1604 = \text{cubic ft.}
       Cabie ft.
                           6.2355 = gallons.
       Gallons (water) x
                          10.0
                                   - pounds.
       Oub. fe. ( ,, ) ×
                          62:27
       Metres
                          39.3704 = inches.
                      ×
       Foot
                         30.4797 = cms.
                      ×
       Pounds (avoir.) × 453-593 = grammes.
                           6.2832 = radians per sec.
       Reve, per sec. x
                           0.005 - metres per "
       Feet ,, min. x
       Metres, sec. x 197
                                   = it per min.
  Joules Equivalent - 1390 lb. cent. units
                    = 4.156 × 107 ergs per gram. °C.
  Acceleration due to Gravity (g) at Greenwich
                      = 32.1908 ft. sec. units
                      -981-17 cm. "
  Density of mercury = 13.596 grammes per c.c.
                       \times 0.7373 = foot lbs. per sec.
Waits
Joules (i. s. Watt secs.) \times 10^7
                                   = ergs.
                       × 0.7373
                                   = ft. lbs.
  J1
                       × 0.239
                                   = calorios,
Calorica
                      × 4·158
                                   = Joules.
Ft. lbs.
                       x 1:35
                                   = ft. Ibs.
                      × 7.233
Kilogrammeters
Ft. lbs.
                       × 0.138
                                   - kilogrammeters.
                      × 746
                                   = Watta
Horse-power
                       × 33000
                                   = ft. lbs. per min.
                       × 550
                                        ,, sec.
                       × 76
                                   = kilogrammeters per sec.
                       × 44.25
                                   = ft, lbs, per min.
                       x 01
                                   - kilogrammeters per sec.
H.P. hours
                      \times 1980000 = ft, lbs.
                       x 2685600 = Joules.
Kilowatt hours
                       x 1:34
                                  = H.P. hours.
                       \times 2656400 = ft. lbs.
  Length of circumference of circle radius (r) = 2\pi r = \pi d.
```

Area of circumference of circle radius $(r) = \pi r^2 = \frac{\pi d^2}{4} = 7854 d^3$.

Ratio of circumference of circle to its diam.

 $(\pi) = 3.14159 = \frac{3.2}{7}$ approx. log, $\pi = 0.4971499$.

Base of hyperbolic or Napierian logarithms (= 2.71828 . . . To convert Napierian into Common logarithms multiply by 0.43429.

To convert Common into Napierian logarithms multiply by 2:30258.

Lbs. per yard of pure copper wire = area in sq. ins. x 11 5625. Ohms per yard of pure copper wire at 60° F. (15.5°C.)

= 0.0000244657 ÷ area in sq. ins.

Pounds per 1000 yards + 10 % = pounds per kilometre.

" " 1000 " ÷ 2 = kilograms per "

LOGARITEMS.

_	_		<u> </u>								_		_				_			
1		٠	<u> </u>	•	•	4		•	7	•	9	h	3	a	4	•	6	7	9	9
Ţ	10	0000	\$ ().68	5086	0128	0170	0212	0253	0294	0334	0874	Ī	8	12	17	21	25	29	88	97
T.	11	0424 0792	0453 0620	0492 0004	9531 9899		0900	0048 1004	1058	0710 1072	1106	ŧ	7	10	14	17	98 21	26 34	80 98	#
-1	ii.	1180 1401 1701	1175 1499 1790	1206 1523 1818	1250 1865 1847	1271 1584 1875	1614	1938 1044 1931	1573 1673 1969	1399 1708 1987		3	6	9	12 13 11	15 15 14		28 21 20	26 24 22	なな
- 1	1.8 1.7	2041 2804	2048 2430	2096 2366	21.52 2360	2148 9405		2201 2455	2227 2480	2258 2504	2270 2520	3	5	8		12	16 15	18 17	21 20	24 27
-1	10.00	\$568 2768 6010	2577 2810 3032	2888	2825 2856 8076	2848 2878 3096		25% 20% 3180	2718 9045 9160	2742 9967 8181	2765 2060 3201	9	4	Ţ	9	11 11 11	14 15 15	16 16 15	18 18 17	21 20 10
- 1	빏	8 923 8424	8948 8444	3268 3464	8994 8463	8804 8609	M224 B522	9345 8541	8563 8560	8585 8519	8404 3508	97.02	:	6	8	10 10	12	14		19
-1	\$5 \$4 \$5	3617 3802 8979	\$636 \$820 \$697	3665 8838 4014	8856 4011	8892 8874 4048		3749 3909 4082	8747 8917 4099	9766 9015 4116	\$784 \$002 4133	2	4	5 5	7	900	11 13 10	13 12 12	16 14 14	17 16 15
	*	4150 4314	41.66 4530	4188 4346	4930 4352	4316 4378	6232 4398	4249 4409	4905 4425	4281 4440	6393 645U	2	9	5	ì	8	10 9	11	29 29	16
	*	4473 4624 4771	4497 4439 4786	4002 4654 4800	6518 6680 6814	4083	4548 4898 4848	4564 4715 4857	4510 4728 4871	4564 4749 4888	6757 6757	1	8		Ü	8 7	9	11 10 10	12 12 11	16 13 13
١	댎	4914 6051	4928 6008	4942 6078	4955 5092		4988 BLIG	4997 6732	5011 51(6	5096 6169	6088 6172	1	5	į	8	ī	8		1 t 21	12 12
	X	5185 8916 8441	6338 6338 6463	5911 5310 5105	5294 5353 5478	5257 6356 5490		6203 5301 5514	8:276 8408 8527	5289 5416 5589	5302 5428 5651	1	3 2 8	4	ā ā		8	9	10 10 10	12 12 11
Ì	×	5568 5683	8578 5004	5587 5706	6609 6717	8611 8729	5623 5740	5035 5753	6647 5703	5688 6775	5670 5786	1	ě	3	5	8	7		10	11 10
0	## ##	6798 5911 6021		6821 4035 6019	5888 5944 5058			6886 6977 6065	5988 6096	8888 4009 6107	5899 5010 6117	1	101	3 8		5 5	7	8		10 10 10
ļ	41 41	6128 6282	6138 6249		6160	8170 8274	5180		8201 6804	6919 (614	6223 6325	ŀ	9	ŀ		5	6 8	7	8	9
}	444	6384 6456 6653	6845 6444 6542	6355 6454	6566		8888 8484	6400	6405 6503 6599	6415 6513	6495 6699	1 1 1	2			5 5 8	5 6	77	8 8 8	D D
	- -	8629 6721	6837 6780	6046 0789	6656	6668 6768	6676	6684 6776	9603 6765	6701	6712 6808	į	2	9		å	;	7 6	7	8
	¥94	6513 6903	6821 6811	0830 6930 7901	6889 6928 7016	6848 6927		8960 0955	6575 6964	6884	6898 6081	i	2	;	1	1	5 5	5	7	8
	12 12	7076	7084	7000	7161 7165	7170	7118	7126	7386	7168	7188	ĺ	:			1	å	6	7	8
	121	7248 7824		7260	7287	7276	7264	7999	7800 7800	7806	7816	i	2	9		14	5 5	6	6	Ť
	느		<u> </u>	ı	<u> </u>	ا		·	<u></u>		!—	11_	_	_		<u>' </u>	1	_	Ц,	

		'				IA	JUAH	ITHE	18.								٠	ŗ	
	•	ī	*	•	4	ŀ	8	7	1	•	1	,	•	4	5	ļ	7	•	
H	7404	7412	7410	7497	7435	7448	7451	7469	7466	7474	1	•	2	8	١,]-	δ	đ	
#	7489	7490	7497	7605	7518	7590	7528	7586	7543	7851	lı	2	2	8	lı	l۵	6	6	
F7	7569	7686	7574	7583	7589	7597		7819	7619	7627	1	F	8	8	4	ō	3	6	
胡林	7684	7642	7649	7667	7004	7072 7745	7979	7066	7004	7701	ļį	ij	2	ā	!	14	5	ĕ	
ö	7709 7782	7716 7780	7792 7793	7908	7788		7752 7825	7700 7822	7767	7774	ŀ	1	2	8	l:	ľ	5	ŝ	
Ц	7658	7860	7668	7878	7881	7689	7896	7908	7910	7917	١,	1	2	•	l	ļ،	4		
ä	1634	7951	1000	104	7952	7959		7978	7080	7087	۱í	û	é	i		Į;	3	å	
6	7003	B000	6007	8014	8021	6028		8041		8055	ī	i	ã	i		li.	ă	š	
Ж	2009	806P	8078	8082	8089	8096	8109	6109	8116	6122		1	9		ı	4	8	Ā	
W	8129	813 4	8149	8149	80.00	8103	9109	8170	8182	8189	Ì	1	1	•]*	ŀ	ð	ā	
10	8198	8201	escs	8216	8223	8238	8935	8941	B248	6254	1	ı	,		1 2	4	5	5	
₫.	8581	926T	8974	8280	8297	8103		8500	8312	8219	1	1	1			!!	5	ā	
	8325 8338	6331 8895	8988 8401	8844 8407	6351 8414	6867 6490	8863 8435	8970 6482	8376 8489	8146	1	i	:	;	3	Įį.	4	į	
	8451	8457	3468	8470	8476	6482		6494	8500	8606	i	i	•	i	ì	1	1	5	
п	8013	BÖTE	8558	8657	8557	8415	SMP	9555	8561	8367	١,	1	,	,	١,	l.	4	5	
7	8678		8585	8091	8517	8808		8813		8627	li	i		i	li	1	ā	ĭ	
ř	8684	6689	8545	806L	8057	8668		8075	6681	BOSD	ī	ī'	1	3	i i	14	41	š	
н	8602	8004	8704		87 La	6722			8739	8745	1	ī,	1	2	Į.	4	4	Δ	
•	etes	8766	6103	8768	8774	8779	8 766	87PE	8797	8502	1	1	1	1	4	8	4	5	
N	6806	8814	8820	8825	883]	68.57	8842	8848	8554	8850	ļ	1	1	1		3	4	ş	
77	6868 1209	8871 8927	8876 8932	8881 8998	8887 8048	009	8859 8859	8904	4010 8065	8618 897 L	1	1	2	1	å	!!	*	•	
ï	9978	6952	8987	8023	8008	P004		9015		5095	ì	i	;	ž	8	3	4	4	
ō	9081	9036	P043	9047	9064	9068	2063	9069	9074	9079	ī	î	ā	3	ă	ī	i	è	
а	9065	9090	9008	9101	#10e	9119	P137	91. 23	p198	et eu	1	1	,	2	ı	8	4	4	
	D188	9148	8148	9154	9189	9 765	9170	P175	0180	9188	ī	1	1	2	3		4	4	
ă.		9196	9201		9439		9222	9257	9332	9288	ij	1	3	\$	8	8	4	4	
×	9943 953 L	9148 9196	9\$5\$ 9804	9958 9509	4916	9890	9125	9279 9880	9284 9385	P280 P840	H	1	2	2	3.	8	:	•	
_											ľ	-1	ž	*	! *`	ľ	1	4	
2	9945	0350	9856	9560	9488	9870	9378	9850	9886	P590	1	1	3	3	3	9	3	•	
7	9395	9400 NJO	9406 9465	9410 9450	9418	9490 9460	0423 0474	8490 0470	9485 9484	9440 9460	2	1	1	2	3	Ľ	!	•	
ï	9414	1400	9504	9500	9518	9518	38	9548	9583	9538	lă	ĭ	1	2	ľ	ı	8	:	
ē	9642	9547	9669	9657	9061	9586	2071	9676		9580	ŏ	i	î	í	ŝ	ľ	i	ì	
ı	6590	9595	9600	9606	9600	9814	9619	9884	9698	9638	١.	1	1	ار	,				
•	9638	9643	9647	9652	0057	9661	9666	9671	9675	9600	ŏ	1	ī	8	12	i	i	i	
ĕ	0000	1009	9694	0000	9700	9708.	97LJ	9717	9792	9727	ļo	3	1	2		ă.		4	
•	978L 9777	9786 9782	9741 9786	9744 9791	9750 9796	9754 9800	9769 9865	9768 9809		0778 9816	8	3	1	9	1	2	3	1	
	1013	(1857)	08.00	9506	66 41		9850	8884	9850	9860		-1	_		,	Į.		Ī	
7	9968	9872	9877	9391	0686	8690	9894	0890	9908	0008	0	i	1	3	1	:	1	1	
ė	POL:	9917	9021	9926	9000	9984	9909	9942	2048	0052	ŏ	ī	1	3	9	i	5	ï	
•	9054	9961	9906	9969	9771	9978	2068	9987	P061	9996	ō	1	1	2	Ī.	ī		i	

ARTI-LOGARITHMS.

	_			_		_	_							_				_		
Ì		٥	1	4	•	4	•	•	7		9	1	•	3	4	6	8	7	,	•
Ì	20	1000	1009	2005	1007	1000	1012	1014	1016	1019	102L	0	0	1	1	1	1	ż	:	1
	98.00	1023 1047 1071	1026 1060 1074	1028 1059 1076	1020 1054 1079	1023 1067 1081		1088 1089 1086	1046 1064 1069	1042 1037 1091	1048 1009 1091	0	0	1	1	1	1	2 2	3 2 2	3 22 2
•	04 05	1096 1122	1000 1148	1103	1104 1180	1107	1109 1185	1313	1114 1140	1117	1119 1148	ě	ĭ	i	î	i	ŝ	3	2	ž
	22	1148 1178	1162 1178	1158 1160	1158 1153	1169 1186	1161 1180	11 64 1191	1167 1194	11 00 1107	1172 1100	0	1	1	1	ì	ă	2	2	2
	883	1909 1280 1250	1286 1288 1362	1938 1938 1966	1939 1958	1215 1949 1271	1216 1216	110I 1210 1247 1276	1223 1250 1378	1955 1958 1989	1958 1986 1986	90	1	1	1	1	2 2	2	2	•
	11	1958 1318	1301 1891	290E 1894	1967 1837	1300 1330	1808 1334	1806 1827	2006 1840	1819 1348		ç	1	1	ì	ŀ	ŀ	8	2	5
Į	11 14 15	1110	1359 1384 1416	1955 1987 1419	1358 1390 1423	1861 1803 1426	1396	1968 1400 1482	1405		1977 1400 1449	000	1	1	1	į	2 2	;	3 3	i
	110	1448 1479	1449 1458	1459	1455 1469	1450 1493	1462 1496	1468 1800	1450 1608	1472 1507	1476 1810	9	1	1	1	ŀ	ŀ	;	3	3
	11	1514	1517 1559 1589	1521	1594	1629 1643 1600	1581 1567 1608	1686 1670	1569	1612 1616 1614	1545	Ö	1	1	1	3	2 2	1	3	3
	휥	1522	1626 1663	1629	1038	2687 1675	1641	2644	1648	1869 1890	1650	è	1	į	9 2	ŀ	3	3	8	:
	# #	1668 1768 1778		1706 1746	1710	1714	1718 1788 1798	1685 1786 1789 1608	1796 1766 1807	1780	1734	Ιá	i	i	2		9 22 8	3	3 5 5	į
ļ	2	1	1824	1828	1885	1887		1845	1849	1854	1858		1	1	•	,	,		3	•
	10 10 10 10 10 10 10 10 10 10 10 10 10 1	1906 1906 1950	1906 1910 1954	1914	1919	1933 1948	1972	18A8 1082 1977	1989	1941 1885	1001	000	1		1	į	3		3	4
	-30 -11	1996	90 id	2061	9050	9061	9065		2075	2080	2064	0	1	1	2	9	'a 2	3	4	4
	13	9089 2189 3189	2143 2143	2148 2196	9168 9208	2156 2908	2168 3318	2168 2218	2178 2238	9178	9188 9284	ľî	1	1	3		;	8		4
1	-11	2589 2591	2206	9201	2007	2919	2017		2928	2253		ı,	1	,	*	ľ		4	:	8
	17	2513 2809 9455	2550 2101 2460		2415		2427 2489	24B9 24B9	2450	9443	\$149	Ιī	1	Ì	1		;	1	1	5
	3	2512 2510	9518 9676	2523	2520	2585	341	2547	9553			ľ	1	1	1	١,	4	4	6	8
	文字字 字	9680 9693	9696 9698 9761	2649	20	2656 2716	9601 9738 9786	5667 9799	2678 2786 2780	2079 \$743	3086 3748	į	i		8 8	į	4	4	8	0
	4	3754 3618	989J 989J	9651 9607	2988 2904	5244 5211	4351	2069	2954	2911		ì	i	3	8	ľ	ì	ě	٥	å
ļ	****	1884 1881 2040	2968 2097	2905 2084	9973 BO41	3048 3048	3065	3012 3012 3013	1902 9002 8003	9006 9076	8018 8088	1	1	1		į	4	ě		ŝ
		3460	300 7	\$106	67.78	8119	C130	11.8	\$141	\$7.40	\$166	1	1	1	,	ľ	-	•	•	4

ANTI-LOCARITHMS.

_										ممسام	_	_	,	_	_	_		٠.	
	o l	1	1	3	4	8	١	7		•	ī	2	3	*	Б	ŀ	7	8	9
1	0 9152	8170	8177	3184	\$102	8159	3206	5214	3221	8226	1	1	2	•	4	١.	5	6	7
1	2 8311		3211 8327 8404	9258 3534 8417	3266 3342 8420	3278 6350 5498	8281 8857 8486	7289 2366 3448	3296 3878 5451	3804 8881 8460	1	20,7	2	88	1	5 5 5	6	4	7
1.5	4 B467	3476	8488 8565	8491 3578	3499 8661	5609 9689	9516 9597	8524 8606	3689 3614	8540 8622	i	2	3	8	4	ě	Ğ	7	17
1	7 8715	3030 2724	3048 3733	8656 3741	9664 8760	5678 8768	808I 8767	8490 8776	5898 8784	8707 8793	į	2 2 2	3	3	4	5 5 5	8	7 7 7	8
1	8890	8811 8890 8990	38J9 3009 8998	3628 8917 4000	\$687 3095 4018	9946 8956 4097	8855 8940 4086	8984 8954 4046		\$653 8972 4064	1	2	3	4	6	5 5	6	7 7	6 6
4	2 4160	6378	4003 4188		4L11 4207	4122 4217		4236	4150 4246	4159 4250	1	2	1	4	5	6	7	8	9
\$	4 4305	4976 4975 4477	4285 4384 4487	4298 4395 4498	4305 4406 4508	4315 4416 4510		4885 4436 4589	4845 4446 4550	4356 4157 4560	l 1 L	2 4	8	1	5	6	777	8	9; 9;
8	7 1677	4581 4668	4692 4699	4608 4710	4018 4721	4824 4782	4684 4742	4646 4763	4656 4784	4667 4776	ı	2	1	:	8	6 7	7	9	10 10
5	1858	4797 4009 5028	4805 6P90 6035	4619 4932 6047	4943 4943 6058		4863 4966 5088	4864 4977 5008	1878 1989 5105	6887 6000 5117	1	2	8	1	6	7	8	9	10 10 11
7		6140 5260	5152 5272	5164 5284	5178 5297	5188 4309	6900 5321	6212 6338	5221 5346	5284 5858	1	2	4		8	7, T	8	10 10	11 11
70	F 2182	ASES 5608 5636	8895 5021 5649	5408 6534 5682	5420	5458	81446 8774 8774	8458 8586 8735	6470 A508 6728		1	8	4	5 5	6	8	9	10 10 10	11 12 12
7	6754	5768 5902	6781 5016	57314 5029	6094	6 82 1	6894 6970	6849 6884	5861 5808	8875 6011	ı	8	:	6	7	B	0 10	11 11	12 12
71 71 84	6026	6039 6180 6334	6035 6194 6339	0067 6209 6368	6081 6220 6388	6095 6297 6888	6109 6252 6397	6124 6260 6419	618B 6261 6427	6762 6296 6443	1	8	4	:	7	9	10 10 10	11 11 12	19 18 18
-81		9171 6002	6486 6637	6501 6655	6516 6688	6581 6688	6548 6629	668) 6714	6577 0780	\$593 6745	3	8	5	î	8	9	11	12 12	14 14
100	6781 6918	6776 6954 7008	6792 6860 7112	0808 6966 7129	68 38 6682	6889 698 1161	6855 7018 7178	6871 7081 7194	6987 7047 7211	6902 7062 7928	2	3	6	6	8	10 10 10	11 11 19	18 13 18	14 16 15
	7844	7882 7480	7918	7998 7454	7831	7828 7496	7848 7816	7862 7584	7879 7551	7806 7568	:	3	5 5	7		10 10	12 12	18	15 16
9 8 9	7586 7762	7803 7780	7521 7706	7888 7816	7555 7884	7674 7880	7091 7870	7700 7880	7797 7707	7748 7925 8110	1 2	4	5	7	999	ii ii ii	12 12 13	14 14 15	16 16 17
1	8128	7968 8147	1080 6166	7996 6186	8017 8204		8064 8841	8071 8260	8091 8279	6299 6492	,	4	6	ï	9	11 11 12	13	18	17 17
8	8511 8710	8807 8581 8780	R356 8661 8780	8976 8570 8770	8596 8590 8790	8414 8610 8610	8483 8630 8801	8468 8650 8851	8472 8670 8872	8690 6892	9 9	4	6	å	ič	18 12	14 14	16 16	18
9		9986 9141	97.62 97.62	9074 9163	2995 9354	901 <i>8</i> 9858	9018 9847	9047 9962	9078 9290	9099 9811	2	4	•	ا	10 13	18 18	15	17 1 7	19 10
2252	9388 9560 9779	9554 9579 9796	9874 9594 9817	9897 9618 9640	9419 9638 9655	944) 966] 9888	9489 9633 9908	0484 9703 9981	9600 9727 9954	9628 9750 9977	2 2	4	7		ñ	11 18 14	15 16 16	17 18 18	90 90 90
L.,	للل						1				١			L	_		_		_

SQUARM OF NUMBERS FROM 1 TO 10,000, CORRECT TO FOUR STORIFICANT FIGURES.

		•	•			- 81	GNI	FICAL	er Fi	QUA:	54.		_							
1		٥	ı	1	•	4	6	•	7	e	9	1	1	а	4	6	•	7		D
	- I)	1000	1020	1040	1061	1083	1102	1124	1145	1166	13%	,	ā	7	P	- 11	19	18	17	19
	51	1210	1282	1,254	1277		1823		1860	1894	1416	9	5		10		14	17		21
	11	1440	1404	1488 1743	1818		1848 1828	1588	1613	1638 1904	1004	3	6		10	13 14	16	18 19		28 25
-	i	10GU	1988		2015	2014	100	2137	2161	1150	1220	l	ŏ				lië	21		27
	u	2250	2280	2810	9341	2872	2400	\$132 2434	2465	2198	2526	4	7	10	13	16	19	22	25	28
	18	2540	2592	2824	2557	5650	2725	9778	2769	2695	9856	ı	7	16	и	17	20	24	27	80
	17	1890	2024	2956	2993	2029	1013	30IM	3183	3168	3204	Ī	7	11	14	18	21	25	28	82
	18	2940	8210	8912	9840		3420		8407	8534	8572	١:			15		23	26	30	34
	19	\$610 4000	2648 4040	8684 4080	8794 4121	4169	1908 1908	4:144	5881 (285	8920 4326	1900 808	1	8				94 25		32	36 57
	_										1	∥⁻	•	`		ľ	1		ļ	
	11	4410	4462	4494	4687 4973		4648 5048		4709	4753	4796 6244	8 5	9		18	22 23		81 30	B4 B(59
	=	4840 5380	4884 5886	4998 6889	5420		5523		8153 5617	5198 5664	6712		10	15	19	2		33	38	43
	H	5760		5850	0406	5056	500B	6052		6160	0200		10		20				40	45
	25	6260	6300	6860	0401	6468	6300	6554	6006	6658	6708	5	11	16	21	26	81	30	41	46
	30	6760	6819	6864	8917	6970	7023	7076	7129	7182	7236	8	13	136	23	97	89	28	49	48
	27	7290	7544	7,998	7468	7508	7683	7018	7678	7725	7764		11		23		31		44	50
	盎	7840	7896 6 L/18	7042 8620	5009 5585	BUCG	8123 8703	9180	8237 8821	8294 8880	8352 8040		13				35	40	48	54 54
	*		9060	8110	9181	0942	1904	9364	9425	9486	9518		13	19	25	šĩ	37	13	49	55
			i					9088	10651)	١,	18	1	26	L	58		51	57
	31. 22	9610 1024	9403 1030	9784 1087	0707 1048		0993 1066		1000	1075	10197	ľí	ï	9	. 8			-		8
	*	1089	1090	1102	1109	1116	1192	1120	1106	1149	1140	1	1	2		1	4		16	6
	22	1150	1163	1170	1176	1153	1190	1107	13404	1211 1282	121A 1289	H	2					6		8
	*	1550	1989	1289	126	1358	سبر	1267	1273	1202	1269	∥,	_	-	•	١.	Ι.	-	1 -	-
	85	1296	1208		1010			1540		1854	1882	1	2							7
_	17 28	1869 1444			1301	1390	1406	11110	1491 1498	1429 1505	1496 1513	ll i	3					8	6	7
•	10	1521	1520			1659	1500	15#3	1576	1584	1492	‼ î	2	9	3	14		ŧ		ż
	10	1500	1608		1024		1640	1048	1666	1665	1073	ľ	3	1	9	1	5	0	7	7
	41	1861	1689	1697	1706	1714	1722	1791	1789	1767	1758	ñ.	2	١,		L	۱,		7	
	a			1781	1709	1708	1800	1815	1828	1892	1640	ņ	2			1	1 6		7	ā
	2	1640	1050		1876	1884	1802 LPRO	1001 1980	1910	1918	1937 2018	R	2							8
	3	1936 2016			2052		2070		2088	2068	2107	lii	ŝ					ř		
	Ι		1			1			1			H.		١.		Ι.	Ι.			
	47	2116		9134 2298	2144	2198	2162	2172 1288	9181 9275	2190 2285	2200 9294	R	2					7		9
	4	280			2333	2348	A51	7504	2972	2361	2901	∥i	2		4			٠,۲	9	
	•	2401	2411	2421	2130	2440	2460	2400		2480	2400	1						7	18	9
	50	2500	2810	9520	2630	2540	₩	2500	2570	2581	2561	יון	8	ľ	•	ľ	1'	7	8	9
	SE.	2001	2611		1032	2642	2053	2668		2588	9604	ļ	•							9
	i	2704	2714	2725	2786		2756	शुक्र		2788	1798	Į,	3							10
	1	\$809 2016			2841 2048			2011		9594 5503	9905 5014	Ηi						8		10
	ì	2000	200	~~	1	1	J	1	1		1	1		1		T`	1	٠	1	
	١	_	·	·	· -	_						_					_			_

Quartes from 1 to 8 contain 1 Squres. Squares from 100 to 310 contain 5 Sq

The differences for squares from 3171 to 3109 are 1, 1, 2, 5, 3, 4, 5, 5, 8.

Squares, or Numbers from 1 to 10,000, Correct to Four Significant Figures.

	0	1	9	8	1	ē		7	•	ø	1	9	В	4	4	ı	7	6	
ij	8025	J 036	5047	2068	5069	3080	8091	8109	8214	3125	1	1	,	ē	8	7		,	
		8147	5155	8170		3192	3204	8226	3994	5288		1	ŧ	ŏ	6	7	Ð	9	
7	8149	9260		8283			8818	8329	J841	8852	1	1	t	ē	5	IJ	8	. 9	
9	848L		8387 8605	8309 8610	5411 6528	8499 8540	8454 8552	8446 8564	8467 8376	8409 8588	lì	;	1	b	6	ł	8	10	
0		8513		3636			8679	8884	2697	8709	i	ŝ	i	ŝ	8	Ť	4	10	
α	872L	878 8	8745	9758		8762	8795	8807	8819	2822	h	ð	4	5			9	19	
8	2844	8466	8924	38B1	3894	8906	8919	888T	2011	8000	1	,	4	8	6		9	10	
3	3 000	8089	8004	1007	4020		4045	4059	4070	4063	Įį.	÷	i:	è	Ţ	١:		10	
4	4096 4255	4100 4258	4192	4134 4264		4160 4290	4178 4903	4180 4516	1390	4212	1	1	1	8	7	å	₽	10	
	4850	4869	4882	4396	4400	4499	4486	4400	4462	4176	١,		l.	ā	7	6	Đ	12	
ř	4480	1502	4516	1529		4558		4588	4597	4610	li.	i	Į.	č	ż	Ьĕ		lii	
	1621	4618	4451	1605	4079	4092	4706	4720	4788	4747	1		4	ā	7	В	10	11	
٠	4761	4775	4789	1002	4816		4544	1856	4871	4886	12	4	4	4	7	8		11	
۰	4900	4914	4928	4942	4950	4970	4984	4906	5018	5027	1		4	đ	7	9	10	13	
1	5041	5055	8000	5084	6098			6141	5156	6170	9	1	4	6	7	Ð	10		
П	5184	5198	5213	5227		6956		5285	5800		3	8	3	6	ļ ?	9		13	
	8829	8844 8491	5858 5506	5578	6398 8585	5409 5560	8417 8685	5680 5680	6446 5594	5461 5610	1	8	5	a	å	8		12	
ì	5478 6 88 5	6640		5670	8086	5700	6714	6780	0746	5761	į	i	5	9	ê	Įŏ	ii	12 12	
8	5776	6791	5906	5892	\$837	5862	6868	5888	5800	5914	9		8	ŧ	8	١,	ji	12	
7	6320	6944	6900		8901	6006	6023	6037	6002	6068	13.	à	6	6	8		11	18	
1	0084 0241	0100 6257	6115 6278	6131 6288	6147 6804		6178 6886	6194 0852	6209 6868	6225	1	1	5	6	8	10		13	
ò	6400	0410	6432	8448	6404	04.90	64.0	6512	6529	8545	i	j	5	ŕ	B			13	
1	655)	6877	Ç598	6610	5016		6659	0676	5591	6708	2	1		7	В	10	12	13	
	6724	6740	6747	5773		0806		0839	6856	6872	2	ā	5	7	8	10	19	18	
	6889		CBAS	CP39	6056		6989	7000	1022	703D	2	3	8	7	9	10	12	14	
1	7066 7298	7071 7948	7000	71U 6 7276	7128 7225	7140 7 3 10	7157 7827	7174 7344	7101 7861	7206 7370	3	4	8	7		10 10		14	
	7806	7428	7430	7448	7466	7489	7600	7517	7584	7563	١,	4	,	7	ı,	11	12	14	
7	7669	7586	7004	7021	7020	7668	7674	7291	7700	1726	Ī	4	Š	7		11	12	14	
å	7744	7762	7779	7797		7809	7650	7968	7885	7903	12	٠	5	Ž		11	13		
8	793L 8100	7980 6118	7967 8186	7974 8154	7002 6172	9195 9195		8326 8326	8044 8044	8062 8503	2	1	6	7	9	ii	13 18	14 26	
ū	4981	8900	9817	6336	8354	8879	8881	8400	8427	8446	2	4	6	7	١	11	18	16	
5	1464	8489	8601	8619	8688	5568	8675	8668	6012	8680	2	ī	ĕ	8	9	11	15	16	
•	8649	POSE	8688	6705	6724	5743	8761		8708		3	4	6	8	20 10	11	18	15	
	8886 8026	8866 8044	\$874 0068	8902 0083	8911 9101		8040 9189	8908 9188	6987 9176	9006 9197	3	4	6	8	10 10	11	14	16 15	
١	9216	9235	9254	9274	9998	9312	9582	98.51	197C	9800	,	Ī	ă		10		14	14	
71	\$400	9458	9448	0467	4487	0.506	9520	9548	1066	0594	17	ï	š	6	iŏ		14	14	
۱	9604	9024	9648	P862	9681	9702	9722	9743	9761	9781	2	ě	å	ē	10	13	14		
ə١	9901	9691	9641	\$860	9880	0000	9020	994D	9960	9980	li	ě	ā		1Ò,		14	10	

RECIPROCALS OF NUMBERS FROM 1 TO 9999,",

· · · · · · · · · · · · · · · · · · ·													_							
Ì		•	,		3	4	5	•	7	•	•	ı	8	3	1	5	•	7	•	•
١	10	0000	100	900t	9700	ģ61A	9531	934	984 6	9310	Š 174	0	18	97	20,	46	54	81	73	81
	냁	6229 6093	9009 8954	8029 8197	8880 8189	6773 8086	8606 8000	8091 7937		8478 7819	840 9 7752	8	18	28 19		88 52	16 38	61 45	61 51	68
-	13 14	7699 7148	7634 7002	7576 7042	19908	7468 6944		7858 0849	7299 6898	7246 6757	7104 8711	8	n	16 14	92 10	27 23	52 25	25 25	48 87	42
-	15 16	6957 6930	6693 6913	6278 6178	6535 6135	6694	6453 6061	6610 6024	5939	!	8289 5017	å	•		17 16	91 19	96 21	29	80 8 F	38
1	17 16	2880 3636	5848 6696	5614	5780 5464		61714 6406	3684		561B	6587 5991	į	6			ĽÓ Ľ4		23 20	20 18	10 26
	19 80	5203 5000	6236 4975		6181 4995	5136 4909	6128. 4878		6076 4881	5051 1606	1095 1765	3	5	7	10 10	18 13		1B 17	81 19	28 21
1	빏	(765 (765	4720 4525	4737 4508	4095 4194	4073 4488	51 43 15 15	4690 4495	4808 6405	4886	4306 4367	2	4	8	9	11 20	18 11	15 18		19 17
ł	H	41.57	489 414 200		4209 4115	497 4098	-001E		4910 4040		4184 4018	8	4	6	7	9	11 10		14	16
	=	#000 #848	8084 8481	2968 2517	8958 8800	8947 6786	3421 3774	9906 9760	5091 5745	9876 9731		1	•	4	Б	7	Ľ	10	11	12
١	# #	8704 8877	8600 82569	8078 8548	8662 8534	3650 3631		2023 8497	3184	8507 8478	粉除	1	3	*	5	6	i	9	10 10	19 11
١	*	6148 6523	다양 보장	849) 881)	\$418 8300	8401 8380	8276 8276	6578 6208	8967 8957	3356 3217	8944 8237	1	3	4	Б Б	6	ŕ	8	i	11 10
ı	絲	8326 8125	8215 8135	2206 2106	8198 8096	8165 9096	#175 5017	3057	5056	8346 9049	8185 8040	1	3	1	5	5	7	7	8	10
	# # #	8050 9941 9861	9091 9988 9849	3012 3994 2841	9008 9016 2888	2507 2507 2535	2985 2899 2817	2076 2890 2809		2959 2874 2798	2050 2005 2784	0	1	2 8	3	4	8	5 5	7 6 7	7
	×	ZITE.	2770	2762	2755	2747	2740	2789	2725	2717	2710	3	•	3	•	4	ŀ		6	7
•	 12 28	\$705 \$482 \$464	2005 9635 2568	2688 2418 2551	2081 2011 2546	2001	2647 2557 2589	2501 2501 2508	2584 2584 2510	26/6 2677 2518	2630 2571 2500	ě	1 2	2 2	3	8	:	5 6 5	8	7 . 6
	40	2500	SADA	2488	2481	2475	2409	2603	2467	2451	2468	Ī	ī	2	3	3.	1	•	•	5
	11	3459 2381 2326	9488 2376 2390	9427 9870 9815	2421 2354 2308	2358	2410 2410 2400	2847	2196 2345 2238	2399 2386 2388	2587 2331 2278	1	1	3	3		i	4	i	0 5 5
1	ä	9278 9292	2508 2511	1969 1911	2257 2208	2239 2208	2917	8100 6244		2232 2182	9297 9179	Ŏ	i	1	ş	8	i	į	i	4
	44 67	91.74 91.98	2169 2123	21.65 21.19	2160 1114	2155 3110	2151 2106	\$146 \$101	2141 2086		2032 2036	8	0	ł	1	;	3	3		4
	ü	9068 9041	2079 2087	9075 9003	5070 5028	2066 2024	9003 9020	2058 2016	2053 2012	2019 2006	2016 2004	į	ì	i	3	2	8	3		4
	an Al	1961	1995	1993	1969	1954	1880 IPAS	1976 1988	1972	1969 1969	1986	ľ	1	,	1	١,	ļ,	8	3	4
	并	1995 1887	1919 1688	1916 1880	1019 1876	1908	1005 1609	1901 1850	1696 1665	1894 1669	1800 1855	į	į	1	1	3	8	3		•
ļ	H	1859	1646	1845	1641	1 85 8	1695	1880	1825	1625	1621	Ľ.	1	1	2	[3	Ľ	8	<u> </u>	3

Reciprocals from 2 to 10=0* Reciprocals from 107 to 1000 =0*00

Nova.—Numbers in difference columns to be subtracted, not added.

. RECIPROCALS OF NUMBERS FROM 1 TO 9999.

			KEC					BKB	FRO			_	20	_				٠	_
	0	1	•	3	4	•	•	7.	•	•	1	3	8	4	5	ŀ	7	٠	•
 5ë	1618	1815	1812	1908	1605	1802	1700	1795	1799	1789	ī	1	1	2	•	[<u>-</u>	ŧ		•
54	1796	1765	1779	1776	1778	1770	1767	1764	1761	1757	1	1	1	1	٠	ŀ	1	:	8
67 68	1764 1724	1761 1721	1748 1716	1745 1716	1742 1712	1789 1700	1786 1706	1753 1704	1730 1701	1727 1898	8	į	i	i	1	3	2	:	1
60 FB	1695 1667	1692 1664	1689 1663	1686 1656	1681 1656	1681 1651	1678 1650	1876 1847	1672 1645	1660 1662	ì	ì	1	1	2	2	2	9	8
ea ea	1639 1613		1684 1608	1651 1606	1629 1603	1696 1600	1625 1597	1621 1595	2618 1502	1616 1590	ģ	1	1	1	1	3	2	:	2
63	1597	1585	1562	1560	1577	1675	1572	1570	1567	1565	ĭ	1	1	1	2	\$	8	1	8
65 65	1503 1538	1500 1688	1558 1534	1665 1691	1568 1529	1650 1527	1548 1524	1646 1522	1543 1520	1641 1617	1	j	1	1	1 2	12	1	2	2
88 67	1515 1495	1518 1490	1611 1488	1608 1486	1606 1484	1504 1481	1502 1470	1499	1497	1405 1473	1	7	1	1	1	ŝ	? 1	3	1
68	1471	1468	1408	1461	1468	1400	1458	1456	1458	1451	ō	1	ī	i	1	8	8	į.	8]
6 9 70	144B 1498	1447 1427	1445 1425	1449 1422	1461 1420	1439 1418	1437 1416	1488		1481 1410	0	0	1	0	1	ļ	1	i	Î
71 78	1408 1989	1406 1567	1404 1386	1403	1401 1851	1299 1379	1897 1877	1895 1376	1898 1874	1891 1871	li.	7	1	1	ł	ŝ	3	2	1
73	1870	1888	1866	1884 1846		1961 1842	1858 1840	1857 2889	1355 1237	1853 1835	ě	Ö	Õ	î	ā	i	ī	1	i
ñ	1851 1838	1331	1848 1830	1928	1326	1325	1893	132	1819	1217	ŏ	ŏ	ŏ	ō	ò	ì	i	í	ź
78 77	1816 1290	1814 1207	1912	1811 1204	1809 1299	1507 1290	1905 1289	1304 1287	1802 1985	1800 1284	0	0	9	10	1.	ŀ	4	1	1
78	1982	1280	1279	1277	1276	1274	1972	1271	1200	1267	ō	i	i	1	ī	ı	1	8	1
H	1260 1260	1264 1248	1263 1247	1542	1250 1244	1958 1242	1256 1263	1255 1230	1268 1288	1259 1286	ô	0	1	0	1	ŀ	1	1	i
61	1295	1233	1232	1250	1220	1227	1235	1994	1222 1208	1221 1206	ō	0	į	ļ	1	ŀ	1	į	1
	1220 1205		2917 1202	1200		1312 1198	1911 1196		1198	1199	1	i		1	1	1	1	l S	ì
W	1190 1176	1169 1175	1156 1176	1186 1172	1184	1188 1170	1182 1168		1179 1166	1178 11 64	0	Ô	ô	0	0	1	0	1	1
86 87	1168 1149	1161 1145	1160 1147	1150 1145	1167 1144	1156 1143	1165 1142	1153 1140	1159 1150	1181 1238	ģ	0	D	1	1	ŀ	1	1	1
Ŷ.	1128	1185	1184	1153	2181	1130	1120	1127	1120	1125	Įŏ	ō	ī	1	1	i	1	3	1
89 81)	1124	1123 1110	1121 1109	1107	1110	1117 1108	1104 1104	1108		11100 1100	0	0	0	3	1	1]	1	ì
ei M	1099 1087	1998 1086	1096 1085	1095 1088	1094 1082	1095 1081	1092 1080	1061 : 1079	1089 1078	1068 1076	ģ	0	1]	1	ŀ	1	į	1
10	1075	1074	1073	1072	1071	1070	1009	1067	1000	1065	ō	0	ò	Ü	ō	ō	0	0	ū
Ħ	1054 1058	1052	1062 1050	1060 1049	1050 1048	1068 1047	1057 1046	1066 1065	1055 1044	1064 1068	ô	0	0	0	1	ì	1	i	1
10 17	2042 2041	1041 1030	1040 1020	1088 1028	1047 1027	1088 1098	1086 1026	1084 1024	1868 1022	1022 1021	Ŷ	0	î	1		0	1	1	;
	1020 2010	1019	1018 1008	1017 1007	1936 1006	1016 1005)014 1004	1018	1012	1011 1001	ô		ė	ô	í	ŀ	i	i	i
	1410	1000	1.000	1001	.000	1000	144.	4000	2002	2001	<u>"</u>		ľ	u	Ľ	ľ		Ľ	

TABLE OF DOUBLED SQUARE ROOTS FOR

-					1 A DIM				1	AWAZZ	
•	0	100	208	306	400	600	600	700	800	#00	
010000	0.000 2.000 2.828 8.464 4.000 4.472	20 00 20 10 20 20 20 30 20 40 20 40	25 43 25 43 26 43 26 55 26 55 26 55	84 64 84 76 84 76 84 81 84 87 84 87	40-00 40-06 40-10 40-16 40-20 40-25	447 447 448 448 448	49 99 49 03 49 07 49 15 49 15 49 15	67-91 67-96 62-99 53-93 63-97 53-10	50 50 50 60 50 67 50 75	80 65 80 65 80 65 80 65 15 80 65 15 80 65 15 80 65 15 80 65 15 80 65 15 80 65 15 80 65 15 80 65 15 15 15 15 15 15 15 15 15 15 15 15 15	· I
97==0	4 809 5 292 5 657 6 000 6 826	20:69 20:49 20:78 20:68 20:08	28-71 28-77 28-34 28-91 25-96	84 00 85 04 86 10 86 15 85 21	40:35 40:49 40:49 40:49 40:49	44°90 45 03 45 06 45°12 45 17	49-97 49-97 49-92 49-96 49-40	53·14 63·18 63·22 68·95 53·29	60-78 86-89 86-85 60-80 80-92	87 27 88 27 88 27 88 28 88 28 88 28 88 28	8 8 10
1 2222	6-618 0-028 7-911 7-468 7-740	21 07 21 17 21 26 21 85 21 45	29 06 29 12 29 19 29 26 29 33	85 85 85 85 85 84 85 86 85 br>85 85 85 85 85 85 85 85 85 85 85 85	40 65 40 60 40 64 40 69 40 74	45-91 45-95 45-90 45-84 45-80	49-44 40-48 49-59 49-56 49-60	59:38 58:87 59:40 50:44 58:48	66-96 56-99 57-03 57-96 57-10	60 87 60 48 60 48 60 48	11 19 18 14 15
16 17 18 19 30	8-000 8-240 8-485 8-718 8-044	21-64 21-69 21-78 21-89 21-91	29 88 29 46 29 63 29 60 29 60	86.56 36.61 86.07 83.73 35.78	40 79 40 84 40 89 40 94 60 99	45 45 45 46 45 56 45 61	49 64 40 68 49 72 49 76 49 80	53°52 53°56 53°59 53°63 53°67	57:15 57:17 57:20 57:24 67:27	888888 888888 8888888	16 17 18 19 80
	9-168 9-581 9-582 9-798 10-000	22 00 22 18 22 27 22 36	29 78 29 80 29 87 29 93 29 93 20 90	\$2 89 \$2 64 \$3 60 \$6 06 \$6 11	41.04 61.08 61.18 41.18 61.28	45:74 45:78 45:83	49:68 49:98 49:96 69:06 80:00	58 74 55 78 58 81 58 85	57 94 67 98 57 41 67 46	60 76 60 76 60 78 60 88	IRRKE B
11 11 11 11 11 11 11 11 11 11 11 11 11	10:198 10:892 10:585 10:770 10:254	22°64 22°63 22°72 22°80	90-88 90-89 90-18	36 17 36 22 86 25 86 25	41 28 41 33 41 88 41 42 41 47	45 91 45 90 46 00 66 04	60 08 60 12 60 16 60 20	53 99 53 96 54 90 41 91	57 52 57 56 57 56 57 58 57 62	60 89 60 98 60 98	27 29 29 30
2 **** ** ** ** ** ** ** ** ** ** ** **	11:186 11:314 11:480 11:682 11:859	92:00 92:06 23:07 93:15 25:24	80 40 80 40 80 53 20 59 80 69	86 30 80 44 50 50 86 56 36 01	61-59 61-57 61-57 61-57 61-71	46°18 46°17 46°29 46°20	50°28 50°32 50°30 60°40	54 11 54 18 54 18 54 22	67-69 67-72 57-76 57-70	61 02 61 06 61 09 61 12 61 14	11 13 14 15 1
	12:000 12:164 12:329 13:490 19:649	25:85 22:41 25:49 25:58 25:50	80 79 80 79 80 85 80 92 80 98	84-66 86-79 96-77 90-92 86-88	41 76 41 61 41 80 41 90 41 96	46°85 46°85 46°99 46°48 48°48	50 44 50 48 50 52 50 55 50 66	54-96 54-90 54-39 54-37 54-41	67 88 67 86 57 96 57 93 57 97	61-19 61-29 61-29 61-29 81-32	26 27 28 48
****	19:805 19:951 19:115 18:866 18:416	99-75 99-85 93-92 94-00 94-06	\$1 05 \$1 71 \$1 18 \$1 24 \$1 80	56 98 56 98 57 04 57 09 37 15	42 00 42 05 42 10 42 14 42 16	46-69 46-56 46-65 46-69	60.64 60.63 60.71 50.75 60.79	64 44 64 48 64 68 64 68 64 58	68-00 68-08 58-07 68-10 58-14	61 85 61 88 61 42 61 46 61 48	4444
44 44 44 44	18:565 18:711 18:686 14:000 14:142	24-43 24-41 24-25 24-17	81-87 81-48 81-50 81-56 81-02	87 90 87 96 87 96 87 96 87 42	42 24 42 29 42 83 42 83 42 83	46-73 46 78 48 82 40-86 48-90	50-68 50-57 50-91 50-96 50-99	64-68 54-50 54-70 54-77	68 21 68 21 58 24 58 26 58 51	61.55 01.55 01.58 01.61 01.84	#0 #1 #0

LORD KELVIN'S STANDARD ELECTRIC BALANCES.

	0	100	200	500	400	680	109	704	809	500	•
19 18 18 17	14-288 14-422 14-660 14-697 14-692	24°58 24°06 24°74 24°82 24°90	81.59 61.75 81.81 81.87 81.94	27-47 27-52 27-52 27-58 27-68	42:47 42:52 42:57 42:57 42:01	46-06 45-99 47-03 47-07 47-13	51:08 51:07 51:11 51:16 51:19	94 83 94 83 94 83 94 83	58:54 58:48 58:41 58:45 58:48	61 48 61 71 61 74 61 77 61 41	# # # #
64 87 68 69	14-967 15-100 15-255 15-603 15-403	24 08 25 06 16 14 25 22 25 30	82°00 32°06 82°12 82°19 31°25	57-74 87-79 87-84 87-89 87-95	4271 4276 4280 4285 4290	47°26 47°20 47°24 47°20 47°83	61-22 61-26 51-86 51-84 61-88	54 09 55 03 55 06 55 10 56 14	58-61 58-65 58-68 58-62 58-65	61:84 61:87 61:90 61:94 61:97	50 57 59 59
61 69 64 65	15-620 16-748 16-875 16-000 16-125	25 48 25 48 25 69 25 61 25 69	82-81 83-97 82-48 80 50 82-68	86 ::0 85 05 86 11 86:16 88:21	62-04 62-09 63-63 63-06 63-18	67 87 67 41 47 40 67 50 47 54	51 46 51 66 61 64 51 64	55 17 55 21 55 24 55 25 55 19	58-69 56-79 58-75 56-79 58-82	62-00 61-06 62-06 02-10 63-12	60 60 60 60 60 60 60 60 60 60 60 60 60 6
81 87 81 77	16-248 16-371 16-613 16-613 16-718	25-77 25-86 25-82 26-00 24-08	82-62 83-68 83-74 83-80 82-86	\$8:26 \$8:31 \$8:37 \$8:42 \$8:47	45:17 43:22 43:27 43:31 43:36	47-58 47-68 47-67 47-71 47-78	61:61 51:66 61:69 61:79 61:77	55 85 55 89 55 48 65 48 65 60	58:96 58:60 58:02 58:90 58:99	63·16 69·19 62·28 62·26 63·29	66 67 68 69 79
TI TI TI TI TI	16:952 16:971 17:088 17:205 17:221	98-16 95-23 95-81 95-86 95-46	52 92 52 98 53 06 53 11 55 17	88-59 88-57 86-63 88-68 88-78	48*41 48 46 48 60 48*64 43*59	47-70 47-83 67-87 47-92 47 Dd	51 -65 51 -65 51 -58 51 -92 51 -96	55 58 55 57 55 61 66 84 56 68	59 08 59 08 59 09 59 18 59 18	68 49 63 49 63 86 63 88	ななない。
70 77 78 60	17-436 17-350 17-064 17-776 17-889	26 61 26 61 26 08 26 76 26 80	\$3 29 \$8 20 \$8 36 \$3 47	38 78 88 68 38 68 88 94 88 99	49 48 47 68 48 78 43 77 49 82	48-00 48-04 48-08 48-19 48-17	69 00 63 04 62 08 63 15 62 15	65 71 65 76 65 78 65 89 65 88	50:26 50:26 50:26 50:80 59:58	62 48 62 51 62 58 62 58 63 61	1000年17日
99 98 91 11	18-000 18-111 18-291 18-83) 18-485	20:01 20 98 27:06 27:18 27:20	88-58 83-59 83-05 88-70 88-74	89-04 89-14 89-19 89-24	48-98 48-91 43-95 44-00 44-05	48-91 48-26 48-29 48-33 46-47	58 19 52 28 52 27 52 81 52 86	65 69 66 98 65 96 65 00 66 04	59:38 50:40 50:43 59:45 59:60	88877477 8888888	RHHHI
85 FF 48 89 99	18/647 18/665 18/769 18/808 18/974	27 -18 27 -25 27 -62 27 -50 27 -67	58-53 58-88 58-94 34-00 54-06	29:20 39:34 39:40 39:45 39:50	44 00 44 14 44 18 44 18 44 28 44 27	48:41 48:46 48:50 48:54 48:48	59:68 59:48 69:46 52:50 63:84	56 07 56 11 56 14 56 18 56 21	59 58 50:57 59:50 59:38 59:51	62:80 62:86 62:86 63:80	50 00 10 E
24 EE EE	19-079 19-188 19-287 19-001 19-004	27 64 27 71 27 78 27 86 27 86	24·12 34·18 24·28 34·29 34·29	88-65 88-66 88-85 89-76	445 445 445 455 455	48-62 48-66 48-70 48-74 48-79	62-87 62-61 62-66 69-66 69-78	56 25 56 28 56 32 50 86 66 89	59-75 59-75 59-75 59-89 59-88	42.00 42.00 43.00 43.00 43.00	***************************************
97 98 99 108	19-596 18-599 19-799 19-900 90-000	28-00 28-07 29-14 29-11 28-25	84-41 84-47 84-58 84-58 84-58	89.65 89.65 89.90 89.95 40.00	44 18 44 18 44 18 44 78 44 72	48-87 48-97 48-91 48-96 48-99	52 76 52 80 52 84 61 88 62 92	66-48 60-46 66-50 68-68 50-67	59 67 59 90 59 68 56 97 50 00	6915 6815 6816 6816 6816 6816	****